## Departamento de Eletrónica, Telecomunicações e Informática

# Deep Learning Convolutional Neural Networks (CNN)

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# Outline

- Deep Neural Networks
- Convolutional Neural Networks (CNN) basic building blocks
- Classical CNN LeNet-5, AlexNet, VGG
- Transfer Learning
- Data Augmentation examples
- Visualization of what convolutional layers learn

# Deep Neural Networks

## Why deep learning?

Hardware get smaller.

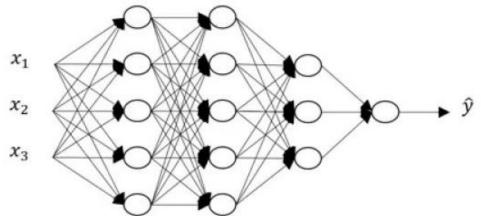
Sensors get cheaper, widely available IoT devices with high sample-rate.

**Data sources:** sound, vibration, image, electrical signals, accelerometer, temperature, pressure, LIDAR, etc.

**Big Data:** Exponential growth of data, (IoT, medical records, biology, engineering, etc.)

How to deals with **unstructured data** (image, voice, text, EEG, ECG, etc.) => needs for feature extraction (data mining).

**Deep Neural Networks**: first extract (automatically) the features, then solve ML tasks (classification, regression)

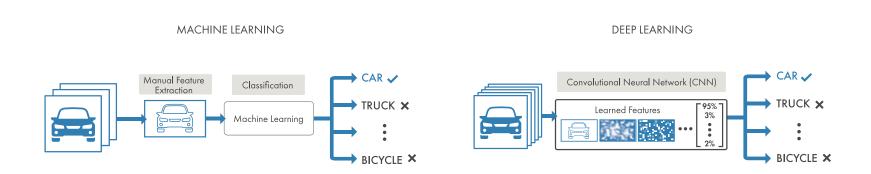


### Deep Learning

Deep learning is a powerful subset of machine learning that utilizes artificial neural networks with multiple layers to learn from data and perform complex tasks.

#### Learning from Data:

Unlike traditional machine learning, deep learning models can learn directly from data, automatically extracting features and patterns without explicit feature engineering.



# Conventional ML vs. Deep Learning

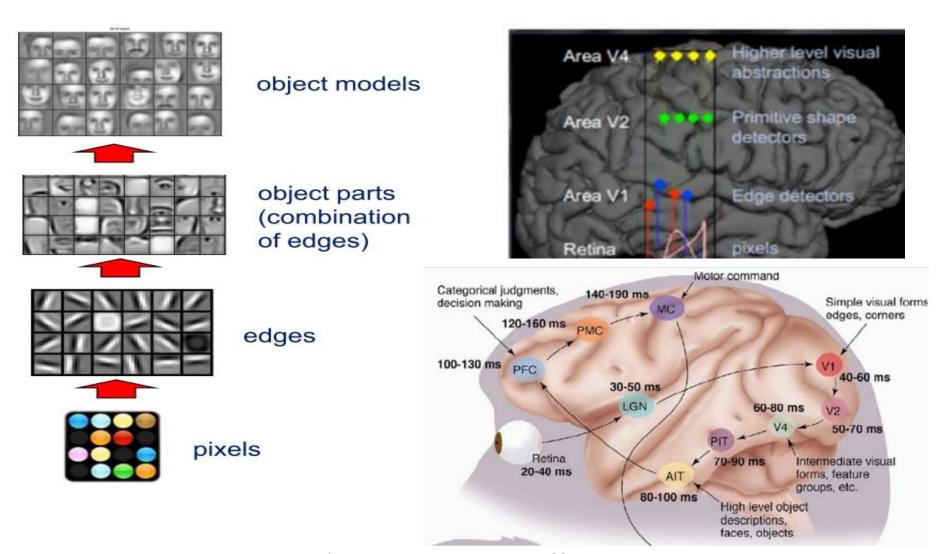
### **Conventional Machine Learning (ML)**

- Needs feature engineering hard, time-consuming task, requires expert knowledge.
- Don't work well with raw data (e.g. pixels/voxels of images).
- Better than DL if good features are found.

### **Deep Learning**

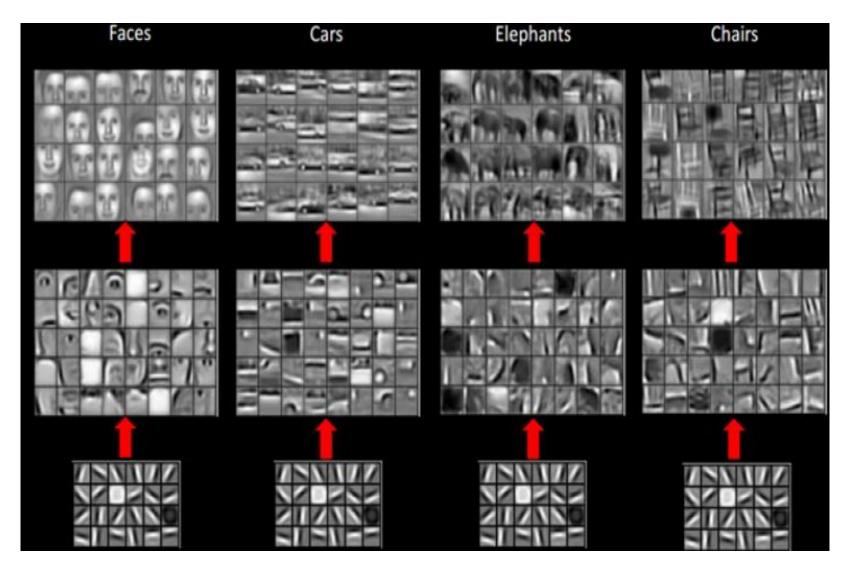
- Representation-learning methods with multiple levels of representation.
- Layers that extract automatically features from raw data (latent structures not seen/difficult to be designed by humans)
- Needs large amounts of labelled training data
- Needs massive computational resources (e.g. GPUs, parallel solvers)

# Representation Learning inspired by visual neuroscience



By Yann LeCun, Yoshua Bengio & Geoffrey Hinton Nature 521, 436-444, 2015, doi:10.1038/nature14539

# Representation Learning



By Yann LeCun, Yoshua Bengio & Geoffrey Hinton Nature 521, 436-444, 2015, doi:10.1038/nature14539

# Deep Learning – major applications

Image, Video, Speech, Text processing (large scale, big data):

- Computer Vision: Identifying objects, faces, and scenes in images
- > Speech Recognition: Converting spoken words into text
- > Natural Language Processing: Understanding and generating human language, including machine translation and text summarization
- Bioinformatics (genomics, drug discovery)
- > Brain imaging: Analyzing medical images for diagnosis and treatment planning.
- > Recommendation Systems: Suggesting products, movies, or other items based on user preferences.
- Fraud Detection: Identifying fraudulent transactions and other malicious activity.

