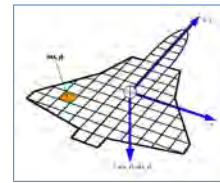
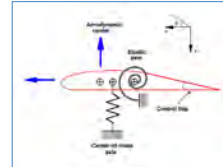


# Aeroelasticity and Fuel Slosh

Robert Stengel, Aircraft Flight Dynamics  
MAE 331, 2014

- Aerodynamic effects of bending and torsion
- Modifications to aerodynamic coefficients
- Dynamic coupling
- Fuel shift and sloshing dynamics



*Flight Dynamics*  
418-419, 549-569, 665-678  
*Airplane Stability and Control*  
Chapter 19

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<http://www.princeton.edu/~stengel/MAE331.html>  
<http://www.princeton.edu/~stengel/FlightDynamics.html>

1

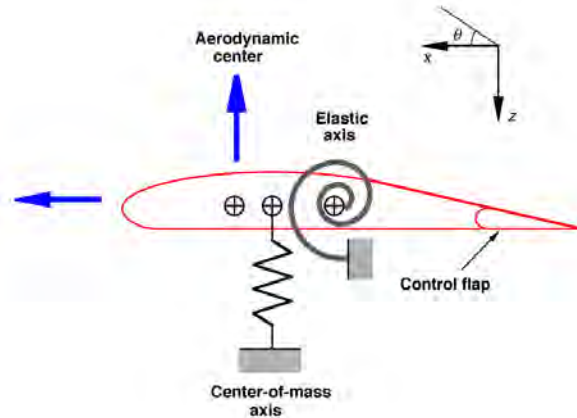
## *The Elastic Airplane*

### Chapter 19, *Airplane Stability and Control*, Abzug and Larrabee

- What are the principal subject and scope of the chapter?
- What technical ideas are needed to understand the chapter?
- During what time period did the events covered in the chapter take place?
- What are the three main "takeaway" points or conclusions from the reading?
- What are the three most surprising or remarkable facts that you found in the reading?

