## Model-independent determination of the CKM angle $\gamma$ in $B^\pm \to (K^+K^-\pi^+\pi^-)_D h^\pm$ decays

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#### Outline

- 1 Introduction to the CKM angle  $\gamma$
- 2 Binned  $\gamma$  analysis of the  $D \to K^+K^-\pi^+\pi^-$  mode
- Binning scheme
- Fit to data
- Systematic uncertainties
- 6 Summary and conclusion of  $KK\pi\pi$  analysis

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- Additional constraints from quasi-GLW observables
- Conclusion

## Introduction to the CKM angle $\gamma$

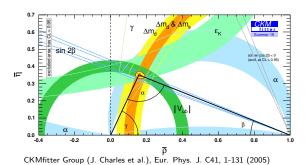
Introduction to the CKM angle  $\gamma$ 

## $\gamma$ and the unitary triangle

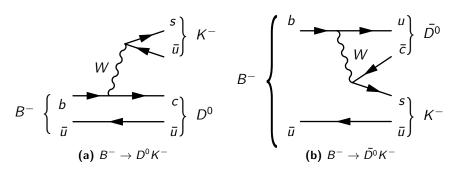
CP violation in SM is described by the Unitary Triangle

$$\gamma = \mathrm{arg}\Big(-rac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\Big)$$

- Only CKM angle accessible at tree level ⇒
  - Negligible theoretical uncertainties
  - Ideal Standard Model benchmark
  - Compare with indirect measurements



## Sensitivity through interference



- ullet Superposition of  $D^0$  and  $ar{D^0}$
- ullet b o uar cs and b o car us interference o Sensitivity to  $\gamma$

$$\mathcal{A}(B^{-}) = \mathcal{A}(D^{0}) + r_{B}e^{i(\delta_{B}-\gamma)}\mathcal{A}(\bar{D^{0}})$$
  
$$\mathcal{A}(B^{+}) = \mathcal{A}(\bar{D^{0}}) + r_{B}e^{i(\delta_{B}+\gamma)}\mathcal{A}(D^{0})$$

## Measurement of $\gamma$ from $B^{\pm} \to DK^{\pm}$ , $D \to K^{+}K^{-}\pi^{+}\pi^{-}$

- First proposed by J. Rademacker and G. Wilkinson
  - Physics Letters B **647** (2007) 400
  - Amplitude model by FOCUS
  - ullet Expected  $\gamma$  precision from amplitude fit with 1000 candidates: 14 $^\circ$
- CLEO amplitude analysis
  - Phys. Rev. D 85 (2012) 122002
  - ullet Expected  $\gamma$  precision from amplitude fit with 2000 candidates:  $11^\circ$
- State of the art amplitude analysis by LHCb:
  - JHEP **02** (2019) 126

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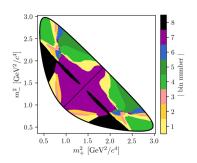
• Use to develop efficient binning scheme

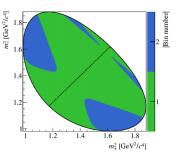
## The $D \rightarrow K^+K^-\pi^+\pi^-$ decay

Binned 
$$\gamma$$
 analysis of the  $D \to K^+K^-\pi^+\pi^-$  mode

## Binned measurement of $\gamma$

- Final measurement will be model-independent
  - Non-optimal binning reduces statistical sensitivity
  - But no bias is induced in final result
- ullet Need strong phases of D decay o Will be measured at BESIII
- ullet Analogous approach to  $B^\pm o D h^\pm$ ,  $D o K_S^0 h^+ h^-$ 
  - JHEP **02** (2021) 0169
  - Single most precise measurement:  $\gamma = (68.7^{+5.2}_{-5.1})^{\circ}$





## The BPGGSZ method

•  $B^{\pm} \rightarrow Dh^{\pm}$  amplitude:

$$\mathcal{A}(B^{-}) = \mathcal{A}(D^{0}) + r_{B}e^{i(\delta_{B}-\gamma)}\mathcal{A}(\bar{D^{0}})$$
  
$$\mathcal{A}(B^{+}) = \mathcal{A}(\bar{D^{0}}) + r_{B}e^{i(\delta_{B}+\gamma)}\mathcal{A}(D^{0})$$

