

Determination of the CKM angle γ in $B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm$ decays

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B2OC Meeting

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Outline

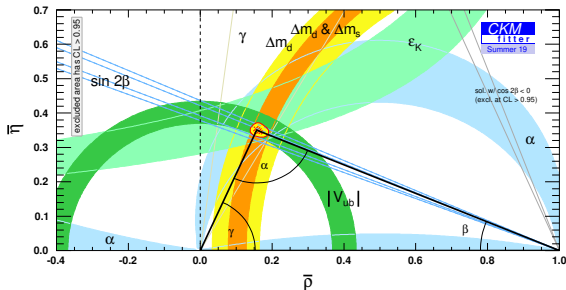
- 1 Introduction to the CKM angle γ
- 2 Binned γ analysis of the $D \rightarrow K^+ K^- \pi^+ \pi^-$ mode
- 3 Binning scheme
- 4 $B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm$ selection
- 5 Backgrounds
- 6 Fit to data
- 7 Systematic uncertainty
- 8 Summary and conclusion

γ and the unitary triangle

- Unitarity of CKM matrix: $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \Rightarrow$

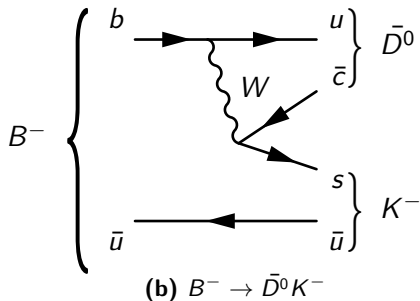
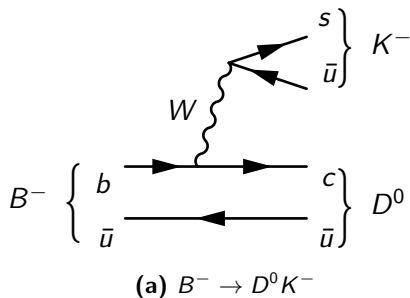
$$\gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$$

- Only CKM angle accessible at tree level \Rightarrow
 - Negligible theoretical uncertainties
 - Ideal Standard Model benchmark
 - Compare with indirect measurements



CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005)

Sensitivity through interference



- Superposition of D^0 and \bar{D}^0
- $b \rightarrow u\bar{c}s$ and $b \rightarrow c\bar{u}s$ interference \rightarrow Sensitivity to γ

$$\begin{aligned}\mathcal{A}(B^-) &= \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D}^0) \\ \mathcal{A}(B^+) &= \mathcal{A}(\bar{D}^0) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0)\end{aligned}$$

Measurement of γ from $B^\pm \rightarrow DK^\pm, D \rightarrow K^+K^-\pi^+\pi^-$

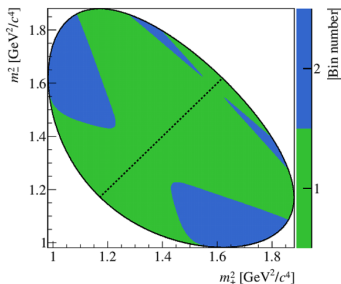
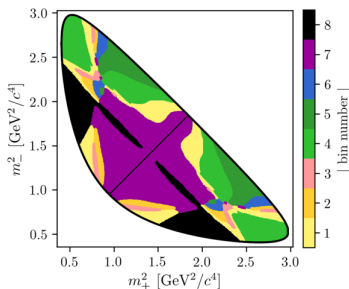
- First proposed by J. Rademacker and G. Wilkinson
 - [arXiv:hep-ph/0611272](#)
 - Amplitude model by FOCUS
 - Expected γ precision with 1000 candidates: 14°
- CLEO amplitude analysis
 - [arXiv:1201.5716](#)
 - Expected γ precision with 2000 candidates: 11°
- State of the art amplitude analysis by LHCb :
 - [LHCb-PAPER-2018-041](#)
 - Use to develop efficient binning scheme

The $D \rightarrow K^+ K^- \pi^+ \pi^-$ decay

Binned γ analysis of the
 $D \rightarrow K^+ K^- \pi^+ \pi^-$ mode

Binned measurement of γ

- Final measurement will be model-independent
 - Poor binning reduces statistical sensitivity \rightarrow No bias!
- Need strong phases of D decay \rightarrow Measure at BESIII
- LHCb-PAPER-2020-019: $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K_S^0 h^+ h^-$
 - Single most precise measurement: $\gamma = (68.7^{+5.2}_{-5.1})^\circ$



The BPGGSZ method

- $B^\pm \rightarrow Dh^\pm$ amplitude:

$$\begin{aligned}\mathcal{A}(B^-) &= \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D}^0) \\ \mathcal{A}(B^+) &= \mathcal{A}(\bar{D}^0) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0)\end{aligned}$$

- $\mathcal{A}(D^0)$ and $\mathcal{A}(\bar{D}^0)$ depend on D phase space
- Strong-phase difference of D^0 and \bar{D}^0 decays inaccessible at LHCb
- Model-independent measurement: Integrate over bins of phase space

Event yield in bin i

$$\begin{aligned}N_i^- &= h_{B^-} \left(F_i + (x_-^2 + y_-^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_- c_i + y_- s_i) \right) \\ N_{-i}^+ &= h_{B^+} \left(F_i + (x_+^2 + y_+^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_+ c_i + y_+ s_i) \right)\end{aligned}$$

The BPGGSZ method

Event yield in bin i

$$N_i^- = h_{B^-} (F_i + (x_-^2 + y_-^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_- c_i + y_- s_i))$$

$$N_i^+ = h_{B^+} (F_i + (x_+^2 + y_+^2) \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (x_+ c_i + y_+ s_i))$$

- CP observables:

- $x_{\pm}^{DK} = r_B^{DK} \cos(\delta_B^{DK} \pm \gamma), \quad y_{\pm}^{DK} = r_B^{DK} \sin(\delta_B^{DK} \pm \gamma)$
- $x_{\xi}^{D\pi} = \text{Re}(\xi^{D\pi}), \quad y_{\xi}^{D\pi} = \text{Im}(\xi^{D\pi}) \quad \left(\xi^{D\pi} = \frac{r_B^{D\pi}}{r_B^{DK}} e^{i(\delta_B^{D\pi} - \delta_B^{DK})} \right)$