# Deep Learning

# What are the benefits of using deep learning models?

- •Can learn complex relationships between features in data: This makes them more powerful than traditional machine learning methods.
- •Large dataset training: This makes them very scalable, and able to learn from a wider range of experiences, making more accurate predictions.
- •Data-driven learning: DL models can learn in a data-driven way, requiring less human intervention to train them, increasing efficiency and scalability. These models learn from data that is constantly being generated, such as data from sensors or social media.

#### Challenges of using deep learning models:

- •Data requirements: Deep learning models require large amounts of data to learn from, making it difficult to apply deep learning to small dataset problems.
- •Overfitting: DL models may be prone to overfitting. This means that they can learn the noise in the data rather than the underlying relationships.
- •Bias: These models can potentially be biased, depending on the data that it's based on. This can lead to unfair or inaccurate predictions.

# CNN - basic building blocks

Convolutional Neural Networks (CNNs), are a type of deep learning algorithm specifically designed for processing and analyzing data with a grid-like structure, such as images. They excel at extracting spatial features and patterns from visual data.

#### **Convolutional Layers:**

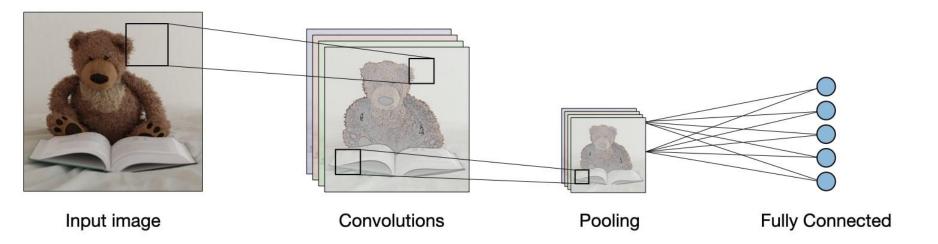
These layers apply a filter (kernel) across the input, learning spatial hierarchies of features from low-level to high-level patterns.

#### **Pooling Layers:**

These layers down-sample the feature maps, reducing dimensionality and computational cost while preserving important features.

#### **Fully Connected Layers:**

These layers connect all neurons from the previous layer to all neurons in the current layer, enabling classification or prediction based on the extracted features.



#### **Feature Extraction:**

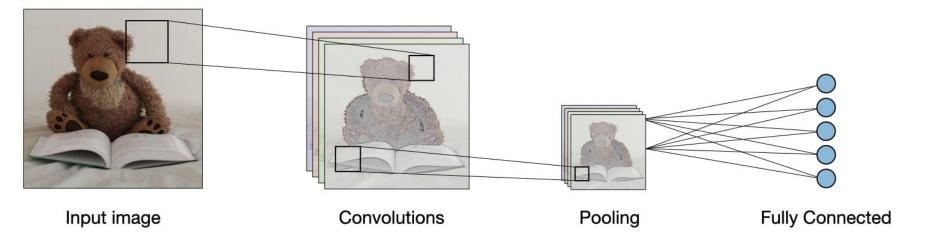
CNNs learn to automatically extract meaningful features from data, such as edges, textures, and objects, without explicit feature engineering.

#### **Hierarchical Feature Learning:**

CNNs learn hierarchical representations of features, where each layer builds upon the previous layer's output, creating a progressively more complex understanding of the input.

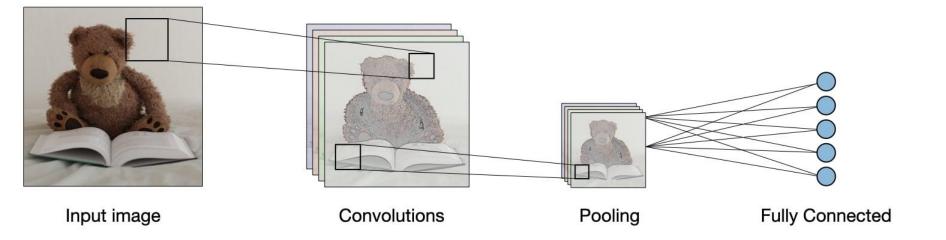
#### **Applications:**

In essence, CNNs leverage the power of deep learning and specialized architecture to efficiently analyze and understand patterns in grid-like data, making them a powerful tool for a wide range of applications.



#### **Important Parameters in Convolution:**

- Filter Dimension
- Stride
- Zero-Padding



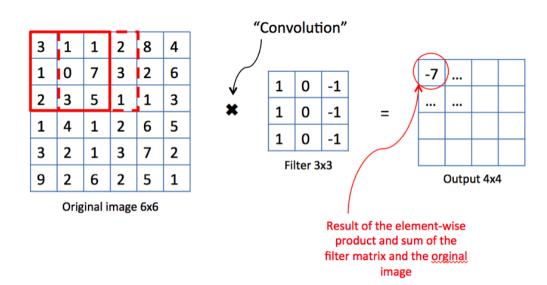
### Why Convolution Learning?