2

# One-Dimensional Model of Aeroelasticity

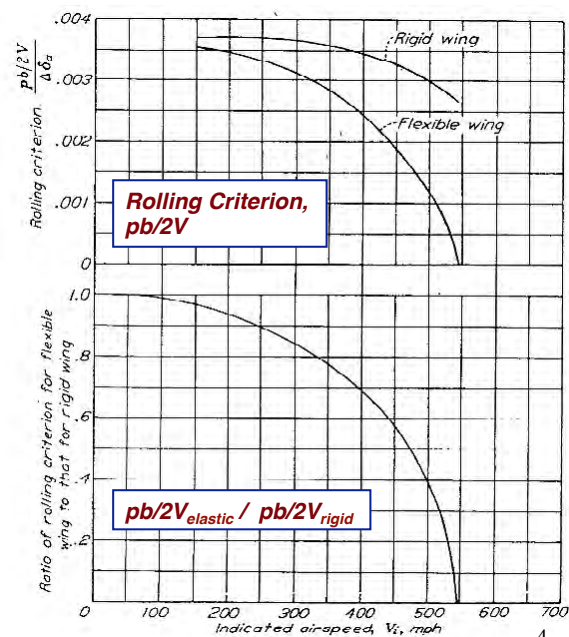


3



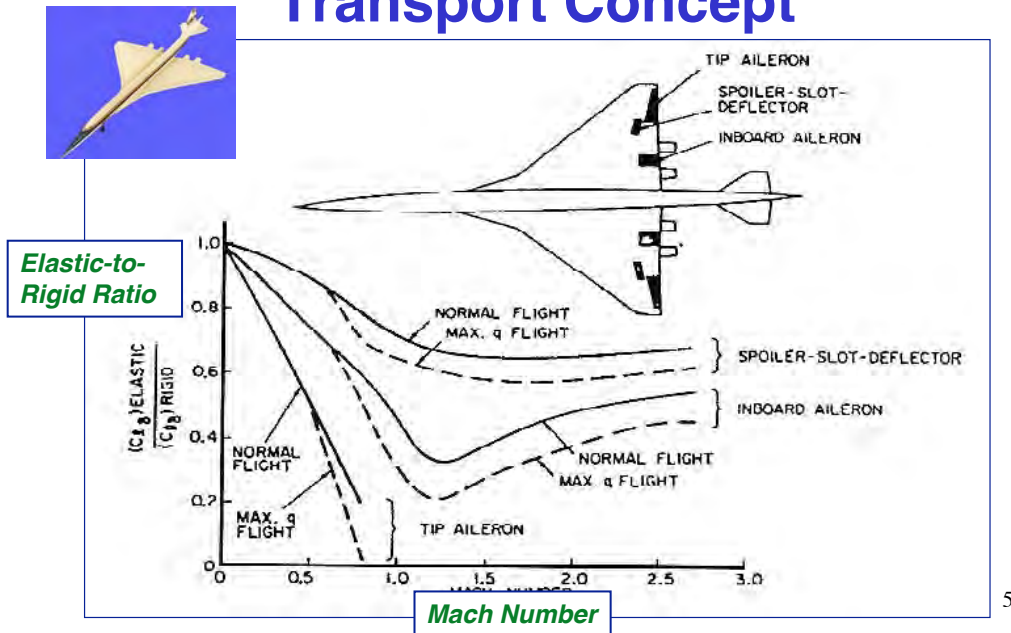
## Reduced Aileron Effect Due to Aeroelasticity

- Wing torsion reduces aileron effect with increasing dynamic pressure



4

# Aeroelastic Aileron Effect of Boeing 2707-300 Supersonic Transport Concept



Elastic-to-Rigid Ratio

Mach Number

5

## Quasi-Static Aeroelastic Model of Aircraft Dynamics: Residualization

- IF elastic modes are fast compared to rigid modes and are stable

$$\begin{bmatrix} \Delta \dot{\mathbf{x}}_{\text{aircraft}} \\ \mathbf{0} \end{bmatrix} \approx \begin{bmatrix} \mathbf{F}_{\text{aircraft}} & \mathbf{F}_{\text{elastic}}^{\text{aircraft}} \\ \mathbf{F}_{\text{aircraft}}^{\text{elastic}} & \mathbf{F}_{\text{elastic}} \end{bmatrix} \begin{bmatrix} \Delta \mathbf{x}_{\text{aircraft}} \\ \Delta \mathbf{x}_{\text{elastic}} \end{bmatrix} + \begin{bmatrix} \mathbf{G}_{\text{aircraft}} \\ \mathbf{G}_{\text{elastic}} \end{bmatrix} \Delta \mathbf{u}_{\text{aircraft}}$$

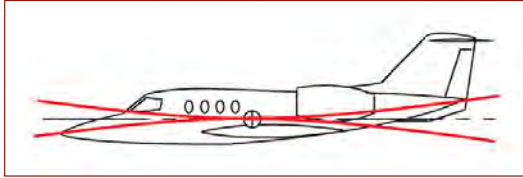
- Residualization reduces aeroelastic model order to rigid-body model order

$$\begin{aligned} \Delta \dot{\mathbf{x}}_a &= \mathbf{F}_a \Delta \mathbf{x}_a - \mathbf{F}_e^a \mathbf{F}_e^{-1} [\mathbf{F}_e^e \Delta \mathbf{x}_a + \mathbf{G}_e \Delta \mathbf{u}_a] + \mathbf{G}_a \Delta \mathbf{u}_a \\ &= \mathbf{F}'_a \Delta \mathbf{x}_a + \mathbf{G}'_a \Delta \mathbf{u}_a \end{aligned}$$