- Fractional bin yield:

- $F_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)|^2}{\sum_j \int_j d\Phi |\mathcal{A}(D^0)|^2}$
- Floated in the fit, mostly constrained by $B^{\pm} \rightarrow D\pi^{\pm}$

- Amplitude averaged strong phases from BESIII:

$$c_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D}^0)| \cos(\delta_D)}{\sqrt{\int_i d\Phi |\mathcal{A}(D^0)|^2 \int_i d\Phi |\mathcal{A}(\bar{D}^0)|^2}}, \quad s_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D}^0)| \sin(\delta_D)}{\sqrt{\int_i d\Phi |\mathcal{A}(D^0)|^2 \int_i d\Phi |\mathcal{A}(\bar{D}^0)|^2}}$$

Binning scheme

A binning scheme must satisfy the following:

- Minimal dilution of strong phases when integrating over bins
- Enhance interference between $B^\pm \rightarrow D^0 h^\pm$ and $B^\pm \rightarrow \bar{D}^0 h^\pm$

How to bin a 5-dimensional phase space?

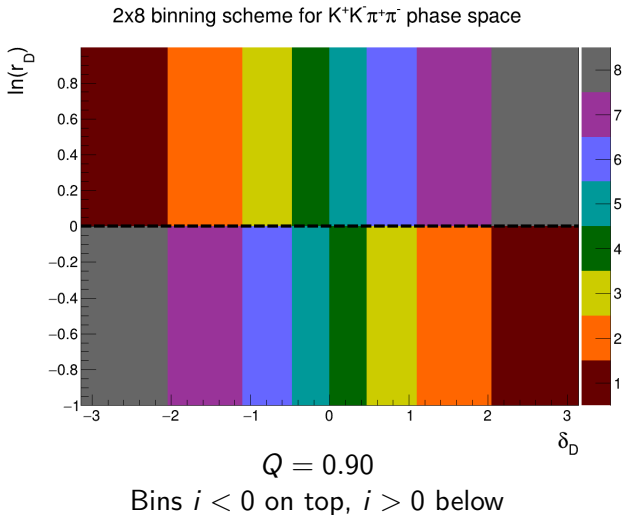
- Generate C++ code for LHCb amplitude model using AmpGen¹
- For each B^\pm candidate, calculate

$$\frac{\mathcal{A}(D^0)}{\mathcal{A}(\bar{D}^0)} = r_D e^{i\delta_D}$$

- Bin along δ_D and r_D , maximize Q -value to optimize

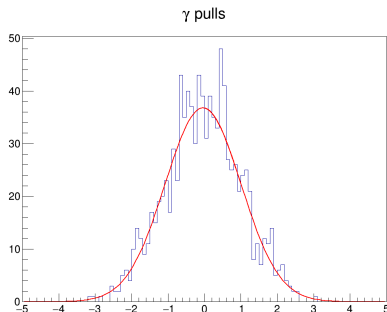
¹AmpGen by Tim Evans

Binning scheme

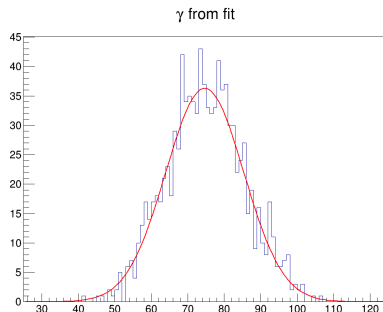


γ precision benchmark

- Generate 2000 $B^\pm \rightarrow DK^\pm$ candidates using LHCb model in AmpGen
- Fit back with same model using AmpGen



(a) Pull of γ

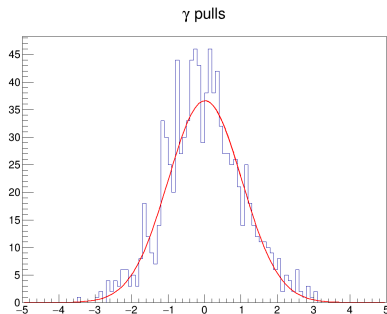


(b) Fitted γ values

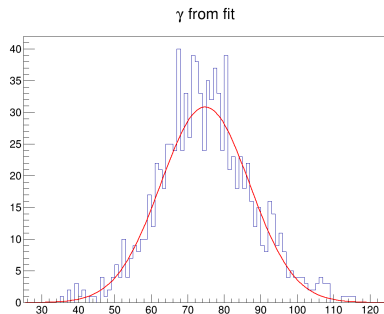
Precision of γ in unbinned fit: 11°

Study of γ precision

- Binned fit setup: Optimized 2×8 bins
- Fit same AmpGen samples, using c_i , s_i and F_i from LHCb model



(a) Pull of γ



(b) Fitted γ values

Precision of γ in binned fit: 12°
Consistent with unbinned fit and Q -value

$$B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm \text{ selection}$$

$$B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm \text{ selection}$$

- Data sample: Full Run 1 and 2
- MC samples: Full Run 1 and 2 excluding 2015
 - AmpGen model
 - Large filtered samples

Stripping lines

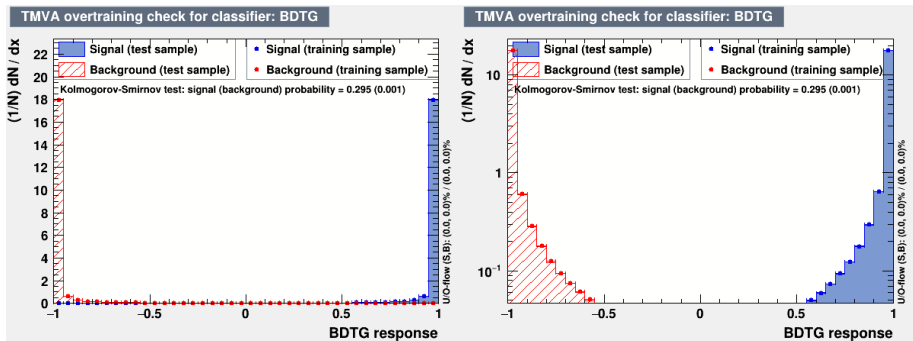
StrippingB2D0PiD2HHHHBeauty2CharmLineDecision

