

# Image Representation

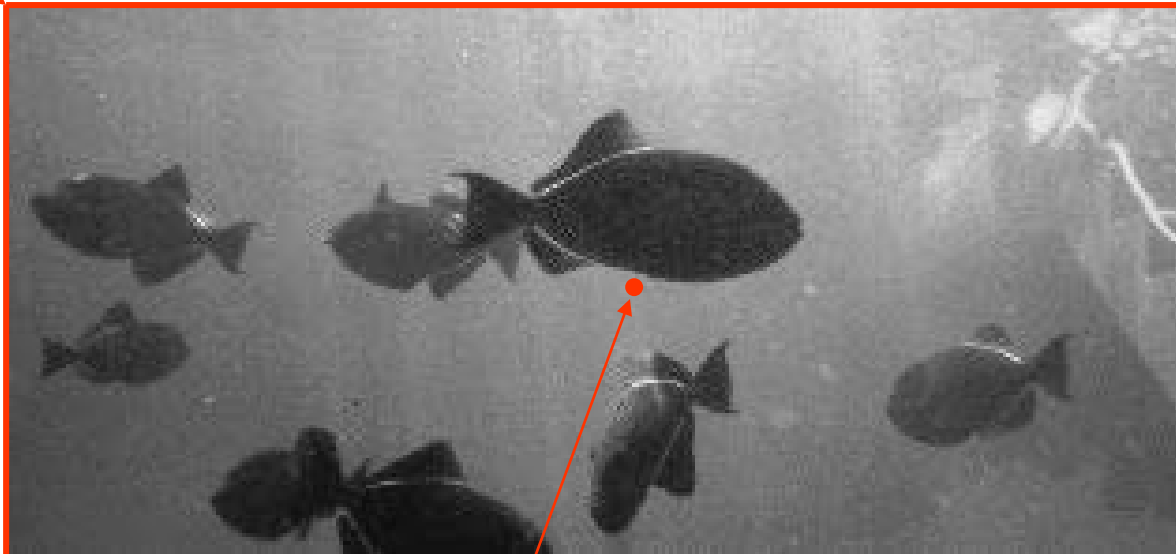
Reference:

[Gonzalez and Woods] Rafael C. Gonzalez and Richard E. Woods, Digital Image Processing, Second Edition, Prentice-Hall, Inc.

<http://www.imageprocessingplace.com/>

# Image representation

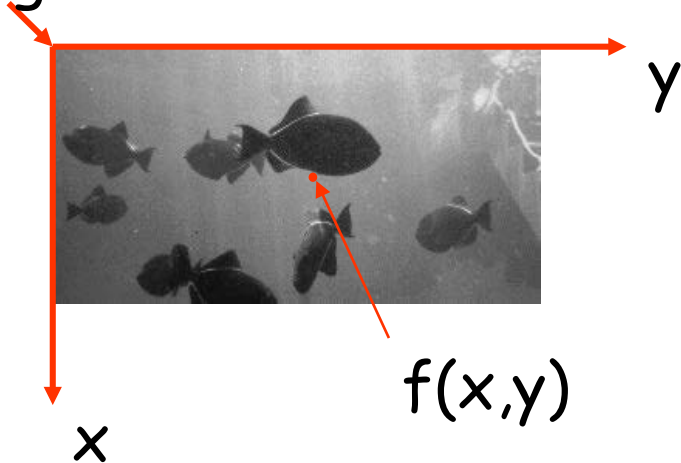
origin (0,0) in  $C$ , and (1,1) in MATLAB



$f(x,y)$ , a 2D function representing image intensity;  $(x,y)$  represents a pair of spatial coordinates