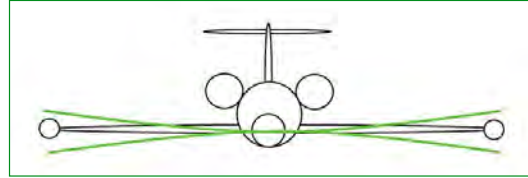
6

# Primary Longitudinal Aeroelastic Mode Shapes

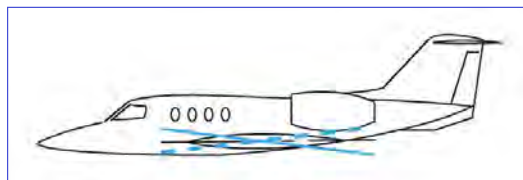
**Fuselage Bending**



**Wing Bending**



**Wing Torsion**



7

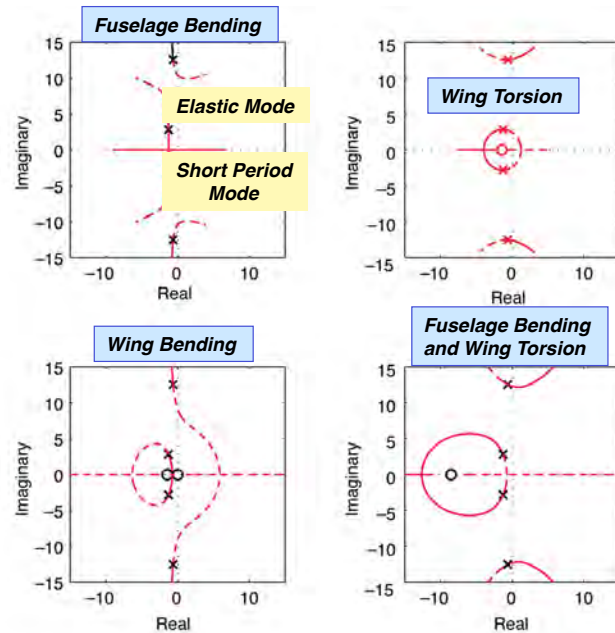
## Aeroelastic Model of Aircraft Dynamics

- Coupled model of rigid-body and elastic dynamics

$$\begin{bmatrix} \Delta \dot{\mathbf{x}}_{\text{aircraft}} \\ \Delta \dot{\mathbf{x}}_{\text{elastic}} \end{bmatrix} = \begin{bmatrix} \mathbf{F}_{\text{aircraft}} & \mathbf{F}_{\text{aircraft}}^{\text{elastic}} \\ \mathbf{F}_{\text{aircraft}}^{\text{elastic}} & \mathbf{F}_{\text{elastic}} \end{bmatrix} \begin{bmatrix} \Delta \mathbf{x}_{\text{aircraft}} \\ \Delta \mathbf{x}_{\text{elastic}} \end{bmatrix} + \begin{bmatrix} \mathbf{G}_{\text{aircraft}} \\ \mathbf{G}_{\text{elastic}} \end{bmatrix} \Delta \mathbf{u}_{\text{aircraft}}$$

8

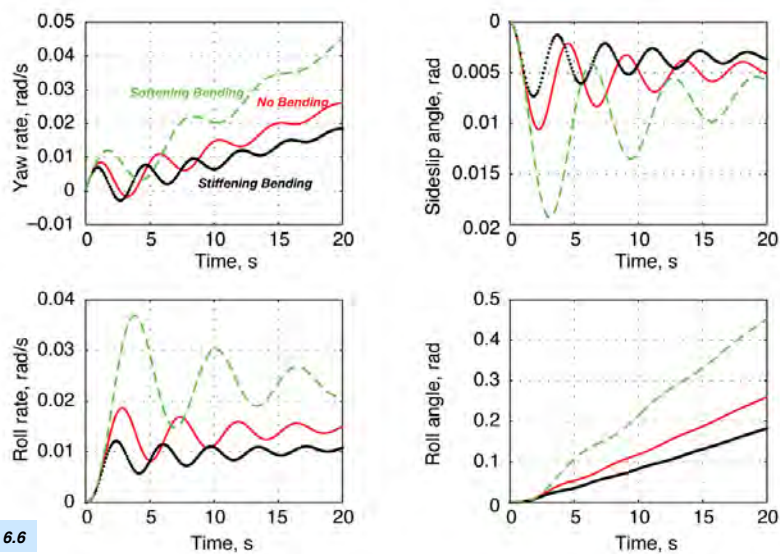
## Effect of Increasing Coupling of Single Aeroelastic Mode with Short Period Roots



