MA5810: Introduction to Data Mining

Week 3; Collaborate Session 1: Logistic Regression

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Housekeeping

- Collaborate 1 = Wednesdays 6-7pm (Martha)
- Collaborate 2 = Thursdays 7-8pm (Hongbin)

For my Collaborate Sessions, you can get the **slides & R code** for each week here:

https://github.com/MarthaCooper/MA5810



Assignment 1 Q1

Explain why you chose the algorithm based on:

- 1) The algorithm assumptions;
- 2) How your data relates to those assumptions.

The question is **not** about calculating a confusion matrix or ROC. You do not need to do that!

Subject: MA5810 Intro to Data Mining

MA5810 Learning Outcomes

- 1. Overview of Data Mining and Examples
- 2. Unsupervised data mining methods e.g. clustering and outlier detection;
- 3. Unsupervised and supervised techniques for dimensionality reduction;
- 4. Supervised data mining methods for pattern classification (Today = Logistic Regression);
- 5. Apply these concepts to real data sets using R (Today).

Today's Goals

- Understand the background behind Logistic Regression
- Apply Logistic Regressions to real datasets using R
- Understand the pros and cons of Logistic Regression

Linear Regression Review

• The simple linear regression model is:

$$Y = \beta_0 + \beta_1 X + \epsilon$$

Where

- ullet Y is the dependent variable
- ullet X is the independent variable
- eta_0 is the intercept (Y when X=0)
- eta_1 is the slope of the regression line
- ϵ is the error term

Multiple Linear Regression Review

ullet Multiple regression with k independent variables

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_k X_k + \varepsilon$$

- When interpreting one of the slopes in multiple regression model, we should take into account the effect of the other variables
- ullet For instance, eta_1 represents the change in Y per 1 unit change in X_1 , holding other variables (X_2,\ldots,X_k) constant

Generalised Linear Models & Classification

- ullet GLM: Appropriate when Y isn't normally distributed but is in the exponential family of distributions
- In classification where Y is binomial (or multinomial)
- Given these features, does this sample belong to class A or B?

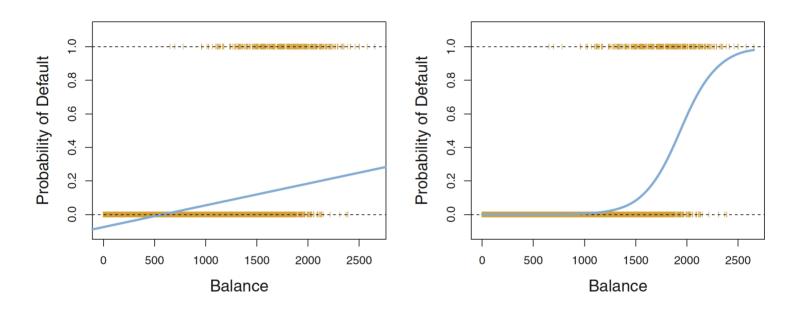
```
cancer \in \{yes, no\} credit\ card \in \{defalt, not\ default\} win\ \in \{yes, no\} drug\ \in \{survived, not\ survived\}
```

Logistic Regression

- Binomial family Generalised Linear Model
- ullet Models the probability that Y belongs to a particular category

Logistic Regression

- Binomial family Generalised Linear Model
- Models the probability that a subject belongs to a particular category

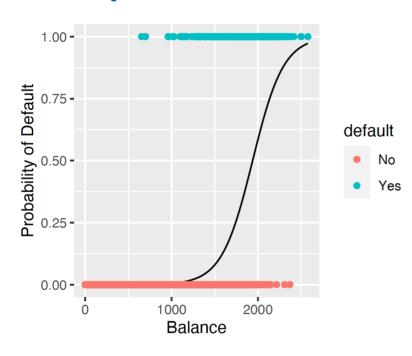


Problems with Linear Regression for Classification

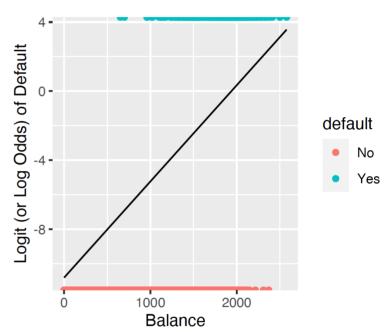
- Some values are outside [0,1]
- For multinomial classification, the order and interval between classes would be considered important and meaningful

The Logistic Model

Probability



Logit or Log Odds



The Logistic Model

Let P(Y=1|X) be the probability that Y=1 given $X=(X_1,\ldots,X_k)$

Probability

$$P(Y=1|X_1,\ldots,X_k)=rac{e^{eta_0+eta_1X_1+\ldots+eta_kX_k}}{1+e^{eta_0+eta_1X_1+\ldots+eta_kX_k}}$$

- where e is the Euler's number.
- This function means that $0 \leq P(Y=1|X) \leq 1$

