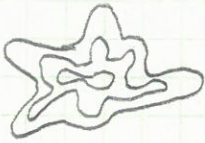


Bread First Search - explores equally in all directions. It is 'incredibly fast and explores everywhere'

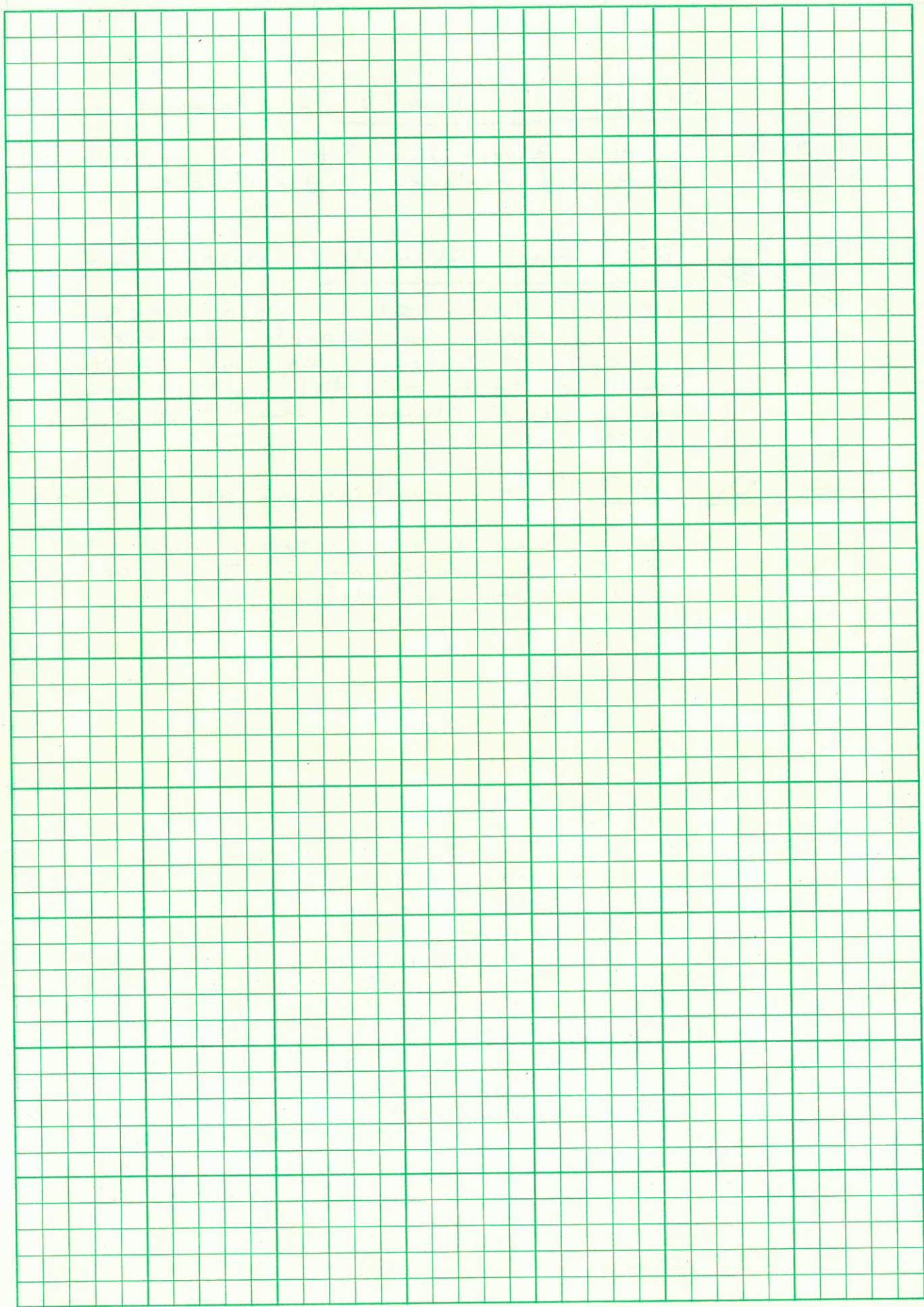


Dijkstra's Algorithm - also called uniform cost search, prioritizes which path to search. However, instead of exploring equally, it looks at the cost of taking a certain route and chooses the cheapest first

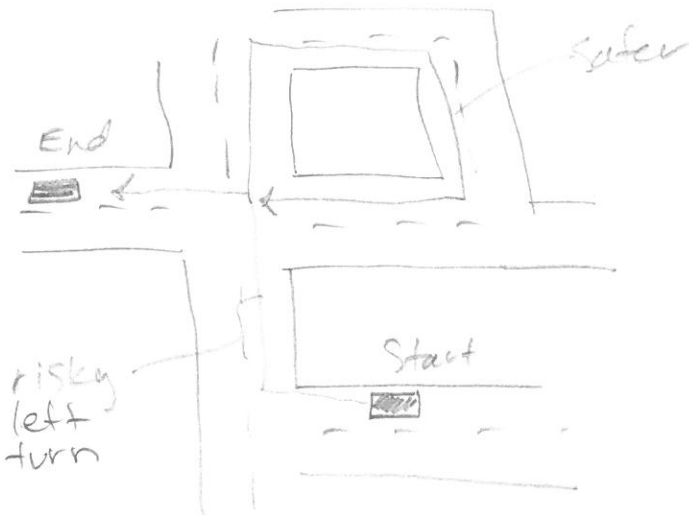


A\* - a modification of Dijkstra's algorithm, but is optimized for a single destination. It uses a heuristic to drive it