#### Deep learning on large images

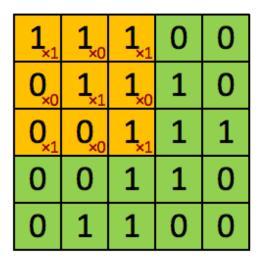
If the image has 1000x1000x3 (RGB) pixels=3 million features (inputs) If the first hidden layer has 1000 nodes => The parameter matrix between the input and the hidden layer has (1000x3million) 3billion parameters.

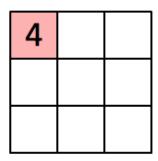
1<sup>st</sup> **problem:** Difficult to get enough data to prevent model overfitting 2<sup>nd</sup> **problem:** Computational (memory) requirements to train such networks are not feasible.

#### Solution: implement convolution operation



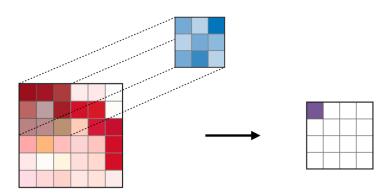
### **OPERATION CONVOLUTION**





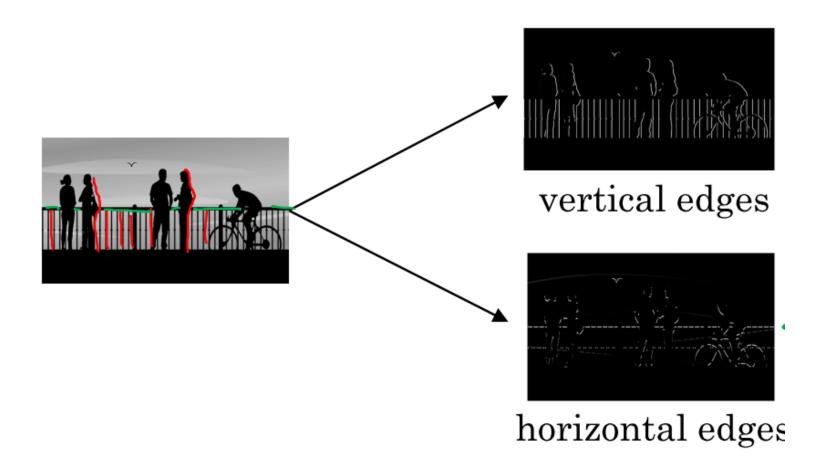
**Image** 

Convolved Feature



The convolution layer (CONV) uses filters that perform convolution operations as it scans the input for its dimensions. Its hyperparameters include the filter size F and stride S. The resulting output O is called a *feature* map or activation map.

## Detect horizontal/vertical edges



### VERTICAL EDGES DETECTOR

#### Ilustrative example:

10 10 10 10	10	10	0	0 0 0 0 0	0 0 0 0 0	*	1 1 1	0 0	-1 -1 -1	=	0 0 0	30 30	30 30 30 30	100
						*								

Detection of bright to dark transition (+30)

## Hand-picked convolutional filters (kernels)

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

=> Horizontal edge detector

$$\begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

 $\Rightarrow$  Sobel filter

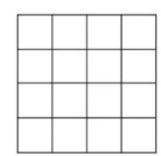
$$\begin{bmatrix} 3 & 0 & -3 \\ 10 & 0 & -10 \\ 3 & 0 & -3 \end{bmatrix}$$

 $\Rightarrow$  Sharr filter

### **CONVOLUTIONAL FILTERS (KERNELS)**

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

$w_1$	$w_2$	w <sub>3</sub>
$W_4$	$w_5$	w <sub>6</sub>
$w_7$	w <sub>8</sub>	W <sub>9</sub>



Hand-picking the filter values is difficult.

Treat the filter numbers as trainable parameters (w), and let the computer learn them automatically.

Other than vertical and horizontal edges, such a computer-generated filter can learn information from different angles (e.g., 45°, 70°, 73°) and is more robust than hand-picking values.

By convention, the conv filter is a square matrix with odd size (typically 3x3, 5x5, 7x7, also 1x1).

It is nice to have a central pixel, and it facilitates the padding.

### **PADDING**

Zero-padding denotes the process of adding *P* zeroes to each side of the boundaries of the input. This value can either be manually specified or automatically set through one of the three modes detailed below

Mode	Valid	Same	Full		
Illustration					
Purpose	<ul> <li>No padding</li> <li>Drops last convolution if dimensions do not match</li> </ul>	<ul> <li>Padding such that feature map size has original size.</li> <li>Output size is mathematically convenient</li> <li>Also called 'half' padding</li> </ul>	<ul> <li>Maximum padding such that end convolutions are applied on the limits of the input</li> <li>Filter 'sees' the input end-to-end</li> </ul>		

### **PADDING**

$$\begin{bmatrix} 3 & 0 & 1 & 2 & 7 & 4 \\ 1 & 5 & 8 & 9 & 3 & 1 \\ 2 & 7 & 2 & 5 & 1 & 3 \\ 0 & 1 & 3 & 1 & 7 & 8 \\ 4 & 2 & 1 & 6 & 2 & 8 \\ 2 & 4 & 5 & 2 & 3 & 9 \end{bmatrix} * \begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix} = \begin{bmatrix} -5 & -4 & 0 & 8 \\ -10 & -2 & 2 & 3 \\ 0 & -2 & -4 & -7 \\ -3 & -2 & -3 & -16 \end{bmatrix}$$

**Ex.** Take  $6 \times 6$  image, apply  $3 \times 3$  conv filter, get  $4 \times 4$  output matrix, because we shift the filter one row down or one column right and therefore we have  $4 \times 4$  possible positions for the  $3 \times 3$  filter to appear in the  $6 \times 6$  input matrix.

**In general:** given  $n \times n$  input matrix and  $f \times f$  filter matrix, the convolution operation will compute  $(n-f+1) \times (n-f+1)$  output matrix by applying one pixel up/down left/right rule.

**1<sup>st</sup> problem:** Shrink the matrix size as we continue to further apply convolution. The image will get very small if we have many convolution layers.

**2<sup>nd</sup> problem**: Pixels on the corner of the image are used only once while the pixels in the centre of the image are used many times. This is uneven, loose of inf.

Solution: Padding.

