

# Atmospheric Hazards to Flight

Robert Stengel,  
Aircraft Flight Dynamics, MAE 331, 2014



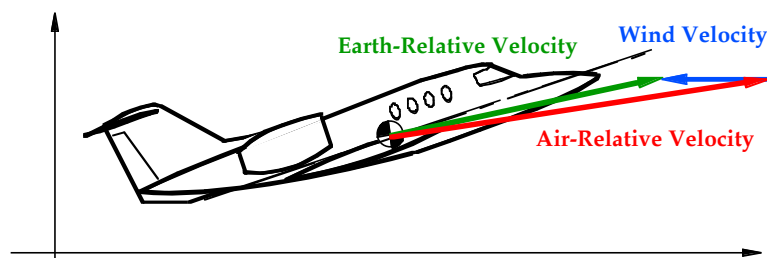
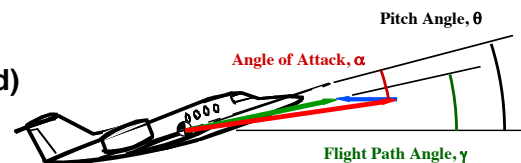
- Microbursts
- Wind Rotors
- Wake Vortices
- Clear Air Turbulence

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<http://www.princeton.edu/~stengel/MAE331.html>  
<http://www.princeton.edu/~stengel/FlightDynamics.html>

## Frames of Reference



- **Inertial Frames**
  - Earth-Relative
  - Wind-Relative (Constant Wind)
- **Non-Inertial Frames**
  - Body-Relative
  - Wind-Relative (Varying Wind)



- [illegible]

[illegible]

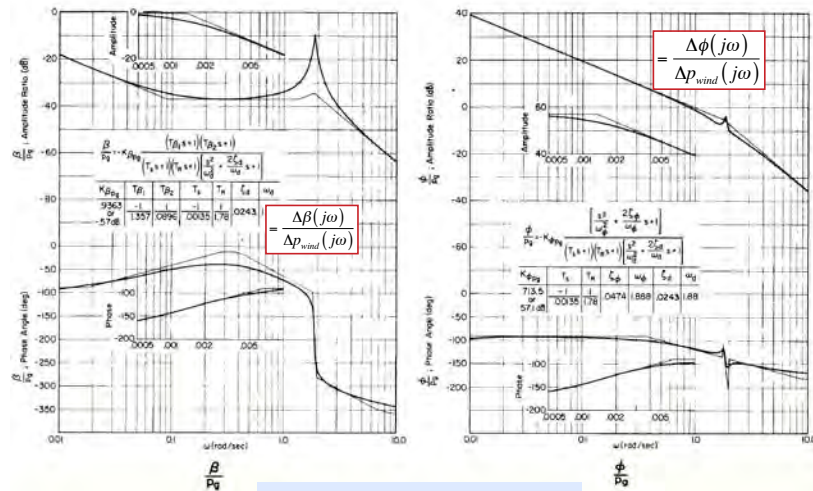
- 
- Figure 10 consists of two plots comparing the magnitude and phase of the transfer function  $\Delta\alpha/\Delta\alpha_{wind}(j\omega)$  (solid line) and  $\Delta\theta/\Delta\alpha_{wind}(j\omega)$  (dashed line).
- The top plot shows the magnitude ratio in dB on the y-axis (from -90 to -40) against wind speed  $\omega$  in rad/sec on the x-axis (log scale from 0.1 to 100.0). The bottom plot shows the phase angle in degrees on the y-axis (from -270 to 180) against wind speed  $\omega$  in rad/sec on the x-axis (log scale from 0.1 to 100.0).
- Both plots include a table of corner frequencies and slopes for the magnitude ratio.
- Magnitude Ratio Table:**
- | Corner Frequency $\omega$ (rad/sec) | Slope (dB/dec) |
|-------------------------------------|----------------|
| 0.0058                              | -21.6 dB/dec   |
| 0.007                               | 0 dB/dec       |
| 0.07                                | -18.0 dB/dec   |
| 0.67                                | -0.7 dB/dec    |
| 1.74                                | -4.2 dB/dec    |
| 4.93                                | -0.7 dB/dec    |
- Phase Angle Table:**
- | Corner Frequency $\omega$ (rad/sec) | Slope (deg/dec) |
|-------------------------------------|-----------------|
| 0.0058                              | -21.6 deg/dec   |
| 0.007                               | 0 deg/dec       |
| 0.07                                | -18.0 deg/dec   |
| 0.67                                | -0.7 deg/dec    |
| 1.74                                | -4.2 deg/dec    |
| 4.93                                | -0.7 deg/dec    |
- The boxed equation in the center of the phase plot is:
- $$\frac{\Delta\theta}{\Delta\alpha_{wind}(j\omega)} = \frac{\Delta\theta}{\Delta\alpha_{wind}(j\omega)}$$

*MacRuer, Ashkenas, and Graham. 1973*

# Sideslip and Roll Angle Frequency Response to Vortical Wind



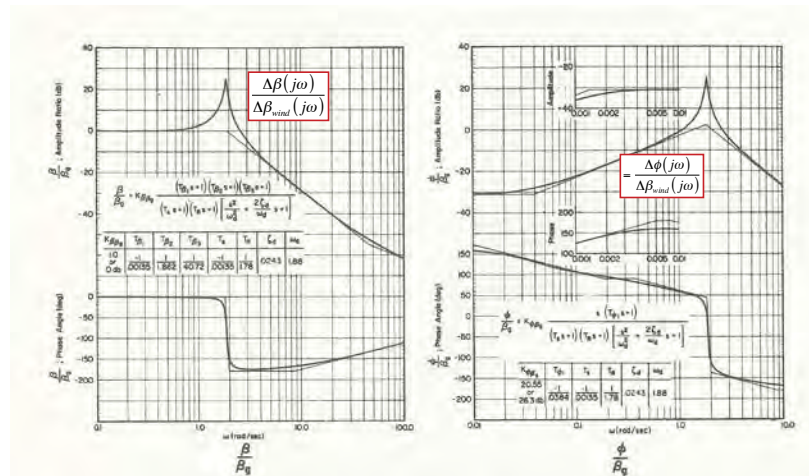
- Sideslip angle resonance at Dutch roll natural frequency
- Roll angle is integral of vortical wind input



