

Lecture 30: Phasors Circuit Analysis and Design Part 2

OBJECTIVES:

1. Learn to apply circuit analysis techniques we already know to solve circuits in the phasor domain

READING

Required: Textbook, section 8.4–8.5, pages 402–426

Optional:

1 Introduction

Today we continue our analysis of phasor circuits. Last class we did examples of:

- 1. Parallel and series combinations of Impedances
- 2. Voltage and Current Division
- 3. Mesh and Node Analysiis

Today we will look at:

- 1. Proportionality and Superposition
- 2. Thevenin and Norton equivalent circuits

All these things still apply to phasor domain circuits. As a reminder, phasor analysis only applies to the steady state sinusoidal responses. Phasor analysis does not tell you anything about the transient response.

2 Proportionality

Back in lesson 8 we introduced this introduced this idea of proportionality which states that for a linear circuit, any change to the input has a proportional change to the output. Stated mathematically:

$$y = Kx$$

where x is the input, y is the output, and K is the proportionality factor.

This also applies to phasors and can be written as:

$$\mathbf{Y} = \mathbf{K}\mathbf{X}$$

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where Y, X, and K are all in general complex.

To make use of proportionality, the book talks about the *Unit Output Method....* I prefer the *Unit Input Method.* Let's do an example:

Example 1– This example is a modified version of textbook exercise 8-22. For the circuit shown in Figure 1, use the Unit Input Method to find I_o

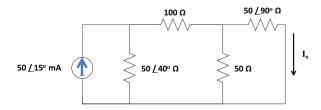
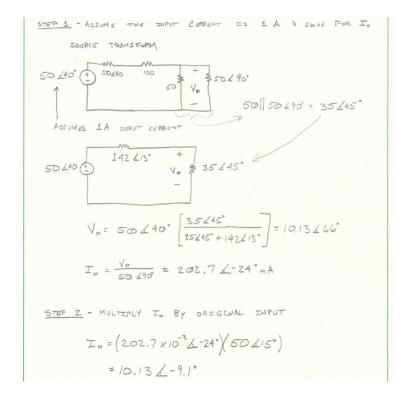


Figure 1: Circuit to accompany example 1



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3 Superposition

Before we jump right into an example, now is a good opportunity to remind you that phasor analysis only works for circuits that are excited by a single sinusoidal frequency. This does not mean we cannot have more than one source, it just means they all have to have the same frequency (ω) .

Example 2 – Textbook Exercise 8-23 — For the circuit in Figure 2, use superposition to find I_x .

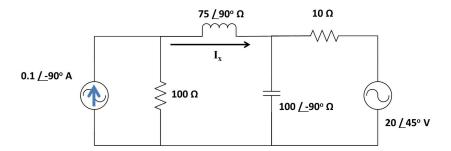
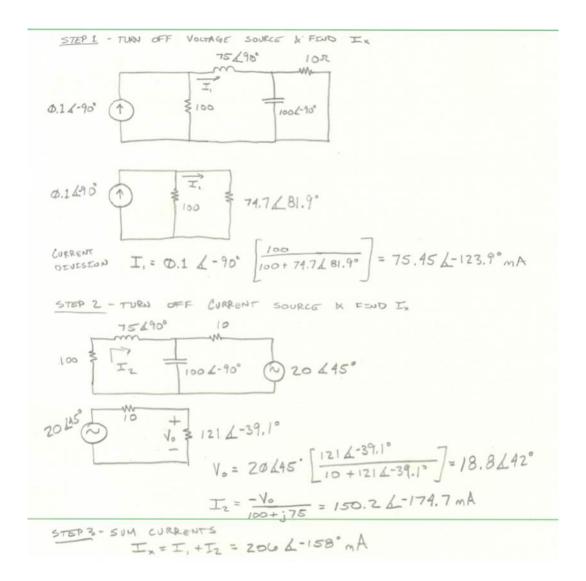


