

Overview

- ALUs - arithmetic logic units
- Shifters
- Number systems

HW #4 LSN 24-27 due LSN 29

Arithmetic Logic Unit (ALU):

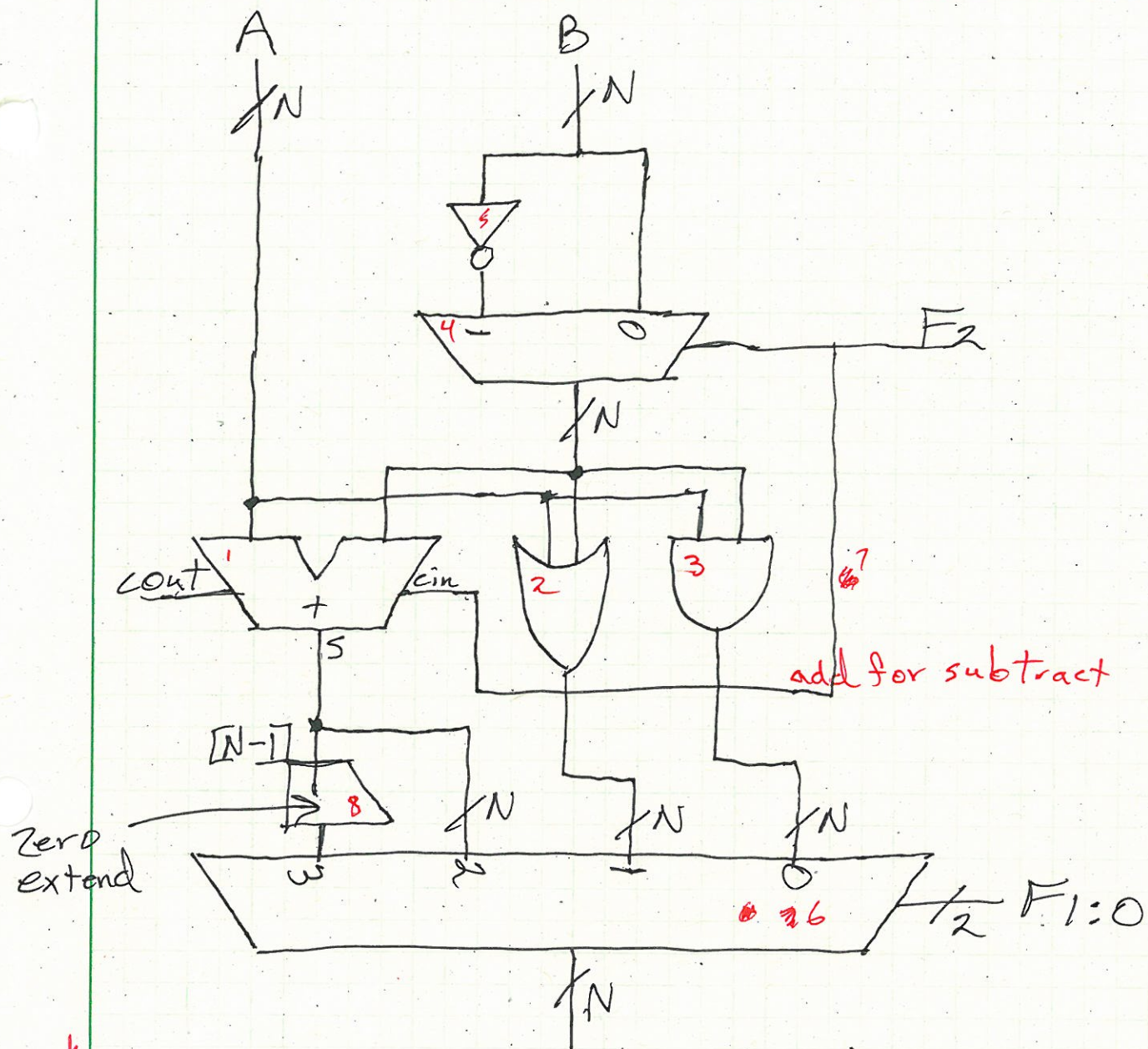
- combines math and logic
- heart of most computers

Does 7 things:

F_2	F_1	F_0	operation
0	0	0	A and B
0	0	1	A or B
0	1	0	A + B
0	1	1	not used
1	0	0	A and \bar{B}
1	0	1	A or \bar{B}
1	1	0	A - B
1	1	1	S L T

ALU Built using what? Logic Functions?

