

Determination of the CKM angle γ in $B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm$ decays

Martin Tat Guy Wilkinson Sneha Malde

University of Oxford

B2OC Meeting

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Outline

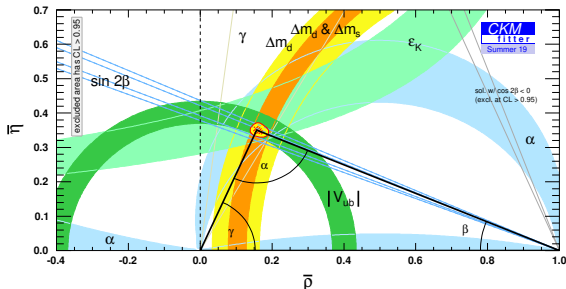
- 1 Introduction to the CKM angle γ
- 2 Binned γ analysis of the $D \rightarrow K^+ K^- \pi^+ \pi^-$ mode
- 3 Binning scheme
- 4 $B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm$ selection
- 5 Backgrounds
- 6 Fit to data
- 7 Systematic uncertainty
- 8 Summary and conclusion

γ and the unitary triangle

- Unitarity of CKM matrix: $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \Rightarrow$

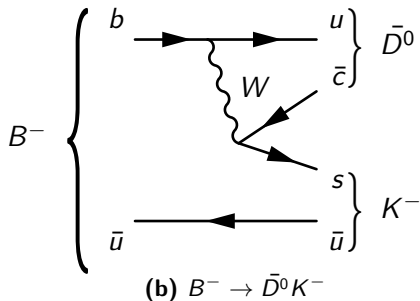
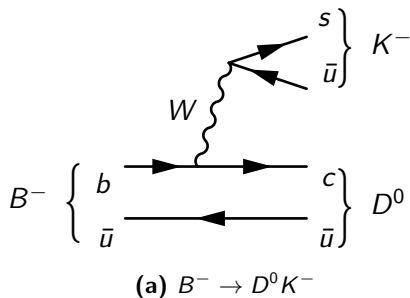
$$\gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$$

- Only CKM angle accessible at tree level \Rightarrow
 - Negligible theoretical uncertainties
 - Ideal Standard Model benchmark
 - Compare with indirect measurements



CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005)

Sensitivity through interference



- Superposition of D^0 and \bar{D}^0
- $b \rightarrow u\bar{c}s$ and $b \rightarrow c\bar{u}s$ interference \rightarrow Sensitivity to γ

$$\begin{aligned}\mathcal{A}(B^-) &= \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D}^0) \\ \mathcal{A}(B^+) &= \mathcal{A}(\bar{D}^0) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0)\end{aligned}$$

Measurement of γ from $B^\pm \rightarrow DK^\pm, D \rightarrow K^+K^-\pi^+\pi^-$

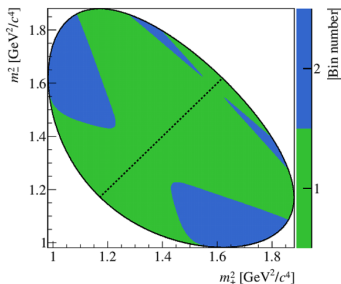
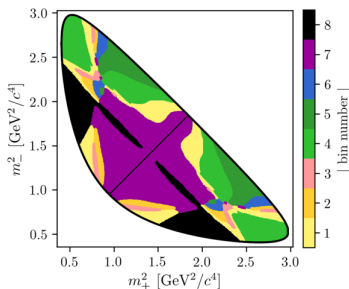
- First proposed by J. Rademacker and G. Wilkinson
 - [arXiv:hep-ph/0611272](#)
 - Amplitude model by FOCUS
 - Expected γ precision with 1000 candidates: 14°
- CLEO amplitude analysis
 - [arXiv:1201.5716](#)
 - Expected γ precision with 2000 candidates: 11°
- State of the art amplitude analysis by LHCb :
 - [LHCb-PAPER-2018-041](#)
 - Use to develop efficient binning scheme

The $D \rightarrow K^+ K^- \pi^+ \pi^-$ decay

Binned γ analysis of the
 $D \rightarrow K^+ K^- \pi^+ \pi^-$ mode

Binned measurement of γ

- Final measurement will be model-independent
 - Poor binning reduces statistical sensitivity \rightarrow No bias!
- Need strong phases of D decay \rightarrow Measure at BESIII
- LHCb-PAPER-2020-019: $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K_S^0 h^+ h^-$
 - Single most precise measurement: $\gamma = (68.7^{+5.2}_{-5.1})^\circ$



The BPGGSZ method

- $B^\pm \rightarrow Dh^\pm$ amplitude:

$$\begin{aligned}\mathcal{A}(B^-) &= \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D}^0) \\ \mathcal{A}(B^+) &= \mathcal{A}(\bar{D}^0) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0)\end{aligned}$$

- $\mathcal{A}(D^0)$ and $\mathcal{A}(\bar{D}^0)$ depend on D phase space
- Strong-phase difference of D^0 and \bar{D}^0 decays inaccessible at LHCb
- Model-independent measurement: Integrate over bins of phase space

Event yield in bin i

$$\begin{aligned}N_i^- &= h_{B^-} \left(F_i + (x_-^2 + y_-^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_- c_i + y_- s_i) \right) \\ N_{-i}^+ &= h_{B^+} \left(F_i + (x_+^2 + y_+^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_+ c_i + y_+ s_i) \right)\end{aligned}$$

The BPGGSZ method

Event yield in bin i

$$N_i^- = h_{B^-} (F_i + (x_-^2 + y_-^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_- c_i + y_- s_i))$$

$$N_i^+ = h_{B^+} (F_i + (x_+^2 + y_+^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_+ c_i + y_+ s_i))$$

- CP observables:

- $x_{\pm}^{DK} = r_B^{DK} \cos(\delta_B^{DK} \pm \gamma), \quad y_{\pm}^{DK} = r_B^{DK} \sin(\delta_B^{DK} \pm \gamma)$
- $x_{\xi}^{D\pi} = \text{Re}(\xi^{D\pi}), \quad y_{\xi}^{D\pi} = \text{Im}(\xi^{D\pi}) \quad \left(\xi^{D\pi} = \frac{r_B^{D\pi}}{r_B^{DK}} e^{i(\delta_B^{D\pi} - \delta_B^{DK})} \right)$