- ullet  $\mathcal{A}(D^0)$  and  $\mathcal{A}(ar{D^0})$  depend on D phase space
- ullet Strong-phase difference of  $D^0$  and  $ar{D^0}$  decays inaccessible at LHCb
- Model-independent measurement: Integrate over bins of phase space

## Event yield in bin i

$$N_{i}^{-} = h_{B^{-}} \Big( F_{i} + (x_{-}^{2} + y_{-}^{2}) \bar{F}_{i} + 2 \sqrt{F_{i} \bar{F}_{i}} (x_{-} c_{i} + y_{-} s_{i}) \Big)$$

$$N_{-i}^{+} = h_{B^{+}} \Big( F_{i} + (x_{+}^{2} + y_{+}^{2}) \bar{F}_{i} + 2 \sqrt{F_{i} \bar{F}_{i}} (x_{+} c_{i} + y_{+} s_{i}) \Big)$$

#### The BPGGSZ method

#### Event yield in bin i

$$\begin{split} N_i^- &= h_{B^-} \big( F_i + (x_-^2 + y_-^2) \bar{F}_i + 2 \sqrt{F_i \bar{F}_i} (x_- c_i + y_- s_i) \big) \\ N_{-i}^+ &= h_{B^+} \big( F_i + (x_+^2 + y_+^2) \bar{F}_i + 2 \sqrt{F_i \bar{F}_i} (x_+ c_i + y_+ s_i) \big) \end{split}$$

- CP observables:
  - $x_{\pm}^{DK} = r_B^{DK} \cos(\delta_B^{DK} \pm \gamma), \quad y_{\pm}^{DK} = r_B^{DK} \sin(\delta_B^{DK} \pm \gamma)$ •  $x_{\xi}^{D\pi} = \text{Re}(\xi^{D\pi}), \ y_{\xi}^{D\pi} = \text{Im}(\xi^{D\pi}) \qquad \left(\xi^{D\pi} = \frac{r_B^{D\pi}}{r_{DK}} e^{i(\delta_B^{D\pi} - \delta_B^{DK})}\right)$
- Fractional bin yield:
  - $F_i = \frac{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2}{\sum_i \int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2}$

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- ullet Floated in the fit, mostly constrained by  $B^\pm o D \pi^\pm$
- Amplitude averaged strong phases can be obtained from BESIII:

$$c_i = \frac{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D^0})| \cos(\delta_D)}{\sqrt{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2 \int_i \mathrm{d}\Phi |\mathcal{A}(\bar{D^0})|^2}} \quad s_i = \frac{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D^0})| \sin(\delta_D)}{\sqrt{\int_i \mathrm{d}\Phi |\mathcal{A}(D^0)|^2 \int_i \mathrm{d}\Phi |\mathcal{A}(\bar{D^0})|^2}}$$

## Binning Scheme

## Binning scheme

## Binning scheme requirements

## A binning scheme must satisfy the following:

- Minimal dilution of strong phases when integrating over bins
- ullet Enhance interference between  $B^\pm o D^0 h^\pm$  and  $B^\pm o ar{D^0} h^\pm$

## How to bin a 5-dimensional phase space?

- Generate C++ code for LHCb amplitude model using AmpGen<sup>1</sup>
- For each  $B^{\pm}$  candidate, calculate

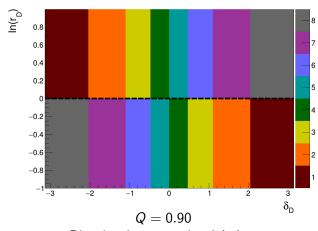
$$\frac{A(D^0)}{A(\bar{D^0})} = r_D e^{i\delta_D}$$

• Bin along  $\delta_D$  and  $r_D$ , maximize Q-value to optimize

<sup>&</sup>lt;sup>1</sup>AmpGen by Tim Evans

## Binning scheme

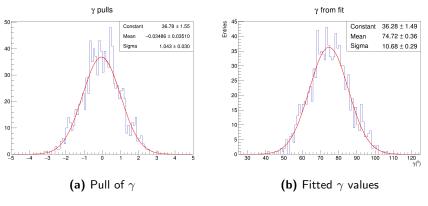
2x8 binning scheme for  $K^+K^-\pi^+\pi^-$  phase space