### SYMMETRIC PADDING

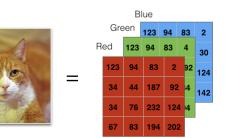
Add *p* extra columns and rows at the image borders with 0 values (zero padding). Output matrix size:  $(n+2p-f+1) \times (n+2p-f+1)$ 

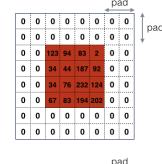
"valid" convolution => no padding

#### "same" covolution =>

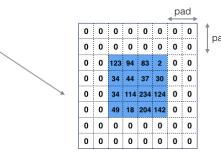
Pad so that output size is the same as the input size. Formula for choosing p (f is usually odd number!):











$$n + 2p - f + 1 = n$$

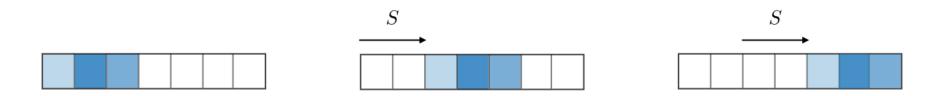
$$2p - f + 1 = 0$$

$$2p = f - 1$$

$$p = (f - 1)/2$$

### Stride

For a convolutional or a pooling operation, the stride S denotes the number of pixels by which the window moves after each operation.



**Increasing** the stride will allow the filter to cover a **larger area of the input image**, which can be useful for capturing **more global features**.

In contrast, lowering the stride will capture finer and more local details.

In addition, increasing the stride will control **overfitting** and **reduce computational efficiency** as it will reduce the spatial dimensions of the feature map.

### STRIDED CONVOLUTION

$$\begin{bmatrix} 2 & 3 & 7 & 4 & 6 & 2 & 9 \\ 6 & 6 & 9 & 8 & 7 & 4 & 3 \\ 3 & 4 & 8 & 3 & 8 & 9 & 7 \\ 7 & 8 & 3 & 6 & 6 & 3 & 4 \\ 4 & 2 & 1 & 8 & 3 & 4 & 6 \\ 3 & 2 & 4 & 1 & 9 & 8 & 3 \\ 0 & 1 & 3 & 9 & 2 & 1 & 4 \end{bmatrix} * \begin{bmatrix} 3 & 4 & 4 \\ 1 & 0 & 2 \\ -1 & 0 & 3 \end{bmatrix} = \begin{bmatrix} 91 & 100 & 83 \\ 69 & 91 & 127 \\ 44 & 72 & 74 \end{bmatrix}$$

**Stride:** how many pixels (steps) we shift to the right or down after each convolution.

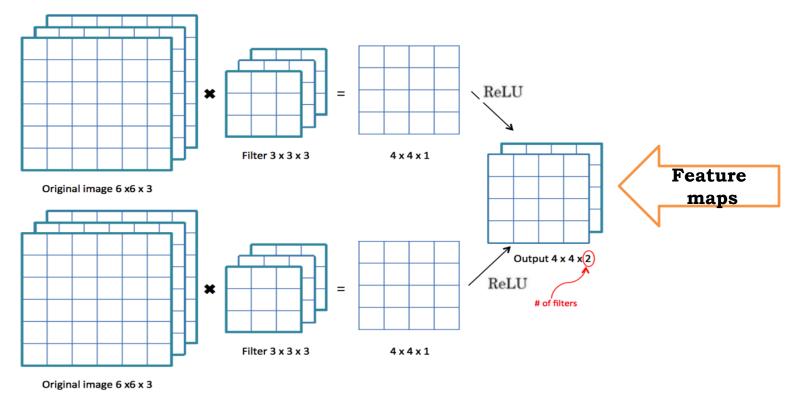
**In general:** given  $n \times n$  input matrix and  $f \times f$  filter with padding p and stride s the convolution operation will compute output matrix with size:

$$\lfloor \frac{n+2p-f}{s} + 1 \rfloor$$
 by  $\lfloor \frac{n+2p-f}{s} + 1 \rfloor$ 

If the formula computes a non-integer value => choose the closest lower integer.

**Ex.**: no padding (p=0), stride s=2 => (7 + 0 - 3)/2 + 1 = 4/2 + 1 = 3 => 3 × 3 matrix

### Multiple Conv Filters over Volumes (3D filters)



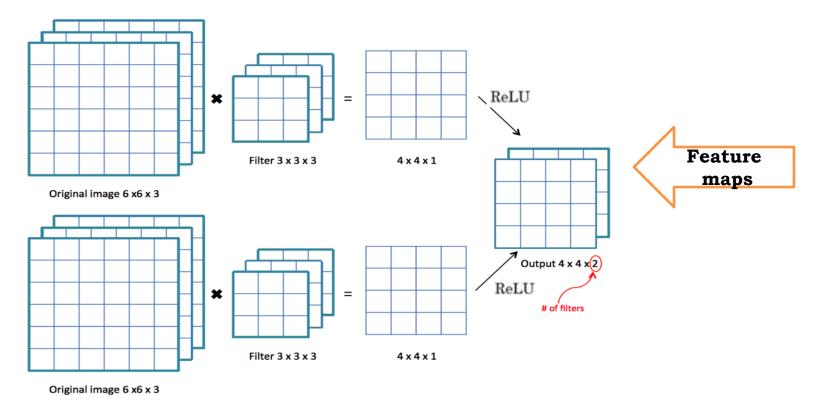
RGB images have 3 dimensions: height, width, and number of channels (3D volume).

The conv filter will be also a 3D volume :  $f \times f \times 3$  (number of channels has to be equal in the image and the filter)

 $(n \times n \times n_c)$  image \*  $(f \times f \times n_c)$  filter =>  $(n-f+1) \times (n-f+1) \times n_c$  filters (no padding)

#### Play conv\_kiank

### ONE CONV LAYER OF CNN



Different 3D filters (kernels) are applied to the 3D input image and the result matrices are stacked to form a 3D output volume.

After the convolution operation the result is passed through an activation function (e.g. ReLU, or sigmoid, linear, etc.).

The outputs of the conv layers are known as feature maps.

