# STAT 443: Assignment 1

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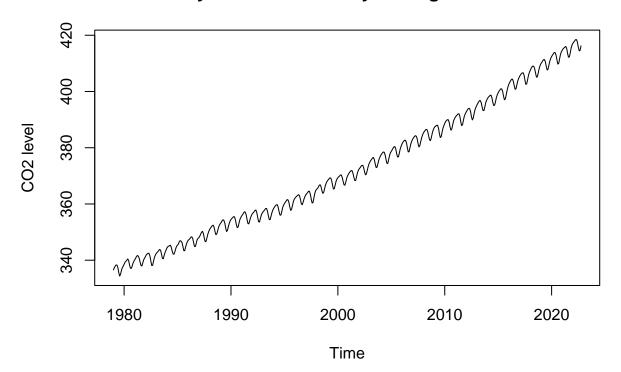
2 Februray, 2022

#### Question 1

a)

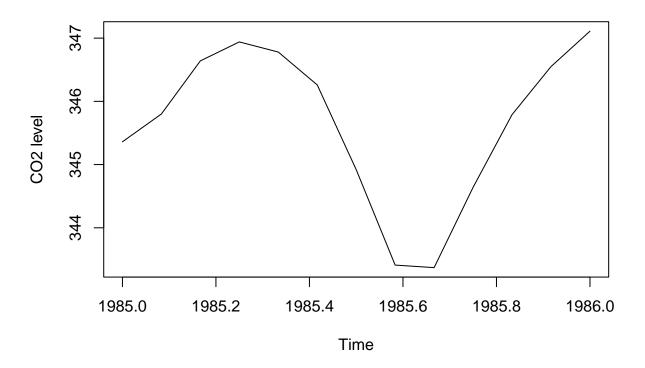
```
co2 <- read.csv("co2_mm_gl.csv", header = TRUE, skip = 55)
co2_ts <- ts(co2[,4], start = c(1979,1), frequency = 12)
plot(co2_ts,
    main = "Monthly Means of Globally Averaged CO2 Level",
    ylab = "CO2 level")</pre>
```

### **Monthly Means of Globally Averaged CO2 Level**



```
plot(window(co2_ts, start = c(1985,1),end = c(1986,1)),
    main = "CO2 Level Variation Within 12 Months",
    ylab = "CO2 level")
```

#### **CO2 Level Variation Within 12 Months**

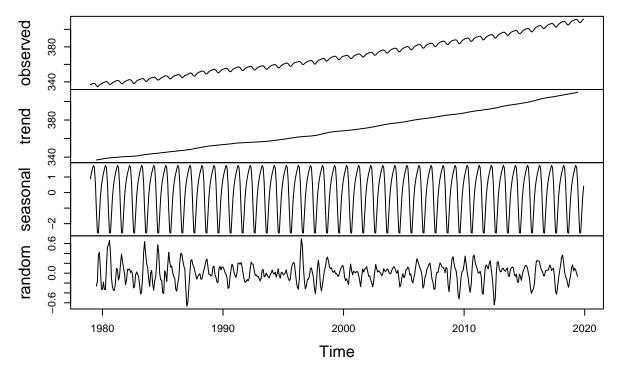


- i) The above time series have a clear **upward trend** such that the monthly means of globally averaged CO2 level is increasing every year despite some variations.
- ii) There appears to be **seasonal variations** in the monthly CO2 level as when we restrict the plot to display the average CO2 level over a 12-month period, we can clear see the CO2 level is high around March and December, low around June. **An additive model is more suitable** as we can see the seasonal effect remains constant over time and the error is also constant over time, therefore an additive model would be more appropriate than a multiplicative model.
- iii) No, the series have a clear upward increasing trend therefore it is not stationary.

b)

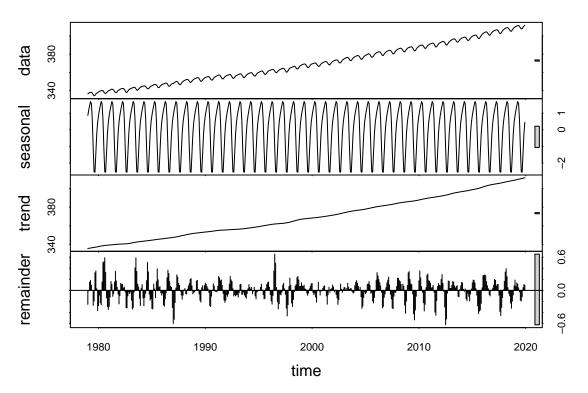
```
co2_train <- window(co2_ts,start = c(1979,1),end = c(2019,12),frequency = 12)
co2_test <- window(co2_ts, start = c(2020,1), end = c(2022,10), frequency = 12)
co2_train_decom <- decompose(co2_train, type = "additive")
plot(co2_train_decom)</pre>
```

