## STAT 443: Time Series and Forecasting Lab 5: Model Fitting and AR processes

- The lab must be completed in R Markdown. Display all the R code used to perform your analysis.
- Create a **pdf** or **html** file and use it as your lab submission.
- Please ensure that the file you submit is in good order (e.g., not corrupted and contains the work you intend to submit). No late (re-)submissions will be accepted.

Given a time series, we can fit possible ARIMA models in R using the arima command. Look at the help page on this function before attempting the following activities.

Suppose  $\{Z_t\}_{t\in\mathbb{N}}$  is a white noise with mean zero and variance  $0.8^2$ . Consider stochastic process  $\{X_t\}_{t\in\mathbb{N}}$  with

$$X_{t} = 0.8 X_{t-1} - \frac{1}{3} X_{t-2} + \frac{0.6}{\sqrt{3}} X_{t-3} + Z_{t}.$$
 (1)

- 1. Name the process defined in equation (1), specifying its order.
- 2. Explain how to recognize this process based on an observed time series and how to determine its order.
- 3. Use the command set.seed(23456) to set the random seed for reproducibility and then use function arima.sim() to generate 1500 observations from the model in (1). Plot the simulated time series.
- 4. Plot the sample autocorrelation function. Comment on the behaviour of the sample acf, and explain whether it appears as you would expect given the model.
- 5. Now plot the sample partial autocorrelation function, using command pacf(). Comment on the behaviour of the sample pacf, and explain whether it appears as you would expect given the model.
- 6. Use function arima() to fit an ARMA model to the simulated time series. You should specify the order (which determines the class of models to be fitted) and decide whether a non-zero mean should be included.

Use the three available estimation methods (CSS-ML, ML and CSS) to fit the model parameters.

Present results of your estimation in a table:

	$\alpha_1$	$\alpha_2$	$\alpha_3$	$\sigma^2$
True values				
CSS-ML				
ML				
CSS				

You can use function kable in R Markdown. Round numeric values in your table to 3 decimal places for presentation purposes. Make sure to include a caption for your table.

Compare parameter estimates under the different estimation procedures as well as with the true model parameters.