MacRuer, Ashkenas, and Graham, 1973

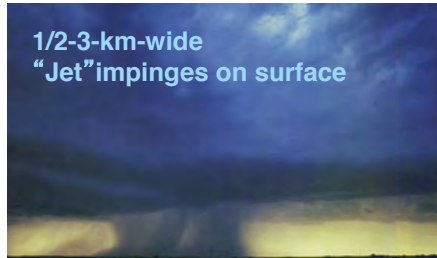
# Sideslip and Roll Angle Frequency Response to Side Wind

- Sideslip and roll angle resonance at Dutch roll natural frequency

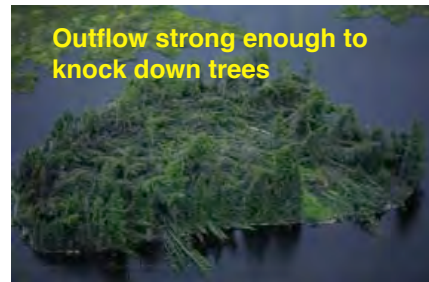
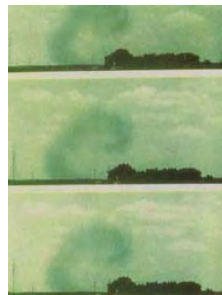


MacRuer, Ashkenas, and Graham, 1973

# Microbursts



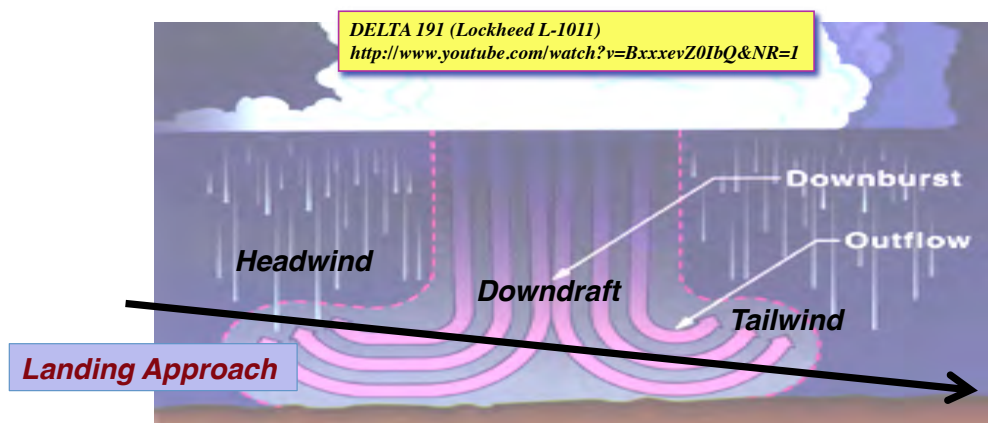
Ring vortex  
forms in  
outflow



## The Insidious Nature of Microburst Encounter



- The wavelength of the phugoid mode and the disturbance input are **comparable**





## Importance of Proper Response to Microburst Encounter

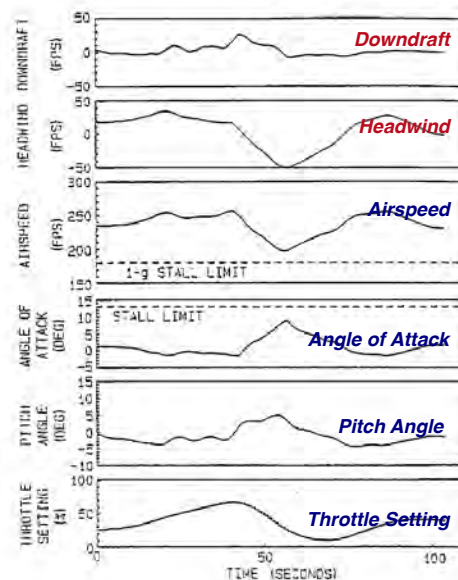
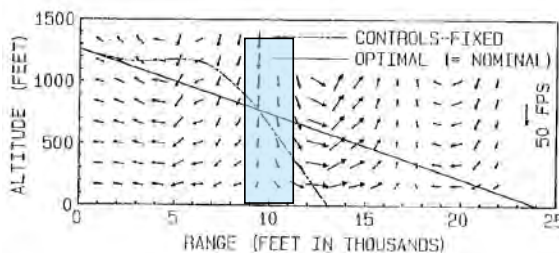


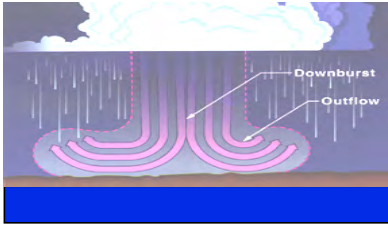
- Stormy evening July 2, 1994
- USAir Flight 1016, *Douglas DC-9*, Charlotte
- Windshear alert issued as 1016 began descent along glideslope
- DC-9 encountered **61-kt windshear**, executed **missed approach**
- Plane continued to descend, striking trees and telephone poles before impact
- Go-around procedure was begun correctly -- aircraft's nose rotated up -- but **power was not advanced**
- That, together with increasing tailwind, caused the aircraft to **stall**
- Crew **lowered nose to eliminate stall**, but descent rate increased, causing ground impact



## Optimal Flight Path Through Worst JAWS Profile

- Graduate research of **Mark Psiaki**
- **Joint Aviation Weather Study (JAWS)** measurements of microbursts (**Colorado High Plains, 1983**)
- **Negligible deviation from intended path** using available controllability
- Aircraft has sufficient performance margins to stay on the flight path