# Image representation

origin

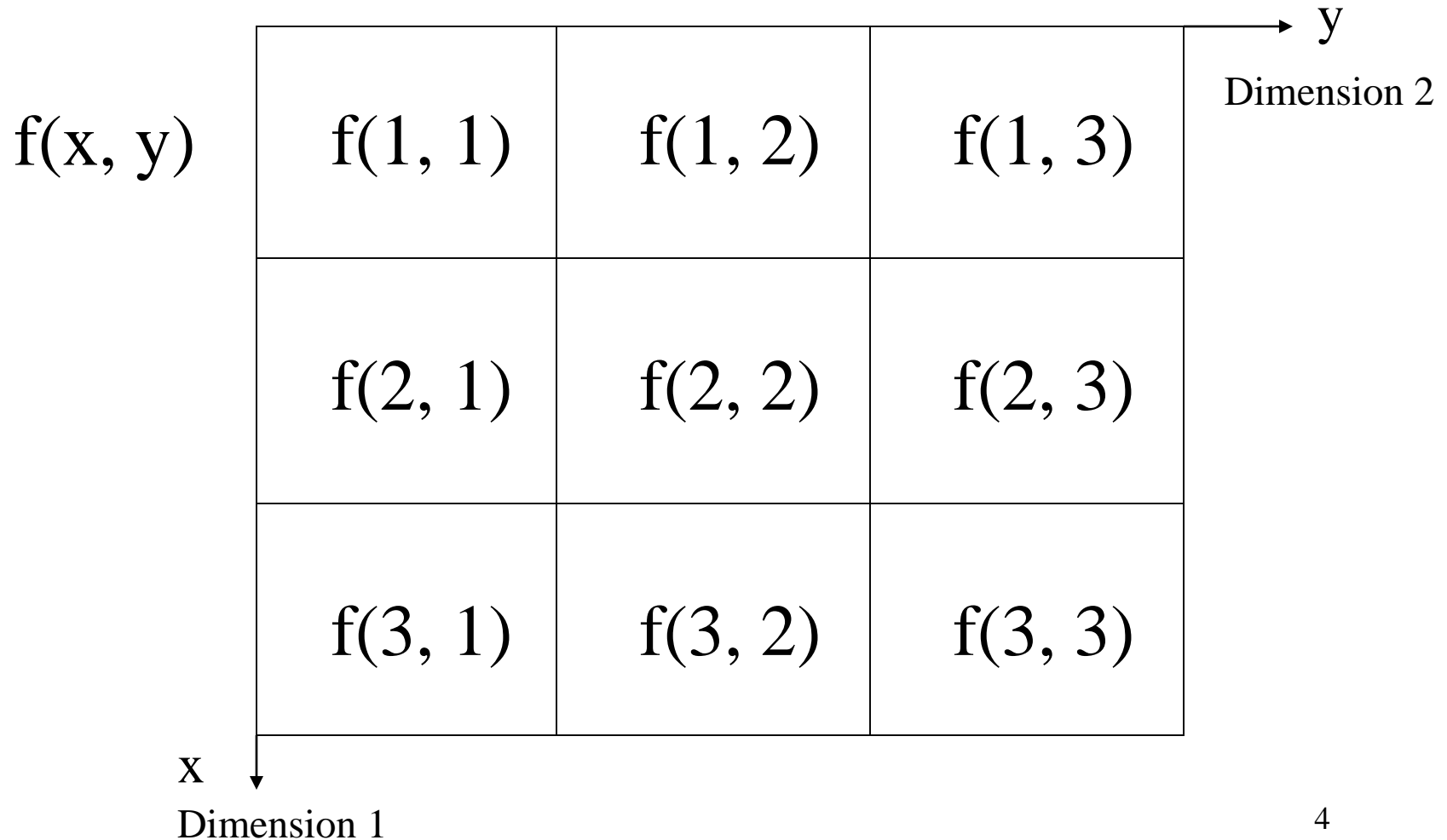


- Discretized in both
  - Spatial coordinates
  - Brightness

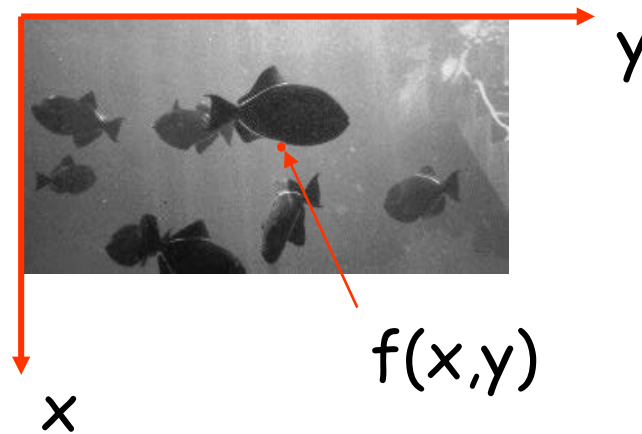
Similar to a matrix in Linear Algebra

Individual elements are called:  
image elements, picture elements (pixels), (image points)

# Image representation (MATLAB convention)



# Image function, $f$ (intensity)

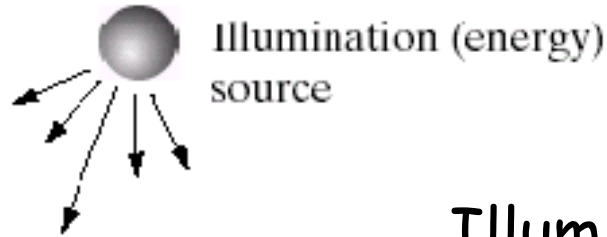


The image function (intensity/color)  $f$  can be characterized by two components:

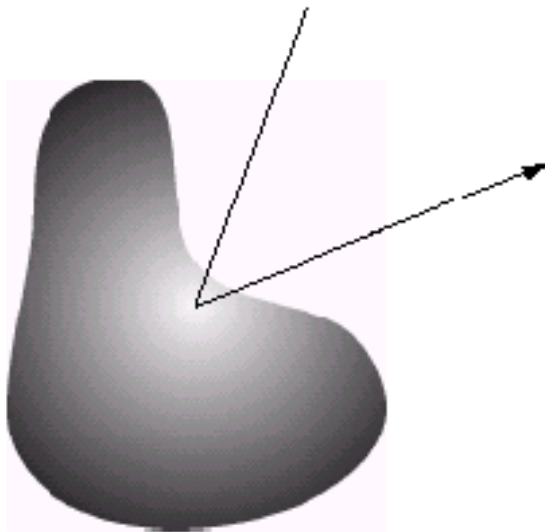
- (1) illumination (light source) and
- (2) reflectance (materials).

Image intensity is depending on these two factors.

# Image function, $f$ (intensity)



Illumination: the amount of source illumination (energy) **incident** on the scene being viewed.



Scene element

Reflectance: the amount of source illumination (energy) **reflected** by the objects (or elements) in the scene.

# Image model

- Basic nature of  $f(x,y)$  has two components:

$$f(x,y) = i(x,y) r(x,y)$$

- $i(x,y)$  is illumination component

$$0 \leq i(x,y) < +\infty$$

- $r(x,y)$  is reflectance component

$$0 \leq r(x,y) \leq 1$$

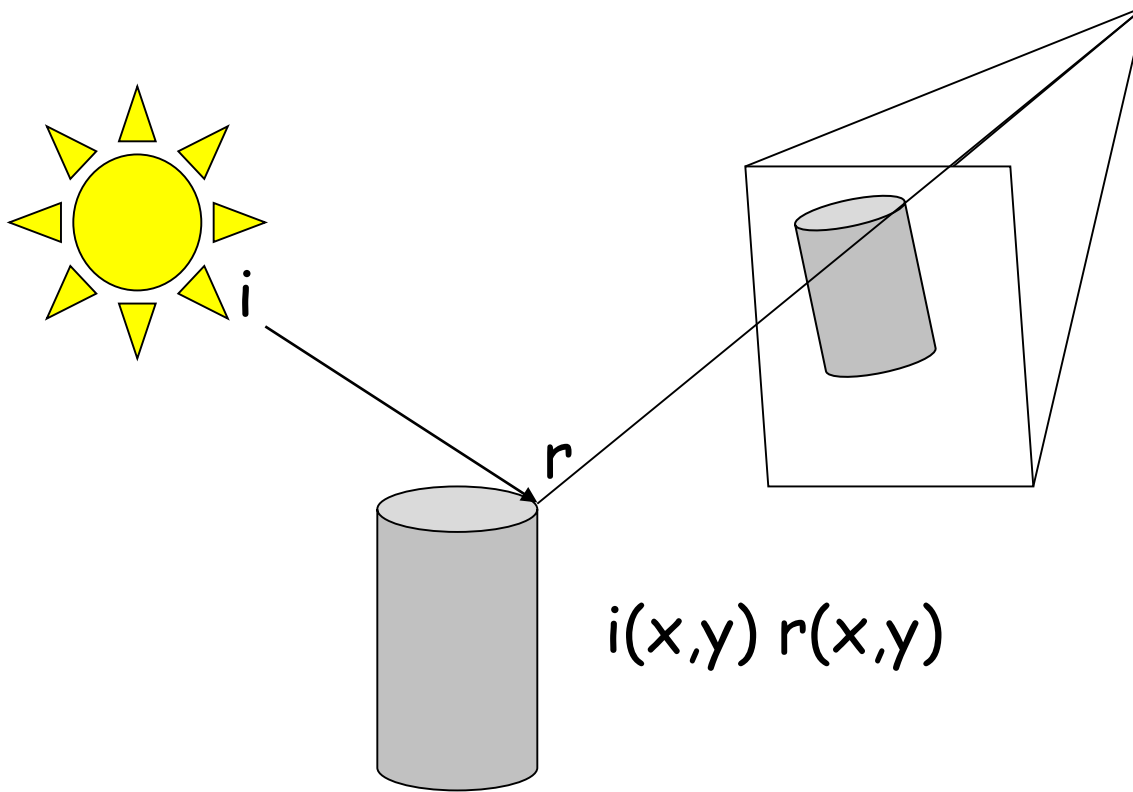
0 = total absorption, 1 = total reflectance.