StrippingB2D0KD2HHHHBeauty2CharmLineDecision

Boosted Decision Tree

- BDTG from TMVA Toolkit
- Signal sample: $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$ MC samples
- Background sample: Data sample with $m_{B^\pm}^{\text{DTF}} \in [5800, 7000]\text{MeV}$
- Random, equal sized test and training samples

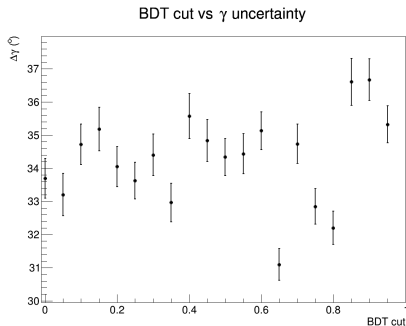
BDT training results



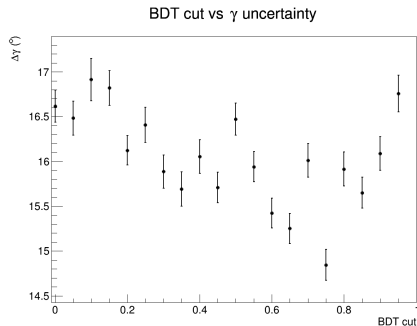
(a) BDT output

(b) BDT output on a logarithmic scale

BDT optimization study



(a) Run 1



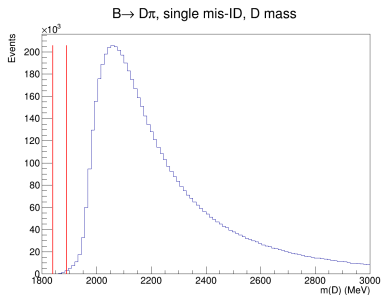
(b) Run 2

- Run 1: Pick BDT working point at 0.65
- Run 2: Pick BDT working point at 0.75

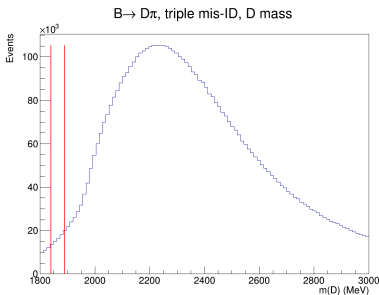
Backgrounds

$D \rightarrow K\pi\pi\pi$ mis-ID background

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K\pi\pi\pi$
- Single mis-ID: $K\pi\pi\pi \rightarrow KK\pi\pi$
- Triple mis-ID: $\pi\pi K\pi \rightarrow KK\pi\pi$
- Use LHCb MC generated with AmpGen, reweight with PIDCalib2



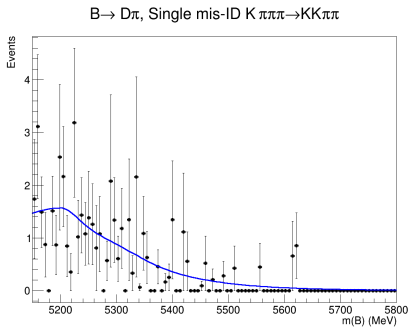
(a) Single mis-ID



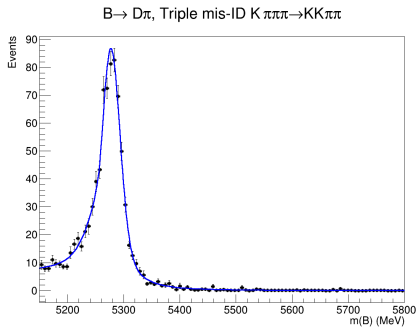
(b) Triple mis-ID

Figure 6: D invariant mass

$D \rightarrow K\pi\pi\pi$ mis-ID background



(a) Single mis-ID



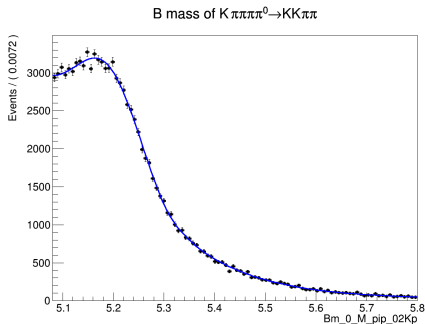
(b) Triple mis-ID

Figure 7: B invariant mass

Conclusion: Negligible impact, include in systematics

$D \rightarrow K\pi\pi\pi\pi^0$ mis-ID background

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K\pi\pi\pi[\pi^0]$
- π^0 not reconstructed \rightarrow Lower D mass
- Single mis-ID: $K\pi\pi\pi \rightarrow KK\pi\pi \rightarrow$ Higher D mass
- Generate RapidSim samples, reweight with PIDCalib2



Conclusion: Fix shape from RapidSim, allow yield to float

Global fit

- PDF shape parameterization identical to LHCb-ANA-2020-001
- Signal: Gaussian + Modified Cruijff
- Shape fixed from MC, yield and width floated
- Exponential background

$$f_{\text{MG}}(m|m_B, \sigma, \alpha_L, \alpha_R, \beta) \propto \begin{cases} \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_L\Delta m^2}\right), & \Delta m = m - m_B < 0 \\ \exp\left(\frac{-\Delta m^2(1+\beta\Delta m^2)}{2\sigma^2+\alpha_R\Delta m^2}\right), & \Delta m = m - m_B > 0 \end{cases}$$

Partially reconstructed background

- $B^\pm \rightarrow D\pi^\pm$:

- ① $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\pi^0])\pi^\pm$

- ② $B^0 \rightarrow (D^{*\mp} \rightarrow D^0[\pi^\mp])\pi^\pm$

- ③ $B^{\pm(0)} \rightarrow D^0[\pi^{0(\mp)}]\pi^\pm$

- ④ $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\gamma])\pi^\pm$

- $B^\pm \rightarrow DK^\pm$:

- ① $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\pi^0])K^\pm$

- ② $B^0 \rightarrow (D^{*\mp} \rightarrow D^0[\pi^\mp])K^\pm$

- ③ $B^{\pm(0)} \rightarrow D^0[\pi^{0(\mp)}]K^\pm$

- ④ $B^\pm \rightarrow (D^{*0} \rightarrow D^0[\gamma])K^\pm$

- ⑤ $B_s^0 \rightarrow \bar{D}^0[\pi^+]K^-$

- ⑥ Mis-ID from partially reconstructed $B^\pm \rightarrow D\pi^\pm$ channel

Global fit

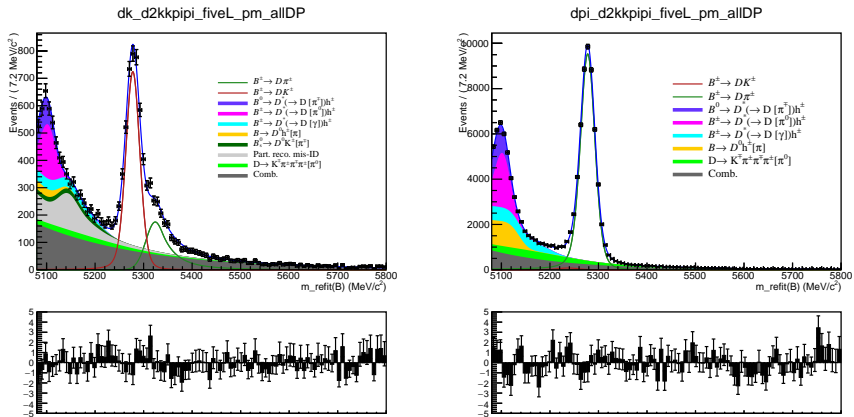


Figure 8: $B^\pm \rightarrow DK^\pm$ channel (left) and $B^\pm \rightarrow D\pi^\pm$ channel (right)

- $B^\pm \rightarrow DK^\pm$ yield: 3543 ± 75
- $B^\pm \rightarrow D\pi^\pm$ yield: $47\,503 \pm 260$

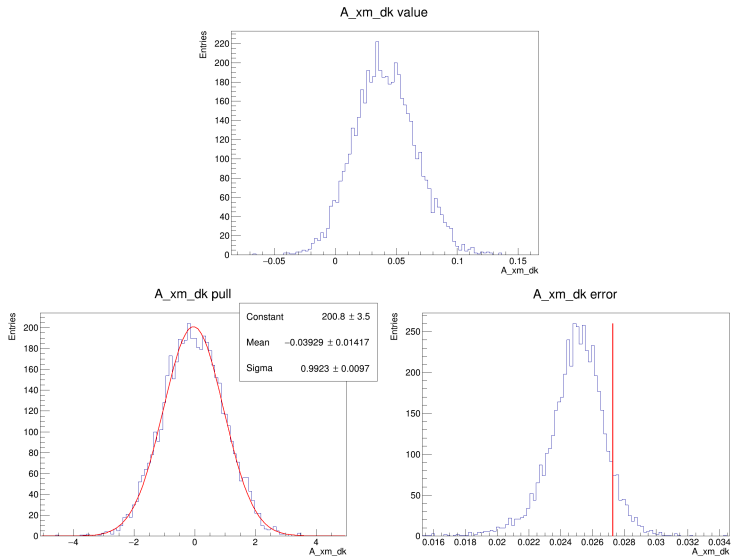
Binned CP fit

Binned CP fit

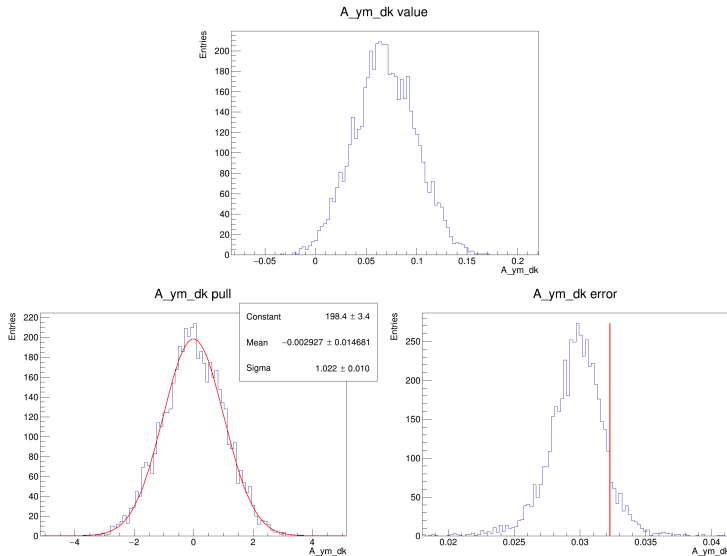
- Use 2×8 bins
- c_i and s_i calculated using MC integration of LHCb amplitude model
- Fit for CP observables
- PDF shape parameters fixed from global fit
- Yield of signal, low mass partially reconstructed background and combinatorial background floated
- Fractional yields F_i floated

$$\mathcal{R}_i = \begin{cases} F_i, & i = -8 \\ F_i / \sum_{j \geq i}, & -8 < i \leq +8 \end{cases}$$