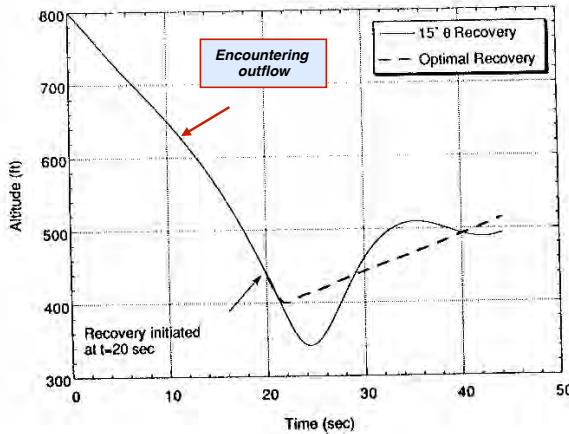




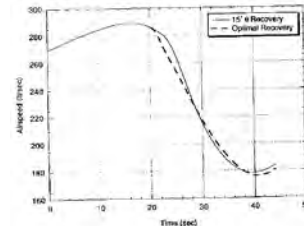
## Optimal and 15° Pitch Angle Recovery during Microburst Encounter

- Graduate Research of *Sandeep Mulgund*

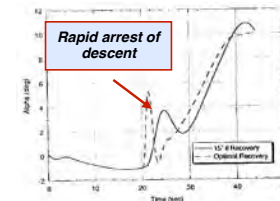
- Altitude vs. Time



- Airspeed vs. Time



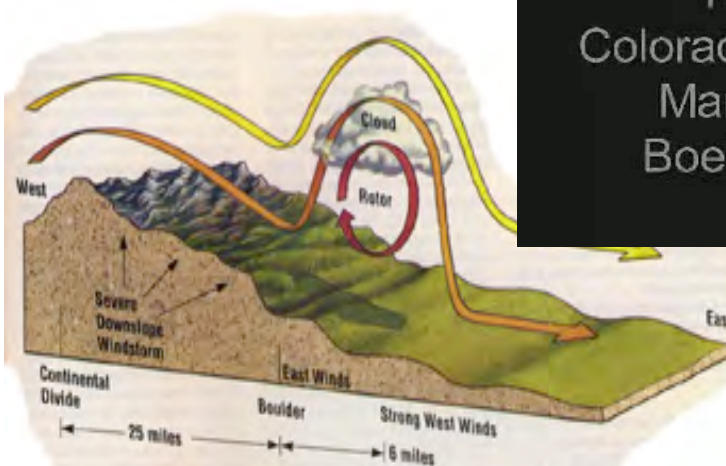
- Angle of Attack vs. Time



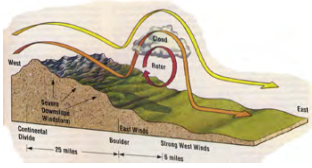
- FAA Windshear Training Aid, 1987*, addresses proper operating procedures for suspected windshear



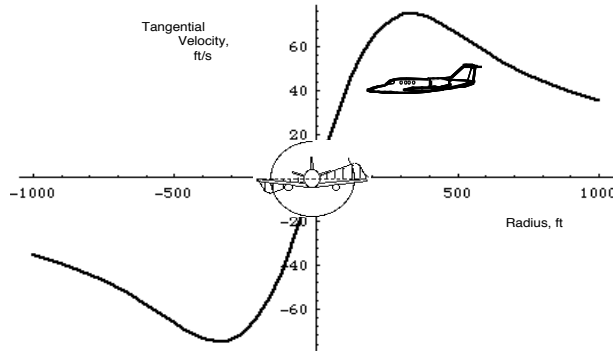
## Wind Rotors



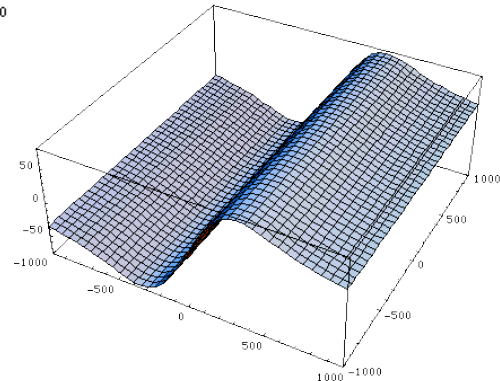
United Airlines  
Flight 585  
Colorado Springs, CO  
March 3, 1991  
Boeing 737-200



# Aircraft Encounters with a Wind Rotor



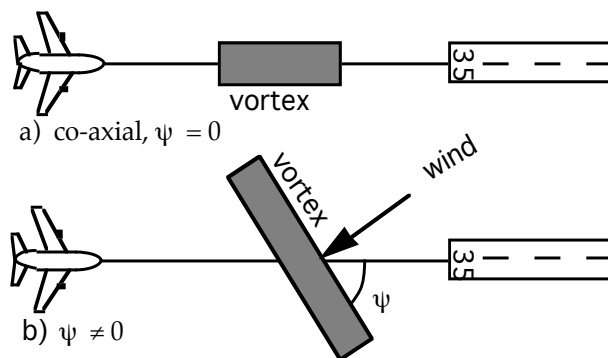
- Tangential velocity vs. radius for *Lamb-Oseen* Vortex