## Number of parameters in one layer

**Ex.** If you have 10 filters that are  $3 \times 3 \times 3$ , in one layer of a CNN, how many parameters does that layer have?

Answer:  $3 \times 3 \times 3 = 27 + 1$  (bias) = 28 x 10 (filters) => in total 280 parameters

#### **Major property of CNN:**

The number of parameters does not depend on the image size (or on the input from the previous layer).

Even in a very large image, we end up with a small number of parameters.

This makes them less prone to overfitting.

The filters detect different features (horizontal, vertical edges, etc.)

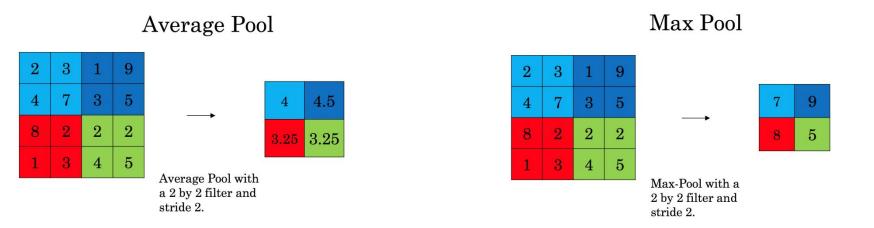
### **Pooling**

The pooling layer is a downsampling operation, typically applied after a convolution layer.

In particular, max and average pooling are pooling strategies where the maximum and average value is taken, respectively.

Туре	Max pooling	Average pooling		
Purpose	Each pooling operation selects the maximum value of the current view	Each pooling operation averages the values of the current view		
Illustration	max	avg		
Comments	<ul> <li>Preserves detected features</li> <li>Most commonly used</li> </ul>	<ul><li>Downsamples feature map</li><li>Used in LeNet</li></ul>		

### POOLING (POOL)



Pooling operation reduces the size of the representation to speed up the computation and make the features more robust.

**Ex.** Divide the input in regions (e.g.  $2 \times 2$  filter), choose stride (e.g. s=2), each output will be the max (**max pooling**) or the average (**average pooling**) from the corresponding regions.

#### Some intuition:

Large number means there is some strong feature (edge, eye) detected in this part of the image, which is not present in another part.

Max Pool: whenever this feature is detected it remains preserved in the output.

### SUMMARY OF POOLING

The size of the regions (f) and the stride (s) are hyper-parameters. Common choice f = 2, s = 2 has the effect of shrinking the height and width of the representation by a factor of 2.

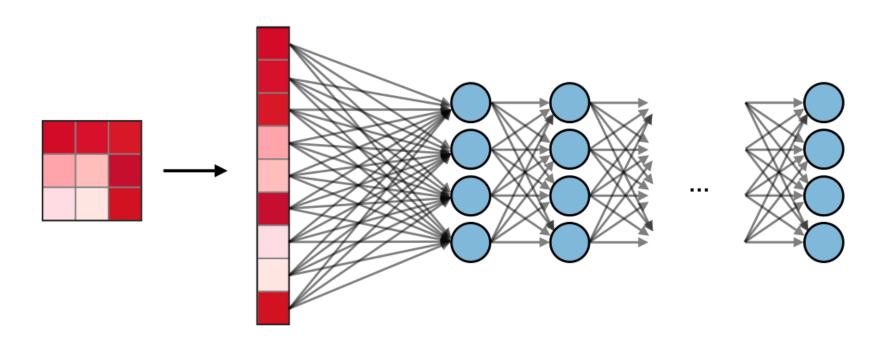
There are no parameters to learn.

Max pooling is much often used than average pooling.

There is no theoretical proofs why pooling works well. It is just a fact in practice that this approach works well with some data sets.

## **Fully Connected**

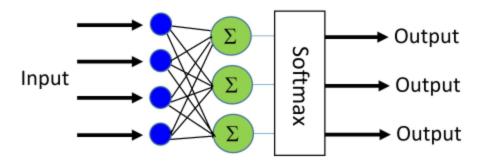
The fully connected layer operates on a flattened input where each input is connected to all neurons. If present, FC layers are usually found towards the end of CNN architectures.



### **Softmax**

The softmax step can be seen as a generalized logistic function that takes as input a vector of scores  $x \in R$  and outputs a vector of output probability  $p \in R$  through a softmax function at the end of the architecture.

$$p = egin{pmatrix} p_1 \ dots \ p_n \end{pmatrix} \quad ext{where} \quad \boxed{p_i = rac{e^{x_i}}{\displaystyle\sum_{j=1}^n e^{x_j}}}$$



### **Softmax Layer**

Softmax Layer (SL) estimates the probability that an example  $x^{(i)}$  belongs to each of the k classes ((j=1,2,..k)).

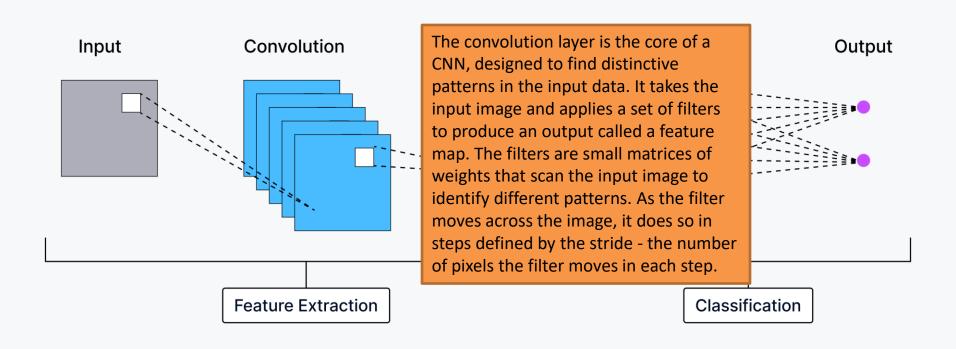
$$p(y^{(i)} = j|x^{(i)}; \theta) = \frac{e^{\theta_j^T x^{(i)}}}{\sum_{l=1}^k e^{\theta_l^T x^{(i)}}}$$