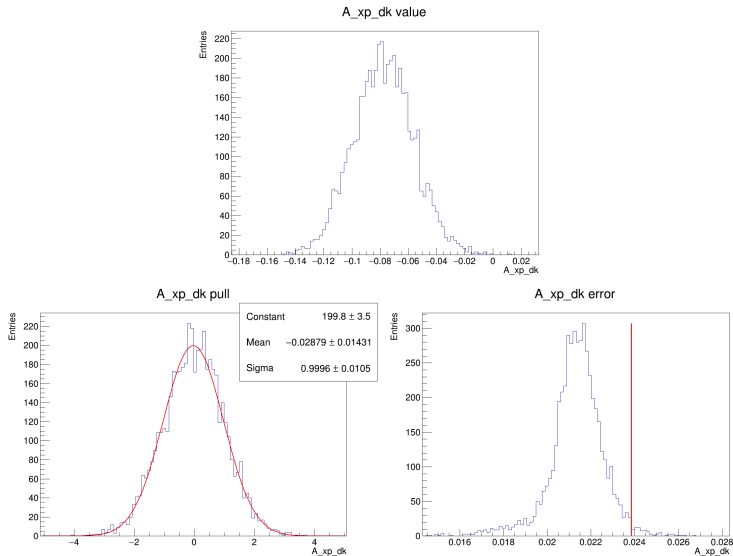
CP observables result: x_-^{DK}



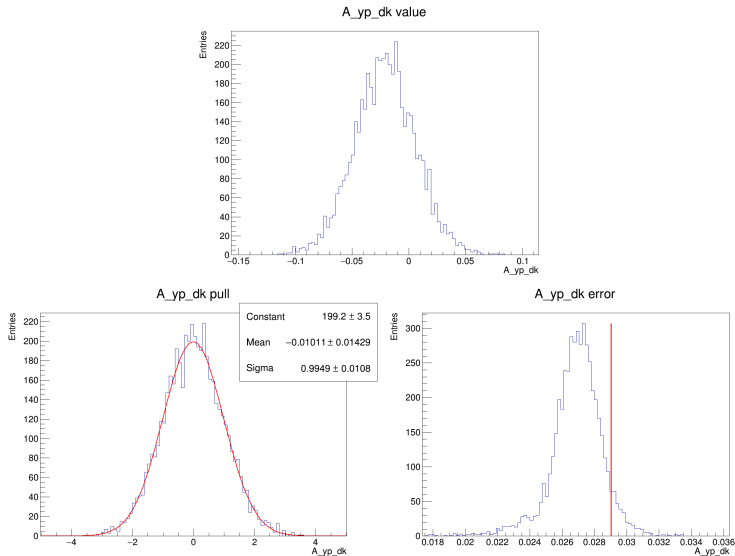
CP observables result: y_-^{DK}



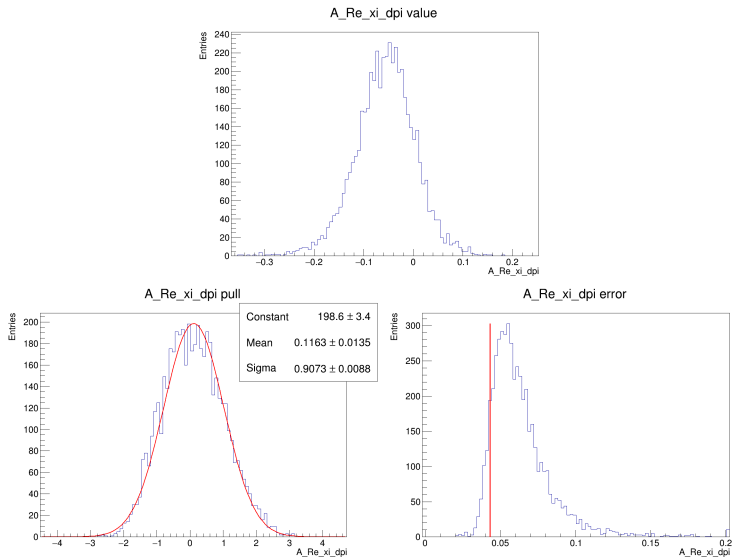
CP observables result: x_+^{DK}



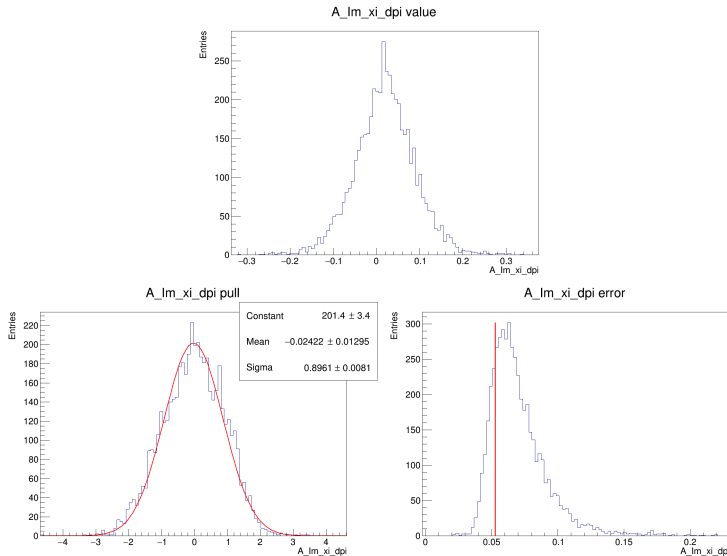
CP observables result: y_+^{DK}



CP observables result: $x_{\xi}^{D\pi}$



CP observables result: $y_{\xi}^{D\pi}$



Systematic uncertainties

c_i and s_i systematic uncertainty

- Uncertainty of c_i and s_i in BESIII analysis (mostly statistical)
- Largest systematic uncertainty
- Take uncertainties from $D \rightarrow 4\pi$ strong phase analysis and extrapolate to 20 fb^{-1}
- Smear c_i and s_i and do many fits to data

Remaining systematic uncertainties

Different strategies for evaluating systematic uncertainties:

- Generate toy datasets with systematics, fit with default model and take the bias as a systematic:
 - Small backgrounds ($D \rightarrow K(X)l\nu_l$, $D \rightarrow K\pi\pi\pi$, $B \rightarrow Dl\nu_l$, Λ_b)
 - Bin dependent mass shape
 - Low mass physics effects
- Do multiple fits to data while smearing parameters:
 - c_i and s_i
 - Mass shape
 - Fixed yield fractions
 - PID efficiency
- Fit bias: Take bias toys as systematic uncertainty

