

BESIII Charm Meeting

Measurement of $\delta_D^{K\pi}$ with $D \rightarrow K_{S,L}\pi^+\pi^-$ tags

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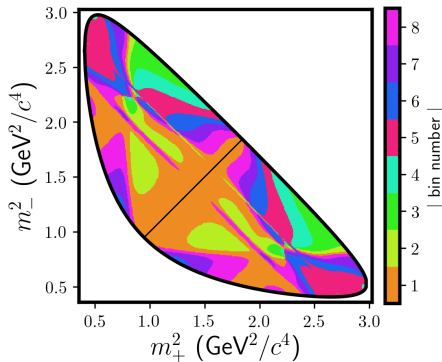
31st August 2021



$$D \rightarrow K_{S,L}^0 \pi^+ \pi^- \text{ tags}$$

Measurement of $\delta_D^{K\pi}$ with $D \rightarrow K_{S,L} \pi^+ \pi^-$ tags

- Measurement of both
 $r_D^{K\pi} \cos \delta_D^{K\pi}$ and $r_D^{K\pi} \sin \delta_D^{K\pi}$
- Equal- $\Delta\delta_D$ phase space binning
- Double tag yields taken from
[Phys. Rev. D **101** \(2020\)](#)
- K_i, c_i, s_i re-determined without
 $D \rightarrow K^- \pi^+$ inputs (by Lei Li)



$D \rightarrow K_{S,L}^0 \pi^+ \pi^-$ inputs

$K^- \pi^+$ vs $K_{S,L}^0 \pi^+ \pi^-$ double tag yield prediction

$$Y(K^- \pi^+ | K_{S,L}^0 \pi^+ \pi^-)_i =$$

$$H^{(\prime)} \left(K_i^{(\prime)} + (r_D^{K\pi})^2 K_{-i}^{(\prime)} \mp 2r_D^{K\pi} \sqrt{K_i^{(\prime)} K_{-i}^{(\prime)}} [c_i^{(\prime)} \cos \delta_D^{K\pi} - s_i^{(\prime)} \sin \delta_D^{K\pi}] \right)$$

- K_i : Flavour tag yields

- $D \rightarrow K_{S,L}^0 \pi^+ \pi^-$ vs $D \rightarrow K^- \pi^+ \pi^0$
- $D \rightarrow K_{S,L}^0 \pi^+ \pi^-$ vs $D \rightarrow K^- \pi^+ \pi^- \pi^+$
- $D \rightarrow K_S^0 \pi^+ \pi^-$ vs $D \rightarrow K^- e^+ \nu_e$
- Updated coherence factors from [J. High Energ. Phys. 2021, 164](#)

- c_i and s_i : Amplitude-averaged strong phases

- Updated with no $D \rightarrow K^- \pi^+$ inputs

Fit setup and results

- Minimize $\chi^2 = \sum \left(\frac{Y_{\text{obs}} - Y_{\text{exp}}}{\Delta Y_{\text{obs}}} \right)^2$
 - ΔY_{obs} statistical uncertainty only
- Systematic uncertainties: Run 10^5 fits with smearing
 - K_i : Independent Gaussian smearing according to uncertainties
 - c_i, s_i : Gaussian smearing according to correlations and uncertainties

Final results

$$r_D^{K\pi} \cos \delta_D^{K\pi} = -0.0547 \pm 0.0084 \pm 0.0049 \pm 0.0010$$

$$r_D^{K\pi} \sin \delta_D^{K\pi} = -0.010 \pm 0.012 \pm 0.007 \pm 0.003$$

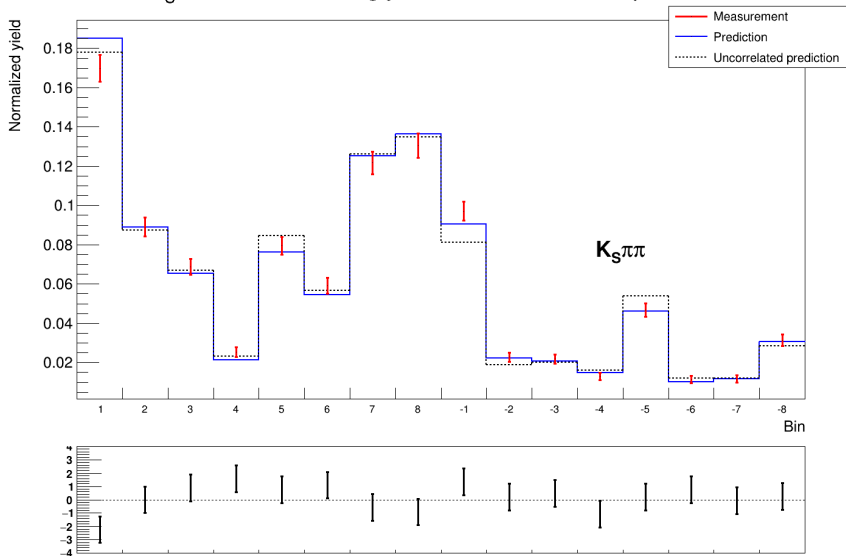
Uncertainties: Statistical \pm K_i systematics \pm c_i/s_i systematics

