## Model-independent determination of the CKM angle $\gamma$ in $B^\pm \to (K^+K^-\pi^+\pi^-)_D h^\pm$ decays

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#### Outline

- 1 Introduction to the CKM angle  $\gamma$
- 2 Binned  $\gamma$  analysis of the  $D \to K^+K^-\pi^+\pi^-$  mode
- Binning scheme
- Fit to data
- Systematic uncertainties
- 6 Summary and conclusion of  $KK\pi\pi$  analysis

## Introduction to the CKM angle $\gamma$

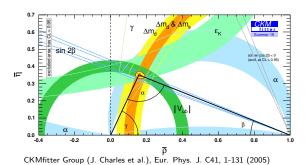
Introduction to the CKM angle  $\gamma$ 

## $\gamma$ and the unitary triangle

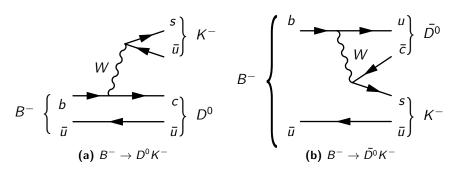
CP violation in SM is described by the Unitary Triangle

$$\gamma = \mathrm{arg}\Big(-rac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\Big)$$

- Only CKM angle accessible at tree level ⇒
  - Negligible theoretical uncertainties
  - Ideal Standard Model benchmark
  - Compare with indirect measurements



## Sensitivity through interference



- ullet Superposition of  $D^0$  and  $ar{D^0}$
- ullet b o uar cs and b o car us interference o Sensitivity to  $\gamma$

$$\mathcal{A}(B^{-}) = \mathcal{A}(D^{0}) + r_{B}e^{i(\delta_{B}-\gamma)}\mathcal{A}(\bar{D^{0}})$$
  
$$\mathcal{A}(B^{+}) = \mathcal{A}(\bar{D^{0}}) + r_{B}e^{i(\delta_{B}+\gamma)}\mathcal{A}(D^{0})$$

## Measurement of $\gamma$ from $B^{\pm} \to DK^{\pm}$ , $D \to K^{+}K^{-}\pi^{+}\pi^{-}$

- First proposed by J. Rademacker and G. Wilkinson
  - Physics Letters B 647 (2007) 400
  - Amplitude model by FOCUS
  - ullet Expected  $\gamma$  precision from amplitude fit with 1000 candidates: 14 $^\circ$
- CLEO amplitude analysis
  - Phys. Rev. D 85 (2012) 122002
  - ullet Expected  $\gamma$  precision from amplitude fit with 2000 candidates:  $11^\circ$
- State of the art amplitude analysis by LHCb:
  - JHEP **02** (2019) 126

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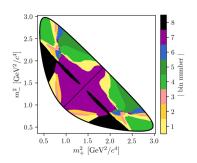
• Use to develop efficient binning scheme

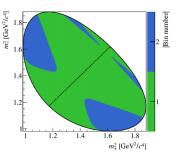
## The $D \rightarrow K^+K^-\pi^+\pi^-$ decay

Binned 
$$\gamma$$
 analysis of the  $D \to K^+K^-\pi^+\pi^-$  mode

## Binned measurement of $\gamma$

- Final measurement will be model-independent
  - Non-optimal binning reduces statistical sensitivity
  - But no bias is induced in final result
- ullet Need strong phases of D decay o Will be measured at BESIII
- ullet Analogous approach to  $B^\pm o D h^\pm$ ,  $D o K_S^0 h^+ h^-$ 
  - JHEP **02** (2021) 0169
  - Single most precise measurement:  $\gamma = (68.7^{+5.2}_{-5.1})^{\circ}$





## The BPGGSZ method

•  $B^{\pm} \rightarrow Dh^{\pm}$  amplitude:

$$\begin{split} \mathcal{A}(B^-) &= \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D^0}) \\ \mathcal{A}(B^+) &= \mathcal{A}(\bar{D^0}) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0) \end{split}$$