Bins i < 0 on top, i > 0 below

## $\gamma$ precision benchmark

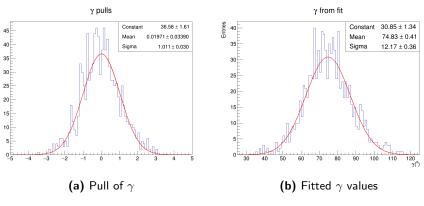
- ullet Generate 2000  $B^\pm o DK^\pm$  candidates using LHCb model in AmpGen
  - Input values:  $\gamma=75^\circ$ ,  $\delta_B=130^\circ$ ,  $r_B=0.1$
- Perform unbinned fit to the same amplitude model using AmpGen



Precision of  $\gamma$  in unbinned fit:  $11^{\circ}$ 

## Study of $\gamma$ precision

- Binned fit setup: Optimized 2 × 8 bins
- Fit same AmpGen samples, using  $c_i$ ,  $s_i$  and  $F_i$  from LHCb model



Precision of  $\gamma$  in binned fit: 12° Consistent with unbinned fit and Q-value

#### Global mass fit

## Global mass fit

## Signal parameterisation

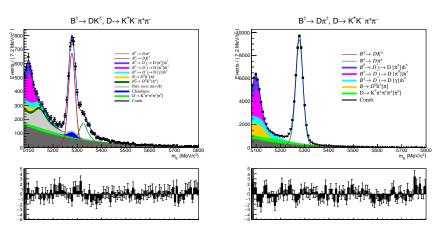
- PDF shape parameterization identical to LHCb-ANA-2020-001
- Signal: Gaussian + Modified Cruijff
- Shape fixed from MC, yield and width floated
- Combinatorial background (exponential)

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Partially reconstructed background (dini shapes)

$$f_{\text{MG}}(m|m_B,\sigma,\alpha_L,\alpha_R,\beta) \propto \begin{cases} \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_L\Delta m^2}\right), & \Delta m=m-m_B<0\\ \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_R\Delta m^2}\right), & \Delta m=m-m_B>0 \end{cases}$$

#### Global mass fit



**Figure 4:** Fit of  $B^{\pm} \to DK^{\pm}$  channel (left) and  $B^{\pm} \to D\pi^{\pm}$  channel (right) using full Run 1 and 2 data

- $B^{\pm} \rightarrow DK^{\pm}$  yield: 3306  $\pm$  75
- $B^{\pm} \rightarrow D\pi^{\pm}$  yield:  $46\,695 \pm 256$

## Binned CP fit

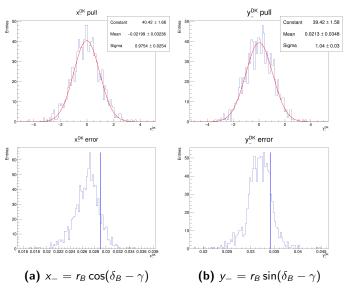
## Binned CP fit

#### Binned CP fit

- Use  $2 \times 8$  bins
- $c_i$  and  $s_i$  not available from BESIII yet  $\Longrightarrow$ 
  - Calculate using MC integration of LHCb amplitude model for now
- Fit for CP observables
- PDF shape parameters fixed from global mass fit
- Yield of signal, low mass partially reconstructed background and combinatorial background floated
- Fractional yields F<sub>i</sub> floated

$$\mathcal{R}_{i} = \begin{cases} F_{i}, & i = -8 \\ F_{i} / \sum_{j \geq i} F_{j}, -8 < i \leq +8 \end{cases}$$

## CP observables result: $x_{-}^{DK}$ and $y_{-}^{DK}$

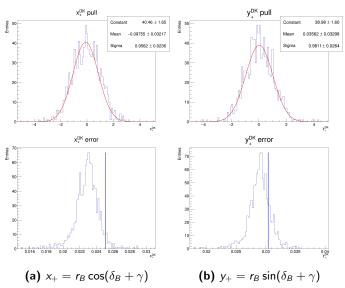


Pulls and uncertainties from toy studies, uncertainty from data fit in blue

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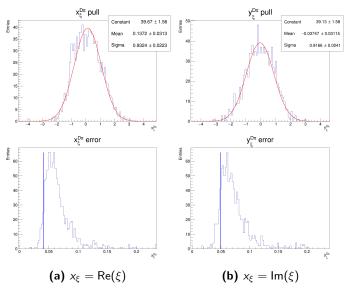
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## CP observables result: $x_{+}^{DK}$ and $y_{+}^{DK}$



