

GEOINFORMATICS PROJECT

Implementation Document

Version 1.0

**Project name: Drone Surveying Planning
(DSP)**



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Revision History

Name	Date	Reason for Changes	Version

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Introduction

The purpose of the Algorithm document is to illustrate the different algorithms used in implementing DSP plugin using three algorithms which give the user the possibility to choose the proper one for his/her flight planning.

The three algorithms are:

- Normal case algorithm.
- Least square method using simulation Data.
- Least square method using DEM.

1. Normal case algorithm.

//Inputs:

Sensor focal length 'c' \leftarrow user input
 Sensor width 'fw' \leftarrow user input
 Sensor height 'fh' \leftarrow user input
 No. of pixels of the sensor in x 'npx' \leftarrow user input
 No. of pixels of the sensor in y 'npy' \leftarrow user input
 Distance of surveying area in X 'X' \leftarrow extracted from Area shape file
 Distance of surveying area in Y 'Y' \leftarrow extracted from Area shape file
 Flight height 'h' \leftarrow user input
 Along track overlapping 'Rl' \leftarrow user input
 Cross track overlapping 'Rt' \leftarrow user input
 Collimation error 'scoll' \leftarrow user input and its default value is 1 in Pix
 Simulation points density 'delta' \leftarrow user input via combo box (Low, Medium, High)

//outputs:

Propagate s2zy and s2zx

Footprint width 'W' \leftarrow (fw*h)/c
 Footprint height 'H' \leftarrow (fh*h)/c

Ground Sample Distance using W 'GSDw' \leftarrow W/npx
 Ground Sample Distance using H 'GSDh' \leftarrow H/npy

Baseline 'b' \leftarrow (1-Rl)*H
 interaxie 'interaxie' \leftarrow (1-Rt)*W

No. of strips in y 'nstrip_y' \leftarrow ceil (Y/b)
 No. of strips in x 'nstrip_x' \leftarrow ceil (X/i)

Real baseline 'b_real' \leftarrow Y/nstrip_y
 Real interaxie 'i_real' \leftarrow X/nstrip_x

Real Along track overlapping 'Rl_real' \leftarrow 1- b_real /H
 Real cross track overlapping 'Rt_real' \leftarrow 1- i_real /W

The x coordinate of the camera position in GCS 'xo' \leftarrow range from i_real/2 to X with step of i_real
 The y coordinate of the camera position in GCS 'yo' \leftarrow range from b_real/2 to Y with step of b_real

mesh grid xo and yo

Assign the z coordinate of the camera h to Zo

Create a flight path matrix 'flpath' with dimension of [nstrip_x* nstrip_y , 2]

for i from 0 to the # of strips in x

fill the first column of flpath from first element to nstrip_y with xo(i)

if yo is odd:

fill the second column with the range of nstrip_y with flipping y0

else:

fill the second column with the range of to nstrip_y with y0

end for

Create simulation X coordinates of a grid 'xGrid' \leftarrow range from $0+\text{delta}/2$ to $X-\text{delta}/2$ with a step of delta

Create simulation Y coordinates of a grid 'yGrid' \leftarrow range from $0+\text{delta}/2$ to $Y-\text{delta}/2$ with a step of delta

Mesh grid xGrid and yGrids

Create a matrix of zeros with the same dimension of yGrid \leftarrow over_y

for i from 0 to the no of strips in y

if ((yGrid greater than or equal yo(i)-H/2 and yGrid less than or equal yo(i)+H/2 and))

increment over_y matrix with 1

end for

Create a matrix of zeros with the same dimension of xGrid \leftarrow over_x

for i from 0 to the no of strips in x

if ((xGrid greater than or equal yo(i)-H/2 and xGrid less than or equal yo(i)+H/2 and))

increment over_x matrix with 1

end for

Mesh grid over_x and over_y

Propagation of the collimation 's2px' \leftarrow $2 * (\text{scoll} * \text{fw} / \text{npx})^2$

Sigma ² of z in longitudinal direction 's2zy' \leftarrow $(h^2 / (c * 0.001 * i_{\text{real}}))^2 * s2px$

Sigma ² of z in transversal direction 's2zx' \leftarrow $(h^2 / (c * 0.001 * b_{\text{real}}))^2 * s2px$

Propagate s2zy and s2zx \leftarrow $\text{sqrt}((s2zy * (\text{Over}_y - 1) + s2zx * (\text{Over}_x - 1))) / ((\text{Over}_y - 1) + (\text{Over}_x - 1))^2$

2. Least square using Data Simulation Algorithm

//Inputs:

Sensor focal length 'c' \leftarrow user input
 Sensor width 'fw' \leftarrow user input
 Sensor height 'fh' \leftarrow user input
 No. of pixels of the sensor in x 'npx' \leftarrow user input
 No. of pixels of the sensor in y 'npy' \leftarrow user input
 Distance of surveying area in X 'X' \leftarrow extracted from Area shape file
 Distance of surveying area in Y 'Y' \leftarrow extracted from Area shape file
 Flight height 'h' \leftarrow user input
 Along track overlapping 'Rl' \leftarrow user input
 Cross track overlapping 'Rt' \leftarrow user input
 Collimation error 'scoll' \leftarrow user input and its default value is 1 in Pix
 Simulation points density 'delta' \leftarrow user input via combo box (Low, Medium, High)

//outputs:

Empirical error matrix in x direction
 Empirical error matrix in y direction
 Empirical error matrix in z direction
 Theoretical error matrix in x direction
 Theoretical error matrix in y direction
 Theoretical error matrix in z direction

Footprint width 'W' \leftarrow (fw*h)/c
 Footprint height 'H' \leftarrow (fh*h)/c

Ground Sample Distance using W 'GSDw' \leftarrow W/npx
 Ground Sample Distance using H 'GSDh' \leftarrow H/npy

Baseline 'b' \leftarrow (1-Rl)*H
 interaxie 'interaxie' \leftarrow (1-Rt)*W

No. of strips in y 'nstrip_y' \leftarrow ceil (Y/b)
 No. of strips in x 'nstrip_x' \leftarrow ceil (X/interaxie)

Real baseline 'b_real' \leftarrow Y/nstrip_y
 Real interaxie 'i_real' \leftarrow X/nstrip_x

Real Along track overlapping 'Rl_real' \leftarrow 1- b_real /H
 Real cross track overlapping 'Rt_real' \leftarrow 1- i_real /W

The x coordinate of the camera position in GCS 'xo' \leftarrow range from i_real/2 to X with step of i_real
 The y coordinate of the camera position in GCS 'yo' \leftarrow range from b_real/2 to Y with step of b_real
 mesh grid xo and yo
 Assign the z coordinate of the camera h to Zo
 Numbering grid point 'ptName' \leftarrow matrix of the same dimensions as XGrid its value with the values from 0: the length of Xgrid

Create a flight path matrix 'flpath' with dimension of [nstrip_x* nstrip_y , 2]

```

for i from 0 to the no of strips in x
  fill the first column of flpath from first element to nstrip_y with x0(i)
  if yo is odd:
    fill the second column with the range of nstrip_y with flipping y0
  else:
    fill the second column with the range of to nstrip_y with y0
end for

```

Create simulation X coordinates of a grid 'xGrid' \leftarrow range from $0+\text{delta}/2$ to $X-\text{delta}/2$ with a step of delta

Create simulation Y coordinates of a grid 'yGrid' \leftarrow range from $0+\text{delta}/2$ to $Y-\text{delta}/2$ with a step of delta