- adder
- inverter
- and
- mux
- or
- comparator



Magnitude comparison: ~~IFF~~^{compute} $A - B$ and looking at the sign (most significant bit) of the result. If the result is negative (i.e. sign bit is 1), then $A < B$. Otherwise A is greater than or equal to B .

How do we multiply in Binary?

$$\begin{array}{r}
 101 \times 3 \\
 \hline
 101 \\
 1010 \\
 00000 \\
 \hline
 1111 \Rightarrow 15
 \end{array}$$

Shifter:

- Logical \rightarrow empty bits ≤ 0 (LSL or LSR)
 - arithmetic \rightarrow on R shifts, keep MSB *useful for mult/div signed numbers*
 - \Rightarrow Shift = shift amount
- ASL is same as LSL!

$$100110 \Rightarrow \text{shift R} \Rightarrow 010011$$

$$32 + 4 + 2 = 38 \qquad 16 + 2 + 1 = 19$$

Shift R divide by 2

$$100110 \Rightarrow \text{shift L} \Rightarrow 001100 = 12$$

We ran out of bits and lost a bit

6-Bit system only goes up to 63!

Rotator:

- Bits that fall off the end move to the other end.

Fixed Point:

- implies binary point btwn integer & fractional bits
- You keep track of radix!

Q2.6

XX, XXXXXX

What is this number in Decimal?

011101.10101 (given in 2's comp)

$$\begin{array}{r}
 16+8+4+1 \\
 = 29 \\
 \uparrow \uparrow \uparrow \uparrow \\
 2^{-1} \quad 2^{-2} \quad 2^{-3} \\
 0.5 \quad 0.25 \quad 0.125 \\
 0.125 \times 2^{-5} = 0.03125
 \end{array}$$

$$\Rightarrow 29.65625$$

101000.00100 (2's comp)

add 1 to LSB

Flip 010111.11100 + 1

~~$$\begin{array}{r}
 101000 \\
 \text{Flip } 010111 \\
 + 1 \\
 \hline
 011000 = 24
 \end{array}$$~~

~~$$\begin{array}{r}
 00100 \\
 \text{Flip } 11011 \\
 + 1 \\
 \hline
 11100
 \end{array}$$~~

$$\begin{array}{r}
 010111.11100 \\
 \downarrow \downarrow \quad \downarrow \downarrow \\
 -23 \quad 0.875
 \end{array}$$

$$\begin{array}{c}
 0.5 \\
 0.25 \\
 0.125
 \end{array}
 \Rightarrow 0.875$$

$$\Rightarrow -23.875$$

Fixed point easier in HW

Floating Point:

- similar to scientific notation

$$\begin{array}{c}
 \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \\
 \text{sign} \quad \text{mantissa} \quad \text{Base} \quad \text{exponent}
 \end{array}
 2.3 \times 10^6$$



Sign

163₁₀

1010 0011

1.0100011 $\times 2^7$
 \Rightarrow 0 00000111 1010001100...0
sign exponent Mantissa

Finally standardized w/

IEEE 754 - floating point ~~notation~~ standard \Rightarrow add 127 to exponent \Rightarrow do not include leading 1
Implicit Leading One
 leading 1 is always 1
 therefore need not be stored
~~This is~~ 0 00000111 1010001100...0
IEEE 0 1 0000110 ~~1010001100...00~~
(Bias)
 7 + 127 = 134

Biased exponent
 for +9 exponents adds another bit for useful data

This is a double = 64 Bits

11 exponent

52 fraction

★ Look at example in book on floating point addition!

★ Figure 5.29 - Floating Point Addition

Floating Point Addition:

- 1) extract exponent & Fraction Bits
- 2) add Leading 1 back to make mantissa
- 3) compare exponents
- 4) shift smaller ~~amount~~ exponent's mantissa
- 5) add mantissas
- 6) shift mantissas and adjust mantissas if necessary
- 7) Round if necessary
- 8) turn back into Legit (IEEE 754) Floating Point