Pulls and uncertainties from toy studies, uncertainty from data fit in blue

## CP observables result: $x_{\xi}^{D\pi}$ and $y_{\xi}^{D\pi}$



Pulls and uncertainties from toy studies, uncertainty from data fit in blue

## Systematic uncertainties

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## c<sub>i</sub> and s<sub>i</sub> systematic uncertainty

- $\bullet$   $c_i$  and  $s_i$  uncertainty will come from BESIII analysis
  - Mostly statistical in origin
- Largest systematic uncertainty
- ullet Use estimated uncertainties corresponding to 20 fb $^{-1}$  at  $\psi(3770)$
- Smear  $c_i$  and  $s_i$  and do many fits to data

## Summary of all systematic uncertainties

Uncertainties of CP observables in units of  $10^{-2}$ 

| Source                      | $x_{-}^{DK}$ | $y_{-}^{DK}$ | $x_{+}^{DK}$ | $y_+^{DK}$ | $x_{\xi}^{D\pi}$ | $y_{\xi}^{D\pi}$ |
|-----------------------------|--------------|--------------|--------------|------------|------------------|------------------|
| Statistical                 | 2.91         | 3.41         | 2.51         | 3.04       | 4.04             | 4.89             |
| $C_i$ , $S_i$               | 0.66         | 1.55         | 0.32         | 1.31       | 1.73             | 1.03             |
| $B^\pm	o D\mu u$ background | 0.04         | 0.03         | 0.02         | 0.15       | 0.30             | 0.10             |
| $D	o K(X) I u_I$ background | 0.15         | 0.05         | 0.11         | 0.03       | 0.35             | 0.25             |
| $D	o K\pi\pi\pi$ background | 0.17         | 0.03         | 0.04         | 0.01       | 0.46             | 0.18             |
| $\Lambda_b$ background      | 0.09         | 0.11         | 0.00         | 0.18       | 0.16             | 0.21             |
| Bin dependent mass shape    | 0.21         | 0.05         | 0.17         | 0.01       | 0.37             | 0.11             |
| Fit bias                    | 0.19         | 0.03         | 0.16         | 0.04       | 0.30             | 0.16             |
| Fixed yield fractions       | 0.02         | 0.03         | 0.02         | 0.02       | 0.01             | 0.01             |
| Low mass physics effects    | 0.05         | 0.09         | 0.05         | 0.18       | 0.41             | 0.48             |
| Mass shape                  | 0.03         | 0.03         | 0.02         | 0.02       | 0.04             | 0.01             |
| PID Efficiency              | 0.03         | 0.03         | 0.02         | 0.02       | 0.04             | 0.01             |
| Total LHCb systematic       | 0.39         | 0.17         | 0.27         | 0.30       | 0.92             | 0.65             |
| Total systematic            | 0.77         | 1.55         | 0.41         | 1.34       | 2.01             | 1.23             |

## Summary and conclusion of $KK\pi\pi$ analysis

# Summary and conclusion of $KK\pi\pi$ analysis

## Summary of CP observables

Measured CP observables:

$$\begin{split} x_{-}^{DK} &= (x.x \pm 2.9 \pm 0.4 \pm 0.7) \times 10^{-2}, \\ y_{-}^{DK} &= (x.x \pm 3.4 \pm 0.2 \pm 1.6) \times 10^{-2}, \\ x_{+}^{DK} &= (x.x \pm 2.5 \pm 0.3 \pm 0.3) \times 10^{-2}, \\ y_{+}^{DK} &= (x.x \pm 3.0 \pm 0.3 \pm 1.3) \times 10^{-2}, \\ x_{\xi}^{D\pi} &= (x.x \pm 4.0 \pm 0.9 \pm 1.7) \times 10^{-2}, \\ y_{\xi}^{D\pi} &= (x.x \pm 4.9 \pm 0.7 \pm 1.0) \times 10^{-2}, \end{split}$$

- Note: Currently using  $c_i$  and  $s_i$  from the LHCb model
- Publication strategy: Publish current results together with binned yields  $\rightarrow$  Redo fit to obtain model-independent CP observables once c; and s; from BESIII are available
- Will update c<sub>i</sub> and s<sub>i</sub> with model-dependent uncertainties