Mesh grid xGrid and yGrids

```

for i in range from 0 to nstrip_y*nstrip_x

```

```

  xsiGrid  $\leftarrow$  (XGrid - Xo(i))/h*c

```

```

  etaGrid  $\leftarrow$  (YGrid - yo(i))/h*c

```

```

  if the absolute value of xsiGrid less than or equal fw/2 and etaGrid less than or equal fh/2

```

```

    mask  $\leftarrow$  1

```

```

  else

```

```

    mask  $\leftarrow$  0

```

```

  Vector of no of observed point 'pt_obs'  $\leftarrow$  vector of [pt_obs; pt_name of where all mask values =1]

```

```

  Vector of no of image containing the point 'im_obs'  $\leftarrow$  vector of [im_obs; i*mask of where all mask values =1]

```

```

  observed xsi 'xsi_obs'  $\leftarrow$  vector of [xsi_obs; xsiGrid where all mask values =1]

```

```

  observed eta 'eta_obs'  $\leftarrow$  vector of [eta_obs; etaGrid where all mask values =1]

```

```

end for

```

```

xsi_obs  $\leftarrow$  xsi_obs + scoll * (fw/npx) * random matrix has the same size of xsi_obs

```

```

eta_obs  $\leftarrow$  eta_obs + scoll * (fh/npv) * random matrix has the same size of eta_obs

```

Create sparse matrix A of size $2 * \text{the length of pt_obs}$, $3 * \text{no of grid points}$

The values in the couples (1: the length of pt_obs , pt_obs) \leftarrow c

Update as well the couples (1: the length of pt_obs , pt_obs+2* no of grid points) \leftarrow xsi_obs

Update as well the couples ((the length of pt_obs+1 to 2* the length of pt_obs , pt_obs+ no of grid points) \leftarrow c

Update as well the couples ((the length of pt_obs+1 to 2* the length of pt_obs , pt_obs+ 2*no of grid points) \leftarrow eta_obs

Observation vector 'yo' \leftarrow [xsi_obs * Zo + c * Xo for each im_obs; eta_obs * Zo + c * Yo for each im_obs]

Normal matrix 'N' \leftarrow transpose of A matrix * the A matrix

Perform the LU decomposition inverse for Normal matrix 'N'

Normal known term nt \leftarrow transpose of A *yo

Extract the estimated values of X

Extract the estimated values of Y

Extract the estimated value of Z

Calculate the residuals vector.

Calculate the posterior variance.

Calculate Empirical standard division vector 's2'.

Calculate theoretical standard division vector 's3'.

Empirical error matrix in x direction

Empirical error matrix in y direction

Empirical error matrix in z direction

Theoretical error matrix in x direction

Theoretical error matrix in y direction

Theoretical error matrix in z direction

3. Least square using Data Simulation Algorithm

3.1 DEM Data Extraction

//Inputs:

rasin \leftarrow user input of Raster representing the DEM
 fn \leftarrow user input of Polygon Shapefile of the surveying area

//outputs:

Matrix of Elevations from DEM

Matrix of mesh gridding values of X and Y coordinates of GCP

Read the survey area shapefile as Geodata frame and save it in variable gdf
 cr \leftarrow The coordinate reference system of the data frame.

Function newpath so you can generate new path for new layers
 pass In : source path , name of the layer with its extension
 path \leftarrow read the source path
 path_len \leftarrow the length of the source path without the last element
 n_path \leftarrow concatenate the source path without last element + the name of the new layer
 pass Out: n_path

End newpath

Initialize x as an array.

Initialize y as an array.

i \leftarrow 0.

for index to the list of exterior coordinates of geometry in the Geodata frame do:

 xy coordinate = list of pt points.

 x \leftarrow x coordinate from xy coordinate

 y \leftarrow y coordinate from xy coordinate

end for

max_x \leftarrow the max of x

max_y the min of x

min_y \leftarrow the max of y

min_x \leftarrow the min of y

p1 \leftarrow [min_x, min_y]

p2 \leftarrow [max_x, min_y]

p3 \leftarrow [max_x, max_y]

p4 \leftarrow [min_x, max_y]

d_xy \leftarrow **Calculate** the Euclidean distances in x and y

X \leftarrow the min distance in d_xy

Y \leftarrow the max distance in d_xy

Create polygon from point list as [p1,p2,p3,p4,p1] **save** it in variable polygon

data \leftarrow feature 'id'= 1 and 'geometry' column = polygon

Create Geodata frame contains the polygon with (data and (cr as string))

shpin_name \leftarrow user input of the name of the new rectangular Polygon Shapefile

shpin \leftarrow **use the new path** function to generate the path of the new rectangle shapefile

Write poly_gdf into ESRI Shape file

```

rasout_name ← user input of the name of the new clipped raster
rasout ← use the new path function to generate the path of the new clipped raster
rect_DEM ← Clipping the rasin raster by shpin shapefile and pass it → rasout ---by using gdal Wrapper
ds ← open rasout raster
band ← read raster band of ds
Set the no data values in the band as nan
Elev ← read the band values as an array
Assign -32767 or -99999 in the Elev array as nan
Zo ← the mean of Elev array + The flight hight
r_n ← Get the number of rows from Elev array
r_n ← Get the number of rows from Elev array
x_0 ← Get the x coordinate of the raster origin
Dem_res_x ← Get the pixel size in x (the resolution in x)
y_0 ← Get the y coordinate of the raster origin
Dem_res_y ← Get the pixel size in y (the resolution in y)
X_f ← x_0 + Dem_res_x × r_n
Y_f ← y_0 + Dem_res_y × c_n
xGrid ← Create an array of values in x axis from x_0 to X_f by steps of Dem_res_x
yGrid ← Create an array of values in y axis from x_0 to Y_f by steps of Dem_res_y
if the absolute value of Dem_res_x and the absolute value of Dem_res_y < 15
    Take the values of xGrid with index step of 2 and assign it to Xgrid
    Take the values of yGrid with index step of 2 and assign it to YGrid
    Take the values of Elev with index step of 2
else:

    Xgrid ← xGrid
    Ygrid ← yGrid
    Elev ← Elev

```

Mesh griding Xgrid and Ygrid

3.2 Least square using DEM Algorithm.

//Inputs:

Sensor focal length 'c' \leftarrow user input
 Sensor width 'fw' \leftarrow user input
 Sensor height 'fh' \leftarrow user input
 No. of pixels of the sensor in x 'npx' \leftarrow user input
 No. of pixels of the sensor in y 'npy' \leftarrow user input
 Distance of surveying area in X 'X' \leftarrow extracted from Area shape file
 Distance of surveying area in Y 'Y' \leftarrow extracted from Area shape file
 Flight height 'h' \leftarrow user input
 Along track overlapping 'Rl' \leftarrow user input
 Cross track overlapping 'Rt' \leftarrow user input
 Collimation error 'scoll' \leftarrow user input and its default value is 1 in Pix
 Simulation points density 'delta' \leftarrow user input and its default value is 1 in m

//outputs:

Empirical error matrix in x direction
 Empirical error matrix in y direction
 Empirical error matrix in z direction
 Theoretical error matrix in x direction
 Theoretical error matrix in y direction
 Theoretical error matrix in z direction

Footprint width 'W' $\leftarrow (fw * h) / c$
 Footprint height 'H' $\leftarrow (fh * h) / c$

Ground Sample Distance using W 'GSDw' $\leftarrow W / npx$
 Ground Sample Distance using H 'GSDh' $\leftarrow H / npy$

Baseline 'b' $\leftarrow (1 - Rl) * H$
 interaxie 'i' $\leftarrow (1 - Rt) * W$

No. of strips in y 'nstrip_y' $\leftarrow \text{ceil}(Y / b)$
 No. of strips in x 'nstrip_x' $\leftarrow \text{ceil}(X / i)$

