

# Multilevel Models Standardized

Technical assistant

2025-12-18

## Modelo 0: Nulo

$$\begin{aligned} \text{identification}_i &\sim N(\alpha_{j[i]}, \sigma^2) \\ \alpha_j &\sim N(\mu_{\alpha_j}, \sigma_{\alpha_j}^2), \text{ for geocodigo } j = 1, \dots, J \end{aligned} \tag{1}$$

## Modelo 1: Individual

$$\begin{aligned} \text{identification}_i &\sim N(\mu, \sigma^2) \\ \mu &= \alpha_{j[i]} + \beta_1(\text{new\_class}_1) + \beta_2(\text{new\_class}_2) + \\ &\quad \beta_3(\text{new\_class}_4) + \beta_4(\text{new\_class}_5) + \beta_5(\text{age}) + \\ &\quad \beta_6(\text{age\_sq}) + \beta_7(\text{sex}) + \beta_8(\text{homeowner}) + \\ &\quad \beta_9(\text{married}) + \beta_{10}(\text{has\_children}) \\ \alpha_j &\sim N(\gamma_0^\alpha + \gamma_1^\alpha(\text{pop\_density}) + \gamma_2^\alpha(\text{pct\_migrant}) + \gamma_3^\alpha(\text{insecurity}), \sigma_{\alpha_j}^2), \text{ for geocodigo } j = 1, \dots, J \end{aligned} \tag{2}$$

## Modelo 2: Contextual

$$\begin{aligned} \text{identification}_i &\sim N(\mu, \sigma^2) \\ \mu &= \alpha_{j[i]} + \beta_1(\text{age}) + \beta_2(\text{age\_sq}) + \\ &\quad \beta_3(\text{sex}) + \beta_4(\text{homeowner}) + \beta_5(\text{married}) + \\ &\quad \beta_6(\text{has\_children}) \\ \alpha_j &\sim N(\gamma_0^\alpha + \gamma_1^\alpha(\text{nse\_barrio\_norm}) + \gamma_2^\alpha(\text{pop\_density}) + \gamma_3^\alpha(\text{pct\_migrant}) + \gamma_4^\alpha(\text{insecurity}), \sigma_{\alpha_j}^2) \end{aligned} \tag{3}$$

## Modelo 3: Full

$$\begin{aligned}
\text{identification}_i &\sim N(\mu, \sigma^2) \\
\mu &= \alpha_{j[i]} + \beta_1(\text{new\_class}_1) + \beta_2(\text{new\_class}_2) + \\
&\quad \beta_3(\text{new\_class}_4) + \beta_4(\text{new\_class}_5) + \beta_5(\text{age}) + \\
&\quad \beta_6(\text{age\_sq}) + \beta_7(\text{sex}) + \beta_8(\text{homeowner}) + \\
&\quad \beta_9(\text{married}) + \beta_{10}(\text{has\_children}) \\
\alpha_j &\sim N(\gamma_0^\alpha + \gamma_1^\alpha(\text{nse\_barrio\_norm}) + \gamma_2^\alpha(\text{pop\_density}) + \gamma_3^\alpha(\text{pct\_migrant}) + \gamma_4^\alpha(\text{insecurity}), \sigma_{\alpha_j}^2)
\end{aligned} \tag{4}$$

## Modelo 4: Interacción

$$\begin{aligned}
\text{identification}_i &\sim N(\mu, \sigma^2) \\
\mu &= \alpha_{j[i]} + \beta_1(\text{new\_class}_1) + \beta_2(\text{new\_class}_2) + \\
&\quad \beta_3(\text{new\_class}_4) + \beta_4(\text{new\_class}_5) + \beta_5(\text{age}) + \\
&\quad \beta_6(\text{age\_sq}) + \beta_7(\text{sex}) + \beta_8(\text{homeowner}) + \\
&\quad \beta_9(\text{married}) + \beta_{10}(\text{has\_children}) \\
\alpha_j &\sim N(\gamma_0^\alpha + \gamma_1^\alpha(\text{nse\_barrio\_norm}) + \gamma_2^\alpha(\text{pop\_density}) + \gamma_3^\alpha(\text{pct\_migrant}) + \gamma_4^\alpha(\text{insecurity}) + \gamma_5^\alpha(\text{age}), \sigma_{\alpha_j}^2)
\end{aligned} \tag{5}$$