#### Bonus measurement

- The mode  $B^\pm o Dh^\pm$ ,  $D o \pi^+\pi^-\pi^+\pi^-$  very similar
- Run this through <u>same</u> selection (including BDT)
- $\bullet$  Quasi-GLW observables provide additional constraints on  $\gamma$
- Measure observables for both  $\pi^+\pi^-\pi^+\pi^-$  and  $K^+K^-\pi^+\pi^-$

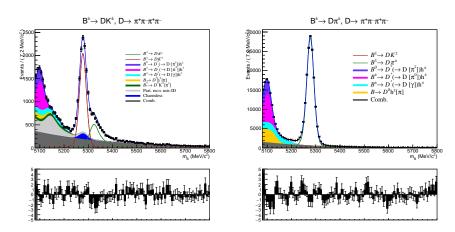
$$A_{h} = \frac{\Gamma(B^{-} \to Dh^{-}) - \Gamma(B^{+} \to Dh^{+})}{\Gamma(B^{-} \to Dh^{-}) + \Gamma(B^{+} \to Dh^{+})},$$

$$R_{\text{CP}} = \frac{R(4h)}{R(K3\pi)},$$

$$R = \frac{\Gamma(B \to DK)}{\Gamma(B \to D\pi)}.$$

•  $B^{\pm} \to D h^{\pm}$ ,  $D \to K \pi \pi \pi$  yields provided by Tim Evans

## Global mass fit of $B^\pm o Dh^\pm$ , $D o \pi^+\pi^-\pi^+\pi^-$



**Figure 8:** Fit of  $B^{\pm} \to DK^{\pm}$  channel (left) and  $B^{\pm} \to D\pi^{\pm}$  channel (right) using full Run 1 and 2 data

• Total yields are consistent with  $KK\pi\pi$ 

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#### Conclusion

- Binned  $\gamma$  analysis of  $B^{\pm} \to (K^+K^-\pi^+\pi^-)_D h^{\pm}$  is mostly complete, with promising results
  - Expect total uncertainty around 12°-14°
- Add quasi-GLW observables of  $K^+K^-\pi^+\pi^-$  and  $\pi^+\pi^-\pi^+\pi^-$  to further constrain  $\gamma$
- Will publish model-dependent measurement for now, update with model-independent results when  $c_i$  and  $s_i$  from BESIII are available
- Analysis note: LHCb-ANA-2021-051

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## Thank you!

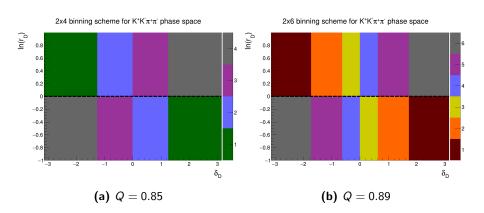
Thank you!

## Backup

## Backup

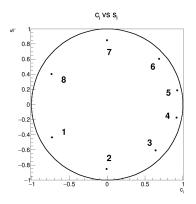


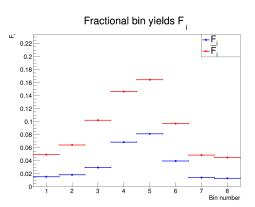
## Binning scheme



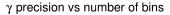


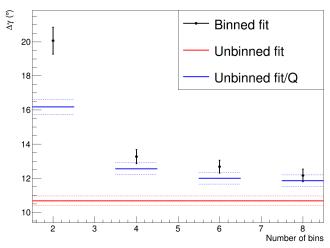
## $c_i$ , $s_i$ and $F_i$





## Comparison of binned fit precision with unbinned fit





## Trigger requirements

| Run 1 trigger | (Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS) |
|---------------|--|
| requirements  | and (Bu_Hlt1TrackAllLODecision_TOS)          |
|               | and (Bu_Hlt2Topo2BodyBBDTDecision_TOS or     |
|               | Bu_Hlt2Topo3BodyBBDTDecision_TOS or          |
|               | Bu_Hlt2Topo4BodyBBDTDecision_TOS or          |
|               | Bu_Hlt2IncPhiDecision_TOS)                   |
| Run 2 trigger | (Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS) |
| requirements  | and (Bu_Hlt1TrackMVADecision_TOS or          |
|               | Bu_Hlt1TwoTrackMVADecision_TOS)              |
|               | and (Bu_Hlt2Topo2BodyDecision_TOS or         |
|               | Bu_Hlt2Topo3BodyDecision_TOS or              |
|               | Bu_Hlt2Topo4BodyDecision_TOS or              |
|               | Bu_Hlt2IncPhiDecision_TOS)                   |