- ullet  $\mathcal{A}(D^0)$  and  $\mathcal{A}(ar{D^0})$  depend on D phase space
- ullet Strong-phase difference of  $D^0$  and  $ar{D^0}$  decays inaccessible at LHCb
- Model-independent measurement: Integrate over bins of phase space

## Event yield in bin i

$$N_{i}^{-} = h_{B^{-}} \Big( F_{i} + (x_{-}^{2} + y_{-}^{2}) \bar{F}_{i} + 2 \sqrt{F_{i} \bar{F}_{i}} (x_{-} c_{i} + y_{-} s_{i}) \Big)$$

$$N_{-i}^{+} = h_{B^{+}} \Big( F_{i} + (x_{+}^{2} + y_{+}^{2}) \bar{F}_{i} + 2 \sqrt{F_{i} \bar{F}_{i}} (x_{+} c_{i} + y_{+} s_{i}) \Big)$$

#### The BPGGSZ method

#### Event yield in bin i

$$\begin{split} N_i^- &= h_{B^-} \big( F_i + (x_-^2 + y_-^2) \bar{F}_i + 2 \sqrt{F_i \bar{F}_i} (x_- c_i + y_- s_i) \big) \\ N_{-i}^+ &= h_{B^+} \big( F_i + (x_+^2 + y_+^2) \bar{F}_i + 2 \sqrt{F_i \bar{F}_i} (x_+ c_i + y_+ s_i) \big) \end{split}$$

- CP observables:
  - $x_{\pm}^{DK} = r_B^{DK} \cos(\delta_B^{DK} \pm \gamma), \quad y_{\pm}^{DK} = r_B^{DK} \sin(\delta_B^{DK} \pm \gamma)$ •  $x_{\xi}^{D\pi} = \text{Re}(\xi^{D\pi}), \ y_{\xi}^{D\pi} = \text{Im}(\xi^{D\pi}) \qquad \left(\xi^{D\pi} = \frac{r_B^{D\pi}}{r_{DK}} e^{i(\delta_B^{D\pi} - \delta_B^{DK})}\right)$
- Fractional bin yield:
  - $F_i = \frac{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2}{\sum_i \int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2}$

- ullet Floated in the fit, mostly constrained by  $B^\pm o D \pi^\pm$
- Amplitude averaged strong phases can be obtained from BESIII:

$$c_i = \frac{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D^0})| \cos(\delta_D)}{\sqrt{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2 \int_i \mathrm{d}\Phi |\mathcal{A}(\bar{D^0})|^2}} \quad s_i = \frac{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D^0})| \sin(\delta_D)}{\sqrt{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2 \int_i \mathrm{d}\Phi |\mathcal{A}(\bar{D^0})|^2}}$$

## Binning Scheme

## Binning scheme

## Binning scheme requirements

## A binning scheme must satisfy the following:

- Minimal dilution of strong phases when integrating over bins
- ullet Enhance interference between  $B^\pm o D^0 h^\pm$  and  $B^\pm o ar{D^0} h^\pm$

## How to bin a 5-dimensional phase space?

- Generate C++ code for LHCb amplitude model using AmpGen<sup>1</sup>
- For each  $B^{\pm}$  candidate, calculate

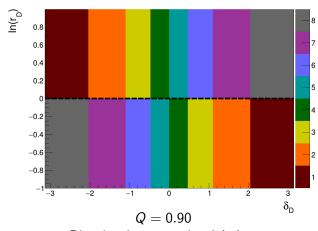
$$\frac{A(D^0)}{A(\bar{D^0})} = r_D e^{i\delta_D}$$

• Bin along  $\delta_D$  and  $r_D$ , maximize Q-value to optimize

<sup>&</sup>lt;sup>1</sup>AmpGen by Tim Evans

## Binning scheme

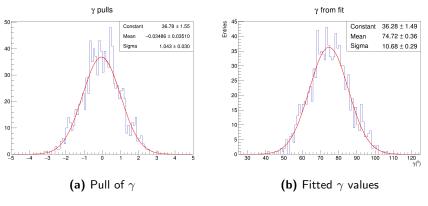
2x8 binning scheme for  $K^+K^-\pi^+\pi^-$  phase space