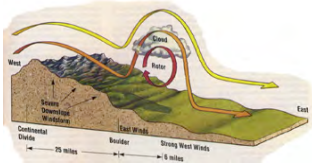


## Geometry and Flight Condition of Jet Transport Encounters with Wind Rotor



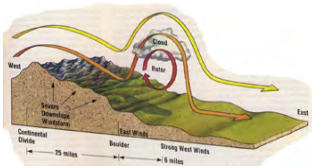
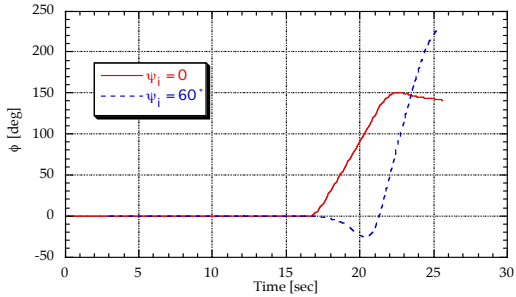
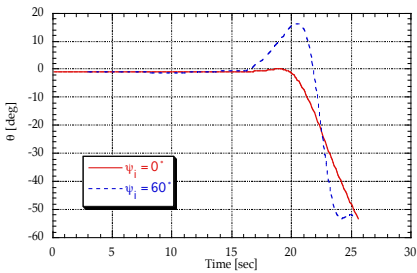
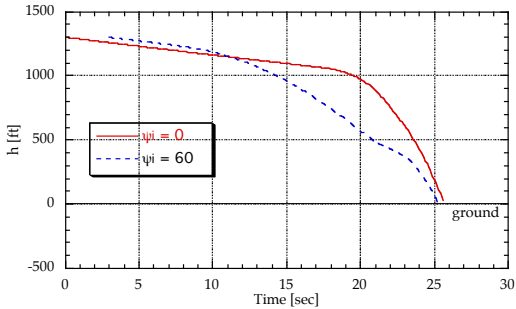
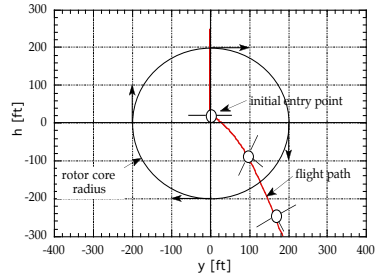
- Graduate research of *Darin Spilman*
- **Flight Condition**
  - True Airspeed = 160 kt
  - Altitude = 1000 ft AGL
  - Flight Path Angle =  $-3^\circ$
  - Weight = 76,000 lb
  - Flaps =  $30^\circ$
  - Open-Loop Control
- **Wind Rotor**
  - Maximum Tangential Velocity = 125 ft/s
  - Core Radius = 200 ft



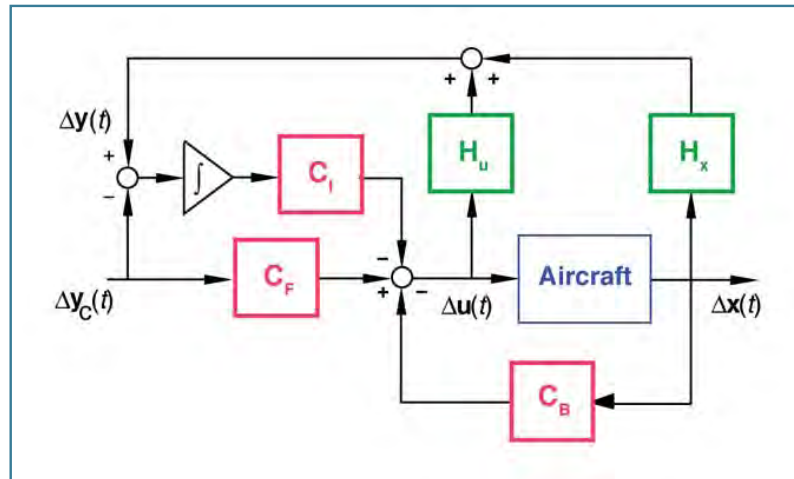


# Typical Flight Paths in Wind Rotor Encounter

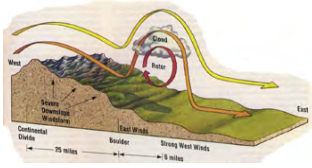
■ from *Spilman*



# Linear-Quadratic/Proportional-Integral Filter (LQ/PIF) Regulator



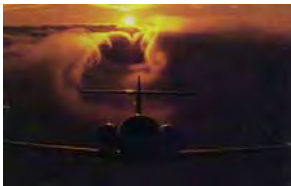
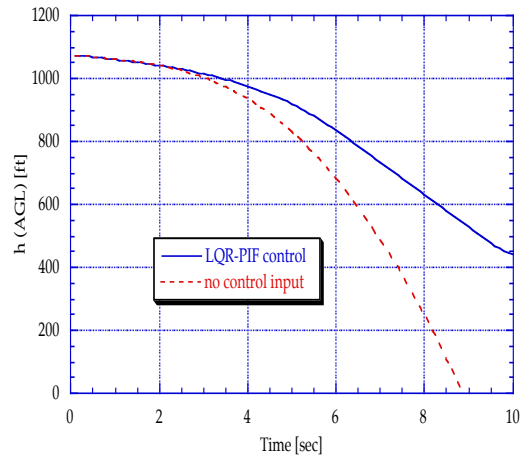
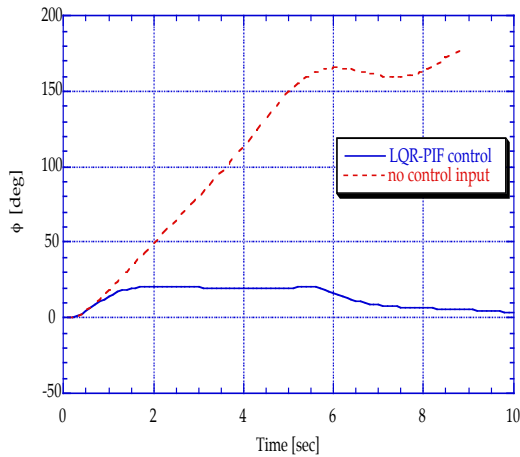




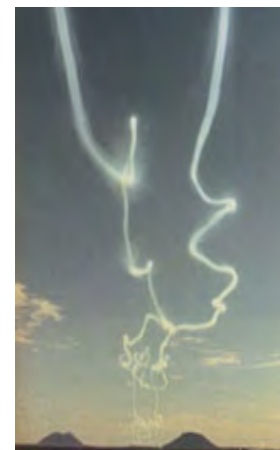
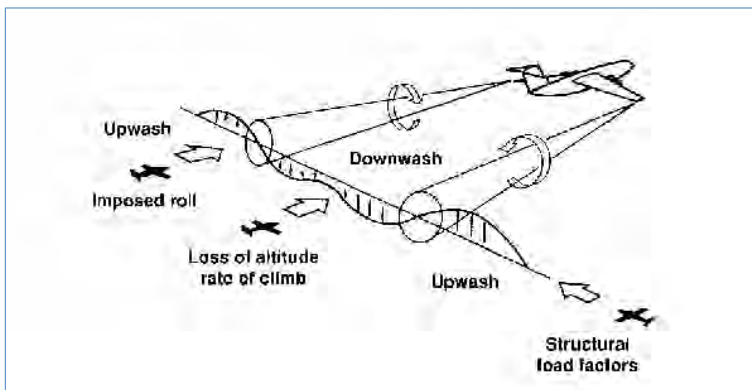
# LQ/PIF Regulation of Wind Rotor Encounter