- Fractional bin yield:

- $F_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)|^2}{\sum_j \int_j d\Phi |\mathcal{A}(D^0)|^2}$
- Floated in the fit, mostly constrained by $B^{\pm} \rightarrow D\pi^{\pm}$

- Amplitude averaged strong phases from BESIII:

$$c_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D}^0)| \cos(\delta_D)}{\sqrt{\int_i d\Phi |\mathcal{A}(D^0)|^2 \int_i d\Phi |\mathcal{A}(\bar{D}^0)|^2}}, \quad s_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D}^0)| \sin(\delta_D)}{\sqrt{\int_i d\Phi |\mathcal{A}(D^0)|^2 \int_i d\Phi |\mathcal{A}(\bar{D}^0)|^2}}$$

Binning scheme

A binning scheme must satisfy the following:

- Minimal dilution of strong phases when integrating over bins
- Enhance interference between $B^\pm \rightarrow D^0 h^\pm$ and $B^\pm \rightarrow \bar{D}^0 h^\pm$

How to bin a 5-dimensional phase space?

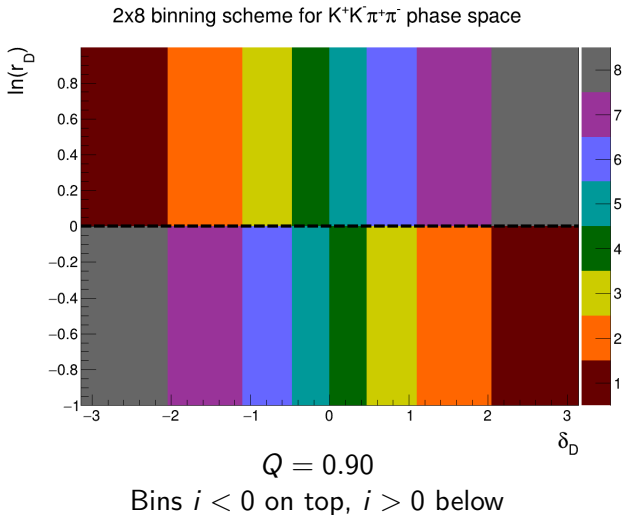
- Generate C++ code for LHCb amplitude model using AmpGen¹
- For each B^\pm candidate, calculate

$$\frac{\mathcal{A}(D^0)}{\mathcal{A}(\bar{D}^0)} = r_D e^{i\delta_D}$$

- Bin along δ_D and r_D , maximize Q -value to optimize

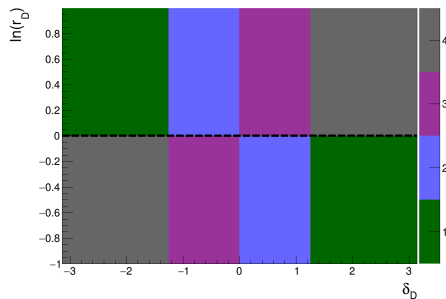
¹AmpGen by Tim Evans

Binning scheme



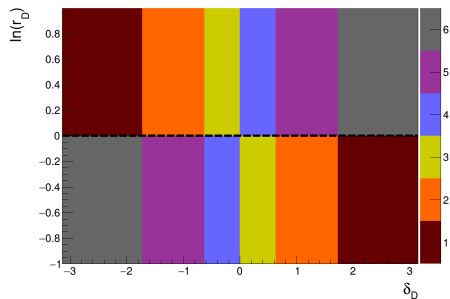
Binning scheme

2x4 binning scheme for $K^+K^-\pi^+\pi^-$ phase space



(a) $Q = 0.85$

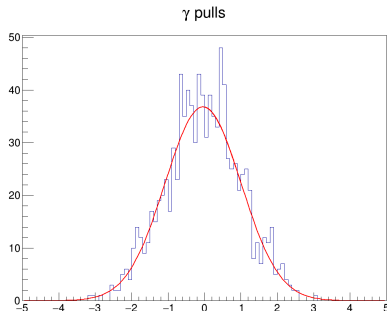
2x6 binning scheme for $K^+K^-\pi^+\pi^-$ phase space



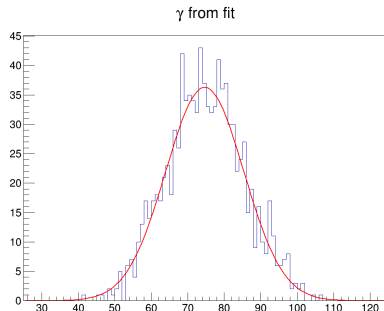
(b) $Q = 0.89$

γ precision benchmark

- Generate 2000 $B^\pm \rightarrow DK^\pm$ candidates using LHCb model in AmpGen
- Fit back with same model using AmpGen



(a) Pull of γ

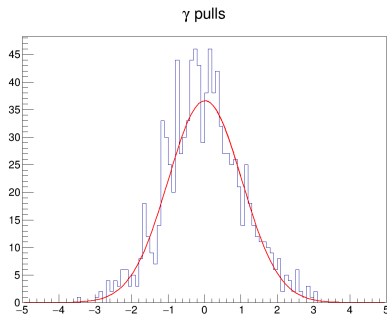


(b) Fitted γ values

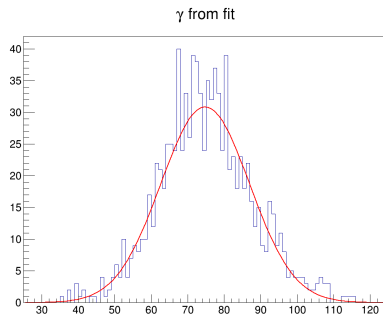
Precision of γ in unbinned fit: 11°

Study of γ precision

- Binned fit setup: Optimized 2×8 bins
- Fit same AmpGen samples, using c_i , s_i and F_i from LHCb model