- $f(x,y)$  is intensity

- $0 \leq f(x,y) < +\infty$

# Image model

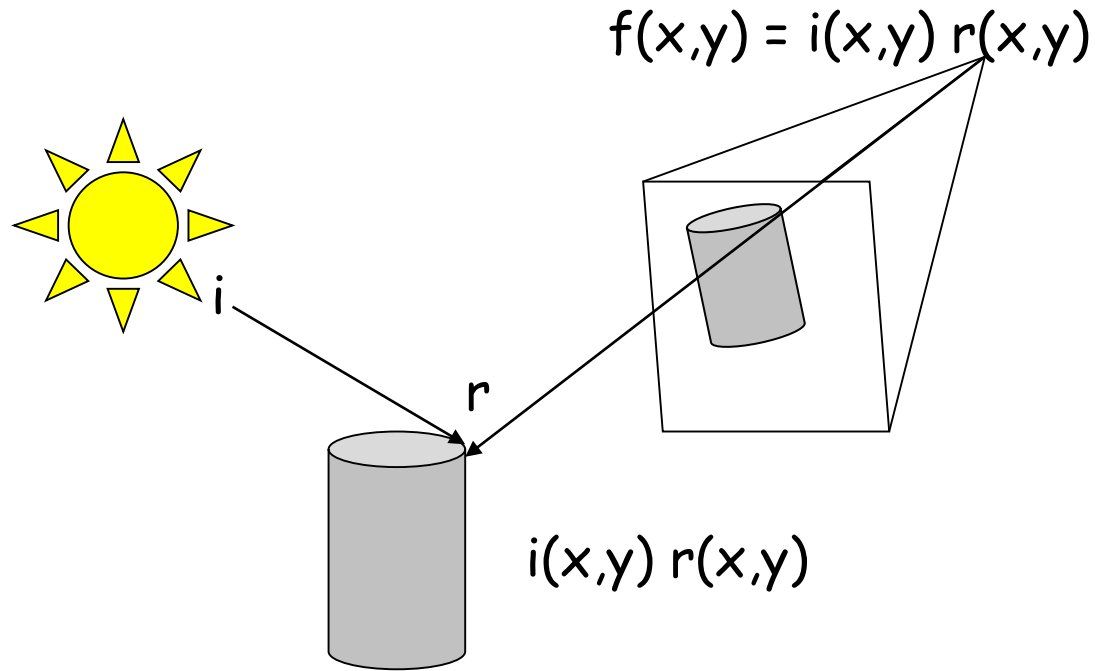
$$f(x,y) = i(x,y) r(x,y)$$



$i$  and  $r$  are continuous functions  
thus  $f(x,y)$  can be continuous

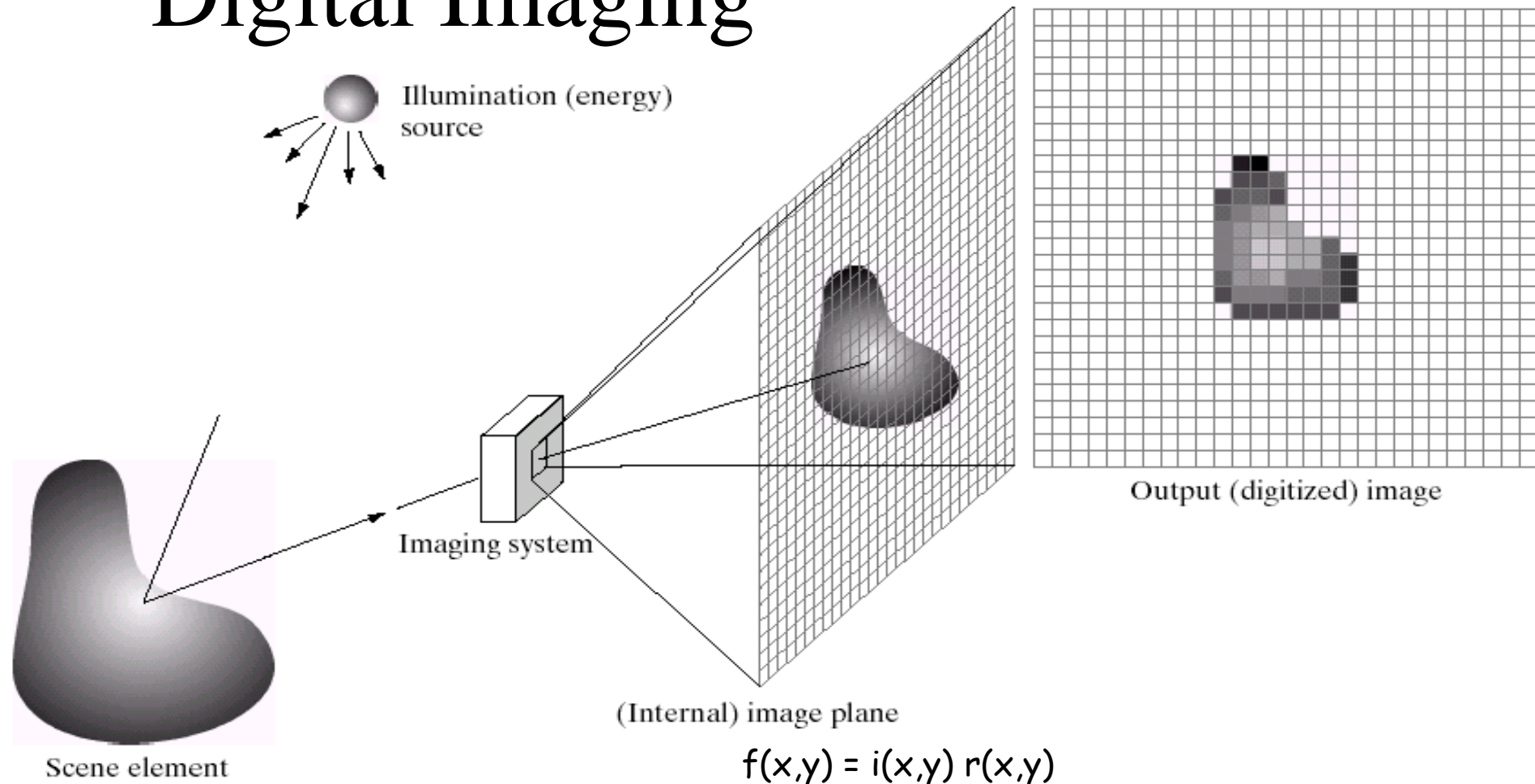


Sampling and quantization are affecting the image quality.