Real baseline 'b_real' $\leftarrow Y / nstrip_y$
 Real interaxie 'i_real' $\leftarrow X / nstrip_x$

Real Along track overlapping 'Rl_real' $\leftarrow 1 - b_real / H$
 Real cross track overlapping 'Rt_real' $\leftarrow 1 - i_real / W$

The x coordinate of the camera position in GCS 'xo' \leftarrow range from min of x + i_real/2 to max of x with step of i_real

The y coordinate of the camera position in GCS 'yo' \leftarrow range from min of y + b_real/2 to max of y with step of b_real

mesh grid x_0 and y_0

Numbering grid point 'ptName' \leftarrow matrix of the same dimensions as XGrid its value with the values from 0: the length of Xgrid

Create a flight path double array matrix 'flpath' with dimension of [nstrip_x* nstrip_y , 2]

for i from 0 to the no of strips in x

fill the first column of flpath from first element to nstrip_y with $x_0(i)$

if y_0 is odd:

fill the second column with the range of nstrip_y with flipping y_0

else:

fill the second column with the range of to nstrip_y with y_0

end for

Create simulation X coordinates of a grid 'xGrid' \leftarrow range from $0+\delta/2$ to $X-\delta/2$ with a step of δ

Create simulation Y coordinates of a grid 'yGrid' \leftarrow range from $0+\delta/2$ to $Y-\delta/2$ with a step of δ

Mesh grid xGrid and yGrids

Create a matrix of zeros with the same dimension of yGrid \leftarrow over_y

for i in range from 0 to nstrip_y*nstrip_x

$x_{siGrid} \leftarrow (XGrid - X_0(i))/h*c$

$\eta_{Grid} \leftarrow (YGrid - y_0(i))/h*c$

if the absolute value of x_{siGrid} less than or equal $fw/2$ and η_{Grid} less than or equal $fh/2$

mask \leftarrow 1

else

mask \leftarrow 0

Vector of no of observed point 'pt_obs' \leftarrow vector of [pt_obs; pt_name of where all mask values =1]

Vector of no of image containing the point 'im_obs' \leftarrow vector of [im_obs; i*mask of where all mask values =1]

observed xsi 'xsi_obs' \leftarrow vector of [xsi_obs; x_{siGrid} where all mask values =1]

observed eta 'eta_obs' \leftarrow vector of [η_{obs} ; η_{Grid} where all mask values =1]

end for

$x_{si_obs} \leftarrow x_{si_obs} + scoll * (fw/np_x) * \text{random matrix has the same size of } x_{si_obs}$

$\eta_{obs} \leftarrow \eta_{obs} + scoll * (fw/np_x) * \text{random matrix has the same size of } \eta_{obs}$

Create sparse matrix A of size $2 * \text{the length of pt_obs}, 3 * \text{no of grid points}$

The values in the couples (0: the length of pt_obs , pt_obs) \leftarrow c

Update as well the couples (0: the length of pt_obs , pt_obs+2* no of grid points) \leftarrow xsi_obs
 Update as well the couples ((the length of pt_obs+1 to 2* the length of pt_obs , pt_obs+ no of grid points) \leftarrow c
 Update as well the couples ((the length of pt_obs+1 to 2* the length of pt_obs , pt_obs+ 2*no of grid points) \leftarrow eta_obs
 Observation vector 'yo' \leftarrow [xsi_obs *Zo+c*Xo for each im_obs; eta_obs *Zo+c*Yo for each im_obs]
 Normal matrix 'N' \leftarrow transpose of A matrix * the A matrix
 Perform the LU decomposition inverse for Normal matrix 'N'
 Normal term tn \leftarrow transpose of A *yo
 Extract the estimated values of X.
 Extract the estimated values of Y.
 Extract the estimated value of Z.
 Calculate the residuals vector.
 Calculate the posterior variance.



Compute The Flight Path
(Sort The Couple X And Y According To The Drone Path)
Algorithm

