Introduction to Uplift Modeling

Dr. Juan Orduz

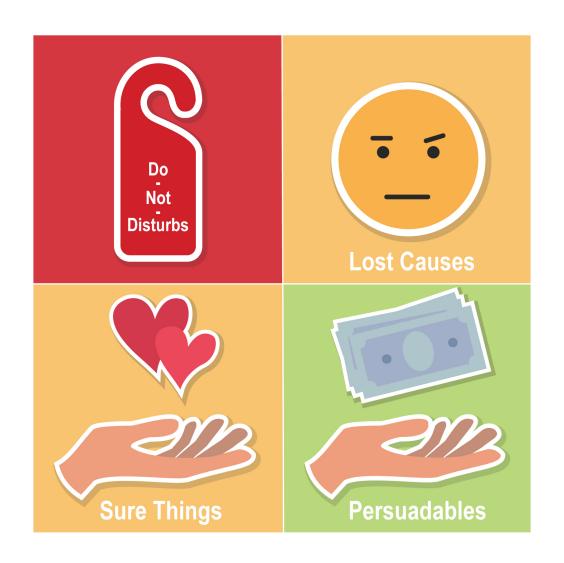
Mathematician & Data scientist

PyConDE & PyData Berlin 2022



Motivation

How can we optimally select customers to be treated by marketing incentives?



We can not send and not send incentives to the same customers at the same time



What is Uplift Modeling?

From Gutierrez, P., & Gérardy, J. Y. (2017). "Causal Inference and Uplift Modelling: A Review of the Literature"

- Uplift modeling refers to the set of techniques used to model the incremental impact of an action or treatment on a customer outcome.
- Uplift modeling is therefore both a Causal Inference problem and a Machine Learning one.

Conditional Average Treatment Effect

- Let Y_i^1 denote person i's outcome when it receives the treatment and Y_i^0 when it does not receive the treatment.
- We are interested in understanding the causal effect $Y_i^1-Y_i^0$ and the conditional average treatment effect $CATE=E[Y_i^1|X_i]-E[Y_i^0|X_i]$, where X_i is a feature vector of the i-th person.
- However, we can not observe them!

Uplift

Let W_i is a binary variable indicating whether person i received the treatment, so that

$$Y_{i}^{obs} = Y_{i}^{1}W_{i} + (1-W_{i})Y_{i}^{0}$$

Unconfoundedness Assumption

If we **assume** that the treatment assignment W_i is independent of Y_i^1 and Y_i^0 conditional on X_i , then we can estimate the CATE from observational data by computing the empirical counterpart:

$$\mathbf{uplift} = \widehat{CATE} = E[Y_i|X_i, W_i = 1] - E[Y_i|X_i, W_i = 0]$$

Estimating Uplift

- Meta Algorithms ← Today
- The Class Transformation Method
- Direct measurements (e.g. trees)

S-Learner

Step 1: Training

$$egin{pmatrix} x_{11} & \cdots & x_{1k} & w_1 \ dots & \ddots & dots & dots \ x_{11} & \cdots & x_{nk} & w_n \end{pmatrix} \stackrel{\mu}{\longrightarrow} egin{pmatrix} y_1 \ dots \ y_n \end{pmatrix}$$

Step 2: Uplift Prediction

$$\widehat{ extbf{uplift}} = \hat{\mu} \left(egin{array}{cccc} x_{11} & \cdots & x_{1k} & 1 \ dots & \ddots & dots & dots \ x_{11} & \cdots & x_{mk} & 1 \end{array}
ight) - \hat{\mu} \left(egin{array}{cccc} x_{11} & \cdots & x_{1k} & 0 \ dots & \ddots & dots & dots \ x_{11} & \cdots & x_{mk} & 0 \end{array}
ight)$$