Flight Dynamics, 5.6

9

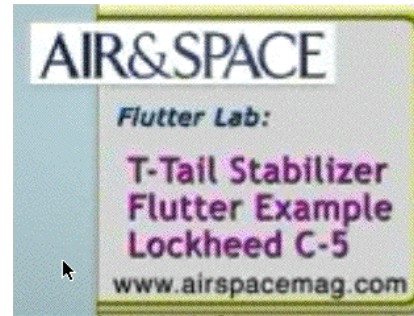
## Effects of Fuselage Aeroelasticity on Lateral-Directional Response to Rudder Step Input



Flight Dynamics, 6.6

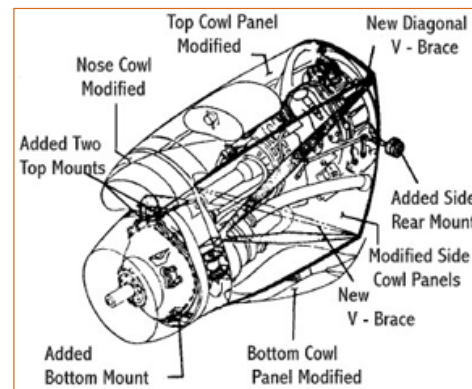
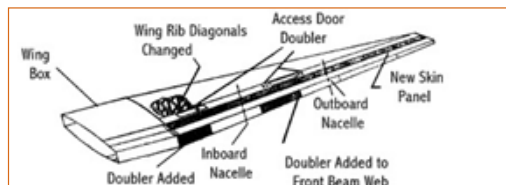
10

# Aeroelastic Oscillations



## Aeroelastic Problems of the Lockheed Electra

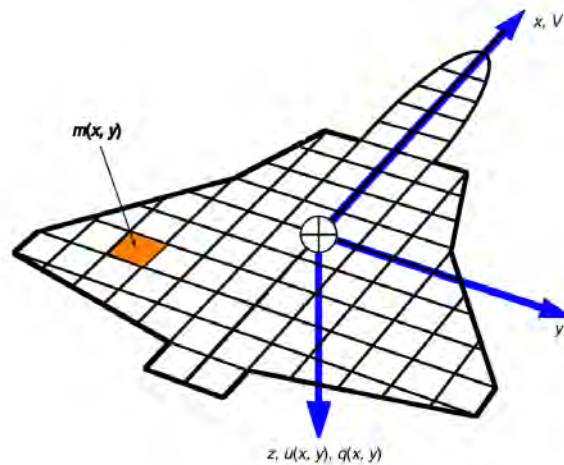
- **Prop-whirl flutter**, 2 fatal accidents (1959-60)
- Structural modifications made; aircraft remained in service until 1992
- Predecessor of *US Navy Orion P-3*, still in service