$i$  and  $r$  are continuous functions  
thus  $f(x,y)$  can be continuous

# Digital Imaging



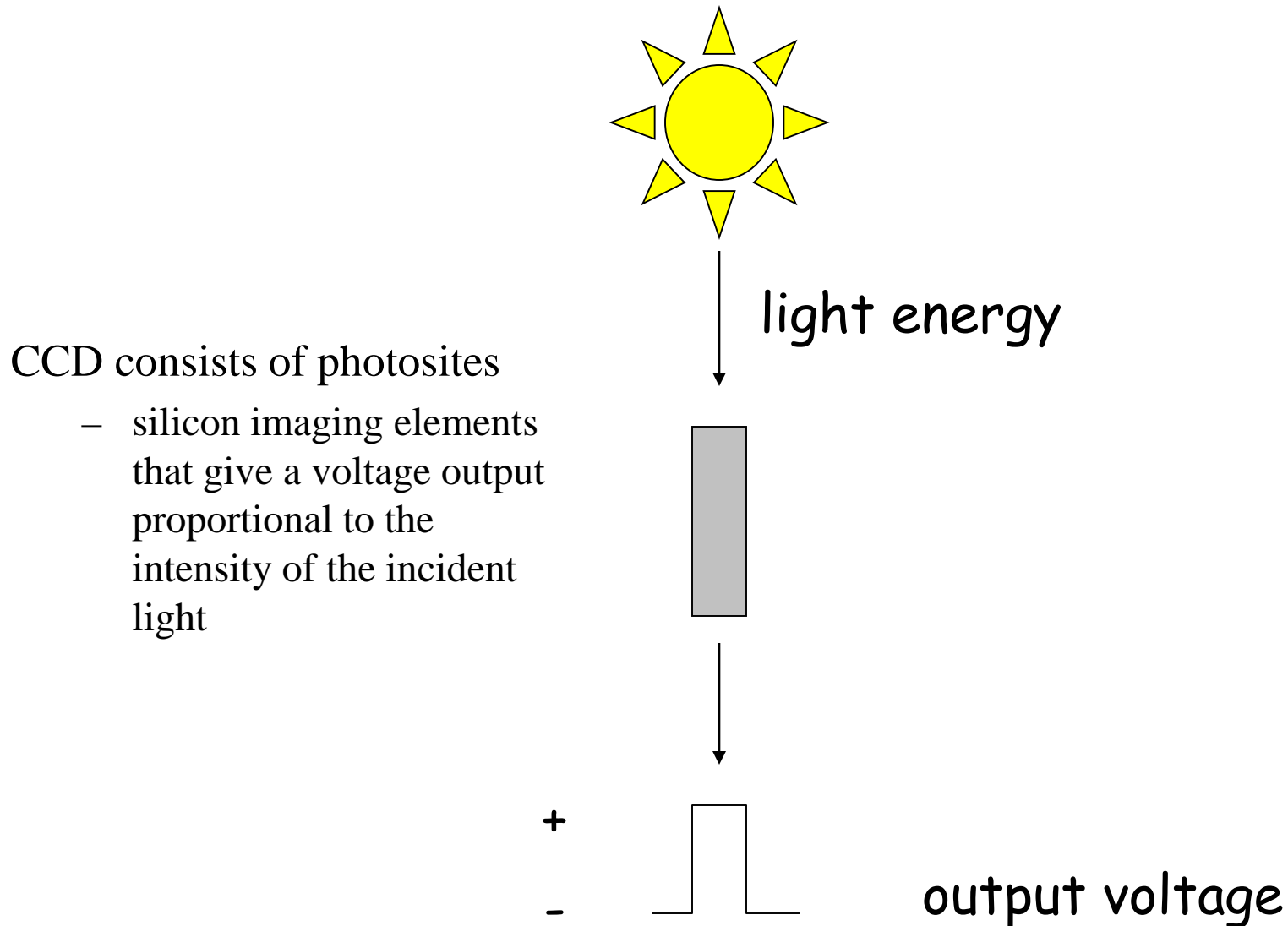
a b c d e

**FIGURE 2.15** An example of the digital image acquisition process. (a) Energy (“illumination”) source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