■ from *Spilman*



# Wake Vortices



C-5A Wing Tip Vortex Flight Test

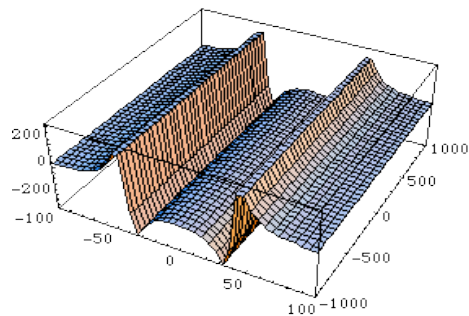
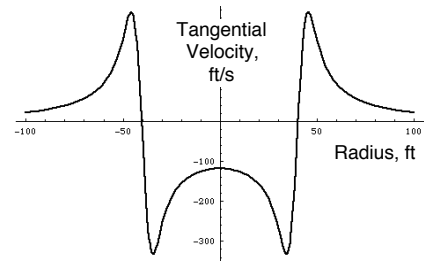
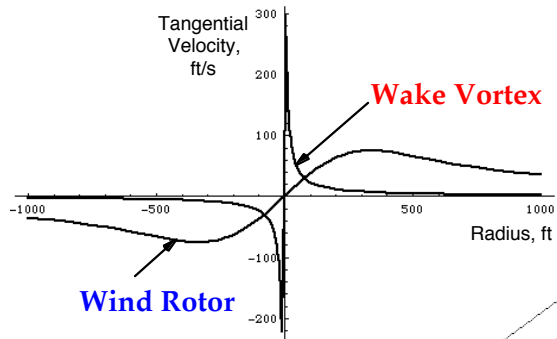
<http://www.dfrc.nasa.gov/gallery/movie/C-5A/480x/EM-0085-01.mov>

L-1011 Wing Tip Vortex Flight Test

<http://www.dfrc.nasa.gov/gallery/movie/L-1011/480x/EM-0085-01.mov>



# Models of Single and Dual Wake Vortices



## Wake Vortex Descent and Downwash

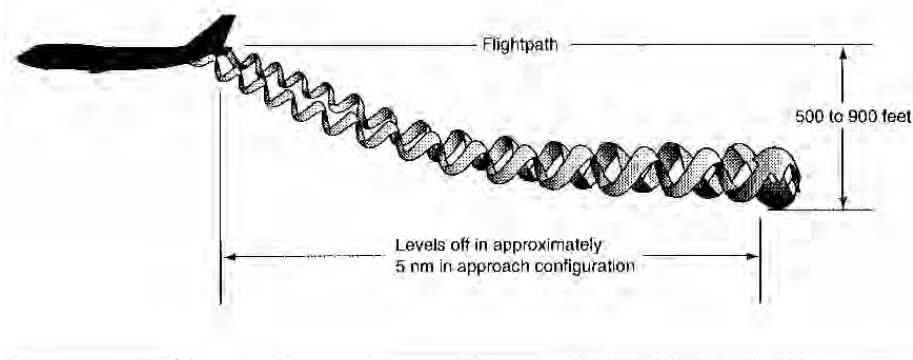




# Wake Vortex Descent and Effect of Crosswind



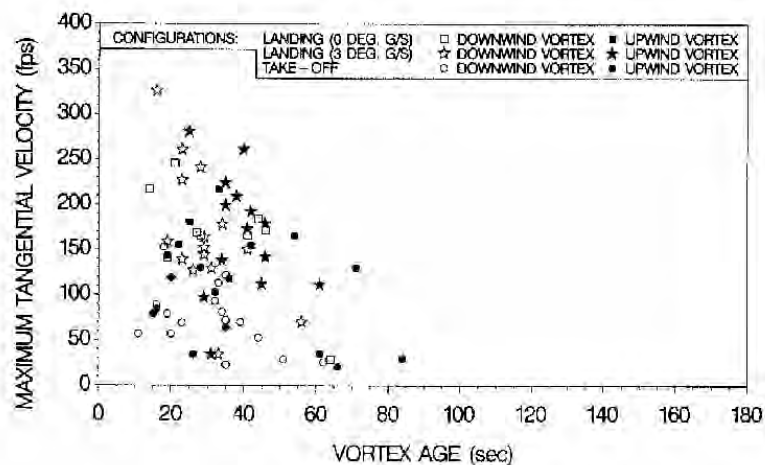
- from *FAA Wake Turbulence Training Aid, 1995*



## Magnitude and Decay of B-757 Wake Vortex



- from *Richard Page et al*, FAA Technical Center



# NTSB Simulation of US Air 427 and FAA Wake Vortex Flight Test



USAir Flight 427  
Aliquippa, PA  
September 8, 1994  
Boeing 737-300



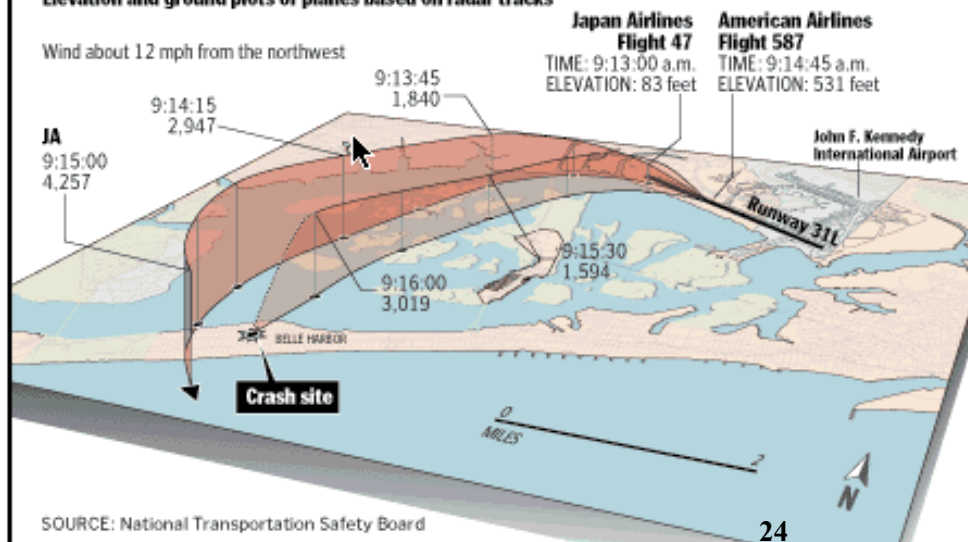
- B-737 behind B-727 in FAA flight test
- Control actions subsequent to wake vortex encounter may be problematical
- US427 rudder known to be hard-over from DFDR

