

5.4 20) $\int (e^x - 2x^2) dx = e^x - 2\left(\frac{1}{3}x^3\right) + C$

21) $\int_{-2}^3 (x^2 - 3) dx = \left[\frac{1}{3}x^3 - 3x + C \right]_{-2}^3 = \left(\frac{1}{3}27 - 9 \right) - \left(\frac{1}{3}(-8) + 6 \right)$
 $0 + \frac{8}{3} - 6 = \frac{8}{3} - \frac{18}{3} = -\frac{10}{3}$

24) $\int_0^3 (1 + 6w^2 - 10w^4) dw = \left(w + 6\left(\frac{1}{3}w^3\right) - 10\left(\frac{1}{5}w^5\right) + C \right) \Big|_0^3$
 $= (3 + 2(27) - 2(243) + C) - (0 + 0 - 0 + C)$
 $= 3 + 54 - 486 = \boxed{-429}$

28) $\int_1^2 (x^2 - 4x^{-3}) dx = \left(\frac{1}{3}x^3 - 4\left(\frac{1}{-2}x^{-2}\right) + C \right) \Big|_1^2$
 $\left(-\frac{1}{2} + 2\left(\frac{1}{4}\right) \right) - \left(-\frac{1}{2} + 2 \right)$
 $= -\frac{1}{2} + \frac{1}{2} + 1 - 2 = \boxed{-1}$

31) $\int_0^1 x(\sqrt[3]{x} + \sqrt[4]{x}) dx = \int_0^1 (x^{4/3} + x^{5/4}) dx = \left[\frac{3}{7}x^{7/3} + \frac{4}{9}x^{9/4} + C \right]_0^1$
 $= \left(\frac{3}{7}(1) + \frac{4}{9}(1) \right) - 0 = \frac{27}{63} + \frac{28}{63} = \boxed{\frac{56}{63}}$

52) $\omega'(t) = \Delta \omega_{\text{avg}}$ $\omega(t)$

53)

18) $\int \frac{\sin 2x}{\sin x} dx = \int \frac{2 \sin(x) \cos(x)}{\sin(x)} dx$ (double angle theorem)
 $2 \int \cos(x) dx = \boxed{2 \sin(x) + C}$

53) $I \Delta Q'(t)$ $I = \text{current}$ $Q = \text{charge}$ $\frac{dQ}{dt} = \frac{\Delta \text{charge}}{\Delta t}$
 $\int_a^b I dt = Q(b) - Q(a)$: change in charge from $t=a$ to $t=b$

54) $100 + \int_0^{15} n(t) dt$: 100 + Δ bees from week 0-15