Summary of all systematic uncertainties

Source	x_-^{DK}	y_-^{DK}	x_+^{DK}	y_+^{DK}	$x_\xi^{D\pi}$	$y_\xi^{D\pi}$
Statistical	2.73	3.23	2.38	2.90	4.30	5.27
c_i, s_i	0.66	1.55	0.32	1.31	1.73	1.03
$B^\pm \rightarrow D\mu\nu$ background	0.04	0.03	0.02	0.15	0.30	0.10
$D \rightarrow K(X)l\nu_l$ background	0.15	0.05	0.11	0.03	0.35	0.25
$D \rightarrow K\pi\pi\pi$ background	0.17	0.03	0.04	0.01	0.46	0.18
Λ_b background	0.09	0.11	0.00	0.18	0.16	0.21
Bin dependent mass shape	0.21	0.05	0.17	0.01	0.37	0.11
Fit bias	0.19	0.03	0.16	0.04	0.30	0.16
Fixed yield fractions	0.02	0.03	0.02	0.02	0.01	0.01
Low mass physics effects	0.05	0.09	0.05	0.18	0.41	0.48
Mass shape	0.03	0.03	0.02	0.02	0.04	0.01
PID Efficiency	0.03	0.03	0.02	0.02	0.04	0.01
Total LHCb systematic	0.39	0.17	0.27	0.30	0.92	0.65
Total systematic	0.77	1.55	0.41	1.34	1.96	1.22

Summary and conclusion

Summary of CP observables

- Measured CP observables:

$$x_-^{DK} = (x.x \pm 2.7 \pm 0.4 \pm 0.7) \times 10^{-2},$$

$$y_-^{DK} = (x.x \pm 3.2 \pm 0.2 \pm 1.6) \times 10^{-2},$$

$$x_+^{DK} = (x.x \pm 2.4 \pm 0.3 \pm 0.3) \times 10^{-2},$$

$$y_+^{DK} = (x.x \pm 2.9 \pm 0.3 \pm 1.3) \times 10^{-2},$$

$$x_\xi^{D\pi} = (x.x \pm 4.3 \pm 0.9 \pm 1.7) \times 10^{-2},$$

$$y_\xi^{D\pi} = (x.x \pm 5.3 \pm 0.6 \pm 1.0) \times 10^{-2},$$

- Note: Currently using c_i and s_i from the LHCb model
- Publication strategy: Publish current results together with binned yields \rightarrow Redo fit to obtain model-independent CP observables once c_i and s_i from BESIII are available

Interpretation in terms of γ

- Interpret in terms of physics parameters:

$$\begin{aligned}\gamma &= (x.x_{-15}^{+14})^\circ, \\ \delta_B^{DK} &= (x.x_{-14}^{+15})^\circ, \\ r_B^{DK} &= x.x_{-0.018}^{+0.019}, \\ \delta_B^{D\pi} &= (x.x_{-63}^{+117})^\circ, \\ r_B^{D\pi} &= x.x_{-0.0024}^{+0.0052}.\end{aligned}$$

- Next steps:
 - ANA note (more or less) ready
 - Calculate model uncertainty of c_i and s_i
 - Other minor details

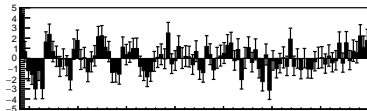
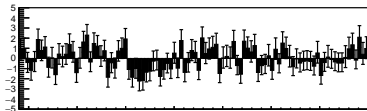
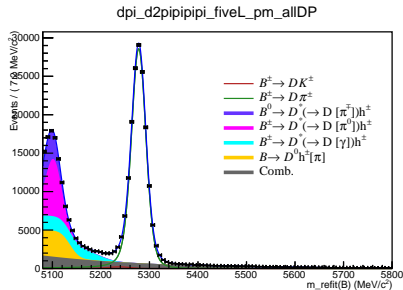
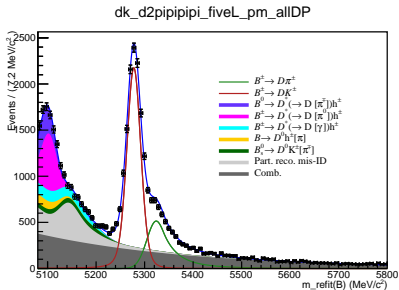
Bonus measurement

- The mode $B^\pm \rightarrow Dh^\pm$, $D \rightarrow \pi^+\pi^-\pi^+\pi^-$ very similar
- Run this through same selection (including BDT)
- Can measure GLW CP observables as additional constraints on γ :

$$A_h = \frac{\Gamma(B^- \rightarrow Dh^-) - \Gamma(B^+ \rightarrow Dh^+)}{\Gamma(B^- \rightarrow Dh^-) + \Gamma(B^+ \rightarrow Dh^+)},$$
$$R_{\text{CP}} = \frac{R(4\pi)}{R(K3\pi)},$$
$$R = \frac{\Gamma(B \rightarrow DK)}{\Gamma(B \rightarrow D\pi)}.$$

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K\pi\pi\pi$ yields provided by Tim Evans

Global fit of $B^\pm \rightarrow Dh^\pm$, $D \rightarrow \pi^+\pi^-\pi^+\pi^-$



$$\frac{\text{Yield}(\pi\pi\pi\pi)}{\text{Yield}(KK\pi\pi)} = \frac{161\,900 \pm 455}{54\,039 \pm 256} = 2.996 \pm 0.017$$

Compare with PDG: 3.06 ± 0.16

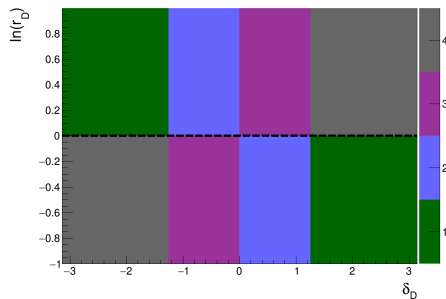
Thank you!

Thank you!