## Flying Into the Wake

Preliminary readings from American Airlines Flight 587's data recorder show that the Airbus A300 twice ran into turbulence. After the second blast, the plane careened sideways seconds before it crashed. The turbulence apparently was caused by the wake of a Japan Airlines 747 flying ahead and above. Wake turbulence can last for minutes as it slowly drops and moves with prevailing winds.

### Elevation and ground plots of planes based on radar tracks

Wind about 12 mph from the northwest



BY RICHARD FURNO—THE WASHINGTON POST

# NTSB Simulation of American Flight 587

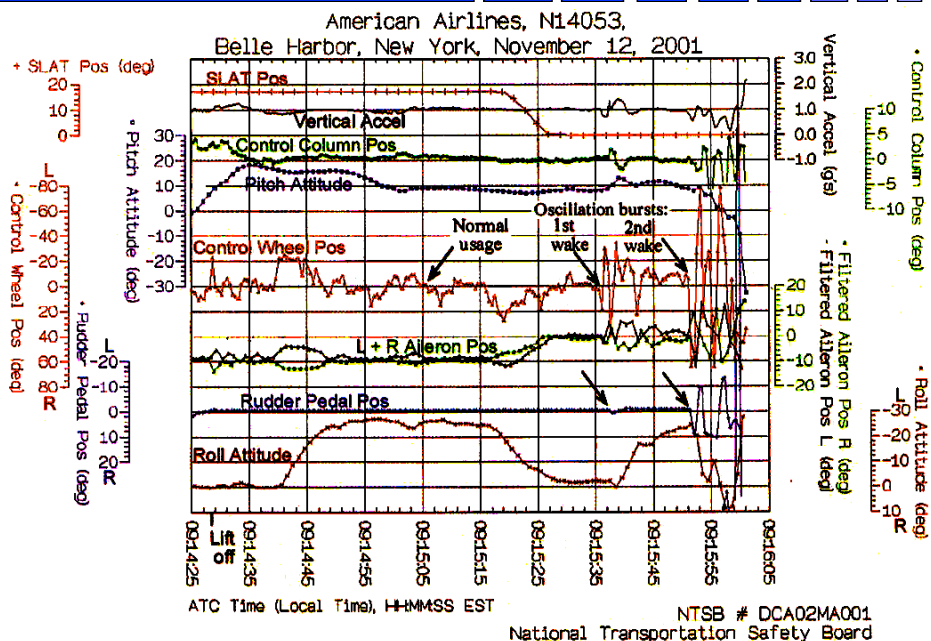
- Flight simulation derived from digital flight data recorder (DFDR) tape



25



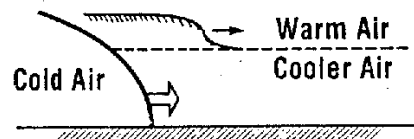
## Digital Flight Data Recorder Data for American 587



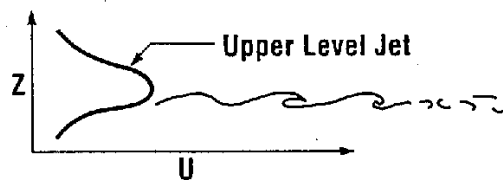


# Causes of Clear Air Turbulence

- from *Bedard*



(C) HYDRAULIC JUMP

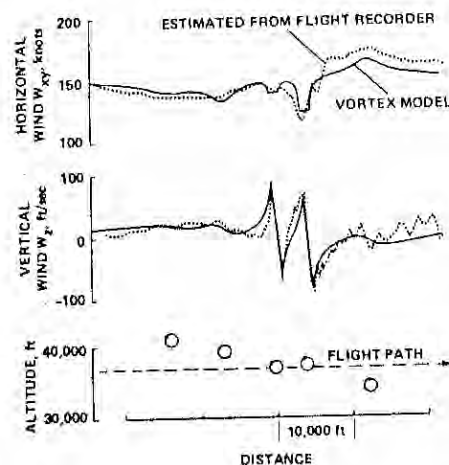
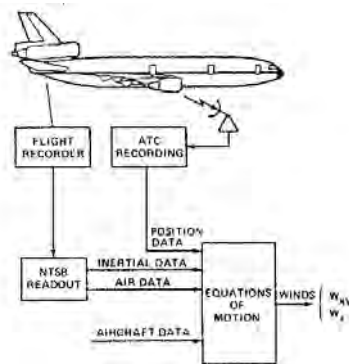


(D) GRAVITY-SHEAR WAVES



## DC-10 Encounter with Vortex-Induced Clear Air Turbulence

- from *Parks, Bach, Wingrove, and Mehta*



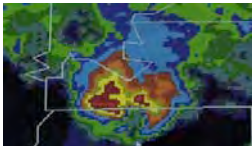
# DC-8 and B-52H Encounters with Clear Air Turbulence



- DC-8: **One engine and 12 ft of wing missing** after CAT encounter over Rockies
- B-52 specially instrumented for air turbulence research after some operational B-52s were lost
- **Vertical tail lost** after a severe and sustained burst (+5 sec) of clear air turbulence violently buffeted the aircraft
- The Boeing test crew flew aircraft to Blytheville AFB, Arkansas and landed safely