### Initial cuts

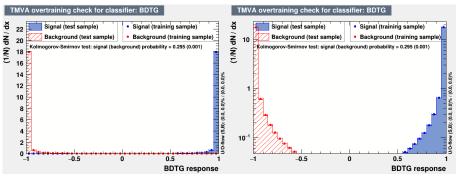
### Rectangular cuts before BDT

| Number | Variable description            | Cut                   |
|--------|---------------------------------|-----------------------|
| 1      | DTF converged                   | True                  |
| 2      | Bachelor momentum               | $< 100 {\sf GeV}$     |
| 3      | Bachelor has RICH               | True                  |
| 4      | D invariant mass                | [1839.84, 1889.84]MeV |
| 5      | $B^\pm$ invariant mass          | [5080, 5800]MeV       |
| 6      | ${\mathcal K}^\pm$ daughter PID | > -10                 |
| 7      | $\pi^\pm$ daughter PID          | < 20                  |

### **Boosted Decision Tree**

- BDTG from TMVA Toolkit
- Signal sample:  $B^\pm \to DK^\pm$  and  $B^\pm \to D\pi^\pm$  MC samples
- Background sample: Data sample with  $m_{B^{\pm}}^{\mathsf{DTF}} \in [5800, 7000] \mathsf{MeV}$
- Random, equal sized test and training samples

### BDT training results



(a) BDT output

(b) BDT output on a logarithmic scale

### Final cuts

#### Rectangular cuts after BDT

| Number | Variable description           | Cut           |
|--------|--------------------------------|---------------|
| 8      | $\mathcal{K}^\pm$ bachelor PID | > 4           |
| 9      | $\pi^\pm$ bachelor PID         | < 4           |
| 10     | Bachelor is muon               | False         |
| 11     | z flight significance          | > 2           |
| 12     | $\mathcal{K}^{\pm}$ PID        | > 0           |
| 13     | $K_S^0$ mass veto              | [477, 507]MeV |

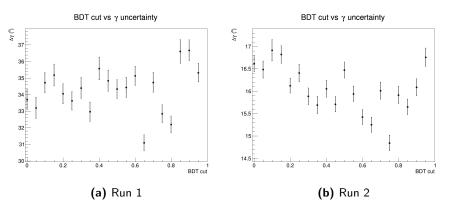
# BDT training variables

| Name                   | Rank (%) | Description                          |
|------------------------|----------|--------------------------------------|
| log(DO_RHO_BPV)        | 7.7      | D radial distance to beamline        |
| log(Bu_FDCHI2_OWNPV)   | 6.3      | $B^\pm$ flight distance $\chi^2$     |
| log(Bu_RHO_BPV)        | 6.1      | $B^\pm$ radial distance to beamline  |
| log(Bach_PT)           | 6.1      | Bachelor transverse momentum         |
| Bu_PTASY_1.5           | 5.3      | $B^\pm$ asymmetry parameter          |
| log(1-D0_DIRA_BPV)     | 5.0      | Angle between PV and $D$             |
| log(Bu_IPCHI2_OWNPV)   | 4.8      | $B^\pm$ impact parameter $\chi^2$    |
| log(1-Bu_DIRA_BPV)     | 4.7      | Angle between PV and $B^\pm$         |
| log(h[1,2]_PT)         | 4.4      | ${\it K}^{\pm}$ transverse momentum  |
| Bu_MAXDOCA             | 4.4      | $B^\pm$ distance of closest approach |
| log(Bach_IPCHI2_OWNPV) | 4.1      | Bachelor impact parameter $\chi^2$   |