(a) Pull of γ

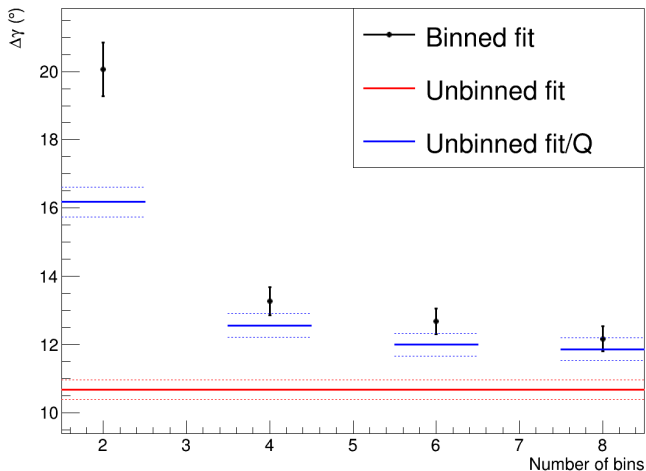


(b) Fitted γ values

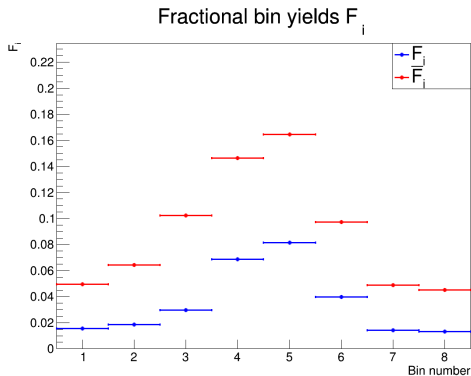
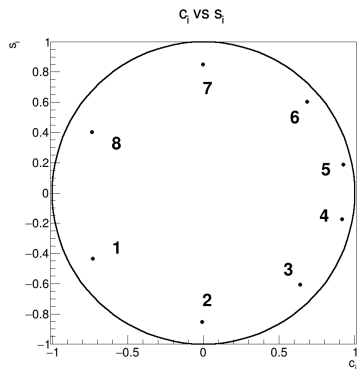
Precision of γ in binned fit: 12°
Consistent with unbinned fit and Q -value

Comparison of binned fit precision with unbinned fit

γ precision vs number of bins



c_i , s_i and F_i



$$B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm \text{ selection}$$

$$B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm \text{ selection}$$

- Stripping lines:
 - StrippingB2D0PiD2HHHHBeauty2CharmLineDecision
 - StrippingB2D0KD2HHHHBeauty2CharmLineDecision
- Data samples: 2011-2018 (Run 1 and 2)
- MC samples: 2011-2018 (excluding 2015), filtered, AmpGen

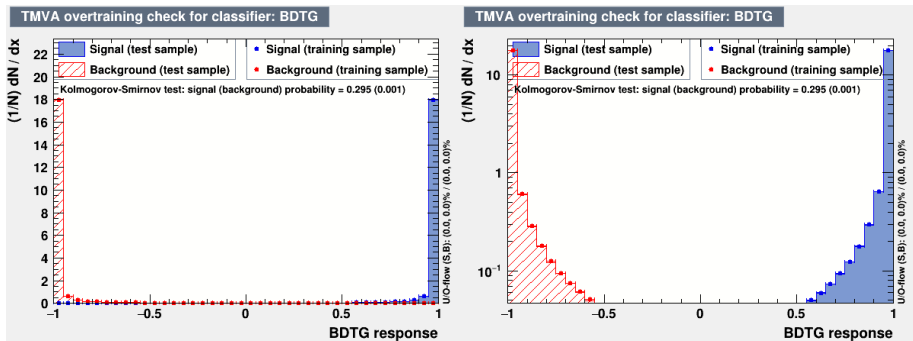
Rectangular cuts before BDT

Number	Variable description	Cut
1	DTF converged	True
2	Bachelor momentum	$< 100\text{GeV}$
3	Bachelor has RICH	True
4	D invariant mass	$[1839.84, 1889.84]\text{MeV}$
5	B^\pm invariant mass	$[5080, 5800]\text{MeV}$
6	K^\pm daughter PID	> -10
7	π^\pm daughter PID	< 20

Boosted Decision Tree

- BDTG from TMVA Toolkit
- Signal sample: $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$ MC samples
- Background sample: $B^\pm \rightarrow D\pi^\pm$ using $m_{B^\pm}^{\text{DTF}} \in [5800, 7000]\text{MeV}$
- Random, equal sized test and training samples

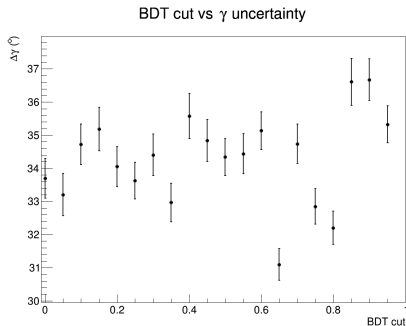
BDT training results



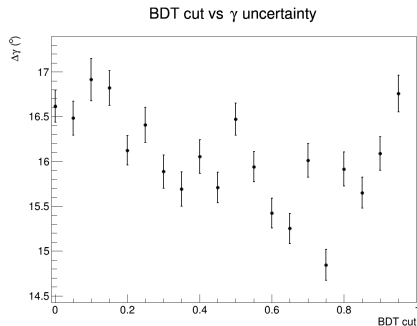
(a) BDT output

(b) BDT output on a logarithmic scale

BDT optimization study



(a) Run 1



(b) Run 2

- Run 1: Pick BDT working point at 0.65
- Run 2: Pick BDT working point at 0.75

Rectangular cuts after BDT

Number	Variable description	Cut
8	K^\pm bachelor PID	> 4
9	π^\pm bachelor PID	< 4
10	Bachelor is muon	False
11	z flight significance	> 2
12	K^\pm PID	> 0
13	K_S^0 mass veto	$[477, 507]\text{MeV}$