Backup

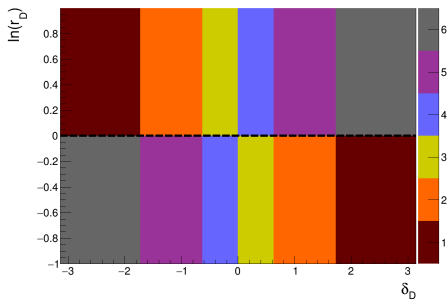
Binning scheme

2x4 binning scheme for $K^+K^-\pi^+\pi^-$ phase space



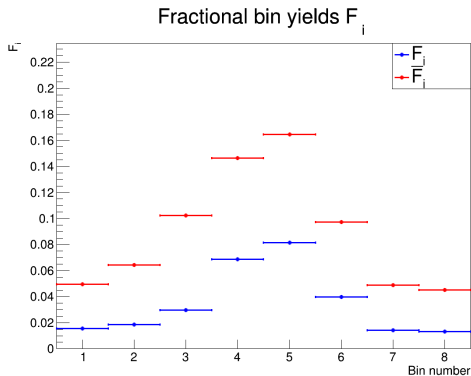
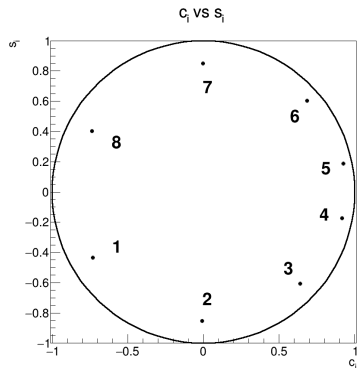
(a) $Q = 0.85$

2x6 binning scheme for $K^+K^-\pi^+\pi^-$ phase space



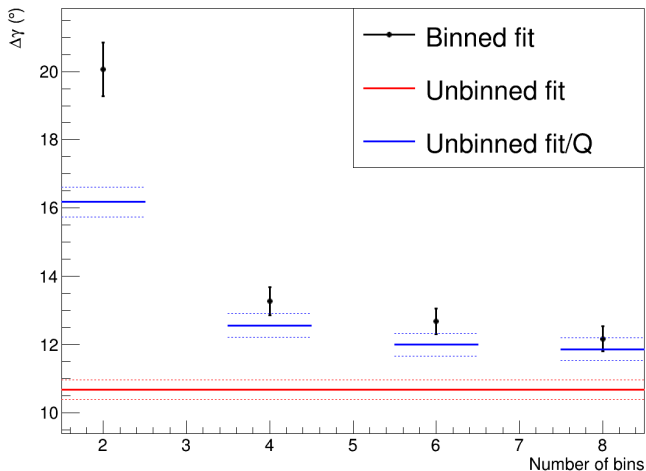
(b) $Q = 0.89$

c_i , s_i and F_i



Comparison of binned fit precision with unbinned fit

γ precision vs number of bins



Trigger requirements

Run 1 trigger requirements	(Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS) and (Bu_Hlt1TrackAllLODecision_TOS) and (Bu_Hlt2Topo2BodyBBDTDecision_TOS or Bu_Hlt2Topo3BodyBBDTDecision_TOS or Bu_Hlt2Topo4BodyBBDTDecision_TOS or Bu_Hlt2IncPhiDecision_TOS)
Run 2 trigger requirements	(Bu_LOGlobal_TIS or Bu_LOHadronDecision_TOS) and (Bu_Hlt1TrackMVADecision_TOS or Bu_Hlt1TwoTrackMVADecision_TOS) and (Bu_Hlt2Topo2BodyDecision_TOS or Bu_Hlt2Topo3BodyDecision_TOS or Bu_Hlt2Topo4BodyDecision_TOS or Bu_Hlt2IncPhiDecision_TOS)

Rectangular cuts before BDT

Number	Variable description	Cut
1	DTF converged	True
2	Bachelor momentum	$< 100\text{GeV}$
3	Bachelor has RICH	True
4	D invariant mass	$[1839.84, 1889.84]\text{MeV}$
5	B^\pm invariant mass	$[5080, 5800]\text{MeV}$
6	K^\pm daughter PID	> -10
7	π^\pm daughter PID	< 20

Rectangular cuts after BDT

Number	Variable description	Cut
8	K^\pm bachelor PID	> 4
9	π^\pm bachelor PID	< 4
10	Bachelor is muon	False
11	z flight significance	> 2
12	K^\pm PID	> 0
13	K_S^0 mass veto	$[477, 507]\text{MeV}$

BDT training variables

Name	Rank (%)	Description
$\log(D0_RHO_BPV)$	7.7	D radial distance to beamline
$\log(Bu_FDCHI2_OWNPV)$	6.3	B^\pm flight distance χ^2
$\log(Bu_RHO_BPV)$	6.1	B^\pm radial distance to beamline
$\log(Bach_PT)$	6.1	Bachelor transverse momentum
$Bu_PTASY_1.5$	5.3	B^\pm asymmetry parameter
$\log(1-D0_DIRA_BPV)$	5.0	Angle between PV and D
$\log(Bu_IPCHI2_OWNPV)$	4.8	B^\pm impact parameter χ^2
$\log(1-Bu_DIRA_BPV)$	4.7	Angle between PV and B^\pm
$\log(h[1,2]_PT)$	4.4	K^\pm transverse momentum
$Bu_MAXDOCA$	4.4	B^\pm distance of closest approach
$\log(Bach_IPCHI2_OWNPV)$	4.1	Bachelor impact parameter χ^2

BDT training particles

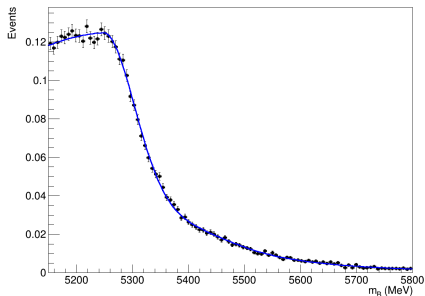
Name	Rank (%)	Description
$\log(\text{Bu_constD0PV_D0_P})$	3.7	D momentum from DTF
$\log(\text{D0_VTXCHI2D0F})$	3.3	$D0$ vertex fit χ^2
$\log(\text{h}[3,4]_{\text{IPCHI2_OWNPV}})$	3.3	π^\pm impact parameter χ^2
$\log(\text{D0_IPCHI2_OWNPV})$	3.2	D impact parameter χ^2
$\log(\text{h}[3,4]_{\text{PT}})$	3.2	π^\pm transverse momentum
$\log(\text{Bu_PT})$	2.8	B^\pm transverse momentum
$\log(\text{h}[1,2]_{\text{P}})$	2.8	K^\pm momentum
$\log(\text{Bach_P})$	2.7	Bachelor momentum
$\log(\text{Bu_constD0PV_P})$	2.6	B^\pm momentum from DTF
$\log(\text{h}[1,2]_{\text{IPCHI2_OWNPV}})$	2.5	K^\pm impact parameter χ^2
D0_MAXDOCA	2.5	D distance of closest approach
$\log(\text{Bu_VTXCHI2D0F})$	2.0	B^\pm vertex fit χ^2
$\log(\text{h}[3,4]_{\text{P}})$	1.9	π^\pm momentum