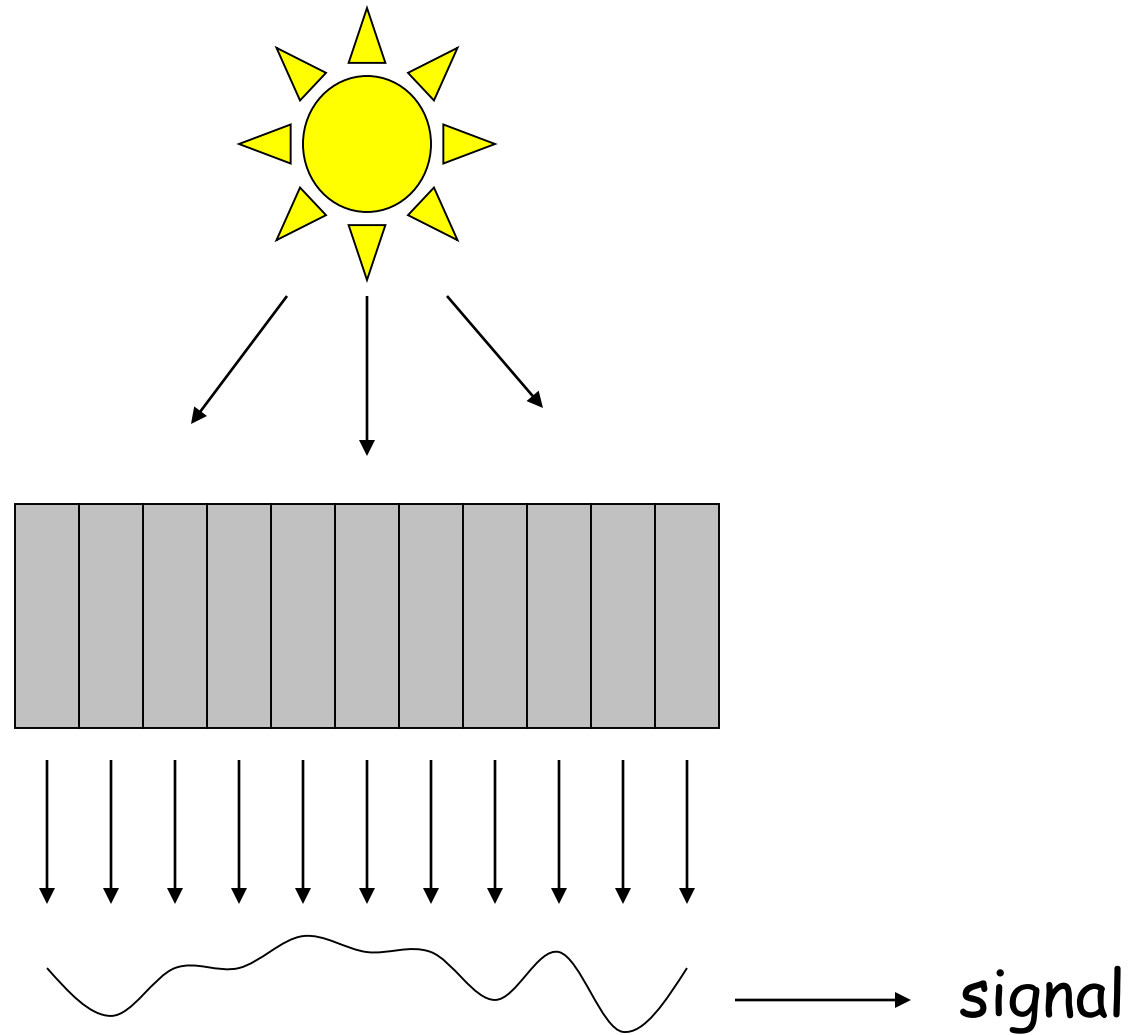
# Digital Imaging

- Charged-Coupled Device (CCD)
  - consists of photosites
    - silicon imaging elements that give a voltage output proportional to the intensity of the incident light
  - linear array (scanner)
  - area array (Camera CCD)
- [http://en.wikipedia.org/wiki/Charge-coupled\\_device](http://en.wikipedia.org/wiki/Charge-coupled_device)