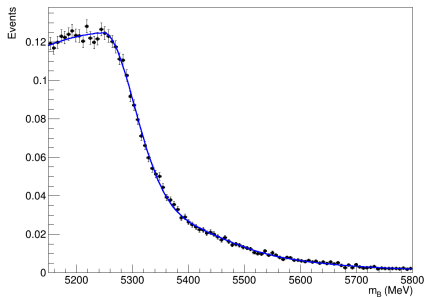
Backgrounds

D semileptonic backgrounds

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K(X)l\nu$, $K(X) \rightarrow K\pi\pi$
 - $K_1(1270)$
 - $K_1(1400)$
 - $K^*(1410)$
 - $K^*(1680)$
 - $K_2^*(1430)$
- Single mis-ID: $K\mu\pi\pi \rightarrow KK\pi\pi$
- Double mis-ID: $K\pi\pi\mu \rightarrow KK\pi\pi$
- Generate Rapidsim samples, reweight with PIDCalib2

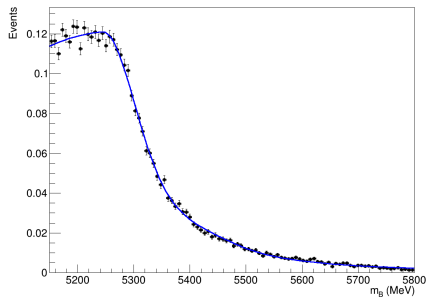
D semileptonic backgrounds

B mass of SL $D \rightarrow K(X)\mu\nu$ backgrounds, $B \rightarrow DK$



(a) $B \rightarrow DK$

B mass of SL $D \rightarrow K(X)\mu\nu$ backgrounds, $B \rightarrow D\pi$

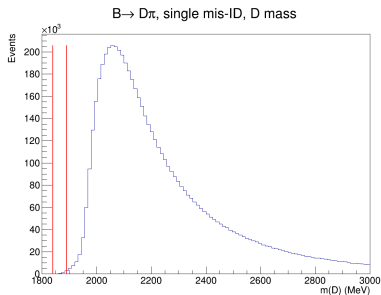


(b) $B \rightarrow D\pi$

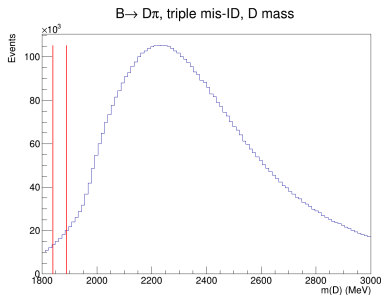
Conclusion: Negligible impact, include in systematics

$D \rightarrow K\pi\pi\pi$ mis-ID background

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K\pi\pi\pi$
- Single mis-ID: $K\pi\pi\pi \rightarrow KK\pi\pi$
- Triple mis-ID: $\pi\pi K\pi \rightarrow KK\pi\pi$
- Use LHCb MC generated with AmpGen, reweight with PIDCalib2



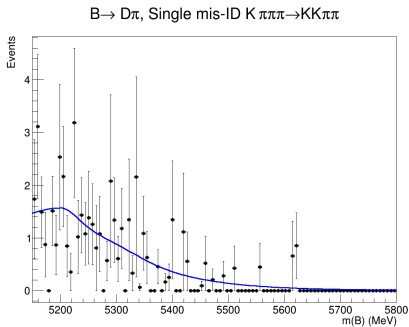
(a) Single mis-ID



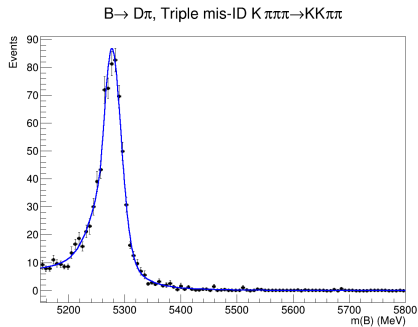
(b) Triple misID

Figure 9: D invariant mass

$D \rightarrow K\pi\pi\pi$ mis-ID background



(a) Single mis-ID



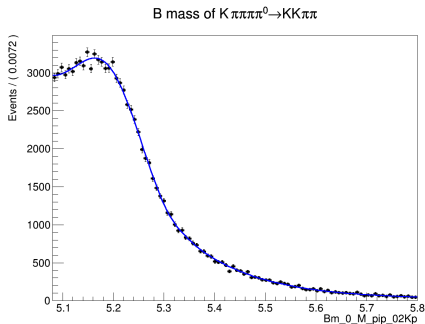
(b) Triple misID

Figure 10: B invariant mass

Conclusion: Negligible impact, include in systematics

$D \rightarrow K\pi\pi\pi\pi^0$ mis-ID background

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K\pi\pi\pi[\pi^0]$
- π^0 not reconstructed \rightarrow Lower D mass
- Single mis-ID: $K\pi\pi\pi \rightarrow KK\pi\pi \rightarrow$ Higher D mass
- Generate RapidSim samples, reweight with PIDCalib2



Conclusion: Fix shape from RapidSim, allow yield to float

Global fit

- PDF shape parameterization identical to LHCb-ANA-2020-001
- Signal: Gaussian + Modified Cruijff
- Shape fixed from MC, yield and width floated
- Exponential background

$$f_{\text{MG}}(m|m_B, \sigma, \alpha_L, \alpha_R, \beta) \propto \begin{cases} \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_L\Delta m^2}\right), & \Delta m = m - m_B < 0 \\ \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_R\Delta m^2}\right), & \Delta m = m - m_B > 0 \end{cases}$$

Partially reconstructed background

- $B^\pm \rightarrow D\pi^\pm$:

- ① $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\pi^0])\pi^\pm$

- ② $B^0 \rightarrow (D^{*\mp} \rightarrow D^0[\pi^\mp])\pi^\pm$

- ③ $B^{\pm(0)} \rightarrow D^0[\pi^{0(\mp)}]\pi^\pm$

- ④ $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\gamma])\pi^\pm$

- $B^\pm \rightarrow DK^\pm$:

- ① $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\pi^0])K^\pm$

- ② $B^0 \rightarrow (D^{*\mp} \rightarrow D^0[\pi^\mp])K^\pm$

- ③ $B^{\pm(0)} \rightarrow D^0[\pi^{0(\mp)}]K^\pm$

- ④ $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\gamma])K^\pm$

- ⑤ $B_s^0 \rightarrow \bar{D}^0[\pi^+]K^-$

- ⑥ Mis-ID from partially reconstructed $B^\pm \rightarrow D\pi^\pm$ channel

Global fit

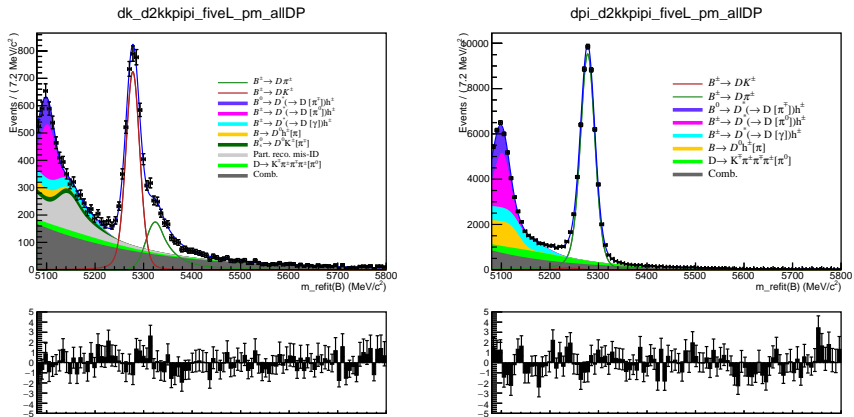


Figure 11: $B^\pm \rightarrow DK^\pm$ channel (left) and $B^\pm \rightarrow D\pi^\pm$ channel (right)

- $B^\pm \rightarrow DK^\pm$ yield: 3543 ± 75
- $B^\pm \rightarrow D\pi^\pm$ yield: $47\,503 \pm 260$

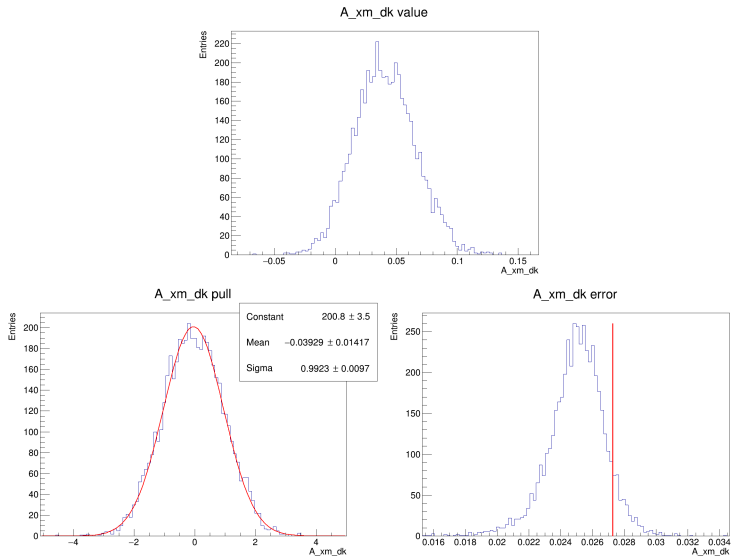
Binned CP fit

Binned CP fit

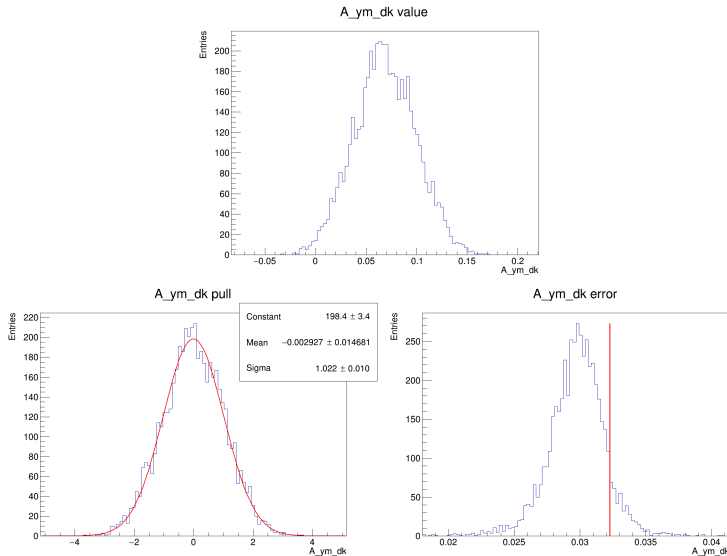
- Use 2×8 bins
- c_i and s_i calculated using MC integration of LHCb amplitude model
- Fit for CP observables
- PDF shape parameters fixed from global fit
- Yield of signal, low mass partially reconstructed background and combinatorial background floated
- Fractional yields F_i floated

$$\mathcal{R}_i = \begin{cases} F_i, & i = -8 \\ F_i / \sum_{j \geq i}, & -8 < i \leq +8 \end{cases}$$