T-Learner

Step 1: Training

$$egin{array}{cccc} egin{pmatrix} x_{11} & \cdots & x_{1k} \ dots & \ddots & dots \ x_{11} & \cdots & x_{n_C k} \end{pmatrix} \stackrel{\mu_C}{\longrightarrow} egin{pmatrix} y_1 \ dots \ y_{n_C} \end{pmatrix} \ egin{pmatrix} X_{| ext{control}} \ egin{pmatrix} x_{11} & \cdots & x_{1k} \ dots & \ddots & dots \ x_{11} & \cdots & x_{n_T k} \end{pmatrix} \stackrel{\mu_T}{\longrightarrow} egin{pmatrix} y_1 \ dots \ y_{n_T} \end{pmatrix} \ egin{pmatrix} X_{| ext{treatment}} \end{array}$$

T-Learner

Step 2: Uplift Prediction

$$\widehat{ extbf{uplift}} = \hat{\mu}_T \left(egin{array}{ccc} x_{11} & \cdots & x_{1k} \ dots & \ddots & dots \ x_{11} & \cdots & x_{mk} \end{array}
ight) - \hat{\mu}_C \left(egin{array}{ccc} x_{11} & \cdots & x_{1k} \ dots & \ddots & dots \ x_{11} & \cdots & x_{mk} \end{array}
ight)$$

X-Learner

Step 1: Training: Same as T-Learner

Step 2: Compute imputed treatment effects

$$ilde{D}^T \coloneqq \left(egin{array}{c} y_1 \ dots \ y_{n_T} \end{array}
ight) - \hat{\mu}_C \left(egin{array}{ccc} x_{11} & \cdots & x_{1k} \ dots & \ddots & dots \ x_{11} & \cdots & x_{n_Tk} \end{array}
ight)$$

$$ilde{D}^C\coloneqq\hat{\mu}_T\left(egin{array}{ccc} x_{11} & \cdots & x_{1k} \ draingle & draingle & draingle \ draingle & \ddots & draingle \ x_{11} & \cdots & x_{n_Ck} \end{array}
ight)-\left(egin{array}{c} y_1 \ draingle \ y_{n_C} \end{array}
ight)$$

X-Learner

Step 3: Train with different targets

$$egin{array}{cccc} egin{pmatrix} x_{11} & \cdots & x_{1k} \ dots & \ddots & dots \ x_{11} & \cdots & x_{n_C k} \end{pmatrix} \stackrel{ au_C}{\longrightarrow} egin{pmatrix} ilde{D}_1^C \ dots \ ilde{D}_{n_T}^C \end{pmatrix} \ egin{pmatrix} ilde{D}_{n_T}^T \ ilde{D}_{n_T}^T \end{pmatrix} \ egin{pmatrix} ilde{X}|_{ ext{treatment}} \end{pmatrix} \stackrel{ au_C}{\longrightarrow} egin{pmatrix} ilde{D}_1^T \ dots \ ilde{D}_{n_T}^T \end{pmatrix}$$

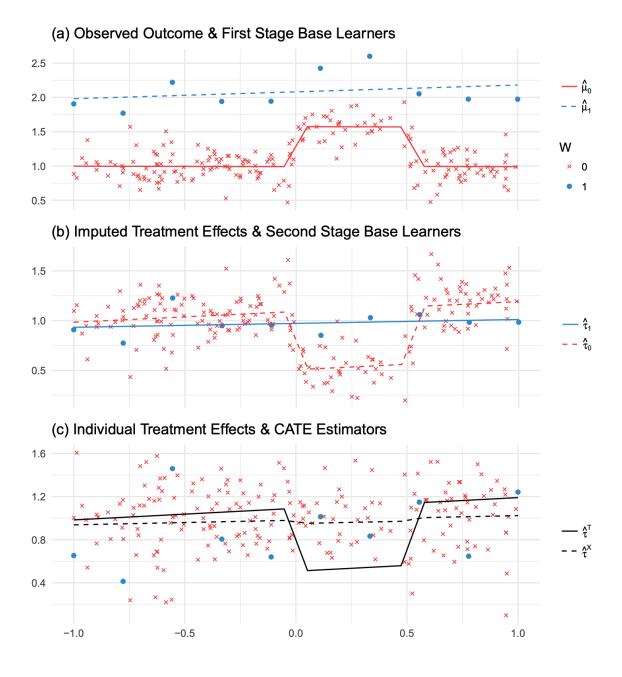
X-Learner

Step 4: Uplift Prediction

$$\widehat{ ext{uplift}} = g(x)\hat{ au}_C(x) + (1-g(x))\hat{ au}_T(x)$$

where $g(x) \in [0,1]$ is a weight function.