Figure 2: Circuit to accompany example 2



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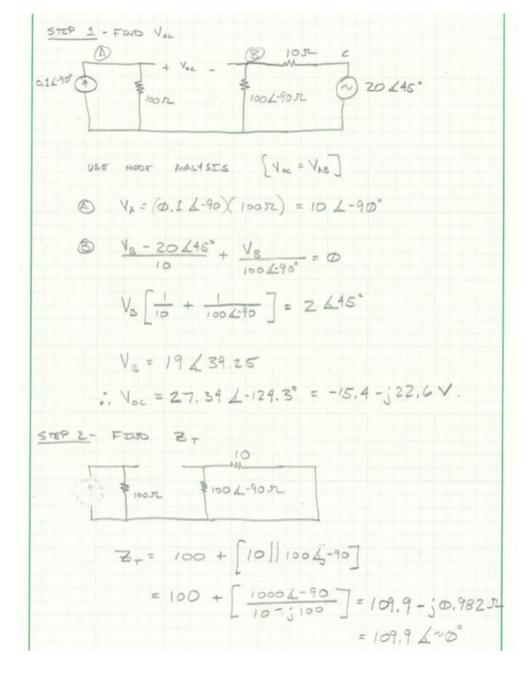
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4 Thevenin's and Norton's Theorems

This section will offer a quick review of Thevenin's and Norton's Theorems before we work a couple of examples.

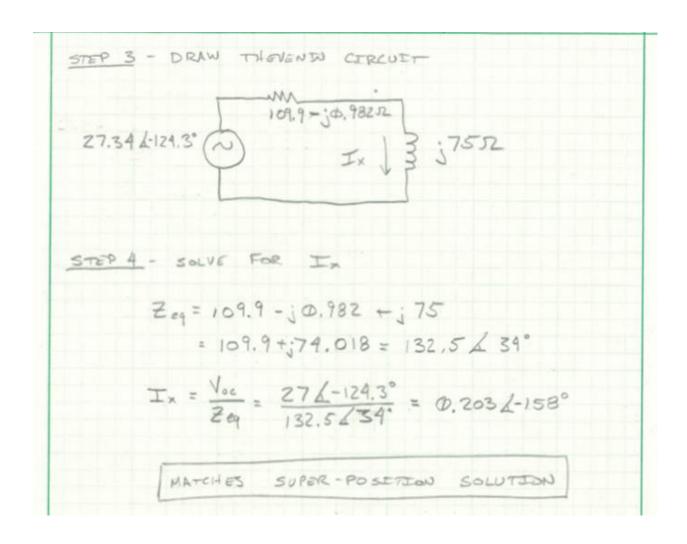
For Thevenins theorem, we will take a *source* circuit that is connected to some *load* circuit and replace the source circuit with a single voltage source in series with a single *impedance*. To do this we must find the value of the source voltage and the *Thevenin impedance*. The source voltage is found by calculating the open circuit voltage if the load is removed. The easiest way to calculate the Thevenin Impedance is by using look-back.

Example 3– Textbook Exercise 8-29 — For the curcuit in example 2 (Figure 2), find the Thevenin circuit seen by the inductor then calculate I_X .



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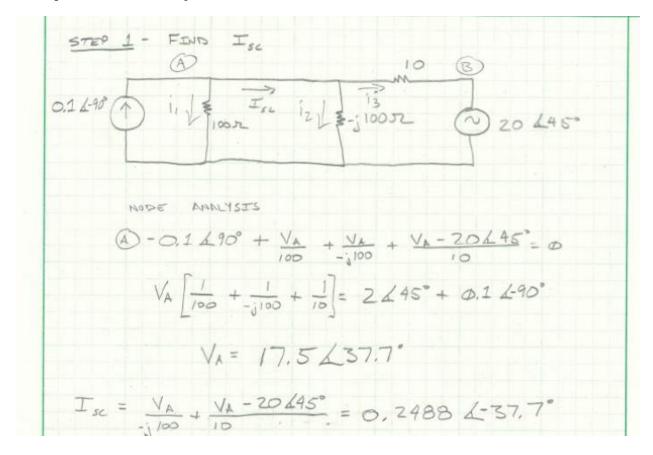


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Norton's Theorem is like Thevenin's except we find a current source in parallel with an impedance.

Example 4 – Rework Example 3 with Norton's Theorem.



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