<http://www.youtube.com/watch?v=d0fFNWANK5M>



# Two-Dimensional Model of Aeroelastic Airplane

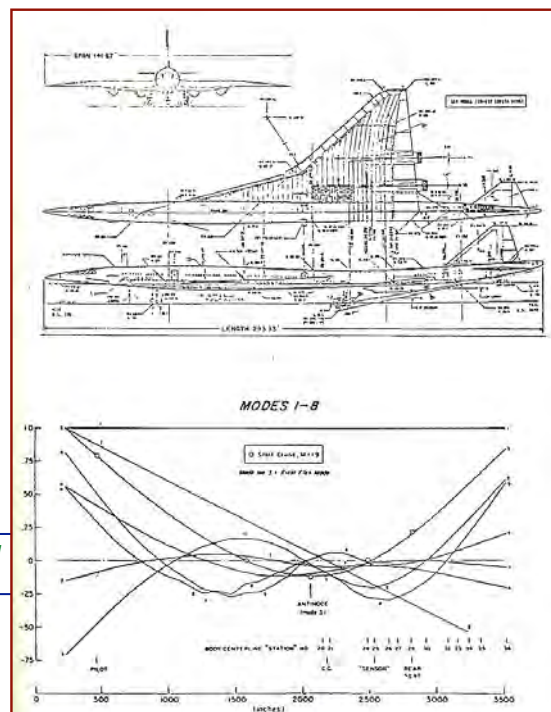


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## Longitudinal Structural Modes of Boeing 2707-300 Supersonic Transport Concept



Normalized Deflection



Centerline station

14

# B-1 Canards for Ride Control

- Elastic modes cause severe, high-*g* cockpit vibration during low-altitude, high-speed flight
- Active canard surfaces reduce amplitude of the oscillations



15

# Ultra-Light Aircraft

- Extreme aeroelasticity
- *AeroVironment Pathfinder, Centurion, PathfinderPlus* (solar-electric)
- *Helios* in turbulence

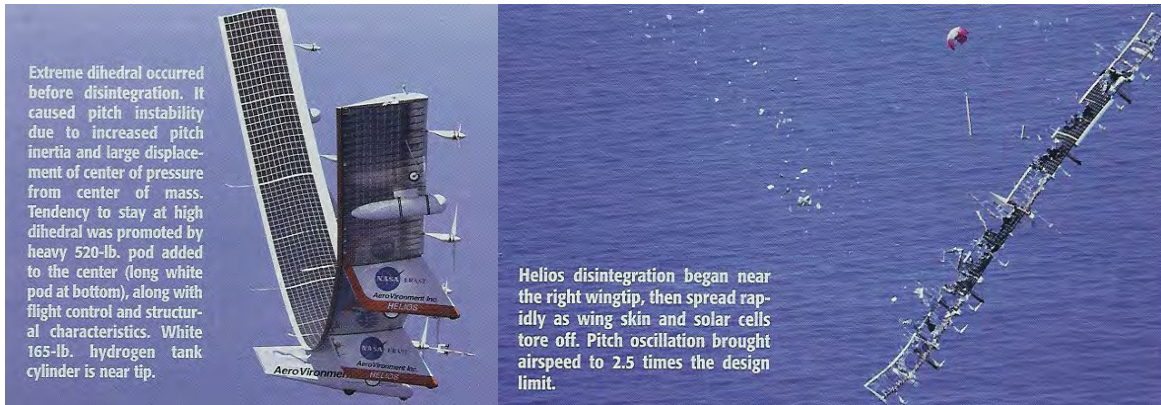


16



## The Last Flight of *Helios*

- **June 6, 2003**
- 2,320 lb., 247-ft wingspan, 72 control surfaces, differential thrust
- Change in weight distribution
- 40-ft tip deflection
- **Divergent pitch oscillations**, doubling every 8 seconds
- **Airspeed > 2.5 x limit**