Intuition behind the X-Learner



Some python implementations

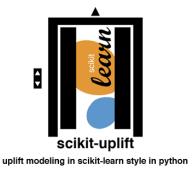
causalml



EconML



• scikit-uplift



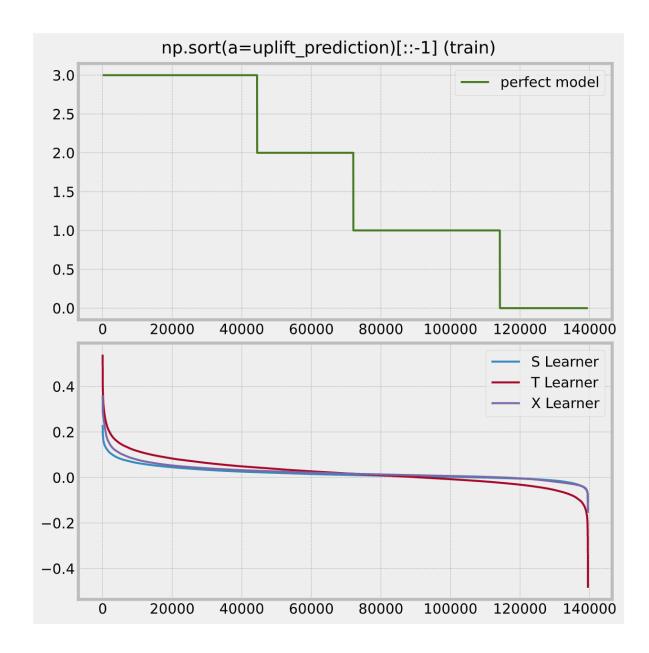
Python code: Example

```
from causalml.inference.meta import BaseTClassifier
from sklearn.ensemble import HistGradientBoostingClassifier
# define ml model
learner = HistGradientBoostingClassifier()
# set meta-model
t_learner = BaseTClassifier(learner=learner)
# compute ate
t_ate_lwr, t_ate, t_ate_upr = t_learner.estimate_ate(X=x, treatment=w, y=y)
# predict treatment effects
t_learnet.predict(X=x)
# access ml models
t_learner.models_c[1]
t_learner.models_t[1]
```

Perfect Uplift Model

A perfect model assigns higher scores to all treated individuals with positive outcomes than any individuals with negative outcomes.

```
# Control Responders
cr_num = np.sum((y_true == 1) & (treatment == 0))
# Treated Non-Responders
tn_num = np.sum((y_true == 0) & (treatment == 1))
summand = y_true if cr_num > tn_num else treatment
perfect_uplift = 2 * (y_true == treatment) + summand
```



Taken from Diemert, Eustache, et.al. (2020) "A Large Scale Benchmark for Uplift Modeling"

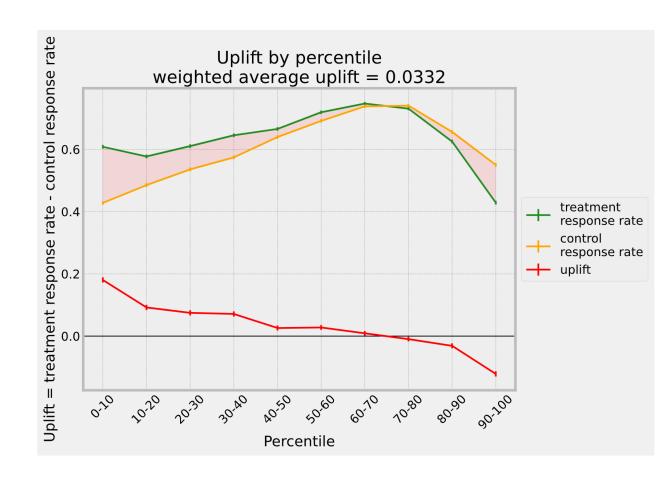
Uplift Evaluation: Uplift by percentile

- 1. Sort uplift predictions by decreasing order.
- 2. Predict uplift for both treated and control observations
- 3. Compute the average prediction per percentile in both groups.
- 4. The difference between those averages is taken for each percentile.