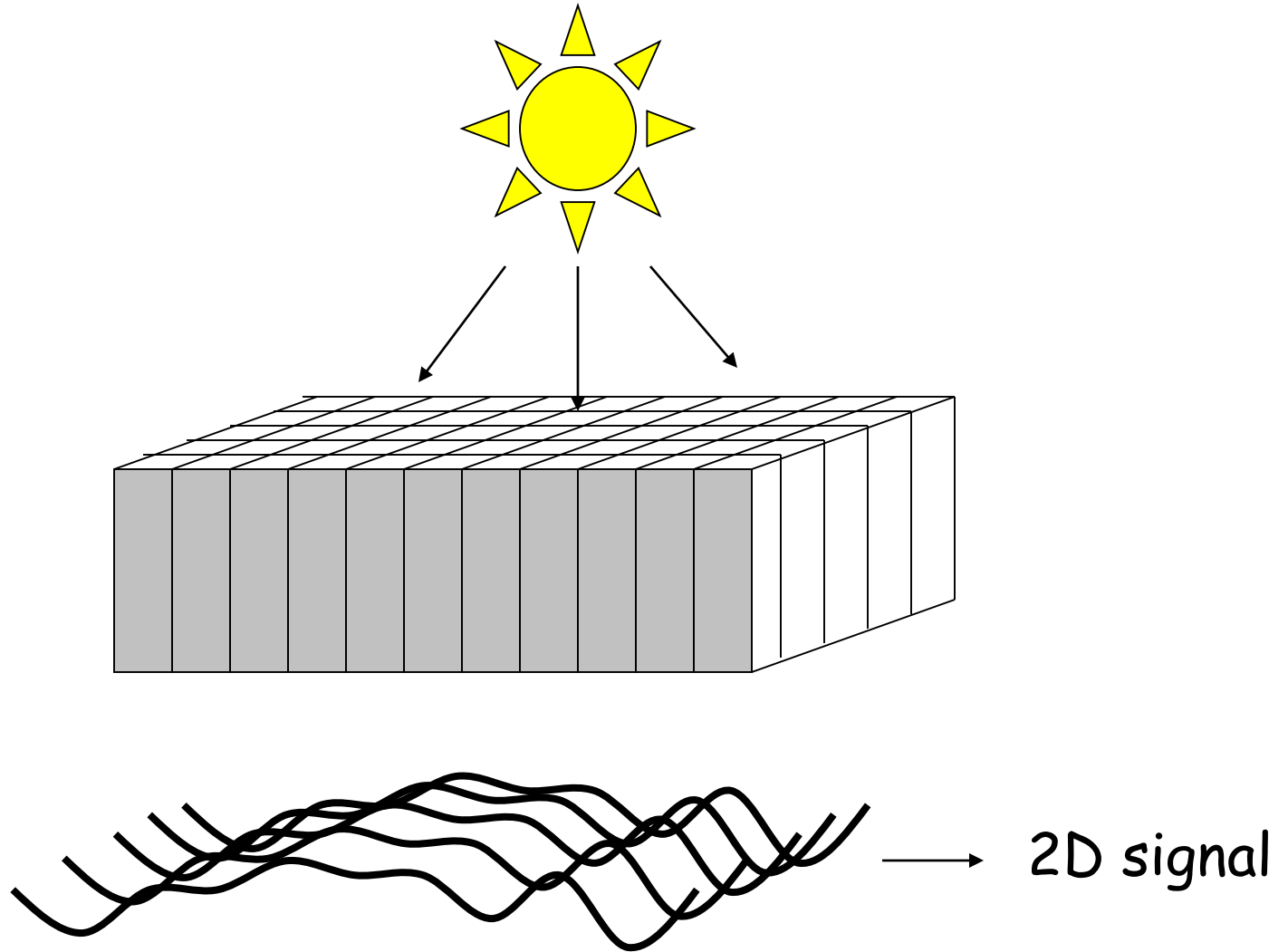
# Photosites



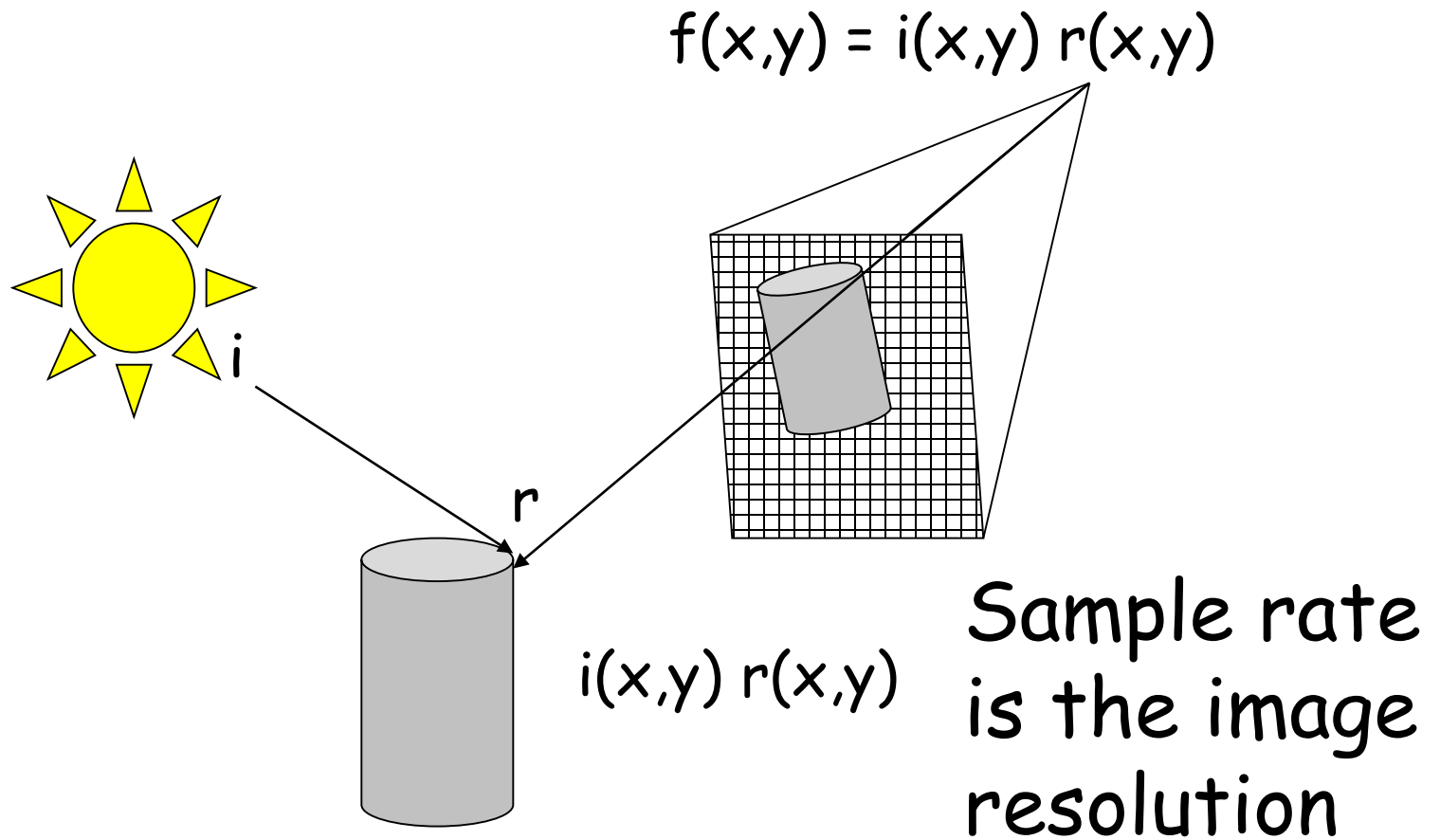
# Line scan sensor



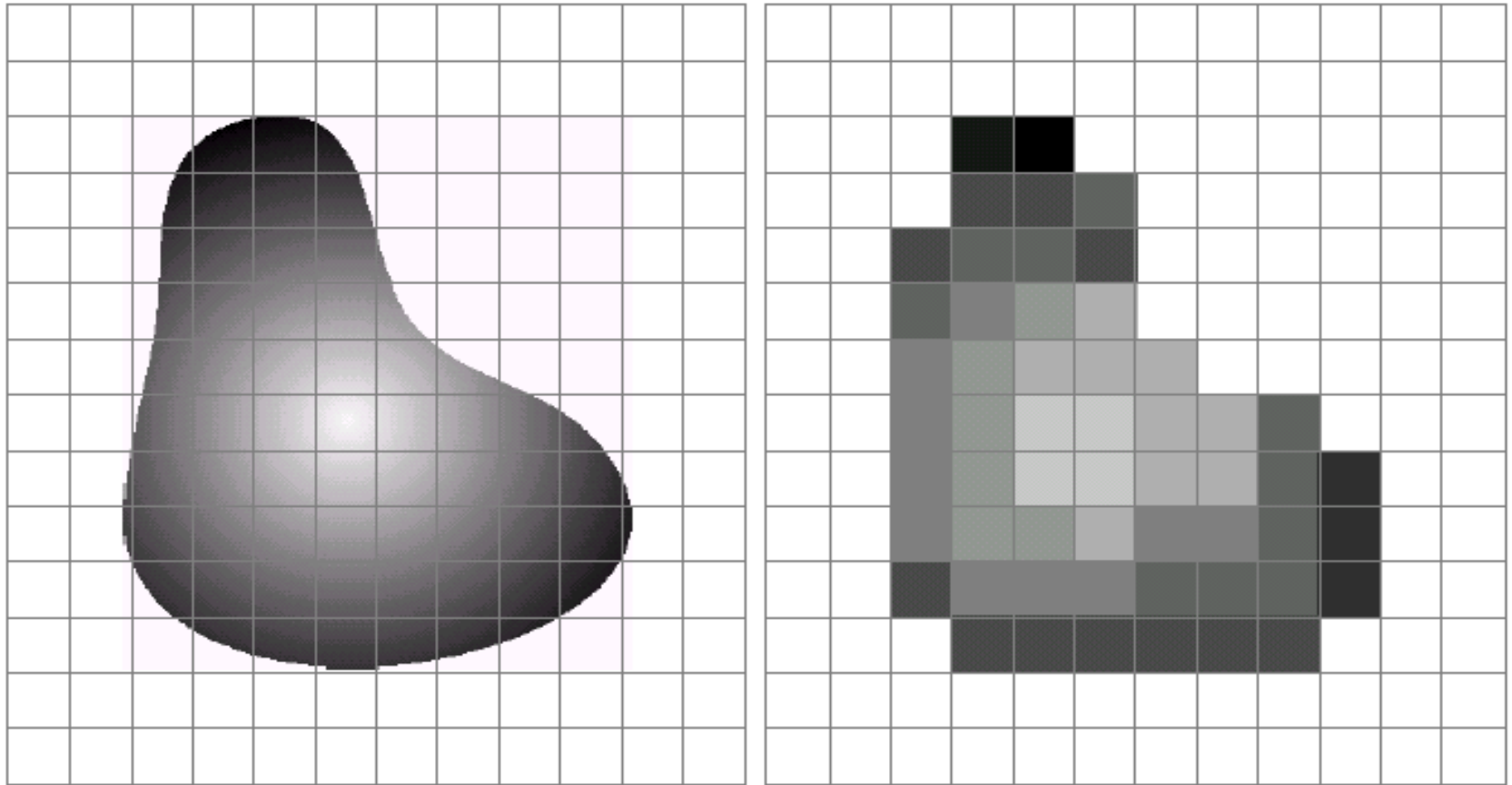
# Area scan sensor



# Image sampling/resolution



# Spatially discretized



a b

**FIGURE 2.17** (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.



# A digital image is discrete

$$f(x,y) \sim \begin{pmatrix} f(0,0) & f(0,1) & . & . & . & f(0, m-1) \\ f(1,0) & f(1,1) & . & . & . & f(1, m-1) \\ . & . & . & . & . & . \\ f(n-1,0) & f(n-1,1) & . & . & . & f(n-1, m-1) \end{pmatrix}$$

