STAT 443: Lab 1

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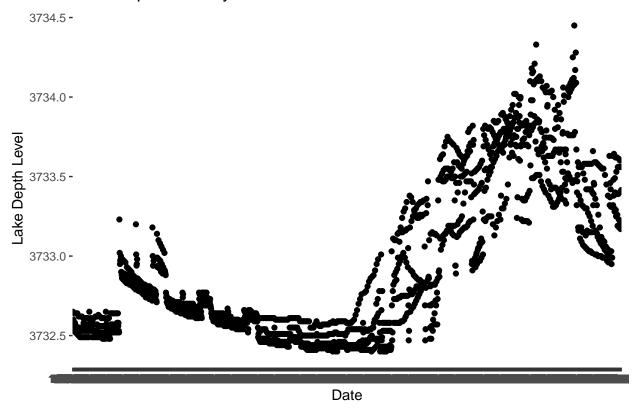
13 January, 2022

Question 1

(a)

```
data <- read.csv("LakeLevels.csv", header = TRUE)</pre>
head(data, 10)
##
           Date LakeLevel
## 1
       1/1/2007
                  3732.65
       1/2/2007
                  3732.65
       1/3/2007
                  3732.65
## 3
## 4
       1/4/2007
                  3732.64
## 5
       1/5/2007
                  3732.64
## 6
       1/6/2007
                  3732.64
## 7
       1/7/2007
                  3732.64
## 8
       1/8/2007
                  3732.64
## 9
       1/9/2007
                  3732.64
## 10 1/10/2007
                  3732.64
data %>%
    ggplot(aes(x = Date, y = LakeLevel)) +
    geom_point() +
    labs(x = "Date",
         y = "Lake Depth Level",
         title = "Lake Depth Level By Date")
```

Lake Depth Level By Date

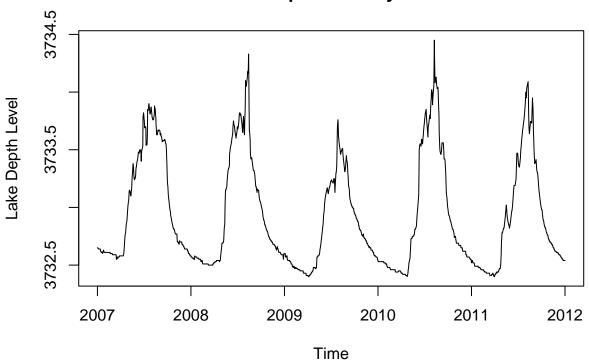


(b)

```
x \leftarrow ts(data = data[,-1], start = c(2007,1), frequency = 365)
```

(c)

Lake Depth Level by Time



- i) In this new plot, we can clearly see the change in lake's depth level according according to time, whereas in the first plot this is not easy to see.
- ii) We observe seasonality from the above plot where the lake's depth is high in the middle of the year and becomes lower at the end of a year.
- iii) We do not observe a trend that there is no overall increase or decrease in lake's depth level year over year.
- iv) The observations are serially dependent.
- v) There is cyclical variation in the above plot, where we see the same pattern of increasing and decreasing depth year over year.

Question 2

(a)

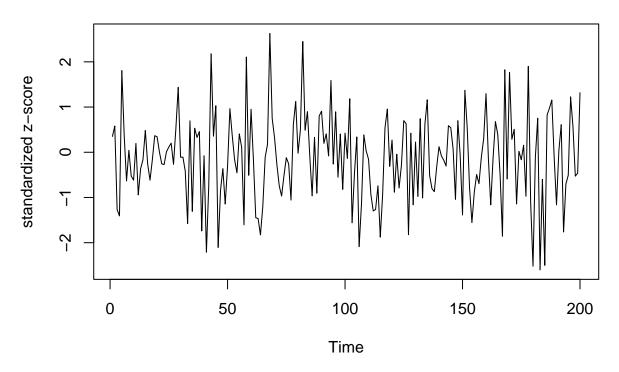
```
set.seed(443)
std_data <- rnorm(200)
std_ts <- ts(std_data)
max(std_data)</pre>
```

[1] 2.627609

(b)

```
plot(std_ts,
    ylab = "standardized z-score",
    main = "Time series plot with standard normal data")
```