SL outputs *k* dimensional vector with estimated probability for each class k:

$$h_{\theta}(x^{(i)}) = \begin{bmatrix} p(y^{(i)} = 1 | x^{(i)}; \theta) \\ p(y^{(i)} = 2 | x^{(i)}; \theta) \\ \vdots \\ p(y^{(i)} = k | x^{(i)}; \theta) \end{bmatrix} = \frac{1}{\sum_{j=1}^{k} e^{\theta_{j}^{T} x^{(i)}}} \begin{bmatrix} e^{\theta_{1}^{T} x^{(i)}} \\ e^{\theta_{2}^{T} x^{(i)}} \\ \vdots \\ e^{\theta_{k}^{T} x^{(i)}} \end{bmatrix}$$

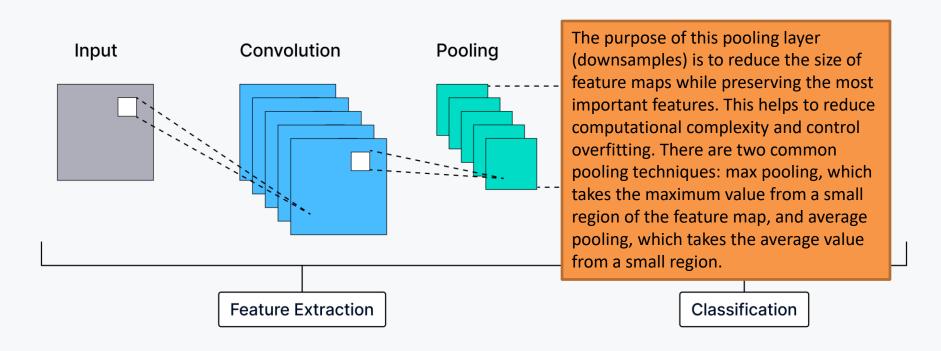
# **Summary of CNN**

#### The Architecture of Convolutional Neural Networks



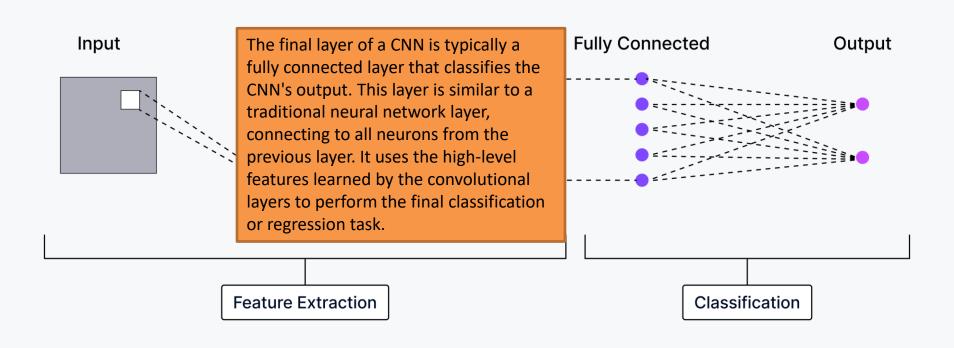
# **Summary of CNN**

#### The Architecture of Convolutional Neural Networks



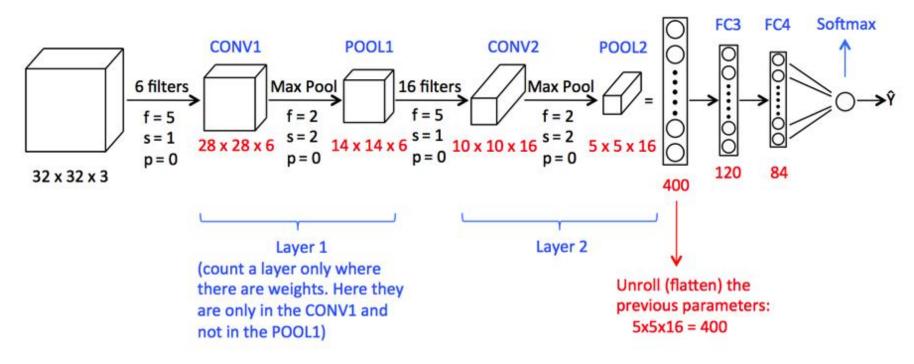
# **Summary of CNN**

#### The Architecture of Convolutional Neural Networks



# Classical CNN – LeNet-5, AlexNet, VGG

## Classical CNN Example: LeNet5\*



\*LeCun et al., 1998, "Gradient-based learning applied to document recognition". Original LeNet5 applied to handwritten digit recognition (grey scale images). Avg pooling, no padding, softmax classifier; ReLU and sigmoid/tanh neurons in the Fully Connected (FC) layers.

The activation function is always present after the convolution, even if it is not drawn on the CNN diagram.

**General trend**: CNNs start with large image, then height and width gradually decrease as it goes deeper in the network, where as the number of channels increase.

## **Convolution Benefits**

Major advantages of conv layers over fully connected (FC) layers:

#### (1) parameter sharing

(2) sparsity of connections

**Ex.** Take  $32 \times 32 \times 3$  RGB image (3,072 inputs), using 6 filters (5 × 5 × 3), we get  $28 \times 28 \times 6$  dimensional output (4,704 neurons). If we connect every neuron to the inputs (as in a fully connected Neural Networks), the number of parameters would be about 14 million. This is a lot of parameters to train and we have just a small ( $32 \times 32 \times 3$ ) image.

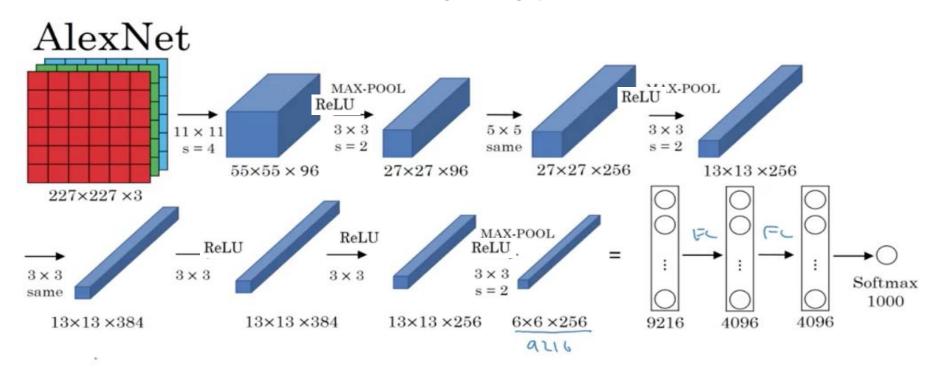
**Parameter sharing** is a feature detector (such as vertical edge detector) that is useful in one part of the image and is probably useful in another part of the image.