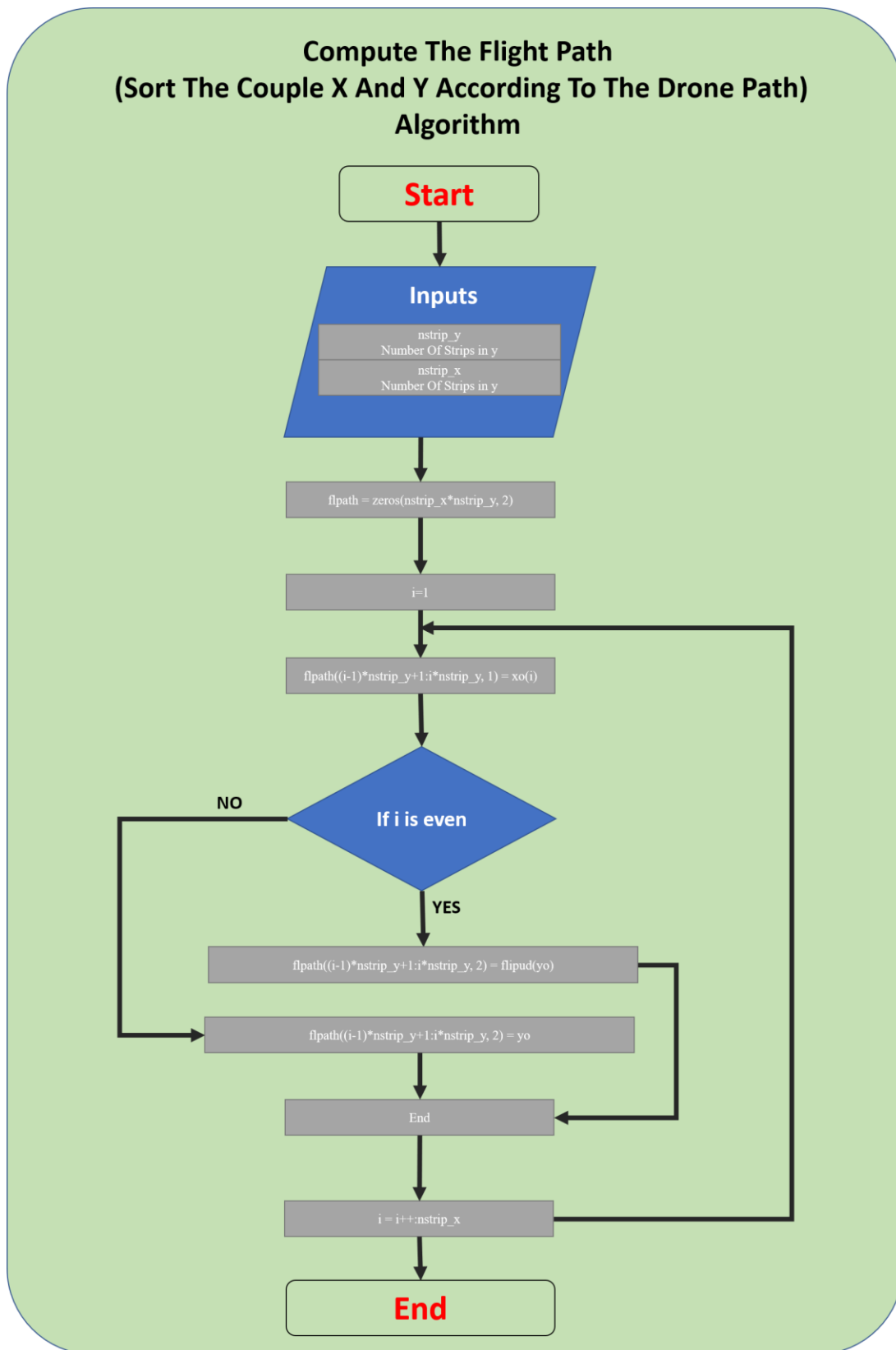


Figure 2Flight Path computation

Map Of The Number Of Images From Which Each Point Is Seen Algorithm

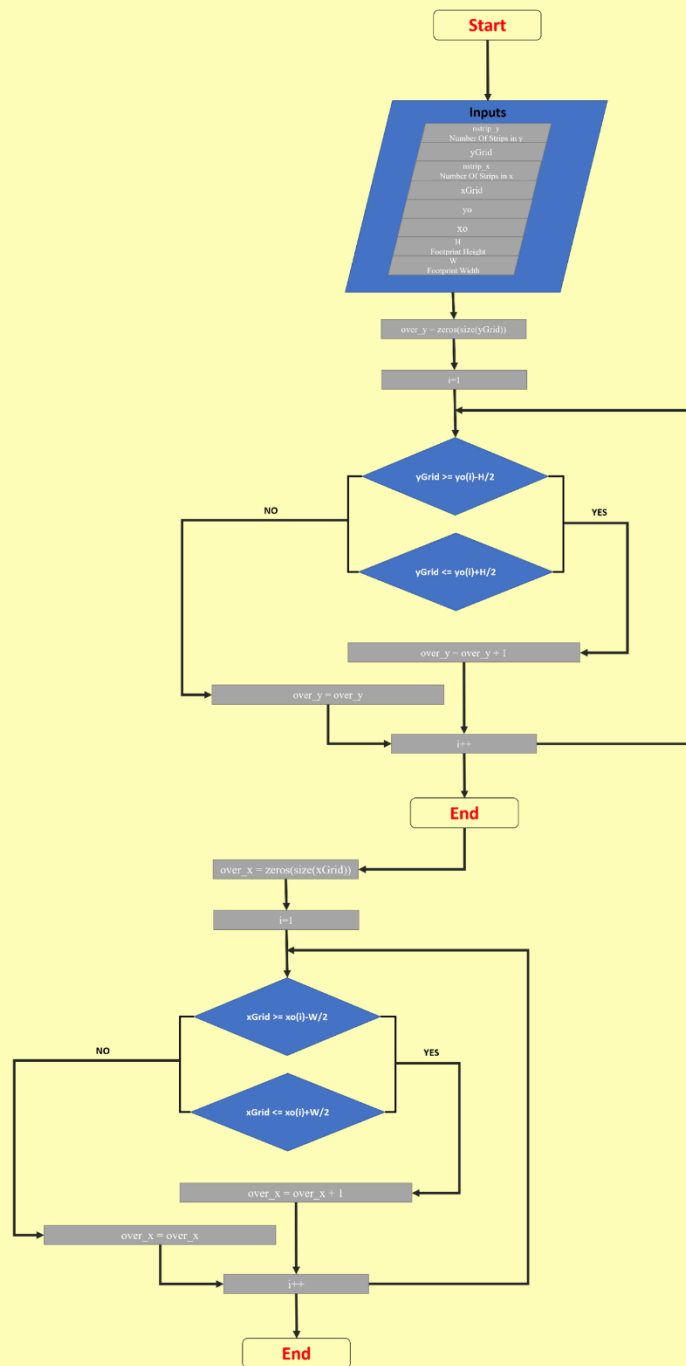


Figure 3 Map of number of images containing each Grid point.

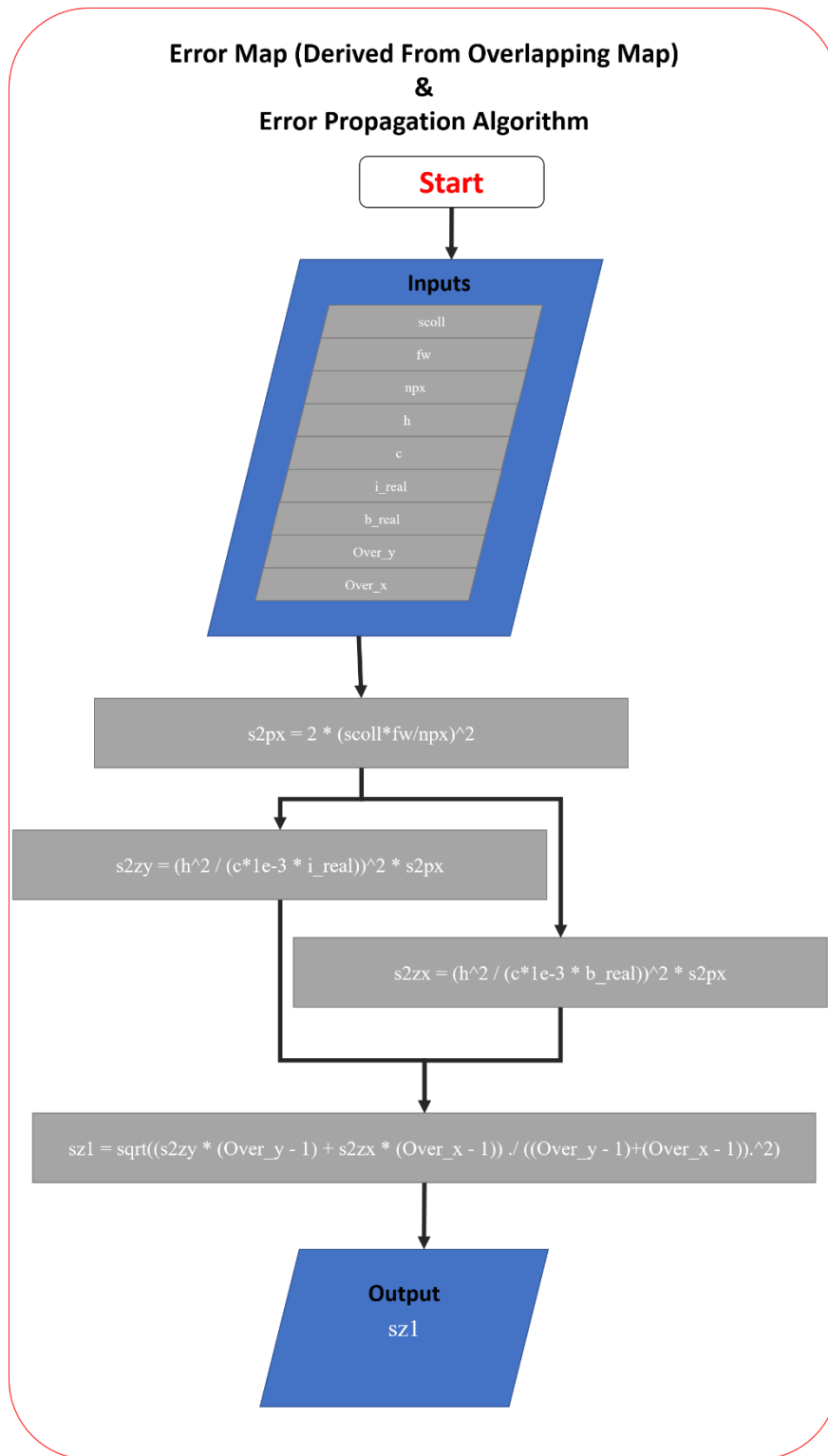


Figure 4 Error map calculation for the Normal Case Algorithm.