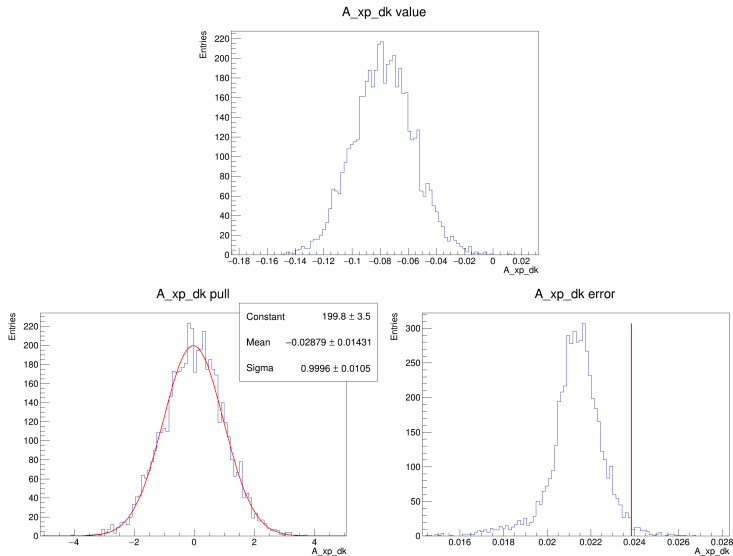
CP observables result: x_-^{DK}



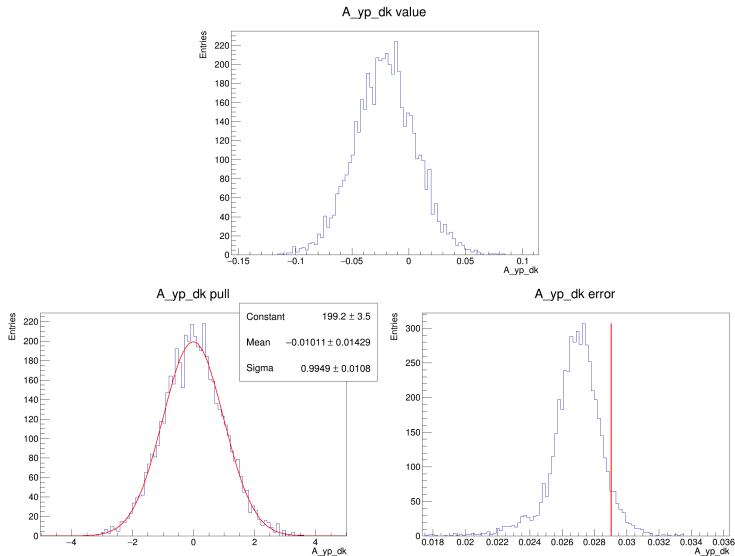
CP observables result: y_-^{DK}



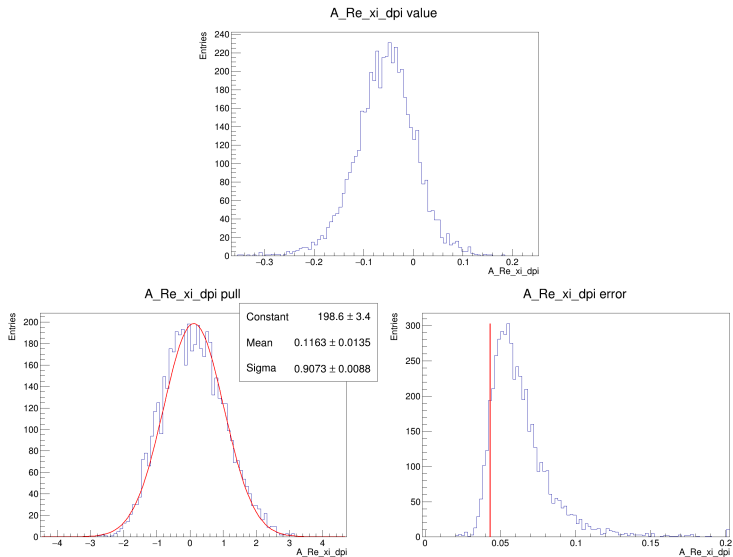
CP observables result: x_+^{DK}



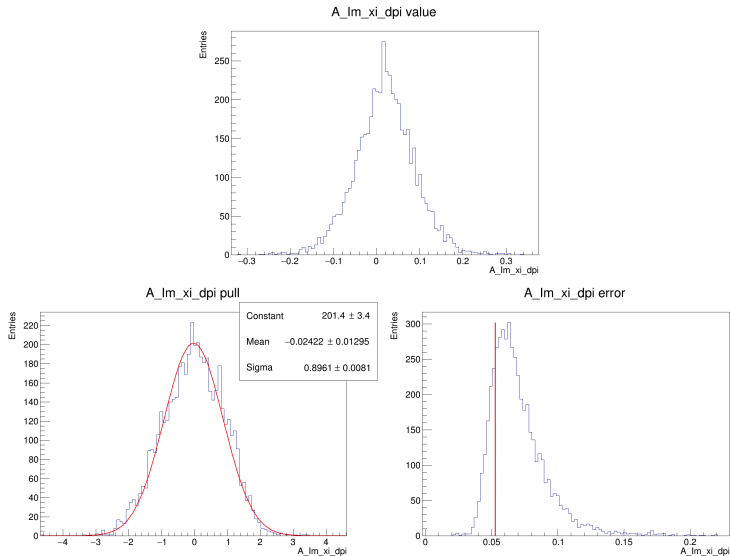
CP observables result: y_+^{DK}



CP observables result: $x_{\xi}^{D\pi}$



CP observables result: $y_{\xi}^{D\pi}$



Systematic uncertainties

c_i and s_i systematic uncertainty

- Uncertainty of c_i and s_i in BESIII analysis (mostly statistical)
- Largest systematic uncertainty
- Take uncertainties from $D \rightarrow 4\pi$ strong phase analysis and extrapolate to 20 fb^{-1}
- Smear c_i and s_i and do many fits to data

Remaining systematic uncertainties

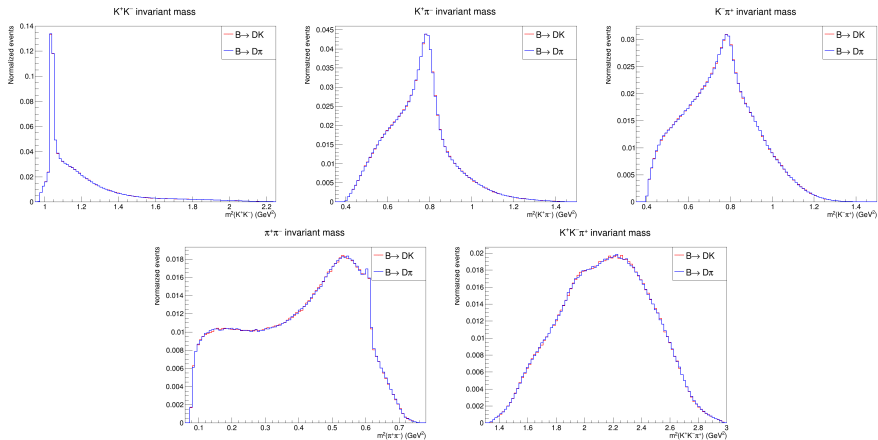
Different strategies for evaluating systematic uncertainties:

- Generate toy datasets with systematics, fit with default model and take the bias as a systematic:
 - Small backgrounds ($D \rightarrow K(X)l\nu_l$, $D \rightarrow K\pi\pi\pi$, Λ_b)
 - Bin dependent mass shape
 - Low mass physics effects
- Do multiple fits to data while smearing parameters:
 - c_i and s_i
 - Mass shape
 - Fixed yield fractions
 - PID efficiency
- Fit bias: Take bias toys as systematic uncertainty

Efficiency related systematics:

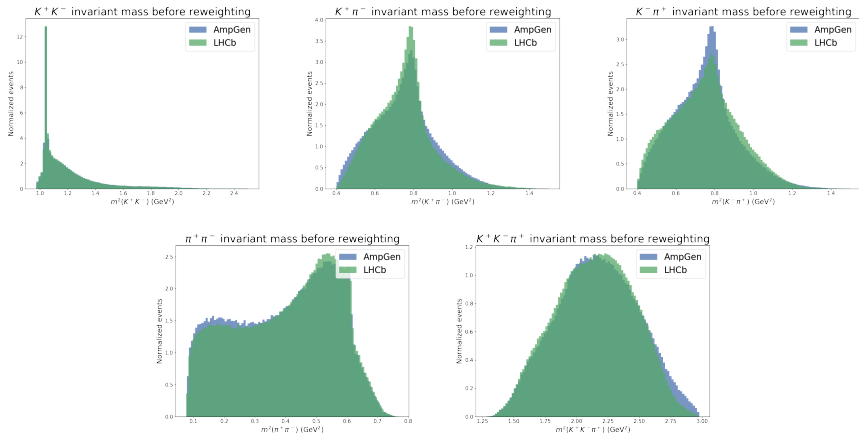
- Difference in $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$ phase space acceptance
- Efficiency correction of c_i and s_i

Efficiency differences between $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$



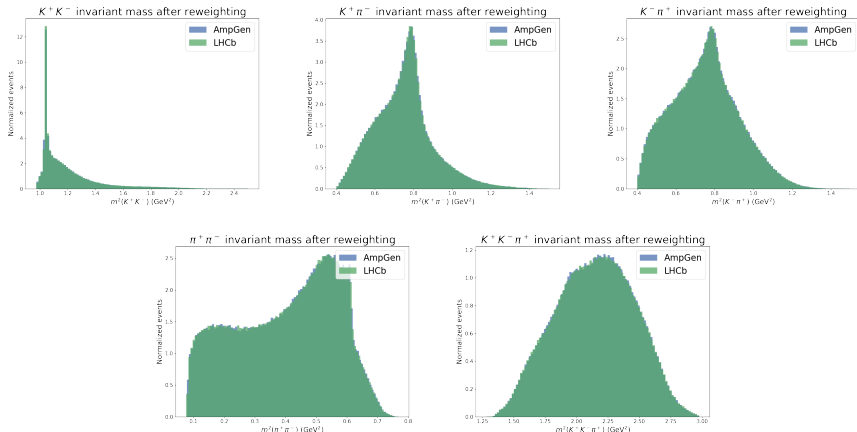
Conclusion: More or less identical phase space acceptance, no systematic uncertainty considered

Efficiency correction of c_i and s_i



Need to reweight events to account for efficiency differences between AmpGen samples and LHCb MC

Efficiency correction of c_i and s_i



After reweighting, use weights to recalculate c_i and s_i

Conclusion: Efficiency correction of c_i and s_i is an order of magnitude smaller than their uncertainties, no systematic uncertainty considered

Summary of all systematic uncertainties

Summary of all systematic uncertainties

Source	x_-^{DK}	y_-^{DK}	x_+^{DK}	y_+^{DK}	$x_\xi^{D\pi}$	$y_\xi^{D\pi}$
Statistical	2.73	3.23	2.38	2.90	4.30	5.27
c_i, s_i	0.66	1.55	0.32	1.31	1.73	1.03
$D \rightarrow K(X)/\nu_l$ background	-0.15	0.05	-0.11	0.03	0.35	-0.25
$D \rightarrow K\pi\pi\pi$ background	-0.17	0.03	-0.04	0.01	0.46	-0.18
Λ_b background	0.09	0.11	-0.00	-0.18	0.16	0.21
Bin dependent mass shape	-0.21	-0.05	-0.17	0.01	0.37	-0.11
Low mass physics effects	0.05	-0.09	-0.05	-0.18	0.41	-0.48
Mass shape	0.03	0.03	0.02	0.02	0.04	0.01
Fixed yield fractions	0.02	0.03	0.02	0.02	0.01	0.01
PID Efficiency	0.03	0.03	0.02	0.02	0.04	0.01
Fit bias	0.19	0.03	0.16	-0.04	0.30	-0.16
Total LHCb systematic	0.39	0.17	0.27	0.26	0.87	0.64
Total systematic	0.76	1.55	0.41	1.33	1.93	1.21

Summary and conclusion

Summary of CP observables

- Measured CP observables:

$$x_-^{DK} = (x.x \pm 2.7 \pm 0.4 \pm 0.7) \times 10^{-2},$$

$$y_-^{DK} = (x.x \pm 3.2 \pm 0.2 \pm 1.6) \times 10^{-2},$$

$$x_+^{DK} = (x.x \pm 2.4 \pm 0.3 \pm 0.3) \times 10^{-2},$$

$$y_+^{DK} = (x.x \pm 2.9 \pm 0.3 \pm 1.3) \times 10^{-2},$$

$$x_\xi^{D\pi} = (x.x \pm 4.3 \pm 0.9 \pm 1.7) \times 10^{-2},$$

$$y_\xi^{D\pi} = (x.x \pm 5.3 \pm 0.6 \pm 1.0) \times 10^{-2},$$

- Note: Currently using c_i and s_i from the LHCb model
- Publication strategy: Publish current results together with binned yields \rightarrow Redo fit to obtain model-independent CP observables once c_i and s_i from BESIII are available