D semileptonic backgrounds

- $B^\pm \rightarrow Dh^\pm$, $D \rightarrow K(X)l\nu$, $K(X) \rightarrow K\pi\pi$
 - $K_1(1270)$
 - $K_1(1400)$
 - $K^*(1410)$
 - $K^*(1680)$
 - $K_2^*(1430)$
- Single mis-ID: $K\mu\pi\pi \rightarrow KK\pi\pi$
- Double mis-ID: $K\pi\pi\mu \rightarrow KK\pi\pi$
- Generate Rapidsim samples, reweight with PIDCalib2

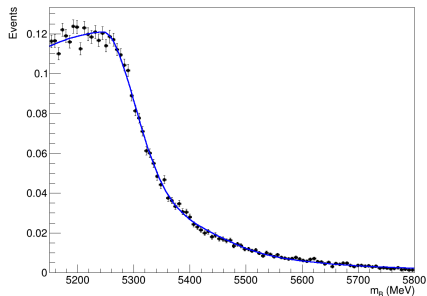
D semileptonic backgrounds

B mass of SL $D \rightarrow K(X)\mu\nu$ backgrounds, $B \rightarrow DK$



(a) $B \rightarrow DK$

B mass of SL $D \rightarrow K(X)\mu\nu$ backgrounds, $B \rightarrow D\pi$



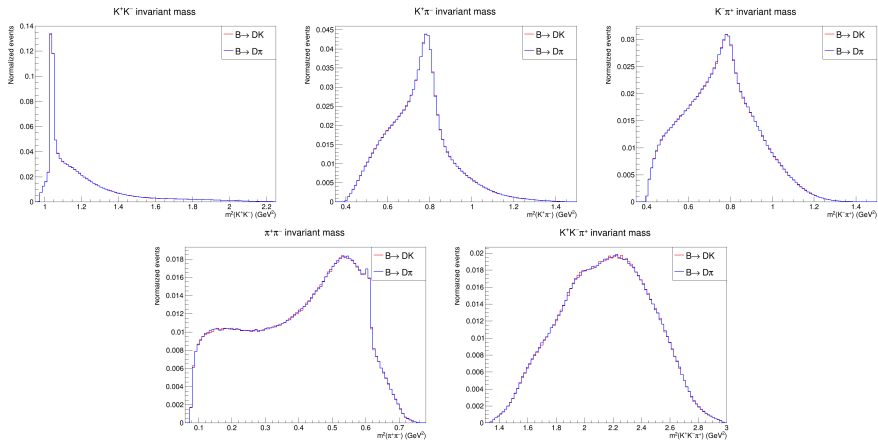
(b) $B \rightarrow D\pi$

Conclusion: Negligible impact, include in systematics

Efficiency related systematics:

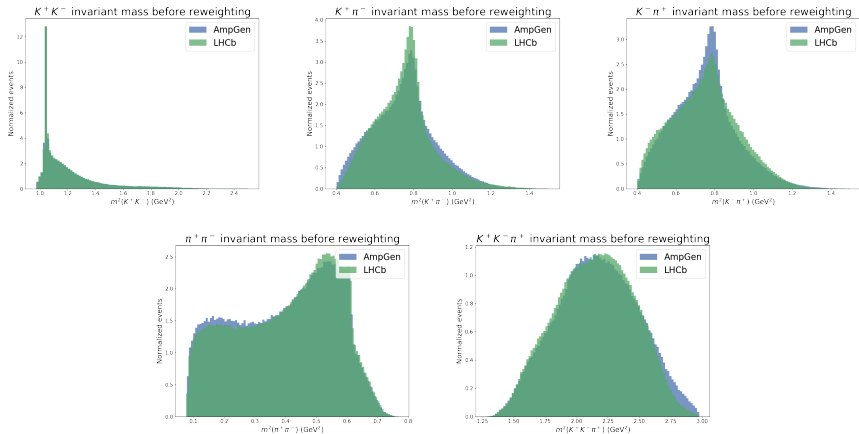
- Difference in $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$ phase space acceptance
- Efficiency correction of c_i and s_i

Efficiency differences between $B^\pm \rightarrow DK^\pm$ and $B^\pm \rightarrow D\pi^\pm$



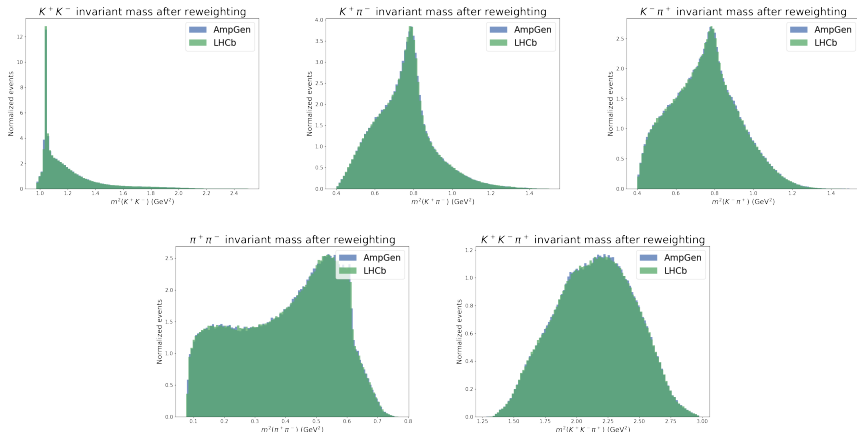
Conclusion: More or less identical phase space acceptance, no systematic uncertainty considered

Efficiency correction of c_i and s_i



Need to reweight events to account for efficiency differences between AmpGen samples and LHCb MC

Efficiency correction of c_i and s_i



After reweighting, use weights to recalculate c_i and s_i

Conclusion: Efficiency correction of c_i and s_i is an order of magnitude smaller than their uncertainties, no systematic uncertainty considered