A digital image is discrete  
(MATLAB convention)

$$f(x,y) \sim \begin{pmatrix} f(1,1) & f(1,2) & . & . & . & f(1,m) \\ f(2,1) & f(2,2) & . & . & . & f(2,m) \\ . & . & . & . & . & . \\ . & . & . & . & . & . \\ f(n,1) & f(n,2) & . & . & . & f(n,m) \end{pmatrix}$$

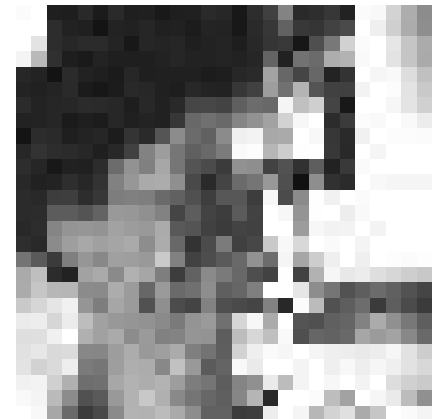
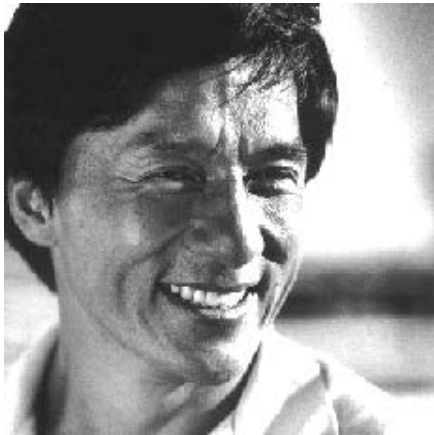
# Effects of spatial resolution



a	b	c
d	e	f

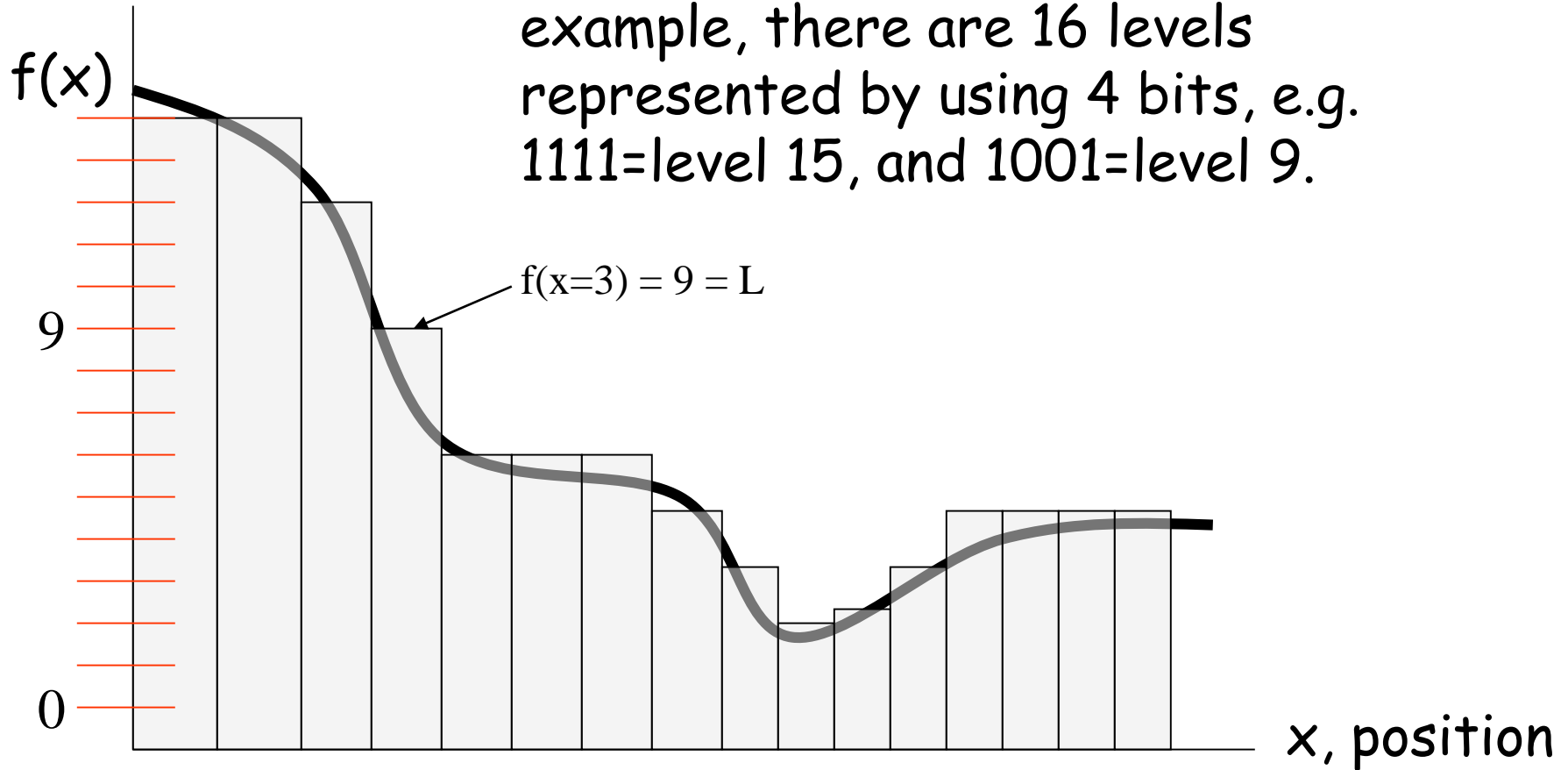
**FIGURE 2.20** (a)  $1024 \times 1024$ , 8-bit image. (b)  $512 \times 512$  image resampled into  $1024 \times 1024$  pixels by row and column duplication. (c) through (f)  $256 \times 256$ ,  $128 \times 128$ ,  $64 \times 64$ , and  $32 \times 32$  images resampled into  $1024 \times 1024$  pixels.

# Effects of spatial resolution



# Intensity quantization

We will call intensity of a monochrome image, its grey level ( $L$ ). In this example, there are 16 levels represented by using 4 bits, e.g. 1111=level 15, and 1001=level 9.



# Effects of intensity quantization

e f  
g h

**FIGURE 2.21**

*(Continued)*

(e)–(h) Image displayed in 16, 8, 4, and 2 gray levels. (Original courtesy of Dr. David R. Pickens, Department of Radiology & Radiological Sciences, Vanderbilt University Medical Center.)