### BDT training particles

| Name                     | Rank (%) | Description                           |
|--------------------------|----------|---------------------------------------|
| log(Bu_constDOPV_DO_P)   | 3.7      | D momentum from DTF                   |
| log(DO_VTXCHI2DOF)       | 3.3      | D0 vertex fit $\chi^2$                |
| log(h[3,4]_IPCHI2_OWNPV) | 3.3      | $\pi^{\pm}$ impact parameter $\chi^2$ |
| log(DO_IPCHI2_OWNPV)     | 3.2      | $D$ impact parameter $\chi^2$         |
| log(h[3,4]_PT)           | 3.2      | $\pi^{\pm}$ transverse momentum       |
| log(Bu_PT)               | 2.8      | $B^\pm$ transverse momentum           |
| log(h[1,2]_P)            | 2.8      | $\mathcal{K}^{\pm}$ momentum          |
| log(Bach_P)              | 2.7      | Bachelor momentum                     |
| log(Bu_constDOPV_P)      | 2.6      | $B^\pm$ momentum from DTF             |
| log(h[1,2]_IPCHI2_OWNPV) | 2.5      | $K^{\pm}$ impact parameter $\chi^2$   |
| DO_MAXDOCA               | 2.5      | D distance of closest approach        |
| log(Bu_VTXCHI2DOF)       | 2.0      | $B^{\pm}$ vertex fit $\chi^2$         |
| log(h[3,4]_P)            | 1.9      | $\pi^{\pm}$ momentum                  |

## BDT optimization study



- Run 1: Pick BDT working point at 0.65
- Run 2: Pick BDT working point at 0.75

# Partially reconstructed background

- $B^{\pm} \rightarrow D\pi^{\pm}$ :
  - **1**  $B^{\pm} \to (D^{*0} \to D^0[\pi^0])\pi^{\pm}$
  - 2  $B^0 \to (D^{*\mp} \to D^0[\pi^{\mp}])\pi^{\pm}$
  - **3**  $B^{\pm(0)} \to D^0[\pi^{0(\mp)}]\pi^{\pm}$
  - **3**  $B^{\pm} \to (D^{*0} \to D^0[\gamma])\pi^{\pm}$
- $B^{\pm} \rightarrow DK^{\pm}$ :
  - **1**  $B^{\pm} \to (D^{*0} \to D^0[\pi^0])K^{\pm}$
  - 2  $B^0 \to (D^{*\mp} \to D^0[\pi^{\mp}])K^{\pm}$
  - **3**  $B^{\pm(0)} \to D^0[\pi^{0(\mp)}]K^{\pm}$
  - **4**  $B^{\pm} \to (D^{*0} \to D^{0}[\gamma])K^{\pm}$

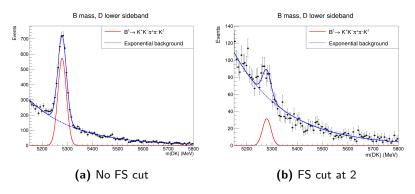
- **6**  $B_s^0 \to \bar{D^0}[\pi^+]K^-$
- **10** Mis-ID from partially reconstructed  $B^\pm o D\pi^\pm$  channel

### Charmless background

- $B \to KK\pi\pi K$  background in  $B \to DK$  channel
- Flight significance cut at 2

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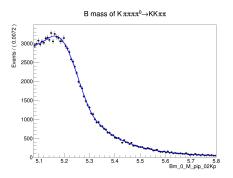
• Fix remaining background with Gaussian shape of lower sideband



**Figure 13:** *B* invariant mass in lower *D* sideband

# $D o K\pi\pi\pi\pi^0$ mis-ID background

- $B^{\pm} \rightarrow Dh^{\pm}$ ,  $D \rightarrow K\pi\pi\pi[\pi^0]$
- $\pi^0$  not reconstructed o Lower D mass
- Single mis-ID:  $K\pi\pi\pi \to KK\pi\pi \to Higher\ D$  mass
- Generate RapidSim samples, reweight with PIDCalib2



Conclusion: Fix shape from RapidSim, allow yield to float

### $D o K\pi\pi\pi$ mis-ID background

- $B^{\pm} \rightarrow Dh^{\pm}$ ,  $D \rightarrow K\pi\pi\pi$
- Single mis-ID:  $K\pi\pi\pi \to KK\pi\pi$
- Triple mis-ID:  $\pi\pi K\pi \to KK\pi\pi$

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Use LHCb MC generated with AmpGen, reweight with PIDCalib2