Bins i < 0 on top, i > 0 below

## $\gamma$ precision benchmark

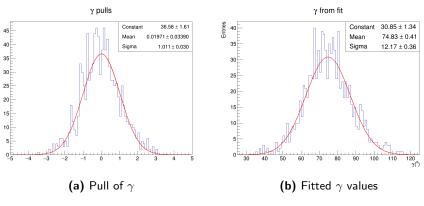
- ullet Generate 2000  $B^\pm o DK^\pm$  candidates using LHCb model in AmpGen
  - Input values:  $\gamma=75^\circ$ ,  $\delta_B=130^\circ$ ,  $r_B=0.1$
- Perform unbinned fit to the same amplitude model using AmpGen



Precision of  $\gamma$  in unbinned fit:  $11^{\circ}$ 

## Study of $\gamma$ precision

- Binned fit setup: Optimized 2 × 8 bins
- Fit same AmpGen samples, using  $c_i$ ,  $s_i$  and  $F_i$  from LHCb model



Precision of  $\gamma$  in binned fit: 12° Consistent with unbinned fit and Q-value

#### Global mass fit

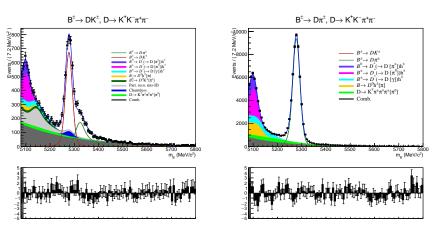
## Global mass fit

## Signal parameterisation

- PDF shape parameterization identical to LHCb-ANA-2020-001
- Signal: Gaussian + Modified Cruijff
- Shape fixed from MC, yield and width floated
- Combinatorial background (exponential)
- Partially reconstructed background (dini shapes)

$$f_{MG}(m|m_B,\sigma,\alpha_L,\alpha_R,\beta) \propto \begin{cases} \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_L\Delta m^2}\right), & \Delta m=m-m_B<0\\ \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_R\Delta m^2}\right), & \Delta m=m-m_B>0 \end{cases}$$

#### Global mass fit



**Figure 4:** Fit of  $B^{\pm} \to DK^{\pm}$  channel (left) and  $B^{\pm} \to D\pi^{\pm}$  channel (right) using full Run 1 and 2 data

- $B^{\pm} \rightarrow DK^{\pm}$  yield: 3306  $\pm$  75
- $B^{\pm} \rightarrow D\pi^{\pm}$  yield:  $46\,695 \pm 256$ Sneha Malde

## Binned CP fit

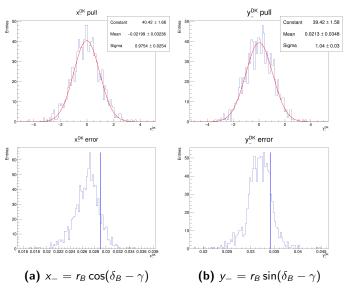
## Binned CP fit

#### Binned CP fit

- Use  $2 \times 8$  bins
- $c_i$  and  $s_i$  not available from BESIII yet  $\Longrightarrow$ 
  - Calculate using MC integration of LHCb amplitude model for now
- Fit for CP observables
- PDF shape parameters fixed from global mass fit
- Yield of signal, low mass partially reconstructed background and combinatorial background floated
- Fractional yields F<sub>i</sub> floated

$$\mathcal{R}_{i} = \begin{cases} F_{i}, & i = -8 \\ F_{i} / \sum_{j \geq i} F_{j}, -8 < i \leq +8 \end{cases}$$

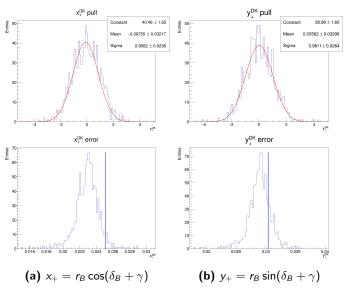
## CP observables result: $x_{-}^{DK}$ and $y_{-}^{DK}$