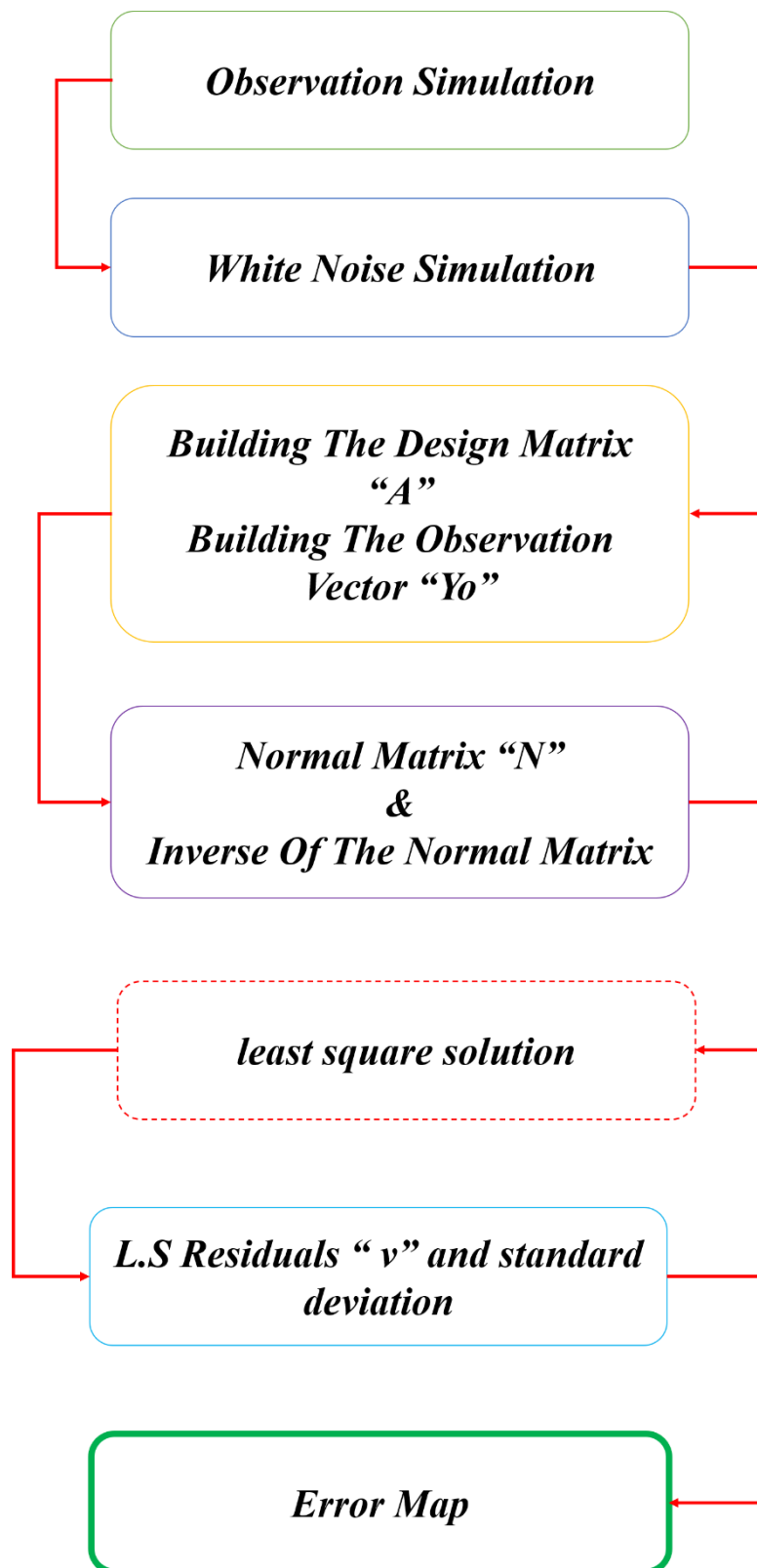


Figure 5 Flowchart for Least square using simulation data Algorithm.

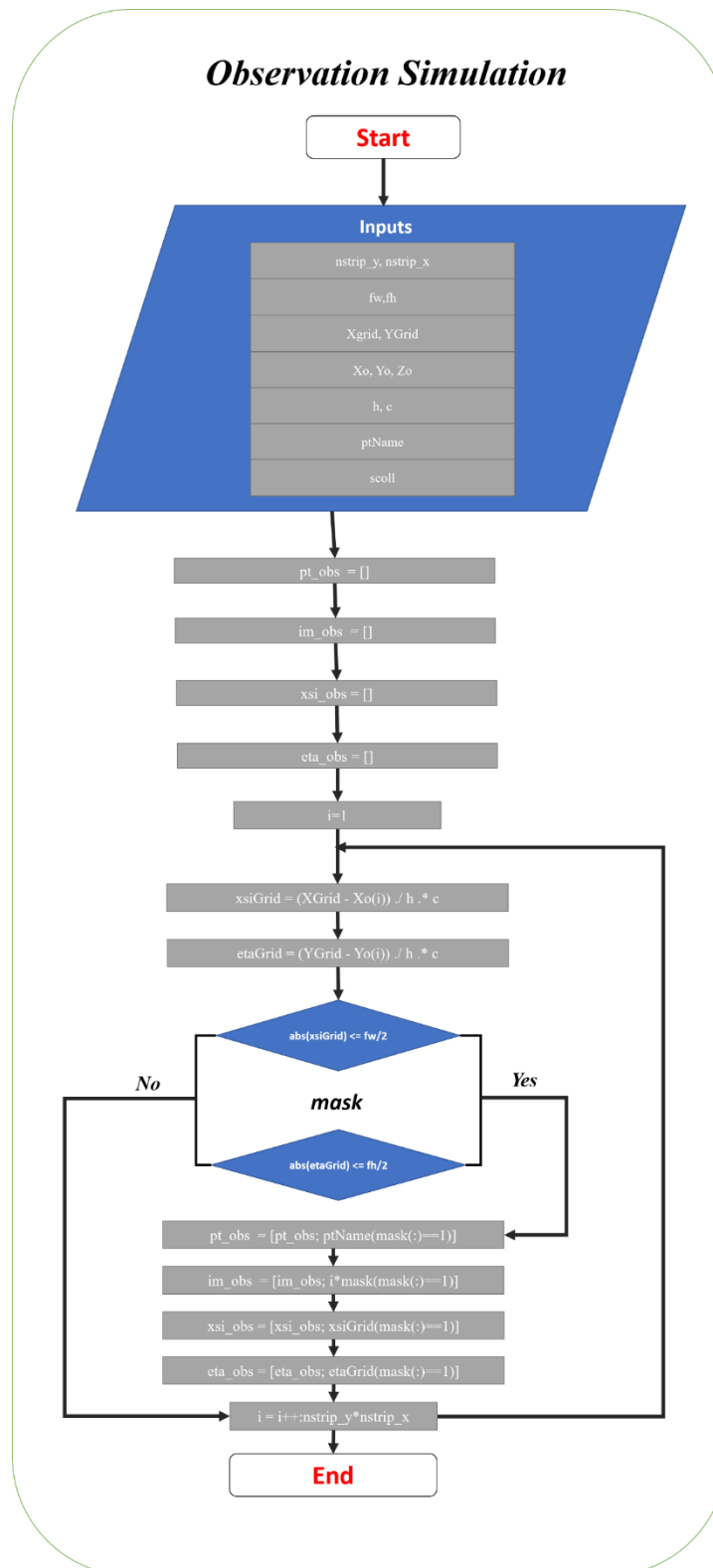


Figure 6 Simulation of the observation flowchart.