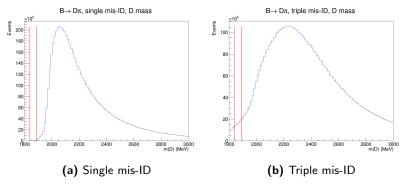


Figure 14: D invariant mass

### $D \to K \pi \pi \pi$ mis-ID background

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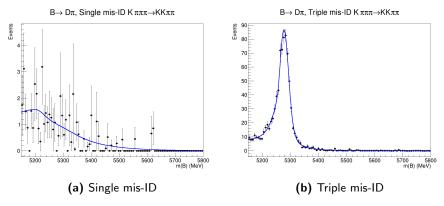


Figure 15: B invariant mass

Conclusion: Negligible impact, include in systematics

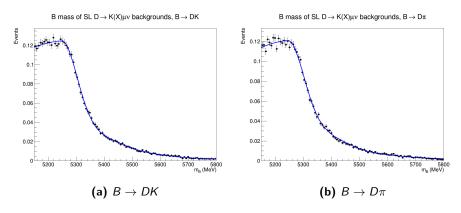
## D semileptonic backgrounds

- $B^{\pm} \rightarrow Dh^{\pm}$ ,  $D \rightarrow K(X)I\nu$ ,  $K(X) \rightarrow K\pi\pi$ 
  - $K_1(1270)$
  - $K_1(1400)$
  - K\*(1410)
  - K\*(1680)
  - $K_2^*(1430)$
- Single mis-ID:  $K\mu\pi\pi \to KK\pi\pi$
- Double mis-ID:  $K\pi\pi\mu \to KK\pi\pi$

Sneha Malde

Generate RapidSim samples, reweight with PIDCalib2

### D semileptonic backgrounds



Conclusion: Negligible impact, include in systematics

### Remaining systematic uncertainties

Different strategies for evaluating systematic uncertainties:

- Generate toy datasets with systematics, fit with default model and take the bias as a systematic:
  - Small backgrounds  $(D \to K(X) I \nu_I, D \to K \pi \pi \pi, B \to D I \nu_I, \Lambda_b)$
  - Bin dependent mass shape
  - Low mass physics effects
- Do multiple fits to data while smearing parameters:
  - $c_i$  and  $s_i$
  - Mass shape
  - Fixed yield fractions

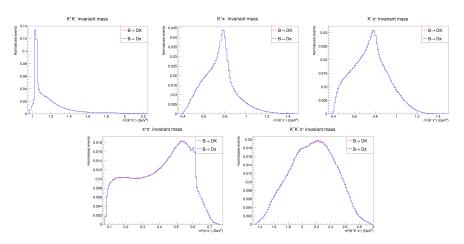
- PID efficiency
- Fit bias: Take bias toys as systematic uncertainty

### Efficiency related systematics

### Efficiency related systematics:

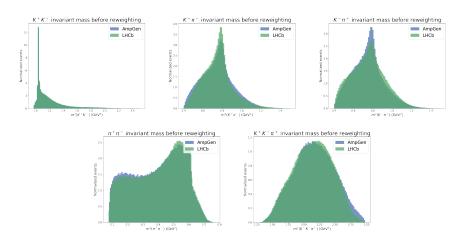
- Difference in  $B^{\pm} \to DK^{\pm}$  and  $B^{\pm} \to D\pi^{\pm}$  phase space acceptance
- Efficiency correction of c<sub>i</sub> and s<sub>i</sub>

## Efficiency differences between $B^\pm o DK^\pm$ and $B^\pm o D\pi^\pm$



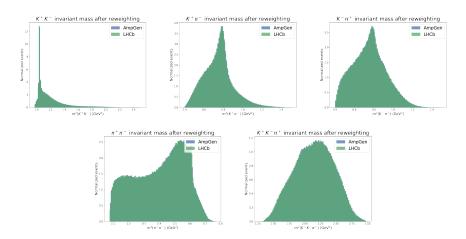
Conclusion: More or less identical phase space acceptance, no systematic uncertainty considered

### Efficiency correction of $c_i$ and $s_i$



Need to reweight events to account for efficiency differences between AmpGen samples and LHCb MC

### Efficiency correction of $c_i$ and $s_i$



After reweighing, use weights to recalculate  $c_i$  and  $s_i$  Conclusion: Efficiency correction of  $c_i$  and  $s_i$  is an order of magnitude smaller than their uncertainties, no systematic uncertainty considered