LECTURE 5:COMMUNITY STRUCTURE IN NETWORKS

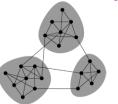
COMP4641: Social Information Network Analysis and Engineering

Announcement

- -
 - □ Project
 - 4 March: Group list and tentative title/topic
 - □ 15 March: Project proposal
 - 3 April: Project milestone report
 - 3 May: Final report
 - Study week?: Final presentation

Networks & Communities

□ We often think of networks "looking"



□ What lead to such conceptual picture?

Networks: Flow of Information

- How information flows through the network?
 - □ What structurally distinct roles do nodes play?
 - □ What roles do different links (short vs. long) play?
 - □ How people find out about new jobs?
 - Mark Granovetter, part of his PhD in 1960s
 - People find the information through personal contacts
 - But: Contacts were often acquaintances rather than close friends
 - This is surprising: One would expect your friends to help you out more than casual acquaintances
 - □ Why is it that acquaintances are most helpful?

Granovetter's Answer

- □ Two perspectives on friendships:
 - Structural: Friendships span different parts of the network
 - Interpersonal: Friendship between two people is either strong or weak
- □ Structural role: Triadic Closure



Which edge is more

If two people in a network have a friend in common there is an increased likelihood they will become friends themselves

Granovetter's Explanation

- Granovetter makes a connection between social and structural role of an edge
- □ First point:
 - □ Structurally embedded edges are also socially strong
 - Edges spanning different parts of the network are socially weak
- □ Second point:
 - The long range edges allow you to gather information from different parts of the network and get a jobak set
 - Structurally embedded edges are heavily redundant in terms of information access



Triadic Closure

☐ Triadic closure == High clustering coefficient

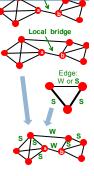
Reasons for triadic closure:

- $\ \square$ If B and $\mathcal C$ have a friend A in common, then:
 - B is more likely to meet C
 - (since they both spend time with A)
 - $\blacksquare B$ and C trust each other
 - (since they have a friend in common)
 - A has incentive to bring B and C together
 - lacksquare (as it is hard for A to maintain two disjoint relationships)
- □ Empirical study by Bearman and Moody:
 - Teenage girls with low clustering coefficient are more likely to contemplate suicide

Granovetter's Explanation

Define: Bridge edge

- □ If removed, it disconnects the graph
- □ <u>Define</u>: Local bridge
 - □ Edge of Span > 2 (Span of an edge is the distance of the edge endpoints if the edge is deleted. Local bridges with long span are like real bridges)
- □ <u>Define</u>: Two types of edges:
 - □ Strong (friend), Weak (acquaintance)
- □ Define: Strong triadic closure:
 - Two strong ties imply a third edge
- Fact: If strong triadic closure is satisfied then local bridges are weak ties!



Local Bridges and Weak ties

- Claim: If node satisfies Strong Triadic Closure and is involved in at least two strong ties, then any local bridge adjacent to must be a weak tie.
 - □ Proof by contradiction:
 - satisfies Strong
 Triadic Closure
 - Let be local bridge and a strong tie
 - Then must exist because of Strong Triadic Closure
 - But then is not





Tie strength in real data

- For many years the Granovetter's theory was not tested
 - But, today we have large who-talks-to-whom graphs:
 - Email, Messenger, Cell phones, Facebook
 - □ Onnela et al. 2007:
 - □ Cell-phone network of 20% of country's population
 - □ Edge strength: # phone calls

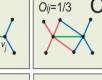
Neighborhood Overlap

□ Edge overlap:

$$O_{ij} = \frac{N(i) \cap N(j)}{N(i) \cup N(j)}$$

- □ N(i) ... a set of neighbors of node i
- Overlap = 0 when an edge is a local bridge







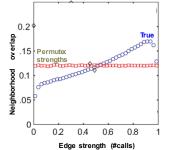


Phones: Edge Overlap vs. Strength

□ Cell-phone network

Observation:

- Highly used links have high overlap!
- Legend:
 - □ True: The data
 - Permuted strengths: Keep the network structure but randomly reassign edge strengths

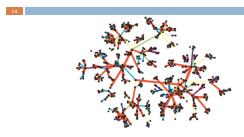


Real Network, Real Tie Strengths

□ Real edge strengths in mobile call graph

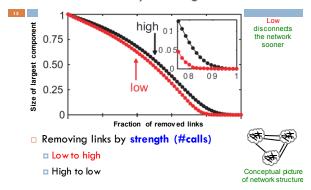
□ Strong ties are more embedded (have higher overlap)

Real Net, Permuted Tie Strengths

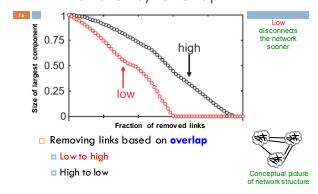


□ Same network, same set of edge strengths but now strengths are randomly shuffled

Link Removal by Strength

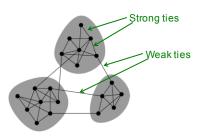


Link Removal by Overlap



Conceptual Picture of Networks

Granovetter's theory leads to the following conceptual picture of networks



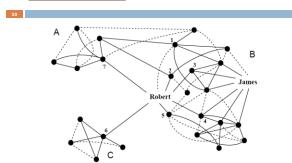
Facebook User's Tie Strength



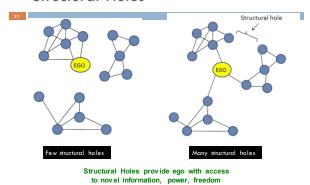
Four different views of a Facebook User's network neighborhood, show the structure of links corresponding respectively to all declared friendships, maintained relationships, one-way communication, and reciprocal communication

SMALL DETOUR: STRUCTURAL HOLES

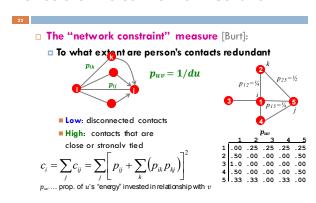
Small Detour: Structural Holes



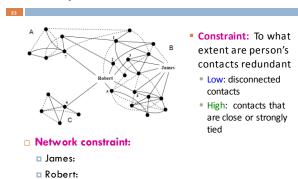
Structural Holes



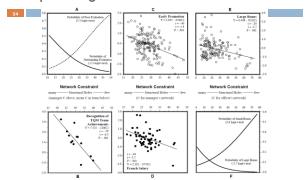
Structural Holes: Network Constraint



Example: Robert vs. James



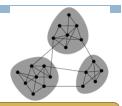
Spanning the Holes Matters





Network Communities

Granovetter's theory
(and common sense)
suggest that networks
are composed of
tightly connected
sets of nodes



□ Network communities:

Sets of nodes with lots of connections inside and few to outside (the rest of the network)

Finding Network Communities

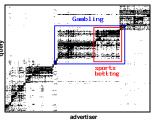
- How to automatically find such densely connected groups of nodes?
- Ideally such automatically detected clusters would then correspond to real groups
- □ For example:



Communities, clusters, aroups, modules

Micro-Markets in Sponsored Search

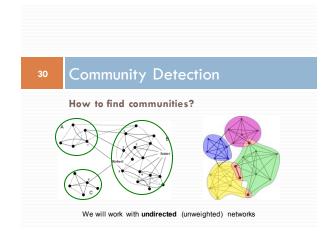
Find micro-markets by partitioning the "query x advertiser" graph:



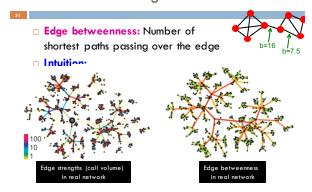
Social Network Data



- □ Zachary's Karate club network:
 - $\hfill \Box$ Observe social ties and rivalries in a university karate club
 - During his observation, conflicts led the group to split
 - Split could be explained by a minimum cut in the network