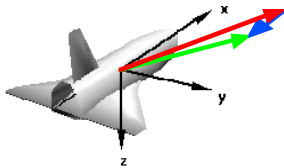
Boeing B-52H 'Stratofortress'  
©USAF Museum Photo Archives



## Conclusions

- Critical role of decision-making, alerting, and intelligence
- Reliance on human factors and counter-intuitive strategies
- Need to review certification procedures
- Opportunity to reduce hazard through flight control system design
  - Disturbance rejection
  - Failure Accommodation
- Importance of **Eternal vigilance**

# Supplemental Material



## Alternative Reference Frames for Translational Dynamics

- Earth-relative velocity in earth-fixed polar coordinates:
- Earth-relative velocity in aircraft-fixed polar coordinates (**zero wind**):
- Body-frame **air-mass-relative velocity**:
- Airspeed, sideslip angle, angle of attack**

$$\mathbf{v}_E = \begin{bmatrix} V_E \\ \gamma \\ \xi \end{bmatrix}$$

$$\mathbf{v}_E = \begin{bmatrix} V_E \\ \beta_E \\ \alpha_E \end{bmatrix}$$

$$\mathbf{v}_A = \begin{bmatrix} (u - u_w) \\ (v - v_w) \\ (w - w_w) \end{bmatrix} = \begin{bmatrix} u_A \\ v_A \\ w_A \end{bmatrix}$$

$$\begin{bmatrix} V_A \\ \beta_A \\ \alpha_A \end{bmatrix} = \begin{bmatrix} \sqrt{u_A^2 + v_A^2 + w_A^2} \\ \sin^{-1}(v_A / V_A) \\ \tan^{-1}(w_A / V_A) \end{bmatrix}$$

# Rigid-Body Equations of Motion

- Rate of change of Translational Position

$$\dot{\mathbf{r}}_I = \mathbf{H}_B^I \mathbf{v}_B$$

- Rate of change of Angular Position

$$\dot{\boldsymbol{\Theta}} = \mathbf{L}_B^I \boldsymbol{\omega}_B$$

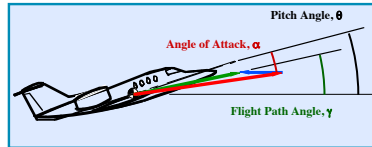
- Aerodynamic forces and moments depend on air-relative velocity vector, not the earth-relative velocity vector

- Rate of change of Translational Velocity

$$\dot{\mathbf{v}}_B = \frac{1}{m} \mathbf{F}_B(\mathbf{v}_A) + \mathbf{H}_I^B \mathbf{g}_I - \tilde{\boldsymbol{\omega}}_B \mathbf{v}_B$$

- Rate of change of Angular Velocity

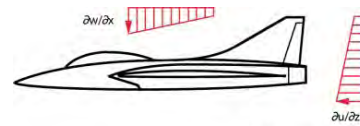
$$\dot{\boldsymbol{\omega}}_B = \mathbf{I}_B^{-1} [\mathbf{M}_B(\mathbf{v}_A) - \tilde{\boldsymbol{\omega}}_B \mathbf{I}_B \boldsymbol{\omega}_B]$$



## Wind Shear Distributions Exert Moments on Aircraft Through Damping Derivatives

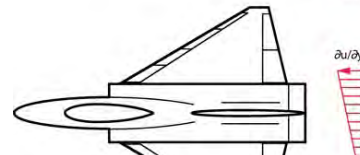
- 3-dimensional wind field changes in space and time

$$\mathbf{w}_E(\mathbf{x}, t) = \begin{bmatrix} w_x(x, y, z, t) \\ w_y(x, y, z, t) \\ w_z(x, y, z, t) \end{bmatrix}_E$$



- Gradient of wind produces different relative airspeeds over the surface of an aircraft

$$\mathbf{W}_E = \begin{bmatrix} \partial w_x / \partial x & \partial w_x / \partial y & \partial w_x / \partial z \\ \partial w_y / \partial x & \partial w_y / \partial y & \partial w_y / \partial z \\ \partial w_z / \partial x & \partial w_z / \partial y & \partial w_z / \partial z \end{bmatrix}$$



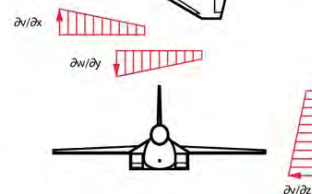
- Wind gradient expressed in body axes

$$\mathbf{W}_B = \mathbf{H}_E^B \mathbf{W}_E \mathbf{H}_B^E$$

$$\Delta C_{l_{shear}} \approx C_{l_{p_{wing}}} \frac{\partial w}{\partial y} - C_{l_{p_{fin}}} \frac{\partial v}{\partial x}$$

$$\Delta C_{m_{shear}} \approx C_{m_{q_{wing, body, stab}}} \frac{\partial w}{\partial x}$$

$$\Delta C_{n_{shear}} \approx C_{n_{r_{fin, body}}} \frac{\partial v}{\partial x}$$



# Aircraft Modes of Motion



- **Longitudinal Motions**

$$\Delta_{Lon}(s) = \left( s^2 + 2\zeta\omega_n s + \omega_n^2 \right)_{Ph} \left( s^2 + 2\zeta\omega_n s + \omega_n^2 \right)_{SP}$$

- **Lateral-Directional Motions**

$$\Delta_{LD}(s) = (s - \lambda_S)(s - \lambda_R) \left( s^2 + 2\zeta\omega_n s + \omega_n^2 \right)_{DR}$$

- **Wind inputs that resonate with modes of motion are especially hazardous**

**Natural frequency :**  $\omega_n, rad / s$

**Natural Period :**  $T_n = \frac{2\pi}{\omega_n}, sec$

**Natural Wavelength :**  $L_n = V_N T_p, m$

# Nonlinear-Inverse-Dynamic Control



- **Nonlinear system** with additive control:

$$\dot{\mathbf{x}}(t) = \mathbf{f}[\mathbf{x}(t)] + \mathbf{G}[\mathbf{x}(t)]\mathbf{u}(t)$$