Pulls and uncertainties from toy studies, uncertainty from data fit in blue

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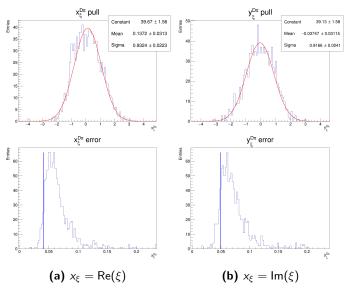
## CP observables result: $x_{+}^{DK}$ and $y_{+}^{DK}$



Pulls and uncertainties from toy studies, uncertainty from data fit in blue

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## CP observables result: $x_{\xi}^{D\pi}$ and $y_{\xi}^{D\pi}$



Pulls and uncertainties from toy studies, uncertainty from data fit in blue

## Systematic uncertainties

## Systematic uncertainties

## c<sub>i</sub> and s<sub>i</sub> systematic uncertainty

- $\bullet$   $c_i$  and  $s_i$  uncertainty will come from BESIII analysis
  - Mostly statistical in origin
- Largest systematic uncertainty
- ullet Use estimated uncertainties corresponding to 20 fb $^{-1}$  at  $\psi(3770)$
- Smear  $c_i$  and  $s_i$  and do many fits to data

## Summary of all systematic uncertainties

Uncertainties of CP observables in units of  $10^{-2}$ 

Source	$x_{-}^{DK}$	$y_{-}^{DK}$	$x_+^{DK}$	$y_+^{DK}$	$x_{\xi}^{D\pi}$	$y_{\xi}^{D\pi}$
Statistical	2.91	3.41	2.51	3.04	4.04	4.89
$C_i, s_i$	0.66	1.55	0.32	1.31	1.73	1.03
$B^\pm o D\mu u$ background	0.04	0.03	0.02	0.15	0.30	0.10
$D o K(X) I u_I$ background	0.15	0.05	0.11	0.03	0.35	0.25
$D o K\pi\pi\pi$ background	0.17	0.03	0.04	0.01	0.46	0.18
$\Lambda_b$ background	0.09	0.11	0.00	0.18	0.16	0.21
Bin dependent mass shape	0.21	0.05	0.17	0.01	0.37	0.11
Fit bias	0.19	0.03	0.16	0.04	0.30	0.16
Fixed yield fractions	0.02	0.03	0.02	0.02	0.01	0.01
Low mass physics effects	0.05	0.09	0.05	0.18	0.41	0.48
Mass shape	0.03	0.03	0.02	0.02	0.04	0.01
PID Efficiency	0.03	0.03	0.02	0.02	0.04	0.01
Total LHCb systematic	0.39	0.17	0.27	0.30	0.92	0.65
Total systematic	0.77	1.55	0.41	1.34	2.01	1.23

## Summary and conclusion of $KK\pi\pi$ analysis

# Summary and conclusion of $KK\pi\pi$ analysis

## Summary of CP observables

Measured CP observables:

$$\begin{split} x_{-}^{DK} &= (x.x \pm 2.9 \pm 0.4 \pm 0.7) \times 10^{-2}, \\ y_{-}^{DK} &= (x.x \pm 3.4 \pm 0.2 \pm 1.6) \times 10^{-2}, \\ x_{+}^{DK} &= (x.x \pm 2.5 \pm 0.3 \pm 0.3) \times 10^{-2}, \\ y_{+}^{DK} &= (x.x \pm 3.0 \pm 0.3 \pm 1.3) \times 10^{-2}, \\ x_{\xi}^{D\pi} &= (x.x \pm 4.0 \pm 0.9 \pm 1.7) \times 10^{-2}, \\ y_{\xi}^{D\pi} &= (x.x \pm 4.9 \pm 0.7 \pm 1.0) \times 10^{-2}, \end{split}$$