**Sparsity of connections** means that, in each layer, each output value depends only on a small number of inputs.

LeNet5 has only 60,000 parameters.

The conv layers have much less parameters than FC layers.

### AlexNet\*

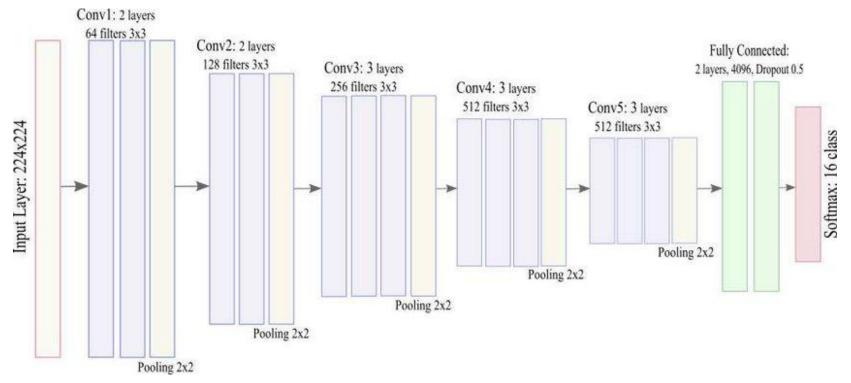


## \* Alex Krizhevsky, Ilya Sutskever, Geoffrey E. Hinton, 2012, ImageNet classification with deep convolutional neural networks.

5 conv layers, 3 FC layers with softmax output, 60 million parameters in total. AlexNet applied to ImageNet LSVRC-2010 dataset to recognize 1000 different classes.

This paper convinced the Computer Vision (CV) community that DL really works and will have a huge impact not only in CV but also in speech/language processing. 41

### VGG-16 \*



# \* Karen Simonyan, Andrew Zisserman, 2015, Very Deep Convolutional Networks for Large-Scale Image Recognition

VGG-16 has 16 layers (with weights !), 138 million parameters. Unified architecture: All conv layers: (3x3) filters, s=1, same; All MaxPool =2x2, s=2.

At each convolution the height and width go down by a factor of 2, the channels go up by a factor of 2.

VGG-19 is a larger version of VGG-16, both have similar performance.

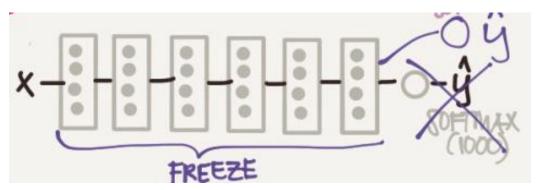
# Transfer Learning

## Transfer Learning

- Starting from an open-source architecture from web (e.g. cloned from github) is faster than implementing code from scratch.
- Training may takes weeks/months, many GPUs, better use a pre-trained model (pre-trained parameters) => that is Transfer Learning (TL)

**Ex.:** your problem has 3 classes (car, pedestrian, neither). You have a small training set.

- Take a DNN trained for 1000 classes.
- Substitute the last classification layer (softmax with 1000 outputs) ) with a softmax with 3 outputs.
- Freeze the parameters in all other layers, train only the softmax layer.
- Comp. trick: pre-compute and save on disc the features before softmax layer.



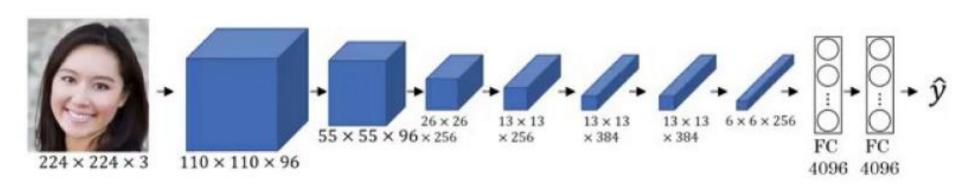
## **Transfer Learning (cont)**

**Ex. (cont):** If you have larger training set: freeze fewer layers, train latter layers.

The more data you have, the more layers you may train.

If you have big training set, you may use the trained DNN only at the initialization stage, starting not from random parameters but from the parameters of the trained DNN. Then update all weights during the optimization.

**Intuition:** Hidden layers earlier in the network extract much more general features not specific to the particular task.



# Data Augmentation - examples

## **Data Augmentation**



- Rotation,
- Random Noise
- Mirroring
- Random Croping
- Color shifting: add distorstions to the R (+20) G (-20) B (+20) channels
- Etc.

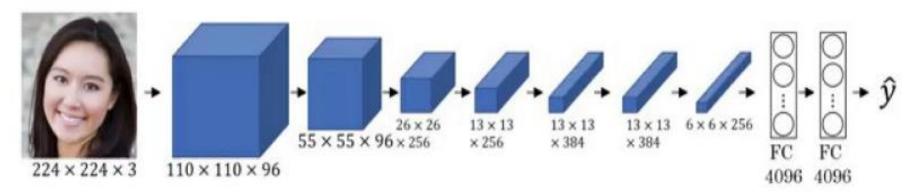
**Off-line:** generate all distortions and save the augmented data set.

**On-line:** common way of implementing data augmentation during training: CPU is constantly loading a stream of images coming from the hard disc and generate distortions to form mini-batches that are constantly passed to a Training algorithm (implemented on a different CPU or GPUs). The two processes (data augmentation and training run in parallel).

Hyper-parameters to choose: what kind of distortion, how much distortion, etc.