White Noise Simulation

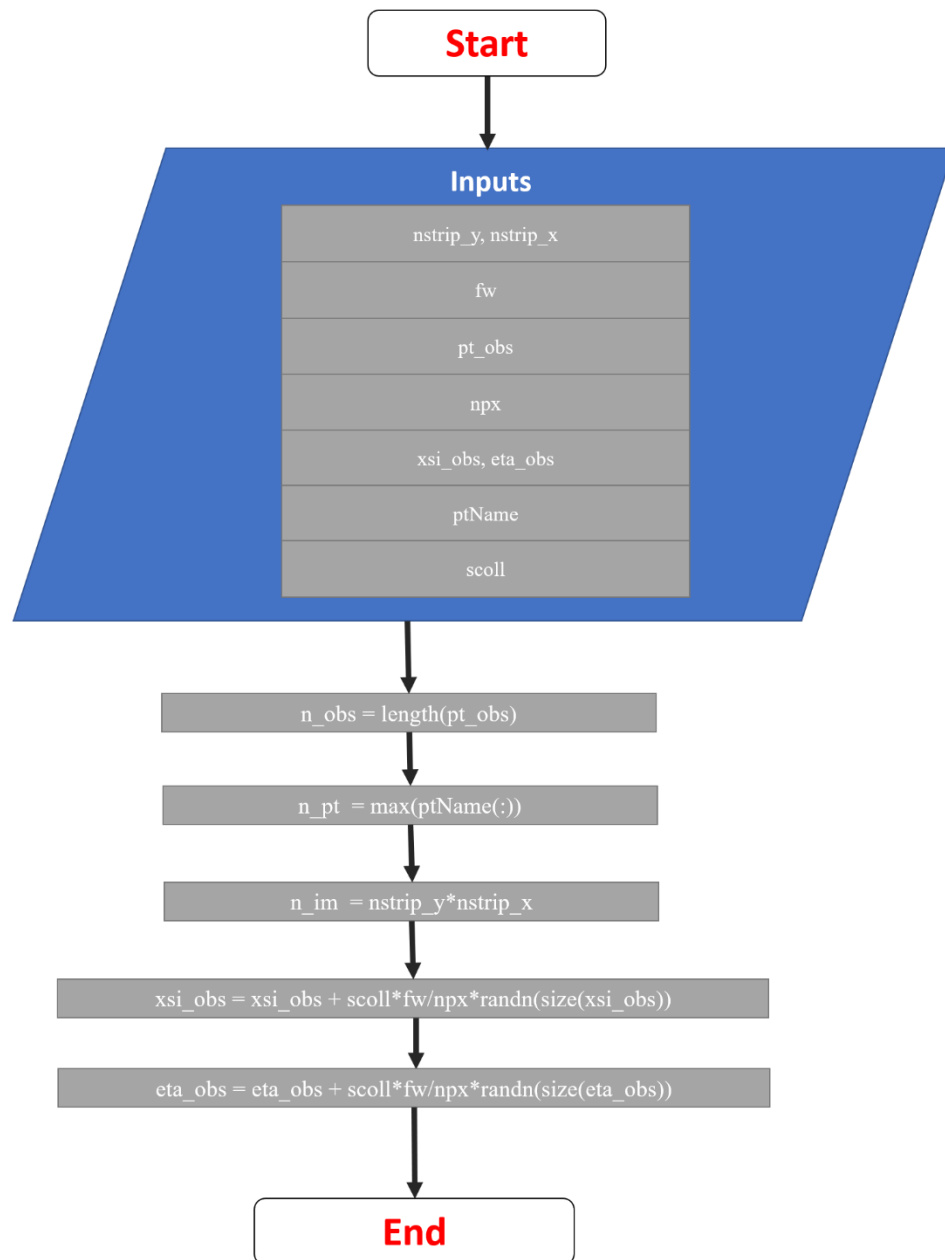


Figure 7 Adding white noise for simulation points.