- Note: Currently using  $c_i$  and  $s_i$  from the LHCb model
- Publication strategy: Publish current results together with binned yields  $\rightarrow$  Redo fit to obtain model-independent CP observables once c; and s; from BESIII are available
- Will update c<sub>i</sub> and s<sub>i</sub> with model-dependent uncertainties

#### Conclusion

- Binned  $\gamma$  analysis of  $B^{\pm} \to (K^+K^-\pi^+\pi^-)_D h^{\pm}$  is mostly complete, with promising results
  - Expect total uncertainty around 12°-14°
- Will publish model-dependent measurement for now, update with model-independent results when  $c_i$  and  $s_i$  from BESIII are available
- Analysis note: LHCb-ANA-2021-051

## Thank you!

Thank you!



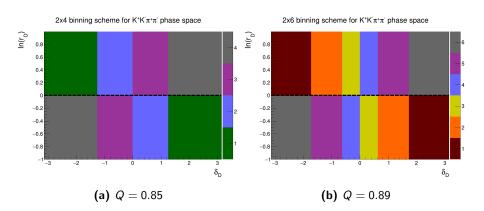
## Backup

## Backup



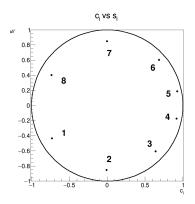
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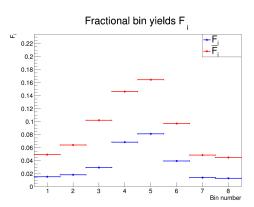
## Binning scheme



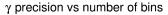


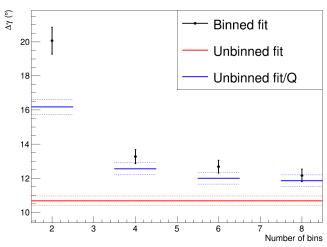
## $c_i$ , $s_i$ and $F_i$





## Comparison of binned fit precision with unbinned fit





## Trigger requirements

Run 1 trigger	(Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS)
requirements	and (Bu_Hlt1TrackAllLODecision_TOS)
	and (Bu_Hlt2Topo2BodyBBDTDecision_TOS or
	Bu_Hlt2Topo3BodyBBDTDecision_TOS or
	Bu_Hlt2Topo4BodyBBDTDecision_TOS or
	Bu_Hlt2IncPhiDecision_TOS)
Run 2 trigger	(Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS)
requirements	and (Bu_Hlt1TrackMVADecision_TOS or
	Bu_Hlt1TwoTrackMVADecision_TOS)
	and (Bu_Hlt2Topo2BodyDecision_TOS or
	Bu_Hlt2Topo3BodyDecision_TOS or
	Bu_Hlt2Topo4BodyDecision_TOS or
	Bu_Hlt2IncPhiDecision_TOS)

## Initial cuts

#### Rectangular cuts before BDT

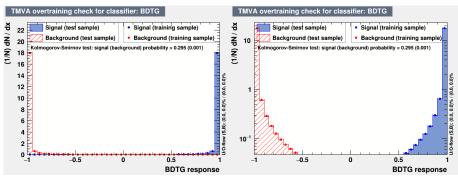
Number	Variable description	Cut
1	DTF converged	True
2	Bachelor momentum	$< 100 {\sf GeV}$
3	Bachelor has RICH	True
4	D invariant mass	[1839.84, 1889.84]MeV
5	$B^\pm$ invariant mass	[5080, 5800]MeV
6	${\mathcal K}^\pm$ daughter PID	> -10
7	$\pi^\pm$ daughter PID	< 20

#### **Boosted Decision Tree**

BDTG from TMVA Toolkit

- Signal sample:  $B^{\pm} \to DK^{\pm}$  and  $B^{\pm} \to D\pi^{\pm}$  MC samples
- Background sample: Data sample with  $m_{R^{\pm}}^{\text{DTF}} \in [5800, 7000] \text{MeV}$
- Random, equal sized test and training samples