# Visualization of what convolutional layers learn

## What are learning Conv Layers \*



Lets say we have trained a ConvNet (e.g. AlexNet like network) and we want to visualize what the hidden units in different layers are computing. Let's start with one hidden unit in Layer 1.

Suppose you scan through your entire training sets and find out what are the <u>9 image</u> patches that maximize that unit's activation.

This particular hidden unit seems to be activated (to see) by edges or lines.

#### Repeat for other units in Layer 1

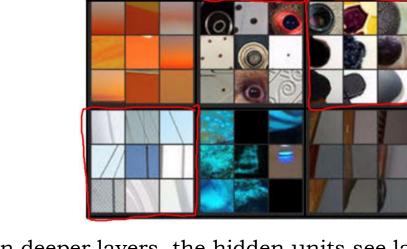
This picture shows 9 different representative neurons and for each of them the 9 image patches that maximally activate them.

The trained hidden units in Layer 1 respond to relatively simple features such as edges or a particular shade of colour.

\* ref. Zeiler&Fergus, 2013 Visualizing and understanding convolutional networks.





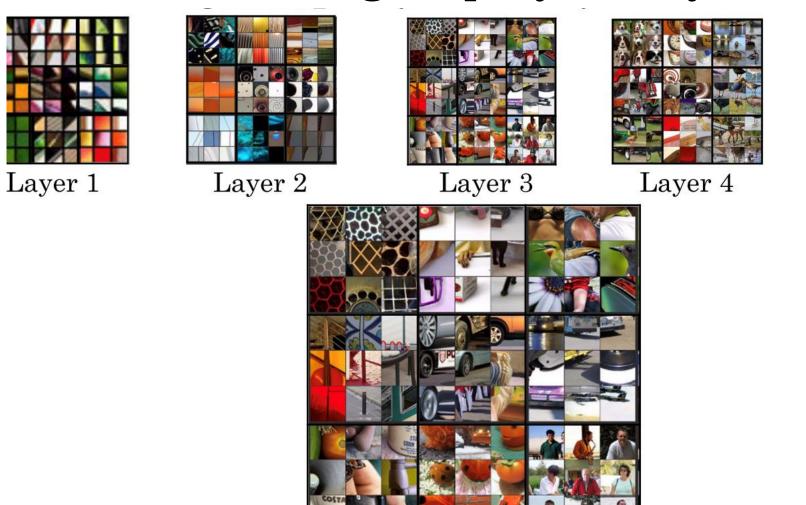


In deeper layers, the hidden units see larger regions of the image.

The units in Layer 2 are activated from more complex shapes and patterns, such as vertical lines with texture, rounder shapes at the left part of the image and so on.

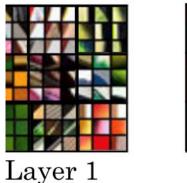
The features that Layer 2 is detecting are getting more complicated.

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In Layer 3, the hidden units start detecting part of cars, irregular texture, even people, other shapes difficult to figure out what they are, but it is clearly starting to detect more complex patterns.

Layer 5







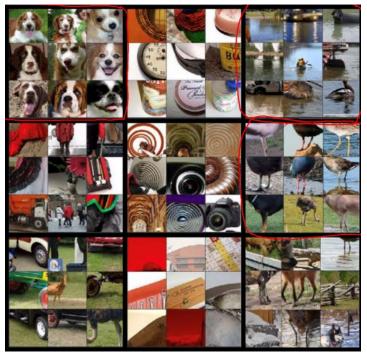




Layer 3

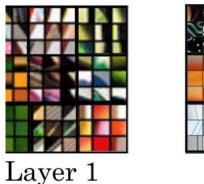
Layer 4

Layer 5



In Layer4, one unit seems to be a dog detector, but all dogs are somehow similar, other unit detects water, other unit detects legs of birds and so on.

Detected patterns are even more complex then in Layer3.











Layer 3

Layer 4

Layer 5



In Layer 5, one neuron seems to be a dog detector, but the detected dogs seem to be more varied; other detects flowers; other neuron seems to detect things with a keyboard like texture, or maybe lots of dots against background; one neuron may detects text, it's always hard to be sure.

#### **Advantages of CNNs**

- 1.Good at detecting patterns and features in images, videos, and audio signals.
- 2. Robust to translation, rotation, and scaling invariance.
- 3.End-to-end training, no need for manual feature extraction.
- 4. Can handle large amounts of data and achieve high accuracy.

#### **Disadvantages of CNNs**

- 1. Computationally expensive to train and require a lot of memory.
- 2.Can be prone to overfitting if not enough data or proper regularization is used.
- 3. Requires large amounts of labeled data.
- 4.Interpretability is limited, it's hard to understand what the network has learned.

#### What is difference between CNN and RNN?

CNN (Convolutional Neural Network) and RNN (Recurrent Neural Network) are both popular types of neural networks, but they serve different purposes and are designed to handle different types of data.

#### **CNN**

- Primarily processes grid-like data, such as images
- •Extracts local features using convolutional layers
- Excels at detecting spatial patterns and relationships
- •No explicit memory of past inputs
- Treats each input independently
- •Suitable for tasks like image recognition and computer vision
- Takes advantage of parallel processing
- •Designed to capture spatial hierarchies and patterns
- Utilizes convolution and pooling layers
- Processes grid-like data with local spatial relationships
- •Does not inherently capture temporal information
- •Suitable for tasks where order of data points is not significant
- •Enables efficient computations on parallel hardware

#### **RNN**

- •Specifically designed for sequential data, like time series or natural language
- •Captures temporal dependencies with recurrent connections
- •Well-suited for capturing sequential patterns and long-term dependencies
- •Has memory of previous inputs through hidden state
- Maintains information flow through time
- •Commonly used in natural language processing, speech recognition, and time series analysis
- Sequential nature limits parallel processing capabilities
- Capable of modeling temporal hierarchies and patterns
- •Employs recurrent connections for information persistence
- Processes sequential data with temporal dependencies
- •Handles tasks where order of data points matters
- Sequential dependency limits parallel processing capabilities