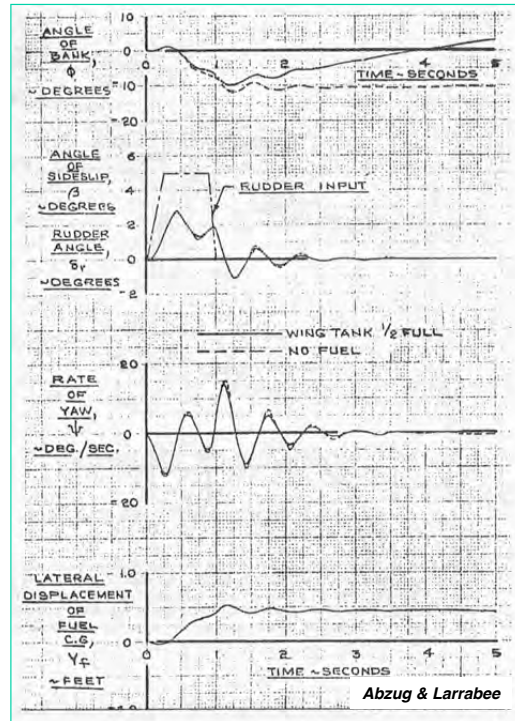
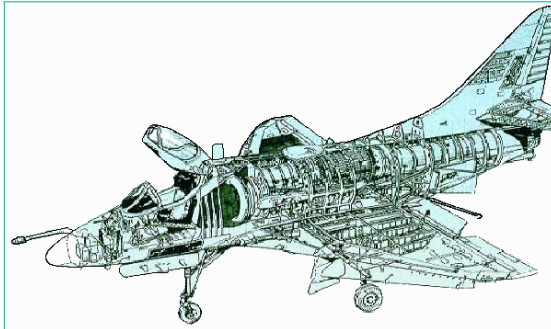
17

## *Fuel Shift and Slosh*

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# Fuel Shift

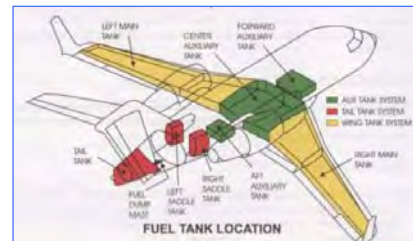
- Problem with *partially filled fuel tank*
- Single wing tank from tip to tip (*A4D*)
- Slow, *quasi-static* shift of fuel c. m.
- *Rudder step* throws fuel to one side, producing a strong rolling moment



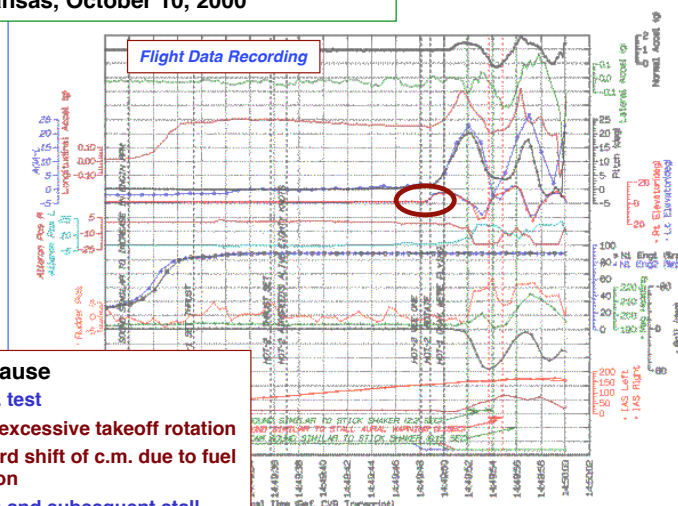
19

# Fuel Shift

- NTSB/AAB-04/01
- Loss of Control and Impact with Terrain,
- Canadair Challenger CL-604 Flight Test Airplane, C-FTBZ,
- Wichita, Kansas, October 10, 2000



Angle of Attack



Normal Acceleration

Pitch Angle

Elevator Angle

IAS

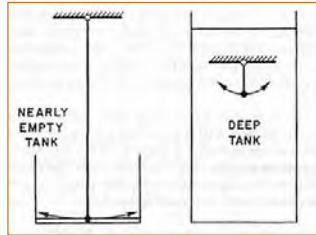
Altitude

- Probable Cause
  - Aft c.m. test
  - Pilot's excessive takeoff rotation
  - Rearward shift of c.m. due to fuel migration
  - Pitchup and subsequent stall
  - Inadequate test planning

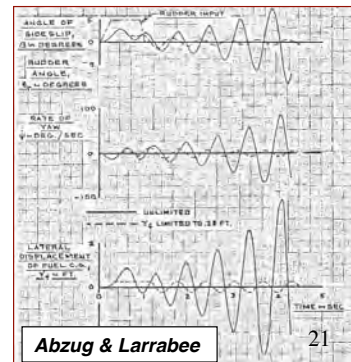
<http://www.nts.gov/investigations/fulltext/aab040120ml>