#### BDT training results



(a) BDT output

(b) BDT output on a logarithmic scale

#### Final cuts

#### Rectangular cuts after BDT

Number	Variable description	Cut
8	${\it K}^{\pm}$ bachelor PID	> 4
9	$\pi^\pm$ bachelor PID	< 4
10	Bachelor is muon	False
11	z flight significance	> 2
12	$\mathcal{K}^{\pm}$ PID	> 0
13	$\mathcal{K}^0_\mathcal{S}$ mass veto	[477, 507]MeV

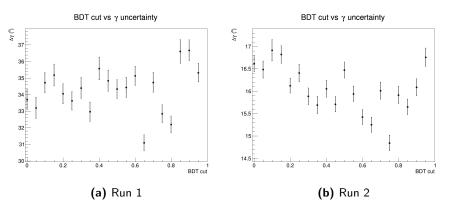
## BDT training variables

Name	Rank (%)	Description
log(DO_RHO_BPV)	7.7	D radial distance to beamline
log(Bu_FDCHI2_OWNPV)	6.3	$B^\pm$ flight distance $\chi^2$
log(Bu_RHO_BPV)	6.1	$B^\pm$ radial distance to beamline
log(Bach_PT)	6.1	Bachelor transverse momentum
Bu_PTASY_1.5	5.3	$B^\pm$ asymmetry parameter
log(1-D0_DIRA_BPV)	5.0	Angle between PV and $D$
log(Bu_IPCHI2_OWNPV)	4.8	$B^\pm$ impact parameter $\chi^2$
log(1-Bu_DIRA_BPV)	4.7	Angle between PV and $B^\pm$
log(h[1,2]_PT)	4.4	${\it K}^{\pm}$ transverse momentum
Bu_MAXDOCA	4.4	$B^\pm$ distance of closest approach
log(Bach_IPCHI2_OWNPV)	4.1	Bachelor impact parameter $\chi^2$

### BDT training particles

Name	Rank (%)	Description
log(Bu_constDOPV_DO_P)	3.7	D momentum from DTF
log(D0_VTXCHI2D0F)	3.3	$D0$ vertex fit $\chi^2$
log(h[3,4]_IPCHI2_OWNPV)	3.3	$\pi^{\pm}$ impact parameter $\chi^2$
log(DO_IPCHI2_OWNPV)	3.2	$D$ impact parameter $\chi^2$
log(h[3,4]_PT)	3.2	$\pi^\pm$ transverse momentum
log(Bu_PT)	2.8	$B^\pm$ transverse momentum
log(h[1,2]_P)	2.8	$\mathit{K}^{\pm}$ momentum
log(Bach_P)	2.7	Bachelor momentum
log(Bu_constDOPV_P)	2.6	$B^\pm$ momentum from DTF
log(h[1,2]_IPCHI2_OWNPV)	2.5	$K^\pm$ impact parameter $\chi^2$
DO_MAXDOCA	2.5	D distance of closest approach
log(Bu_VTXCHI2DOF)	2.0	$B^{\pm}$ vertex fit $\chi^2$
log(h[3,4]_P)	1.9	$\pi^{\pm}$ momentum

## BDT optimization study



- Run 1: Pick BDT working point at 0.65
- Run 2: Pick BDT working point at 0.75

## Partially reconstructed background

- $B^{\pm} \rightarrow D\pi^{\pm}$ :

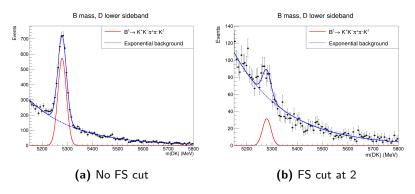
  - 2  $B^0 \to (D^{*\mp} \to D^0[\pi^{\mp}])\pi^{\pm}$
  - **3**  $B^{\pm(0)} \to D^0[\pi^{0(\mp)}]\pi^{\pm}$
  - **4**  $B^{\pm} \to (D^{*0} \to D^0[\gamma])\pi^{\pm}$
- $B^{\pm} \rightarrow DK^{\pm}$ :
  - **1**  $B^{\pm} \to (D^{*0} \to D^0[\pi^0])K^{\pm}$
  - ②  $B^0 \to (D^{*\mp} \to D^0[\pi^{\mp}])K^{\pm}$
  - **3**  $B^{\pm(0)} \to D^0[\pi^{0(\mp)}]K^{\pm}$
  - **4**  $B^{\pm} \to (D^{*0} \to D^0[\gamma])K^{\pm}$
  - **5**  $B_s^0 \to \bar{D^0}[\pi^+]K^-$
  - **10** Mis-ID from partially reconstructed  $B^\pm o D\pi^\pm$  channel