	n_treatment	n_control	response_rate_treatment	response_rate_control	uplift
percentile					
0-10	6870	7082	0.608297	0.427845	0.180452
10-20	6974	6978	0.577144	0.485096	0.092048
20-30	7082	6870	0.610421	0.535662	0.074758
30-40	7200	6751	0.645278	0.574137	0.071141
40-50	7086	6865	0.665538	0.639476	0.026062
50-60	6959	6992	0.719213	0.691362	0.027851
60-70	6955	6996	0.747088	0.738136	0.008952
70-80	7002	6949	0.730934	0.740538	-0.009604
80-90	6927	7024	0.624946	0.656179	-0.031233
90-100	6667	7284	0.428679	0.550110	-0.121431
total	69722	69791	0.636743	0.603531	0.033213

Uplift Evaluation: Uplift by percentile

A well performing model would have large values in the first percentiles and decreasing values for larger ones



Uplift Evaluation: Cumulative gain chart

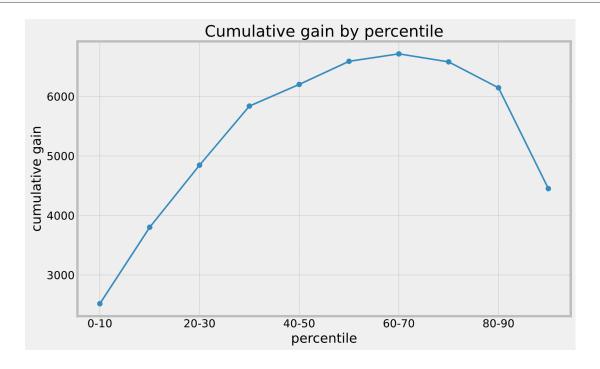
Predict uplift for both treated and control observations and compute the average prediction per decile (bins) in both groups. Then, the difference between those averages is taken for each decile.

$$\left(rac{Y^T}{N^T} - rac{Y^C}{N^C}
ight) (N^T + N^C)$$

- ullet Y^T/Y^C : sum of the treated / control individual outcomes in the bin.
- ullet N^T/N^C : number of treated / control observations in the bin.

Uplift Evaluation: Cumulative gain chart

```
(x["uplift"] * (x["n_treatment"] + x["n_control"])).cumsum()
```



- From this plot we see if the treatment has a global positive or negative effect and if they can expect a better gain by targeting part of the population.
- We can thus choose the decile that maximizes the gain as the limit of the population to be targeted.

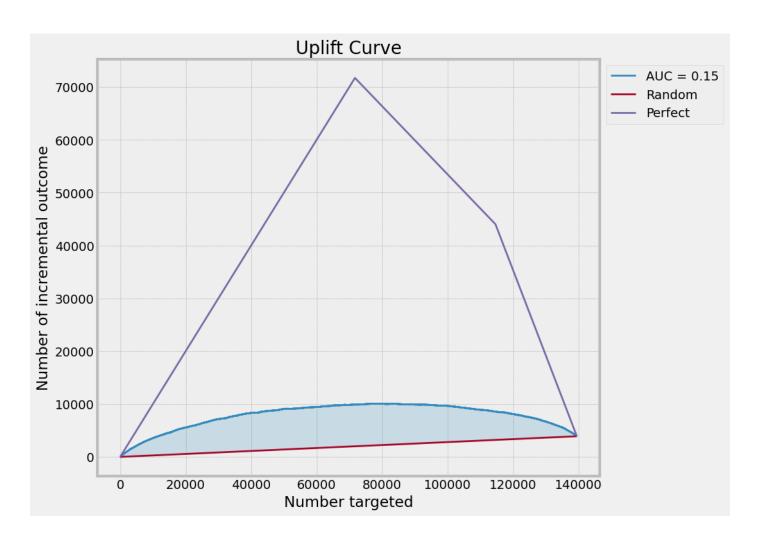
Uplift Metrics: Uplift Curve

We can generalize the cumulative gain chart for each observation of the test set:

$$f(t) = \left(rac{Y_t^T}{N_t^T} - rac{Y_t^C}{N_t^C}
ight) \left(N_t^T + N_t^C
ight)$$