***Building The Design Matrix
“A”
Building The Observation Vector “Yo”***

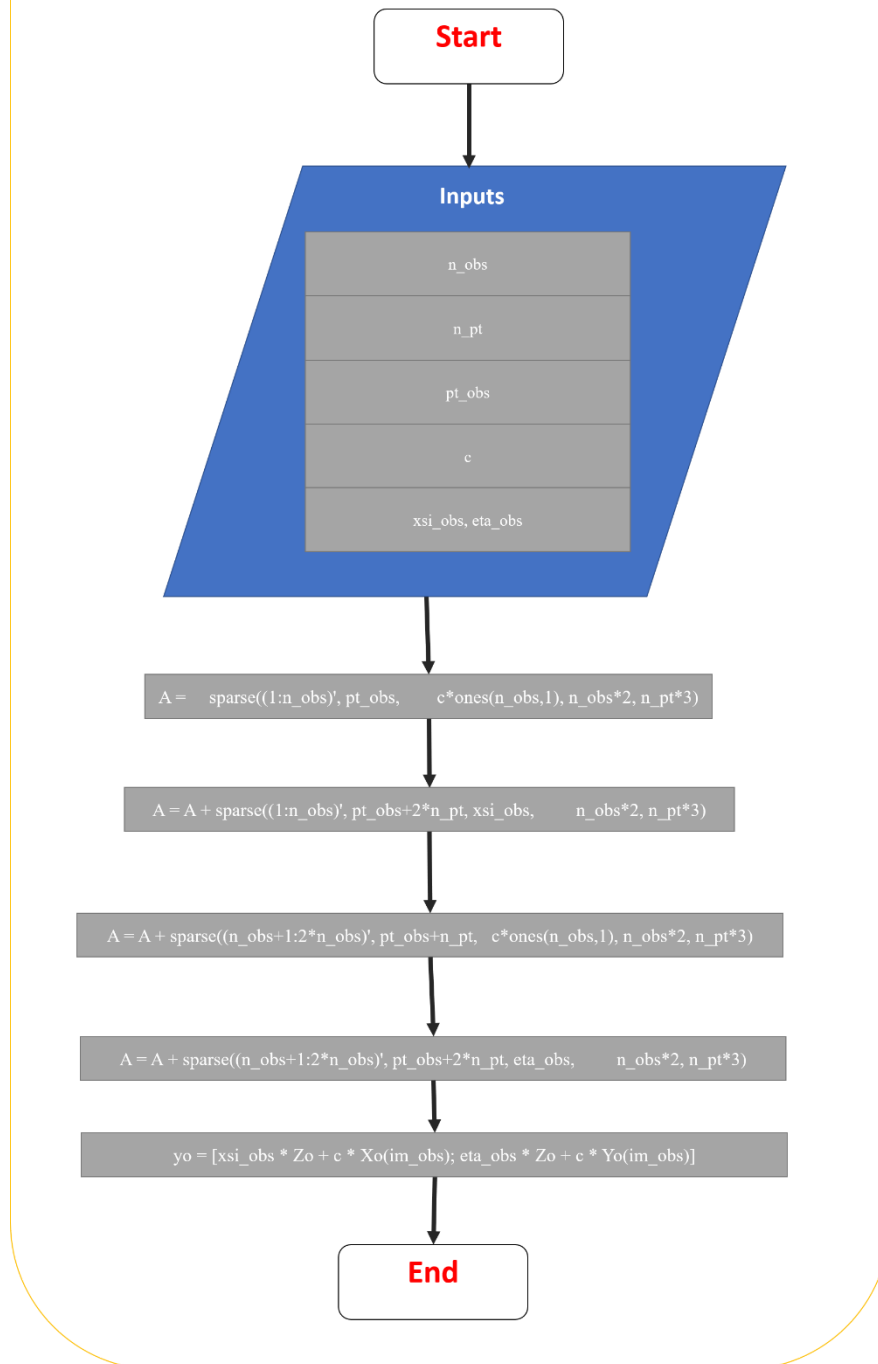


Figure 8 A matrix and Observation vector Y0 creation

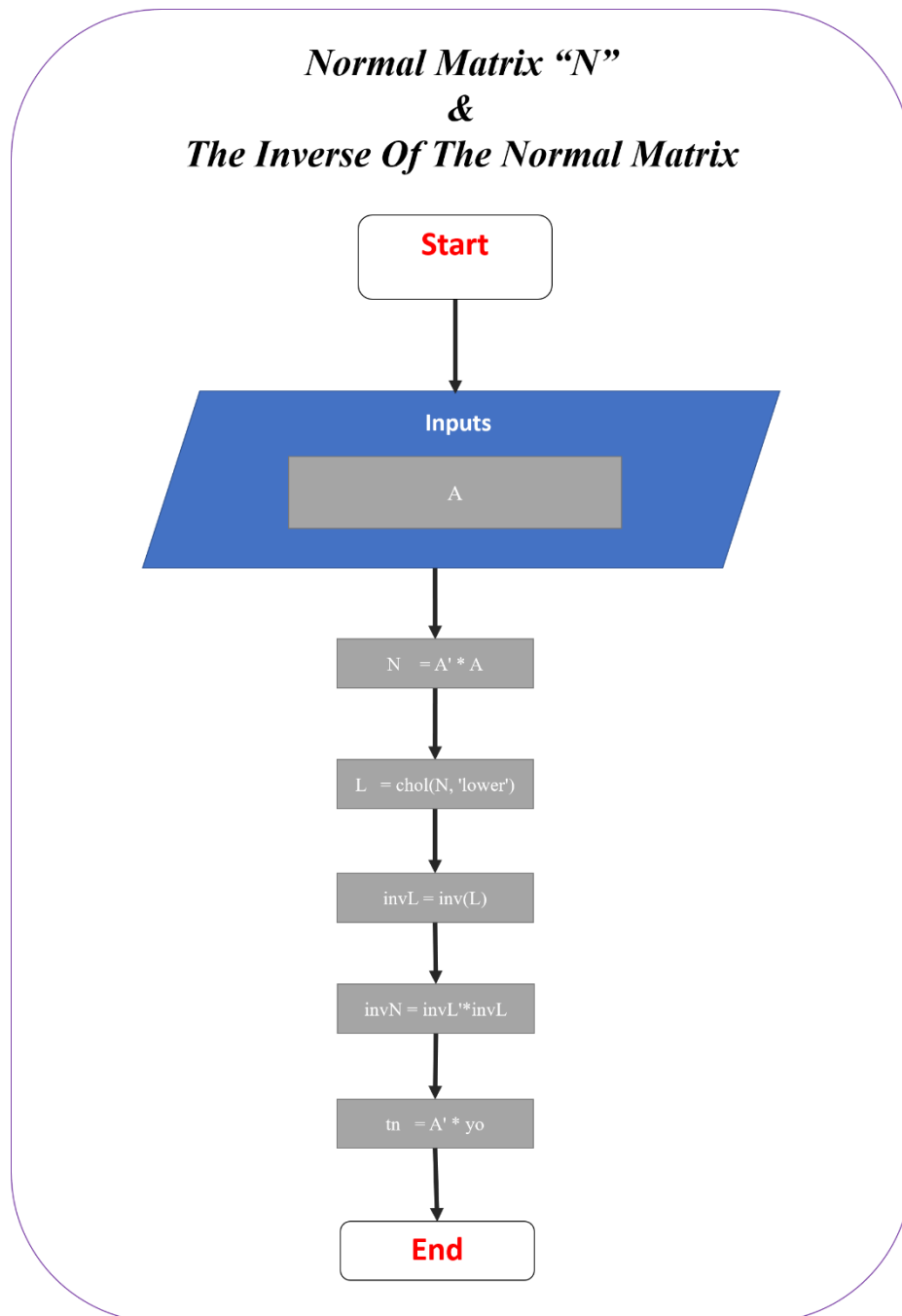


Figure 9 Normal matrix calculation and inversion.

Least Square Solution

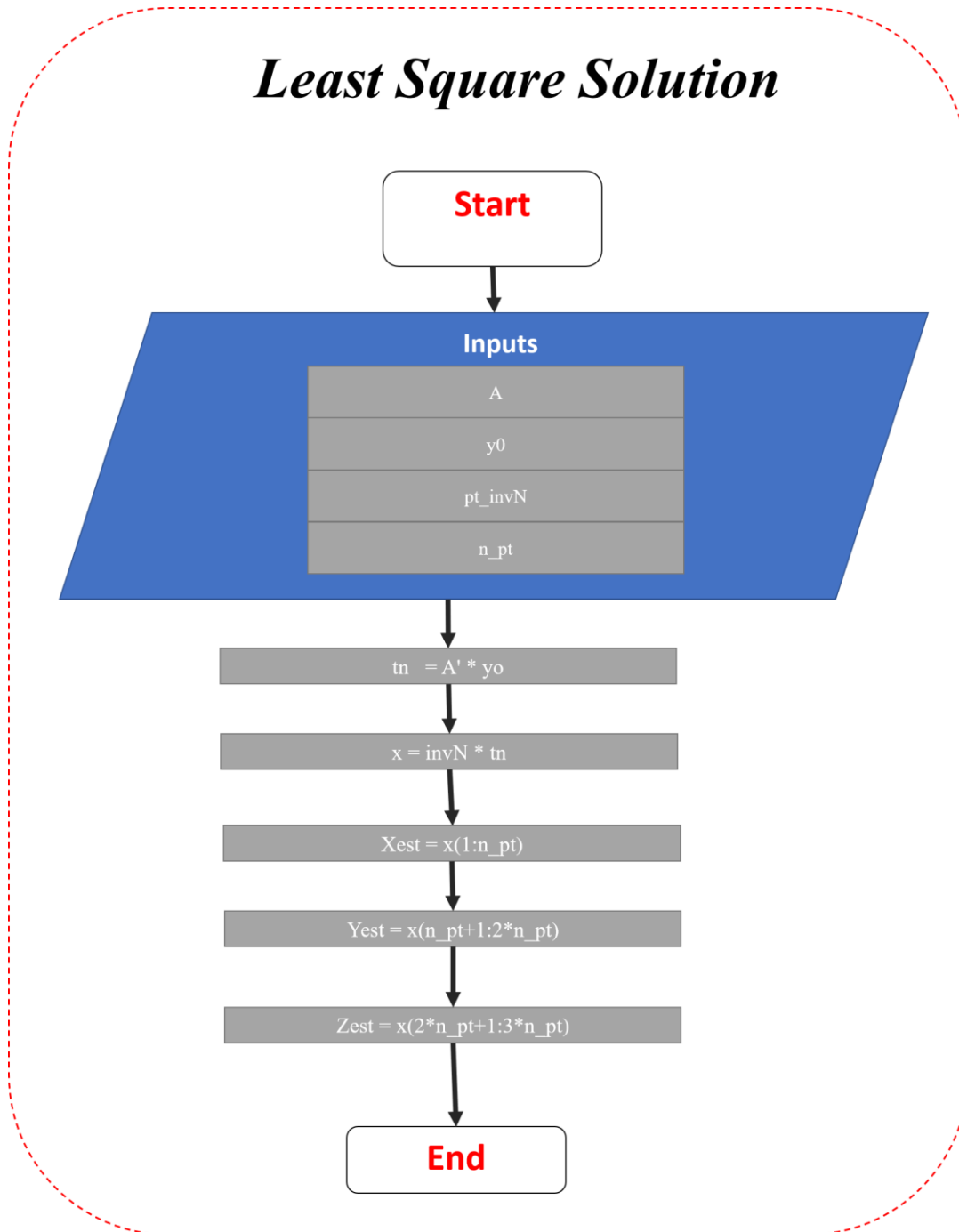


Figure 10 Least square solution.