### Charmless background

- $B \to KK\pi\pi K$  background in  $B \to DK$  channel
- Flight significance cut at 2

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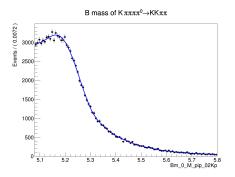
Fix remaining background with Gaussian shape of lower sideband



**Figure 12:** *B* invariant mass in lower *D* sideband

# $D o K\pi\pi\pi\pi^0$ mis-ID background

- $B^{\pm} \rightarrow Dh^{\pm}$ ,  $D \rightarrow K\pi\pi\pi[\pi^0]$
- $\pi^0$  not reconstructed  $\to$  Lower D mass
- Single mis-ID:  $K\pi\pi\pi \to KK\pi\pi \to Higher\ D$  mass
- Generate RapidSim samples, reweight with PIDCalib2



Conclusion: Fix shape from RapidSim, allow yield to float

Martin Tat

### $D o K\pi\pi\pi$ mis-ID background

- $B^{\pm} \rightarrow Dh^{\pm}$ ,  $D \rightarrow K\pi\pi\pi$
- Single mis-ID:  $K\pi\pi\pi \to KK\pi\pi$
- Triple mis-ID:  $\pi\pi K\pi \to KK\pi\pi$

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Use LHCb MC generated with AmpGen, reweight with PIDCalib2

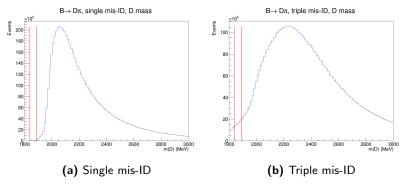


Figure 13: D invariant mass

### $D o K\pi\pi\pi$ mis-ID background

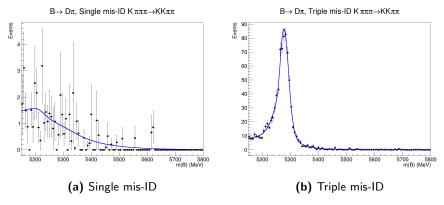


Figure 14: B invariant mass

Conclusion: Negligible impact, include in systematics

### D semileptonic backgrounds

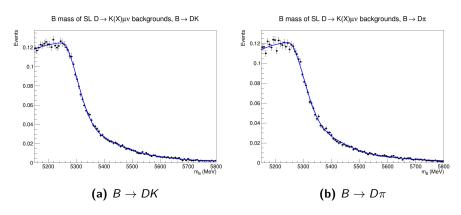
- $B^{\pm} \rightarrow Dh^{\pm}$ ,  $D \rightarrow K(X)I\nu$ ,  $K(X) \rightarrow K\pi\pi$ 
  - $K_1(1270)$
  - $K_1(1400)$
  - K\*(1410)
  - K\*(1680)
  - $K_2^*(1430)$
- Single mis-ID:  $K\mu\pi\pi \to KK\pi\pi$
- Double mis-ID:  $K\pi\pi\mu \to KK\pi\pi$

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Generate RapidSim samples, reweight with PIDCalib2

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### D semileptonic backgrounds



Conclusion: Negligible impact, include in systematics

#### Remaining systematic uncertainties

Different strategies for evaluating systematic uncertainties:

- Generate toy datasets with systematics, fit with default model and take the bias as a systematic:
  - Small backgrounds  $(D \to K(X) l \nu_l, \ D \to K \pi \pi \pi, \ B \to D l \nu_l, \ \Lambda_b)$
  - Bin dependent mass shape
  - Low mass physics effects
- Do multiple fits to data while smearing parameters:
  - $c_i$  and  $s_i$
  - Mass shape
  - Fixed yield fractions