- **Output vector:**

$$\mathbf{y}(t) = \mathbf{h}[\mathbf{x}(t)]$$

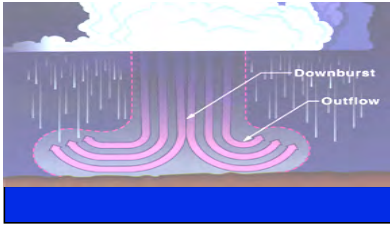
- **Differentiate output until control appears in each element of the derivative output:**

$$\mathbf{y}^{(d)}(t) = \mathbf{f}^*[\mathbf{x}(t)] + \mathbf{G}^*[\mathbf{x}(t)]\mathbf{u}(t) \triangleq \mathbf{v}(t)$$

- **Inverting control law:**

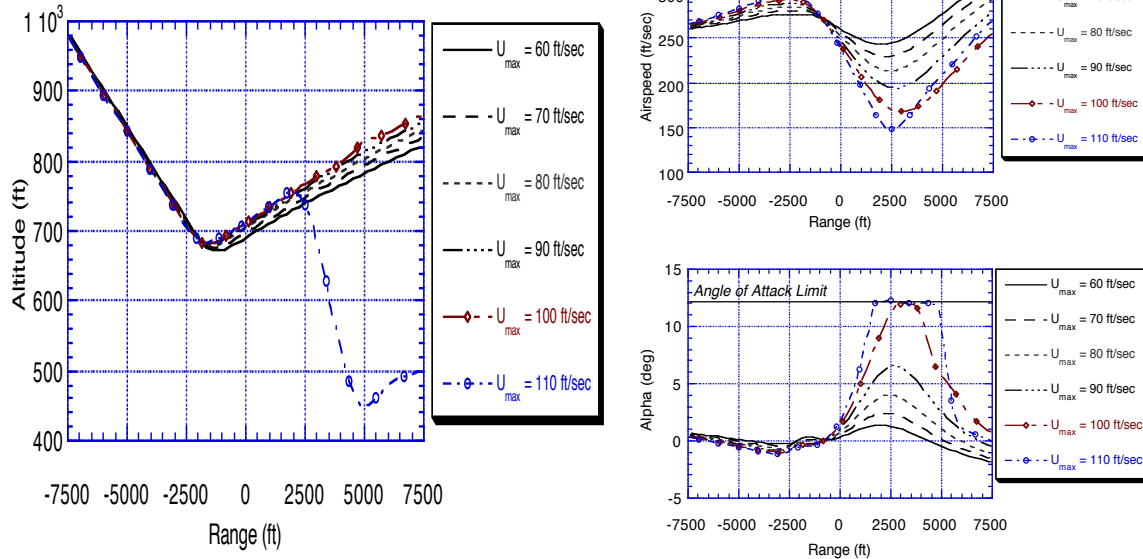
$$\mathbf{u}(t) = \mathbf{G}^*[\mathbf{x}(t)] [\mathbf{v}_{command} - \mathbf{f}^*[\mathbf{x}(t)]]$$





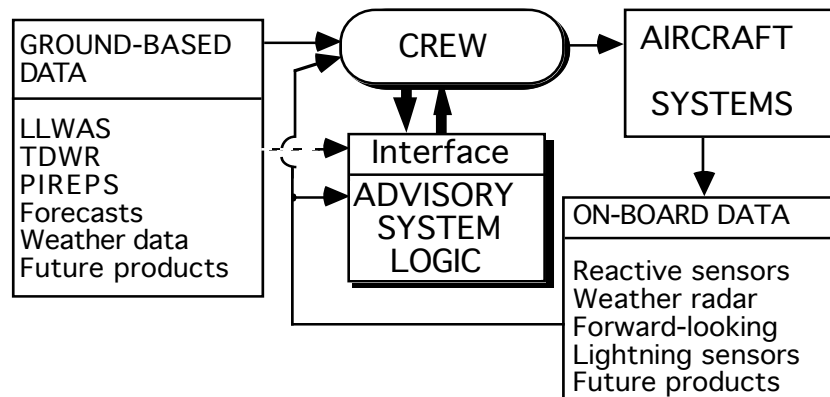
## Landing Abort using Nonlinear-Inverse-Dynamic Control

### from Mulgund



## Wind Shear Safety Advisor

- Graduate research of *Alexander Stratton*
- LISP-based expert system*

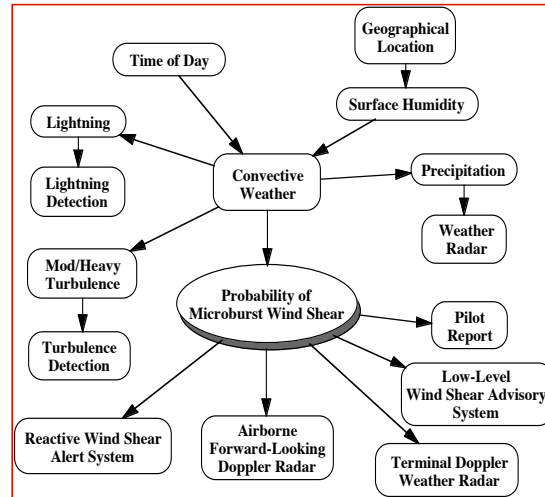


# Estimating the Probability of Hazardous Microburst Encounter

## Bayesian Belief Network

### Infer probability of hazardous encounter from

- pilot/control tower reports
- measurements
- location
- time of day



## Aircraft as Wake Vortex Generators and Receivers

- **Vorticity,  $\Gamma$** , generated by lift in **1-g** flight

$$\Gamma = \frac{K_{generator} W}{\rho V_N b}$$

$$K_{generator} \approx \frac{4}{\pi}$$

- Rolling acceleration **response to vortex** aligned with the aircraft's longitudinal axis

$$\dot{p} = \frac{K_{receiver} \frac{1}{2} \rho V_N^2 S b}{I_{xx}} \Gamma$$

$$K_{receiver} \approx \frac{C_{L_a}}{2\pi V_N b}$$

# Rolling Response vs. Vortex-Generating Strength for 125 Aircraft



- Undergraduate summer project of *James Nichols*