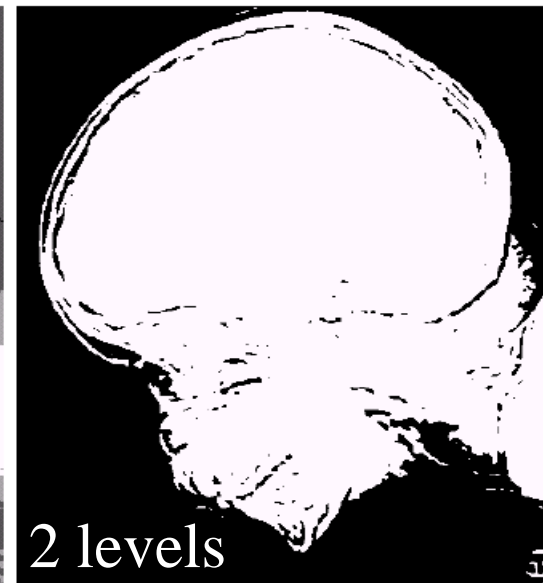
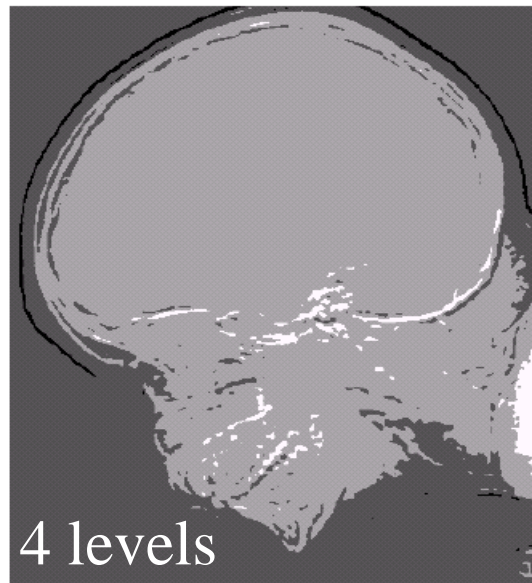
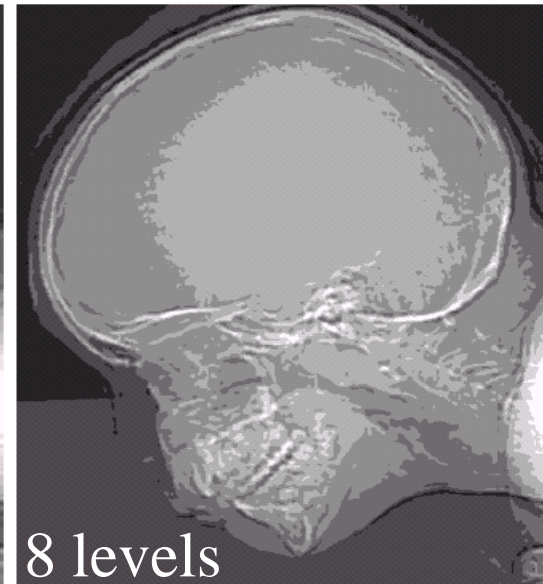


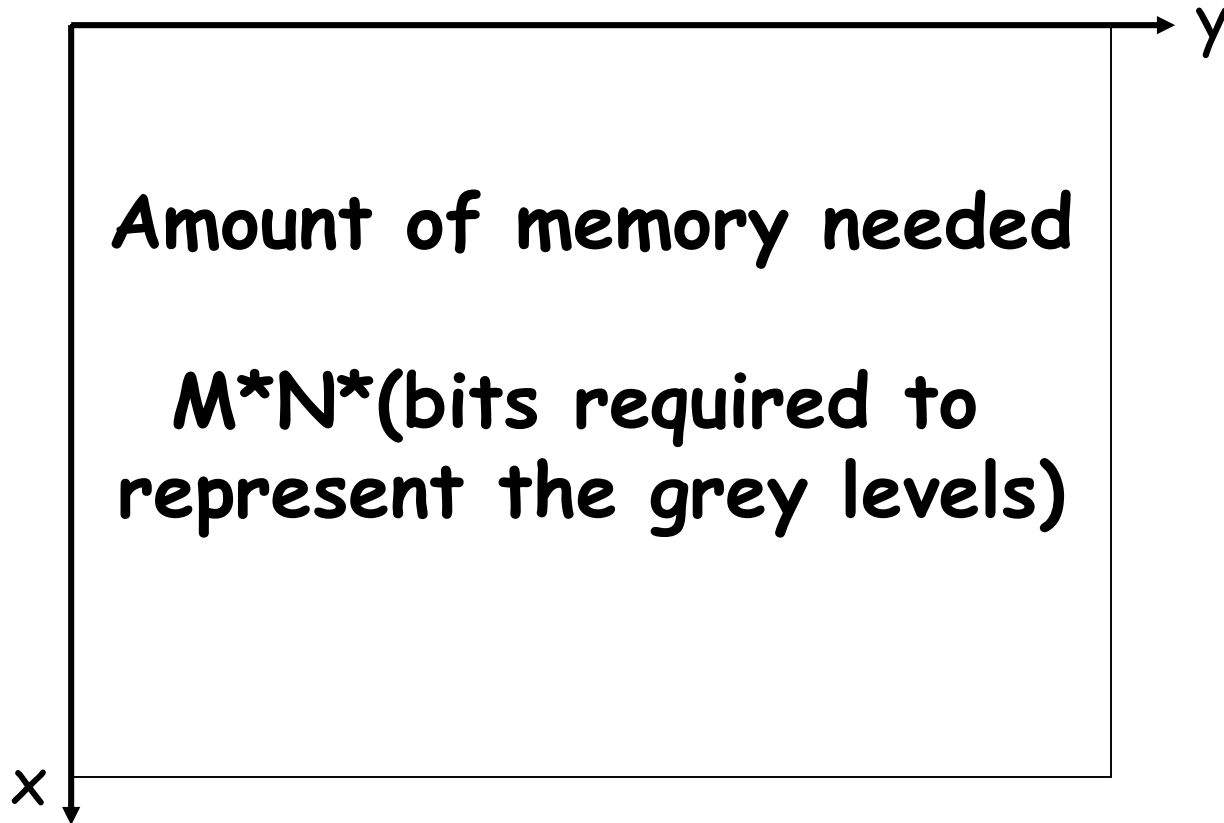
Image resolution is fixed but the number of gray levels decreases.

# Effects of intensity quantization



# Storage requirements

$M$  = number of columns,  
"Width" in MATLAB



$N$  = number of rows, "height" in MATLAB