2D extension of SCSD

Objective

SCSD: New method for fast 3D convolutions Internship + CEMRACS: Extend to 2D

$$q_k = \sum_{l=1}^N G(x_k - x_l) f_l \quad G(x) : \text{ PDE radial kernel}$$

$$\left| \begin{array}{c|c} SCSD \ (3D \to x_k \in \mathbb{R}^3) \end{array} \right| \text{ SBD } (2D \to x_k \in \mathbb{R}^2)$$

$$\text{Expansion} : \quad G \approx \sum_{p=1}^P \alpha_p \text{sinc}(\lambda_p|x|) \quad G \approx \sum_{p=1}^P \alpha_p J_0(\rho_p|x|)$$

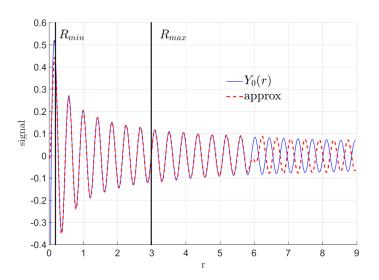
$$\text{Offline} : \quad O(N \log(N)) \quad O(N^{3/2})$$

$$\text{Online} : \quad O(N \log(N)) \quad O(N \log(N))$$

Achieved

- Error + complexity analysis
- Test case 5e7, off: 21 min, on: 6 min

Approximation of Y_0 in Bessel series



Numerical results