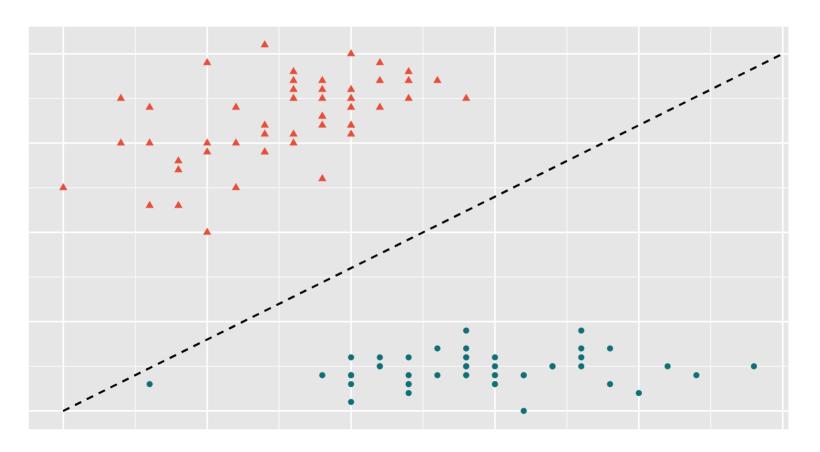
Logit (Log Odds)

$$\log(\frac{P(Y=1|X_1,\ldots,X_k)}{1-P(Y=1|X_1,\ldots,X_k)}) = \beta_0 + \beta_1 X_1 + \ldots + \beta_k X_k$$

- ullet Where log is the natural log, \log_e
- Interpretation: eta_1 represents the change in \log odds of Y per 1 unit change in X_1 , holding other variables (X_2,\ldots,X_k) constant

Estimating the coefficients

Maximum Likelihood



Logistic Regression Pros and Cons

Pros

- Identify which features are important for classification
- Interpret how important each feature is for classification

Cons

- Doesn't perform well if the decision boundary isn't linear
- Two groups (although extensions make more possible)

Logistic Regression in R

```
#load data
library(ISLR, warn.conflicts = F, quietly = T) #for data
library(caret, warn.conflicts = F, quietly = T) #for splitting the data
library(dplyr, warn.conflicts = F, quietly = T) #for piping
data("Default") #credit card default data from ISLR
str(Default)
#split into training (80%) and test
split <- createDataPartition(Default$default, p = 0.8, list = F)</pre>
train <- Default[split, ]</pre>
test <- Default[-split, ]
c(nrow(train), nrow(test)) # print number of observations in test vs. to
table(train$default) %>% prop.table() # Proportions of people that default)
#Train the model to predict the likelihood of default status based on ci
def logmod1 <- glm(default ~ balance, data = train, family = "binomial")</pre>
```

Interpretting the coefficients

summary(def_logmod1)\$coef #interpret the coefficients

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -10.750888865 0.4111675862 -26.14722 1.059975e-150
## balance 0.005563878 0.0002505912 22.20301 3.212218e-109
```

- β_0 : Log odds
- β_1 : Log odds ratio

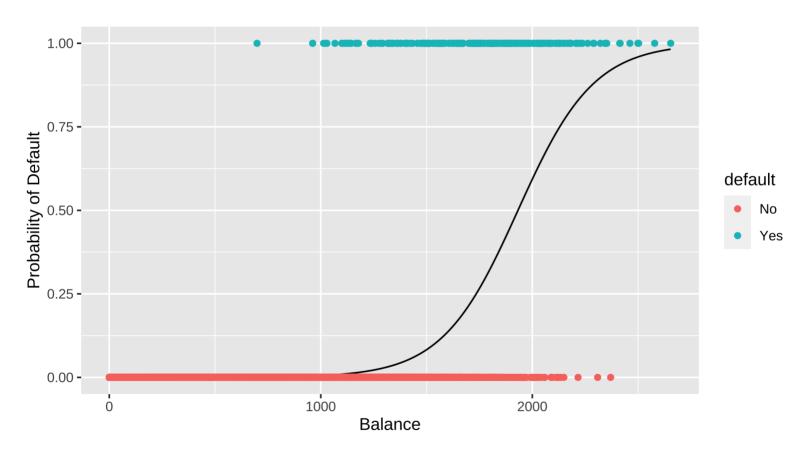
Making predictions in R

• make predictions based on training data

```
lodds <- predict(def_logmod1, type = "link")#log odds
preds_lodds = ifelse(lodds > 0, "Yes", "No") #using log odds
confusionMatrix(as.factor(preds_lodds), train$default) #confusion matrix
```

Plot the model

• We are aiming for a plot like this:



Plot the model

```
def logmod1$coef #look at coefs
#save coefficients
b0 <- def logmod1$coef[1] #beta0
b1 <- def logmod1$coef[2] #beta1
#calculate probabilities
x range <- seq(from = min(train$balance), to = max(train$balance)) #range
#calculate the logits
default logits <- b0 + b1*x range
#calculate probabilities to plot
default probabilities <- exp(balance logits)/(1 + exp(balance logits))
probabilities to_plot <- data.frame("balance" = x_range,</pre>
                                     "probabilitiy of default" = default
ggplot(probabilities to plot, aes(x = balance, y = probabilitiy of defailed)
  geom line()+ #plot model
  geom point(data = train, aes(x = balance,
                               v = ifelse(default == "Yes", 1, 0),
                               colour = default))+#add training data
  xlab("Balance")
```

Making predictions in R

• make predictions based on test data

```
test_lodds <- predict(def_logmod1, newdata = test, type = "link") #logis
test_preds_lodds = ifelse(test_lodds > 0, "Yes", "No") #using logits
confusionMatrix(as.factor(test_preds_lodds), test$default) #confusion ma
```

Extra reading

- Chapter 4 of James et al., ISLR
- Chapter 10 of David Dalpiaz, R for Statistical Learning

References

- James et al., ISLR
- David Dalpiaz, R for Statistical Learning

Slides

• xaringhan, xaringanthemer, remark.js, knitr, R Markdown