Time series plot with standard normal data



```
# calculate percentage of observation fall outside of +/- 2
mean(std_data < -2.0 | std_data > 2.0)
```

[1] 0.05

```
# expected percentage of observations fall outside of +/- 2
round(2*pnorm(2.0, lower.tail = FALSE),4)
```

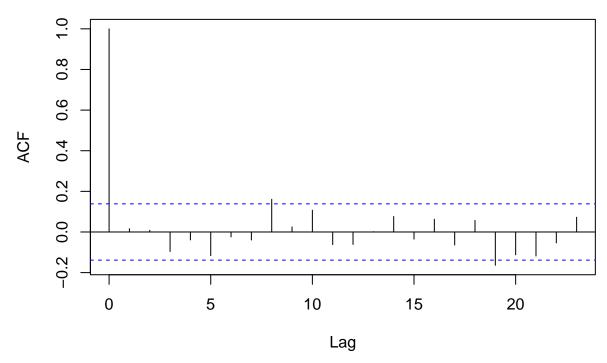
[1] 0.0455

- i) About 5% of the observations fall outside of the range ± 2
- ii) Since the observations are draw from a standard normal distribution, we would expect around 4.55% of the observations to fall outside of the range ± 2 .

(c)

```
acf(std_ts, type = "correlation")
```

Series std_ts



Looking at the above correlogram, most of the sample auto-correlations are within the $\pm 2/\sqrt{200}$ bound, so they are likely to come from a completely random series. We do not see the acf alternates, nor there is any oscillation. We do not observe any indication of positive or negative temporal correlation.

More information on R Markdown

This is an R Markdown document, which can be used as a template for STAT 443 labs and assignments. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see http://rmarkdown.rstudio.com.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

summary(cars)

```
##
        speed
                          dist
##
    Min.
            : 4.0
                    Min.
                            :
                               2.00
    1st Qu.:12.0
                    1st Qu.: 26.00
##
##
    Median:15.0
                    Median: 36.00
##
    Mean
            :15.4
                    Mean
                            : 42.98
    3rd Qu.:19.0
                    3rd Qu.: 56.00
##
    Max.
            :25.0
                    Max.
                            :120.00
```

Using the function kable, it produces a nicer table

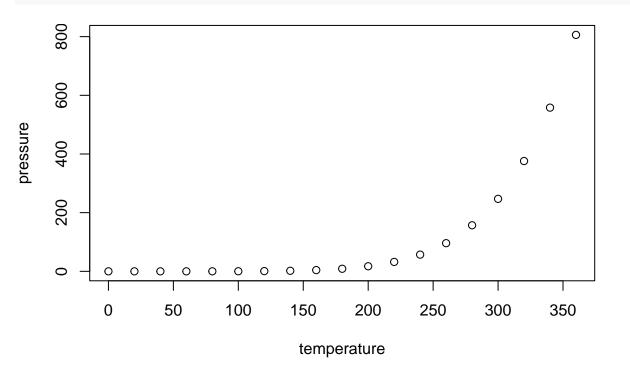
kable(summary(cars))

speed	dist
Min.: 4.0	Min.: 2.00
1st Qu.:12.0	1st Qu.: 26.00
Median $:15.0$	Median: 36.00
Mean:15.4	Mean: 42.98
3rd Qu.:19.0	3rd Qu.: 56.00
Max. $:25.0$	Max. $:120.00$

Including Plots

You can also embed plots, for example:

plot(pressure)



Note that specifying echo = FALSE parameter would prevent printing of the R code that generated the plot. This is something you may want to do for larger reports that would not require display of the R code.

You can also modify the size and alignment of the figure.

plot(pressure)

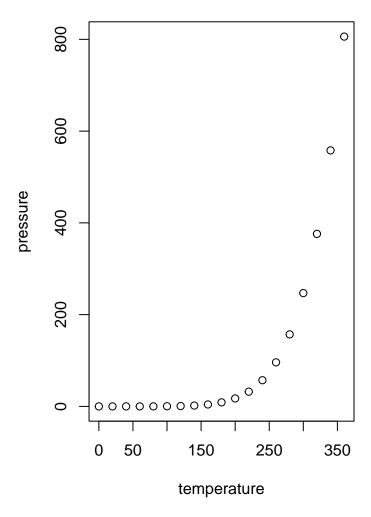


Figure 1: title