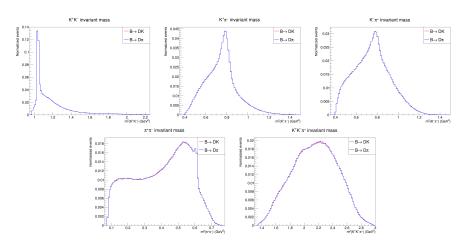
- PID efficiency
- Fit bias: Take bias toys as systematic uncertainty

### Efficiency related systematics

Efficiency related systematics:

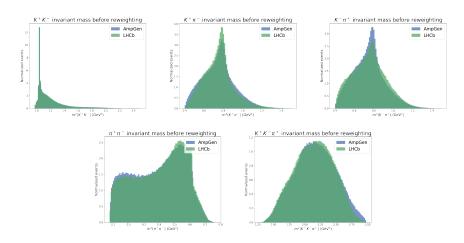
- ullet Difference in  $B^\pm o D K^\pm$  and  $B^\pm o D \pi^\pm$  phase space acceptance
- Efficiency correction of  $c_i$  and  $s_i$

## Efficiency differences between $B^\pm o DK^\pm$ and $B^\pm o D\pi^\pm$



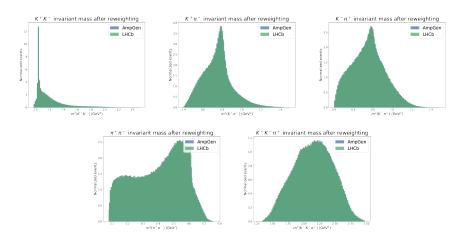
Conclusion: More or less identical phase space acceptance, no systematic uncertainty considered

### Efficiency correction of $c_i$ and $s_i$



Need to reweight events to account for efficiency differences between AmpGen samples and LHCb MC

### Efficiency correction of $c_i$ and $s_i$



After reweighing, use weights to recalculate  $c_i$  and  $s_i$  Conclusion: Efficiency correction of  $c_i$  and  $s_i$  is an order of magnitude smaller than their uncertainties, no systematic uncertainty considered

#### Bonus measurement

- The mode  $B^\pm o Dh^\pm$ ,  $D o \pi^+\pi^-\pi^+\pi^-$  very similar
- Run this through <u>same</u> selection (including BDT)
- ullet Quasi-GLW observables provide additional constraints on  $\gamma$
- Measure observables for both  $\pi^+\pi^-\pi^+\pi^-$  and  $K^+K^-\pi^+\pi^-$

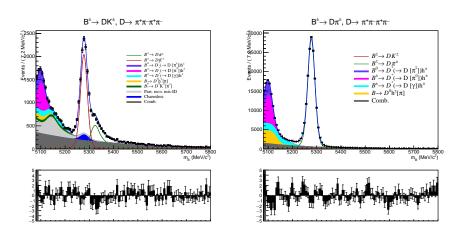
$$A_{h} = \frac{\Gamma(B^{-} \to Dh^{-}) - \Gamma(B^{+} \to Dh^{+})}{\Gamma(B^{-} \to Dh^{-}) + \Gamma(B^{+} \to Dh^{+})},$$

$$R_{\text{CP}} = \frac{R(4\pi)}{R(K3\pi)},$$

$$R = \frac{\Gamma(B \to DK)}{\Gamma(B \to D\pi)}.$$

•  $B^{\pm} \to D h^{\pm}$ ,  $D \to K \pi \pi \pi$  yields provided by Tim Evans

### Global mass fit of $B^\pm o Dh^\pm$ , $D o\pi^+\pi^-\pi^+\pi^-$



**Figure 19:** Fit of  $B^{\pm} \to DK^{\pm}$  channel (left) and  $B^{\pm} \to D\pi^{\pm}$  channel (right) using full Run 1 and 2 data

• Total yields are consistent with  $KK\pi\pi$ 

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