Method 1: Strength of Weak Ties



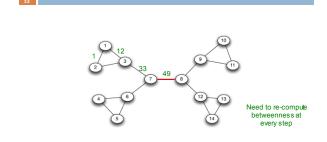
Method 1: Girvan-Newman

Divisive hierarchical clustering based on the notion of edge betweenness:

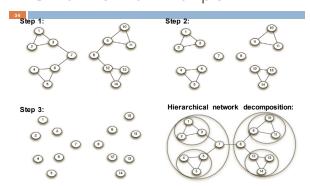
Number of shortest paths passing through the edge

- □ Girvan-Newman Algorithm:
 - Undirected unweighted networks
 - Repeat until no edges are left:
 - Calculate betweenness of edges
 - Remove edges with highest betweenness
 - Connected components are communities
 - □ Gives a hierarchical decomposition of the network

Girvan-Newman: Example



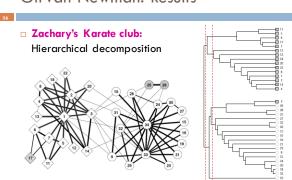
Girvan-Newman: Example



Girvan-Newman: Results



Girvan-Newman: Results



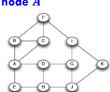
We need to resolve 2 questions

- 1. How to compute betweenness?
- 2. How to select the number of clusters?

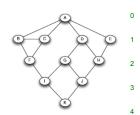


How to Compute Betweenness?

■ Want to compute betweenness of paths starting at node A

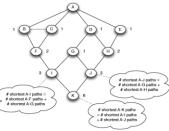


□ Breath first search starting from A:



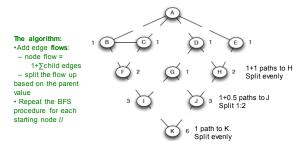
How to Compute Betweenness?

□ Count the number of shortest paths from A to all other nodes of the network:



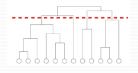
How to Compute Betweenness?

Compute betweenness by working up the tree: If there are multiple paths count them fractionally



We need to resolve 2 questions

- 1. How to compute betweenness?
- 2. How to select the number of clusters?



Network Communities

- Communities: sets of tightly connected nodes
 - □ <u>Define</u>: Modularity **Q**
 - A measure of how well a network is partitioned into communities
 - □ Given a partitioning of the network into groups $S \in S$:

 $Q \propto \sum_{s \in S} [(\# \text{ edges within group } s) - (\text{expected } \# \text{ edges within group } s)]$

Need a null model!

Null Model: Configuration Model

□ Given real on nodes and edges, construct rewired network

- □ Same degree distribution but random connections
- □ Consider as a multigraph
- □ The expected number of edge between nodes
 - i and j of degrees k_i and k_j equals to: $k_i \cdot \frac{k_j}{2m} = \frac{k_i k_j}{2m}$ The expected number of edges in (multigraph) G':

$$\begin{array}{l} \blacksquare = \frac{1}{2} \sum_{i \in N} \sum_{j \in N} \frac{k_i k_j}{2m} = \frac{1}{2} \cdot \frac{1}{2m} \sum_{i \in N} k_i \Big(\sum_{j \in N} k_j \Big) = \\ \blacksquare = \frac{1}{4m} \, 2m \cdot 2m = m \end{array}$$

Modularity

□ Modularity of partitioning S of graph G:

 $extbf{Q} \propto \sum_{s \in S} [(\# \text{ edges within group } s) -$ (expected # edges within group s)

$$Q(G,S) = \frac{1}{2m} \sum_{s \in S} \sum_{i \in s} \sum_{j \in s} \left(A_{ij} - \frac{k_i k_j}{2m} \right)$$
Normalizing cost: -1

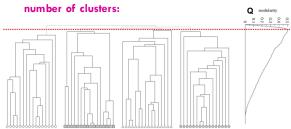


□ Modularity values take range [-1,1]

- It is positive if the number of edges within groups exceeds the expected number

Modularity: Number of clusters

Modularity is useful for selecting the



Why not optimize modularity directly?