L.S Residuals “v” and standard deviation

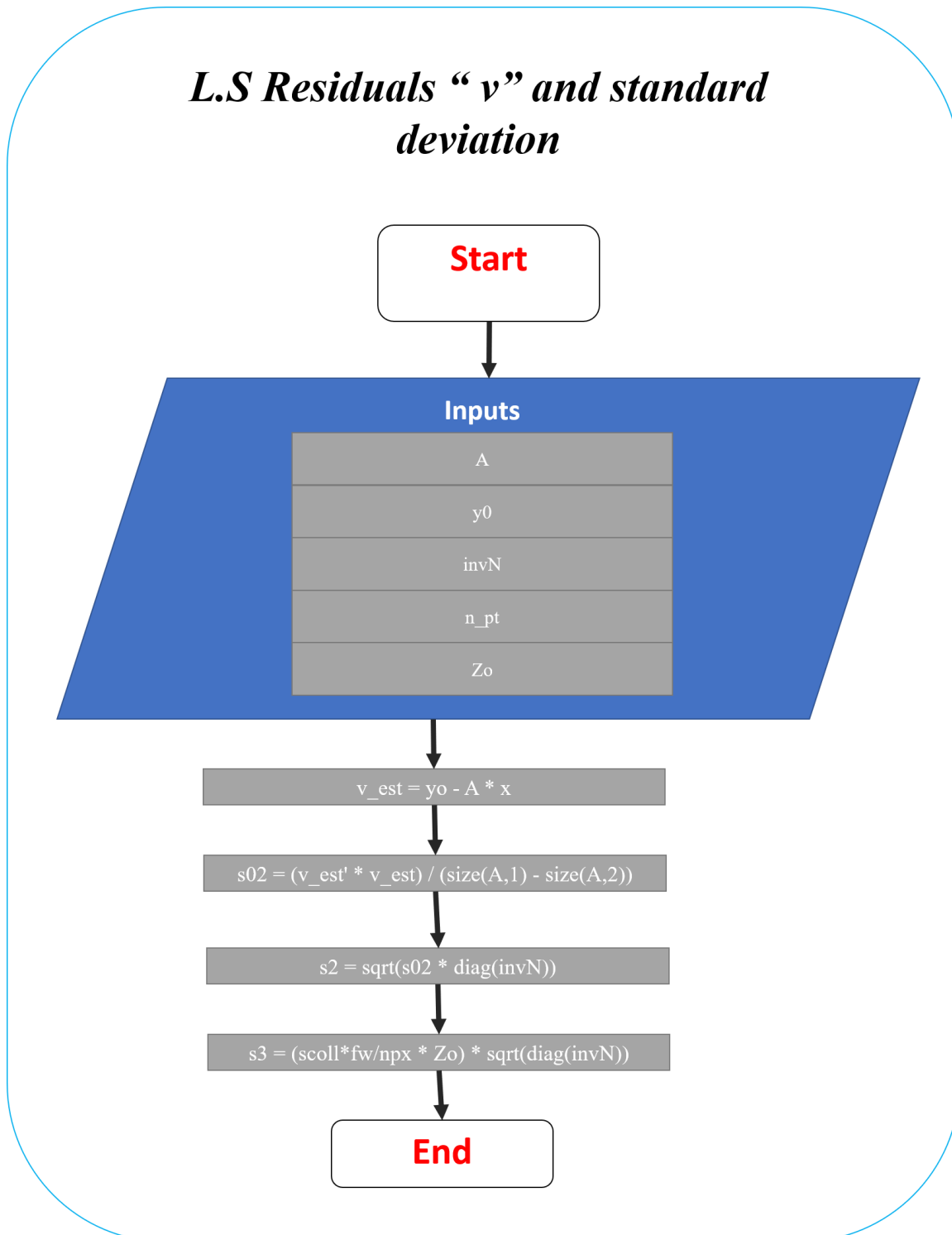


Figure 11 Residuals and standard division calculation

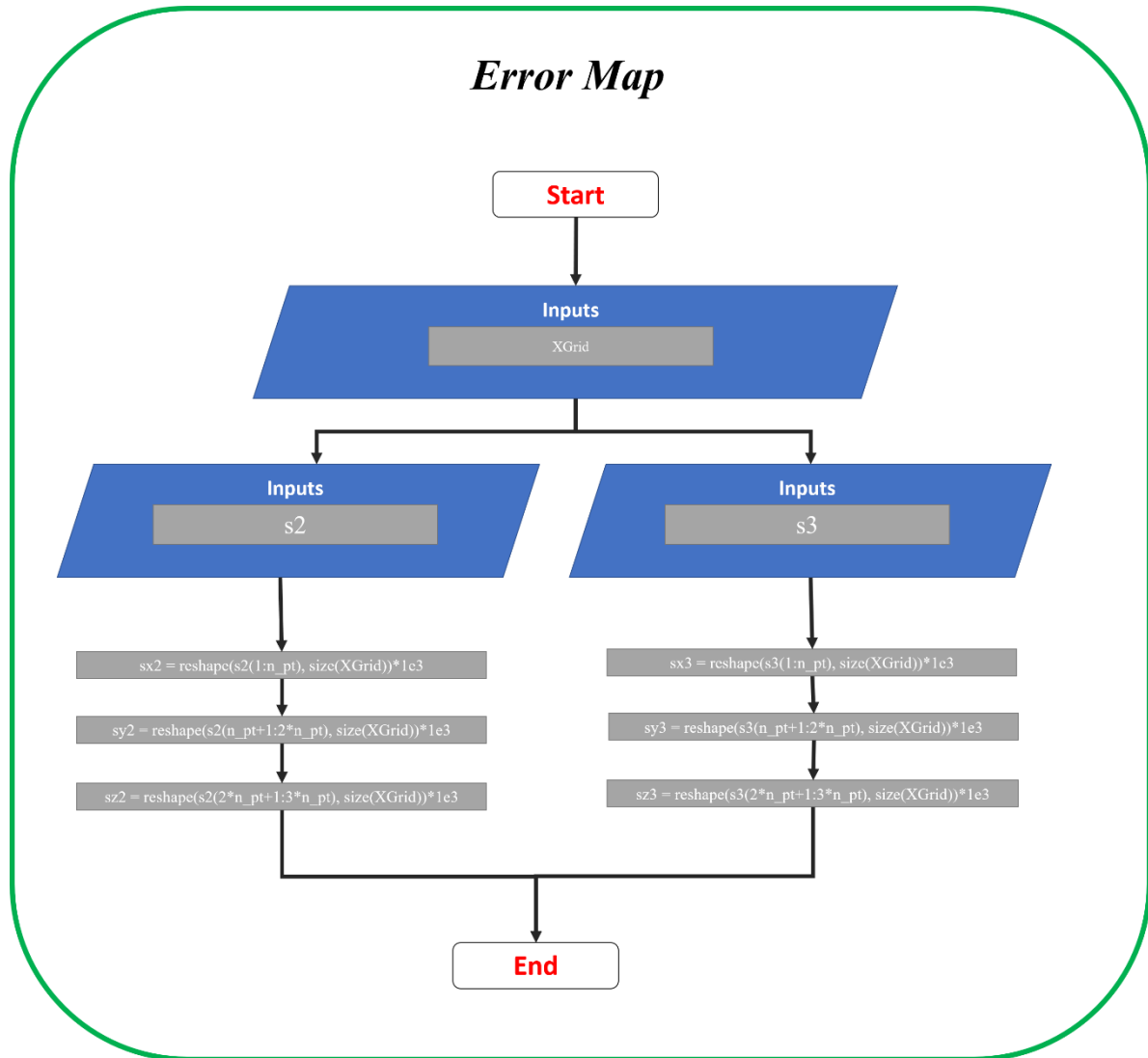


Figure 12 Error map Generation