# Motion Planning



BFS or Dijkstra's Alg (DA) 2

Give: Map

Goal, Start loc  
Cost function

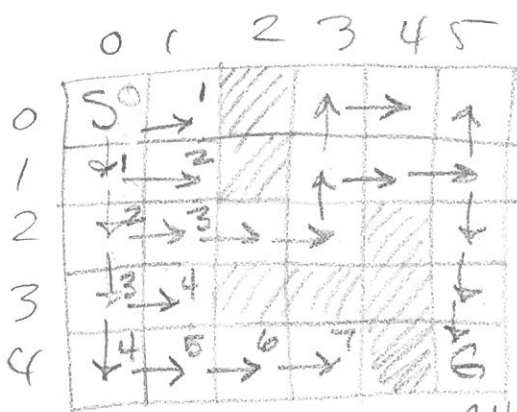
actions  
move:  
turn:

\* FedEx, Ups, etc plans routes w/ right turns during rush hours

Diagram illustrating a grid-based motion planning environment. A car starts at 'Start' and moves towards 'End'. A 'right' turn is indicated at a junction. A 'left' turn is also indicated.

	Forward	Left turn	right turn	Cost	
				left	right
BFS	1	1	1	<u>6</u>	10
DA	1	10	1	<u>15</u>	16
	1	20	1	<u>25</u>	<u>16</u>

- Both BFS + DA give us solutions
- BFS causes us to make a dangerous or time consuming left turn in heavy traffic
- DA must be tuned to avoid the left turn
  - there maybe situations where a left turn is ok or better ... it depends
- Both of these explore the whole map
  - for a static environment, you could pre compute all of this



3

Path Plan - Shortest sequence

Cost: 11 actions

g-value ~ gives us the shortest path  
 ↓ expand down and check if goal

open = ~~[0,0] 0~~ <sup>not 4</sup>  
 frontier → ~~[1,0] 2~~ ~~[0,1] 1~~  
~~[2,0] 2~~ ~~[1,1] 2~~  
~~[3,0] 3~~ ~~[2,1] 3~~  
~~[4,0] 4~~ ~~[3,1] 4~~  
~~[4,1] 5~~  
~~[4,2] 6~~  
~~[4,3] 7~~

$[x, y]$  cost-value

↑  
 f-value - a function that returns the cost of the move, this will be more complex w/ A\*

✓  
 $f\_value = cost\_value$

BFS or Dijkstra

- ① Expand frontier
  - move in all possible directions
  - calculate cost of move
  - stop when there is no longer any place to explore
- ② start from goal and move to start taking the lowest cost path

\* Both explore entire environment from the start and expand outward in all directions

A\* is similar

4

A\* always expands to goal

- Heuristic Function (h) - often gradient decent

A → B  
4 steps  
check it!

A	4	3	2
3		2	1
2	1	B	0

← optimistic guess to goal  
w/o obstacles

$h(x,y) \leq$  distance to goal  
from  $x,y$

- \* Doesn't have to be accurate, just guide the robot
- \* If it was accurate, then you probably already solved it

open [0,0] g-value f-value

$$f\text{-value} = g + h(x,y)$$

↑  
now look @ this when moving

	0	1	2	3
0	0	1		
1	1			
2	2			
3	3			
4	4	5	6	7

open [4,1] 5, 9  
g f = 5 + 4

expand node lower f-val  
and closer to goal

[4,2] 6, 9

[3,2] 7, 11 [4,3] 7, 9

[3,3] 8, 11 [4,4] 8, 9 ← this will take you goal

↑ exp Note: don't expand the open area

# Dynamic Programming

5

Given Map + Goal  
Outputs Best path from anywhere

has policy  $x, y \rightarrow \text{action}$

- thus if you find yourself somewhere other than where you thought, you know how to navigate
- Good in dynamic environment
- every grid pt tells you direction to go

value function (f) for each cell

$$f(x, y) = \min f(x', y') + 1$$

5	4	3	2
6	2	1	
7	1	0	Goal

Start

hill climbing action

## A\* Summary

Cost -

2		1	G 2
1	S 0		1
2		1	2

f\_value

heuristic

2		1	G 0
3	S 2		1
3	3		2

heuristic would never let you search in the shaded cells

4	2	G 2
4	S 2	2
5	4	4

both solutions are the same