# **Decomposition of additive time series**



```
co2_train_loess <- stl(co2_train,s.window = "periodic")
plot(co2_train_loess,
    main = "Decomposition of an Additive Time Series via Loess Smoothing")</pre>
```

### Decomposition of an Additive Time Series via Loess Smoothing



c)

```
# MA method
ma_trend <- co2_train_decom$trend</pre>
ma_seas <- co2_train_decom$seasonal</pre>
ma_error <- co2_train_decom$random</pre>
# Loess smoothing
loess_trend <- co2_train_loess$time.series[,"trend"]</pre>
loess_seas <- co2_train_loess$time.series[,"seasonal"]</pre>
loess_error <- co2_train_loess$time.series[,"remainder"]</pre>
# creating data frame
lm_data <- data.frame(ma_trend = ma_trend,</pre>
                      loess_trend = loess_trend,
                      time = c(1:length(co2_train)))
# Fitted Models
lm_ma <- lm(ma_trend~time, data = lm_data)</pre>
lm_loess <- lm(loess_trend~time, data = lm_data)</pre>
summary(lm ma)
##
## Call:
## lm(formula = ma_trend ~ time, data = lm_data)
## Residuals:
##
                1Q Median
       Min
                                 3Q
                                        Max
## -2.9933 -1.6701 -0.3312 1.2281 4.7441
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.329e+02 1.819e-01 1830.0 <2e-16 ***
## time
              1.488e-01 6.433e-04
                                      231.3
                                               <2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.953 on 478 degrees of freedom
     (12 observations deleted due to missingness)
## Multiple R-squared: 0.9911, Adjusted R-squared: 0.9911
## F-statistic: 5.349e+04 on 1 and 478 DF, p-value: < 2.2e-16
summary(lm_loess)
##
## Call:
## lm(formula = loess_trend ~ time, data = lm_data)
## Residuals:
##
                1Q Median
       Min
                                 3Q
                                        Max
## -3.0771 -1.7471 -0.3894 1.2344 4.9349
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.329e+02 1.832e-01 1817.6 <2e-16 ***
              1.491e-01 6.439e-04
## time
                                     231.5 <2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.028 on 490 degrees of freedom
## Multiple R-squared: 0.9909, Adjusted R-squared: 0.9909
## F-statistic: 5.361e+04 on 1 and 490 DF, p-value: < 2.2e-16</pre>
```

i) Fitted model using MA method:

```
\hat{m}_t = 0.03329 + 0.1488 * t
```

Fitted model using loess smoothing method:

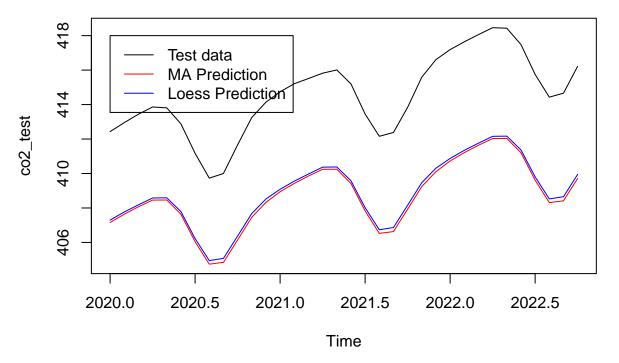
$$\hat{m_t} = 0.03329 + 0.1491 * t$$

- ii) The trend component is significant at 95% confidence level under both method.
- iii) I think the trend component is a good predictor because the trend is linear over the entire time range of the time series data looking at the trend component plot in part b); second, from the output of the linear models we observe that  $R^2 > 0.99$ f ro both models. This indicates that majority of the variation within the time series is explained by the trend component.

iv)

## Warning in ma\_trend\_pred + seasonals\$shat\_ma: longer object length is not a
## multiple of shorter object length

## Warning in loess\_trend\_pred + seasonals\$shat\_loess: longer object length is not
## a multiple of shorter object length



```
## # A tibble: 1 x 2
## mspe_ma mspe_loess
## <dbl> <dbl>
## 1 34.1 32.1
```

Looking at the above table, the loess smoothing method result in lower MSPE on the test data. Therefore I would recommend to use the prediction model from the loess smoothing decomposition.