Interpretation in terms of γ

- Interpret in terms of physics parameters:

$$\begin{aligned}\gamma &= (x.x_{-15}^{+14})^\circ, \\ \delta_B^{DK} &= (x.x_{-14}^{+15})^\circ, \\ r_B^{DK} &= x.x_{-0.018}^{+0.019}, \\ \delta_B^{D\pi} &= (x.x_{-63}^{+117})^\circ, \\ r_B^{D\pi} &= x.x_{-0.0024}^{+0.0052}.\end{aligned}$$

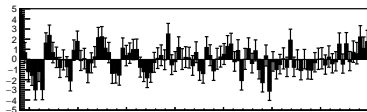
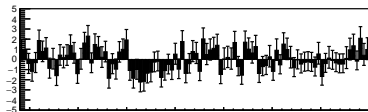
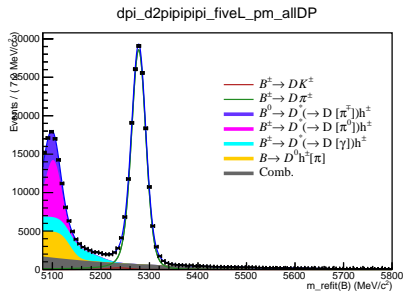
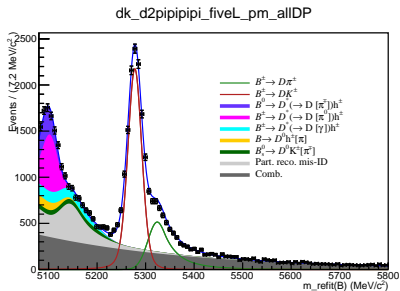
Bonus measurement

- The mode $B^\pm \rightarrow Dh^\pm$, $D \rightarrow \pi^+\pi^-\pi^+\pi^-$ very similar
- Run this through same selection (including BDT)
- Can measure GLW CP observables as additional constraints on γ :

$$A_h = \frac{\Gamma(B^- \rightarrow Dh^-) - \Gamma(B^+ \rightarrow Dh^+)}{\Gamma(B^- \rightarrow Dh^-) + \Gamma(B^+ \rightarrow Dh^+)},$$
$$R_{\text{CP}} = \frac{R(4\pi)}{R(K3\pi)},$$
$$R = \frac{\Gamma(B \rightarrow DK)}{\Gamma(B \rightarrow D\pi)}.$$

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K\pi\pi\pi$ yields provided by Tim Evans

Global fit of $B^\pm \rightarrow Dh^\pm$, $D \rightarrow \pi^+\pi^-\pi^+\pi^-$



$$\frac{\text{Yield}(\pi\pi\pi\pi)}{\text{Yield}(KK\pi\pi)} = \frac{161\,900 \pm 455}{54\,039 \pm 256} = 2.996 \pm 0.017$$

Compare with PDG: 3.06 ± 0.16

Thank you!

Thank you!

Backup

Trigger requirements

Run 1 trigger requirements	(Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS) and (Bu_Hlt1TrackAllLODecision_TOS) and (Bu_Hlt2Topo2BodyBBDTDecision_TOS or Bu_Hlt2Topo3BodyBBDTDecision_TOS or Bu_Hlt2Topo4BodyBBDTDecision_TOS or Bu_Hlt2IncPhiDecision_TOS)
Run 2 trigger requirements	(Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS) and (Bu_Hlt1TrackMVADecision_TOS or Bu_Hlt1TwoTrackMVADecision_TOS) and (Bu_Hlt2Topo2BodyDecision_TOS or Bu_Hlt2Topo3BodyDecision_TOS or Bu_Hlt2Topo4BodyDecision_TOS or Bu_Hlt2IncPhiDecision_TOS)

BDT training variables

Name	Rank (%)	Description
$\log(D0_RHO_BPV)$	7.7	D radial distance to beamline
$\log(Bu_FDCHI2_OWNPV)$	6.3	B^\pm flight distance χ^2
$\log(Bu_RHO_BPV)$	6.1	B^\pm radial distance to beamline
$\log(Bach_PT)$	6.1	Bachelor transverse momentum
$Bu_PTASY_1.5$	5.3	B^\pm asymmetry parameter
$\log(1-D0_DIRA_BPV)$	5.0	Angle between PV and D
$\log(Bu_IPCHI2_OWNPV)$	4.8	B^\pm impact parameter χ^2
$\log(1-Bu_DIRA_BPV)$	4.7	Angle between PV and B^\pm
$\log(h[1,2]_PT)$	4.4	K^\pm transverse momentum
$Bu_MAXDOCA$	4.4	B^\pm distance of closest approach
$\log(Bach_IPCHI2_OWNPV)$	4.1	Bachelor impact parameter χ^2

BDT training particles

Name	Rank (%)	Description
$\log(\text{Bu_constD0PV_D0_P})$	3.7	D momentum from DTF
$\log(\text{D0_VTXCHI2D0F})$	3.3	$D0$ vertex fit χ^2
$\log(\text{h}[3,4]_{\text{IPCHI2_OWNPV}})$	3.3	π^\pm impact parameter χ^2
$\log(\text{D0_IPCHI2_OWNPV})$	3.2	D impact parameter χ^2
$\log(\text{h}[3,4]_{\text{PT}})$	3.2	π^\pm transverse momentum
$\log(\text{Bu_PT})$	2.8	B^\pm transverse momentum
$\log(\text{h}[1,2]_{\text{P}})$	2.8	K^\pm momentum
$\log(\text{Bach_P})$	2.7	Bachelor momentum
$\log(\text{Bu_constD0PV_P})$	2.6	B^\pm momentum from DTF
$\log(\text{h}[1,2]_{\text{IPCHI2_OWNPV}})$	2.5	K^\pm impact parameter χ^2
D0_MAXDOCA	2.5	D distance of closest approach
$\log(\text{Bu_VTXCHI2D0F})$	2.0	B^\pm vertex fit χ^2
$\log(\text{h}[3,4]_{\text{P}})$	1.9	π^\pm momentum