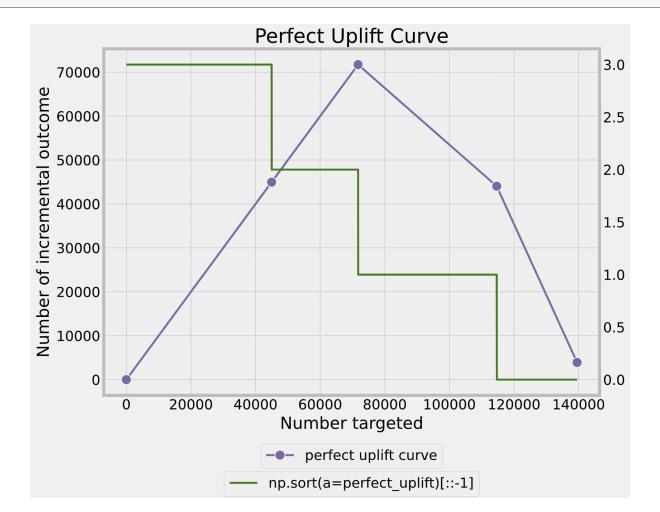
where the t subscript indicates that the quantity is calculated for the first t observations, sorted by inferred uplift value.

Uplift Metrics: Uplift Curve & AUC



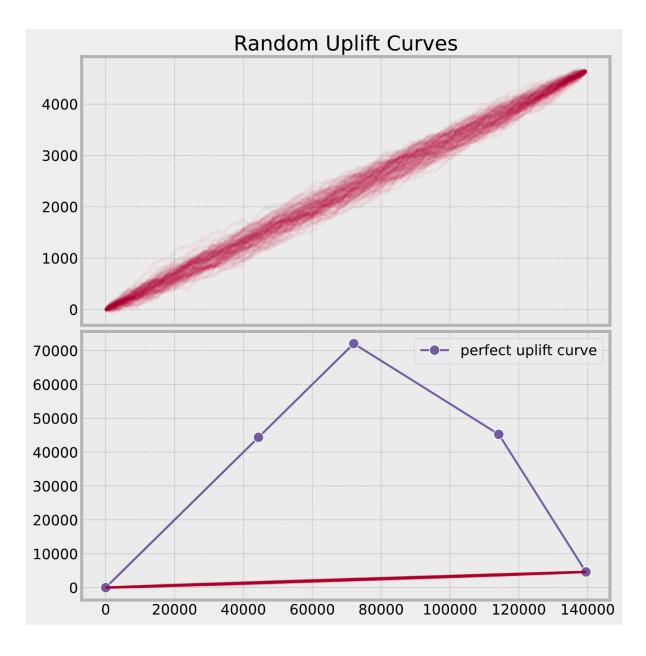
Perfect Uplift Curve

```
from sklift.metrics import uplift_curve
a, b = uplift_curve(y_true=y_true, uplift=perfect_uplift, treatment=treatment)
```



Random Uplift Curves

```
np.random.uniform(
    low=-1,
    high=1,
    size=(n, n_samples),
)
```



Data Collection

1. Randomly subset the customer base to create a representative model base.

Model Base

Customer Base

scikit-uplift

Demo

Notebook Link

References:

- Diemert, Eustache, et.al. (2020) "A Large Scale Benchmark for Uplift Modeling"
- Gutierrez, P., & Gérardy, J. Y. (2017). "Causal Inference and Uplift Modelling: A Review of the Literature"
- Karlsson, H. (2019) "Uplift Modeling: Identifying Optimal Treatment Group Allocation and Whom to Contact to Maximize Return on Investment"
- Sören, R, et.al. (2019) "Meta-learners for Estimating Heterogeneous Treatment Effects using Machine Learning"

Thank you!

More Info: juanitorduz.github.io