# Fuel Slosh

- **Dynamic oscillation** of fuel center of mass, wave motion at the fuel's surface
- Pendulum and spherical-tank analogies
- **Problem is greatest when tank is half-full**
- **Fore-aft slosh in wing-tip tanks coupled with the *short period mode* (P-80)**

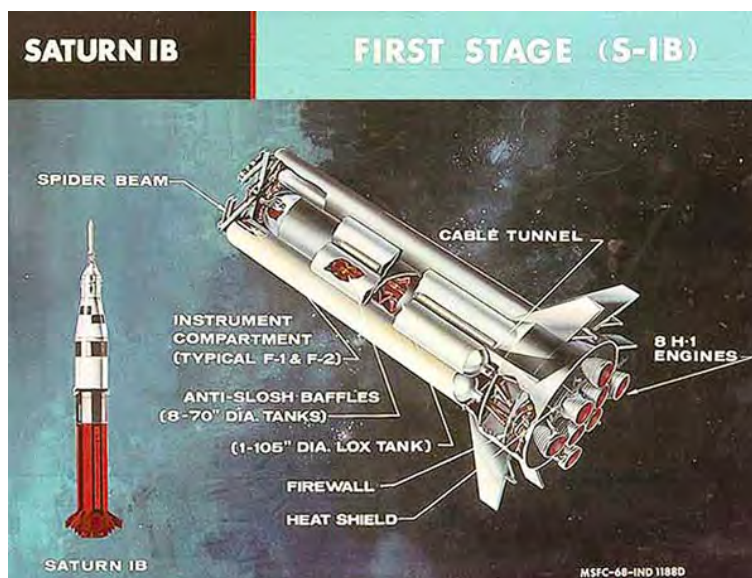


- **Fuselage tank forward of the aircraft's center of mass (A4D)**
  - Yawing motion excites oscillatory slosh that couples with *Dutch roll mode*



# Fuel Slosh

- **Solution: Fuel-tank baffles**
  - Slow down fuel motion
  - Force resonances to higher frequencies due to smaller cavities
  - Wing internal bracing may act as baffle





# Problems of Fuel Slosh and Aeroelasticity



- **Coupling of non-rigid dynamic modes with rigid-body modes**
- **Resonant response**
  - Dynamically coupled modes of motion with similar frequencies
  - With light damping, oscillatory amplitudes may become large

$$\begin{bmatrix} \Delta \dot{\mathbf{x}}_{\text{aircraft}} \\ \Delta \dot{\mathbf{x}}_{\text{elastic}} \\ \Delta \dot{\mathbf{x}}_{\text{slosh}} \end{bmatrix} = \begin{bmatrix} \mathbf{F}_{\text{aircraft}} & \mathbf{F}_{\text{aircraft elastic}} & \mathbf{F}_{\text{aircraft slosh}} \\ \mathbf{F}_{\text{elastic aircraft}} & \mathbf{F}_{\text{elastic}} & \mathbf{F}_{\text{elastic slosh}} \\ \mathbf{F}_{\text{slosh aircraft}} & \mathbf{F}_{\text{slosh elastic}} & \mathbf{F}_{\text{slosh}} \end{bmatrix} \begin{bmatrix} \Delta \mathbf{x}_{\text{aircraft}} \\ \Delta \mathbf{x}_{\text{elastic}} \\ \Delta \mathbf{x}_{\text{slosh}} \end{bmatrix} + \mathbf{G} \Delta \mathbf{u}$$

- **Coupling between longitudinal and lateral-directional effects**
- **Nonlinear aerodynamics**
- **Exacerbated by floating control surfaces, high hinge moments, and high aerodynamic angles**

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*Next Time:  
High Speed and Altitude*

**Flight Dynamics**  
470–480  
**Airplane Stability and Control**  
Chapter 11

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