- $r_D^{K\pi} \cos \delta_D^{K\pi} / r_D^{K\pi} \sin \delta_D^{K\pi}$
correlations are small:

| $K^-\pi^+$ | $K_i^{(\prime)}$ | $c_i^{(\prime)}, s_i^{(\prime)}$ |
|------------|------------------|----------------------------------|
| 0.035 | -0.005 | 0.021 |

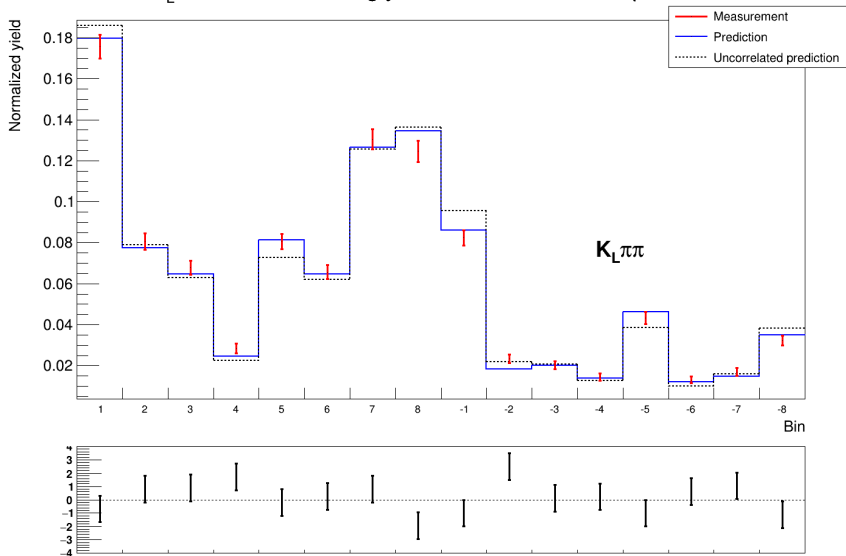
Bin yield yield vs fit prediction

$K_S hh$ vs $K\pi$ double tag yield measurement and prediction

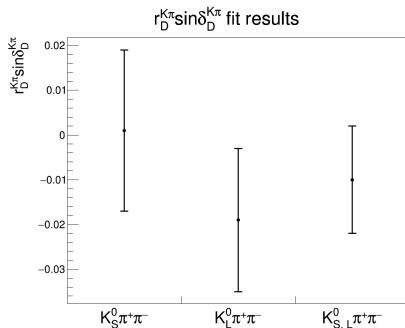
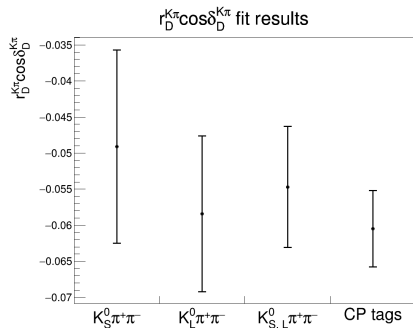


Bin yield yield vs fit prediction

$K_L h h$ vs $K\pi$ double tag yield measurement and prediction



Separate $K_S^0\pi^+\pi^-$ and $K_L^0\pi^+\pi^-$ fits



| Sample | $r_D^{K\pi} \cos \delta_D^{K\pi}$ | $r_D^{K\pi} \sin \delta_D^{K\pi}$ | χ^2/ndf |
|-----------------------|-----------------------------------|-----------------------------------|--------------|
| $K_S^0\pi^+\pi^-$ | -0.0491 ± 0.0134 | 0.001 ± 0.018 | 14.4/14 |
| $K_L^0\pi^+\pi^-$ | -0.0584 ± 0.0108 | -0.019 ± 0.016 | 20.1/14 |
| $K_{S,L}^0\pi^+\pi^-$ | -0.0547 ± 0.0084 | -0.010 ± 0.012 | 35.4/30 |
| CP tags | -0.0605 ± 0.0053 | - | |

Combination of measurements

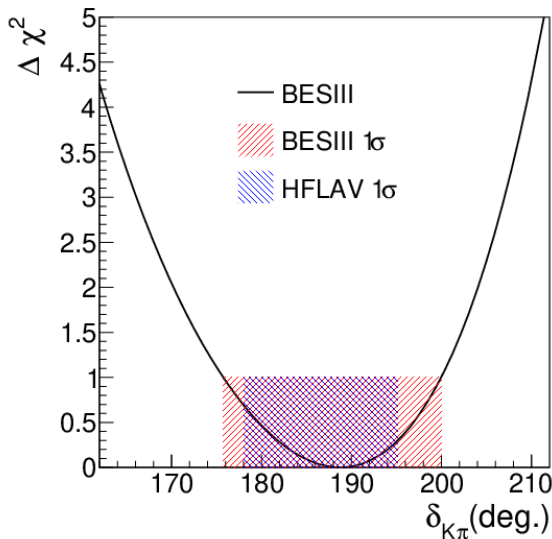
Inputs to combination:

- $r_D^{K\pi} \cos \delta_D^{K\pi} = -0.0588 \pm 0.0052$
 - $K_{S,L}^0 \pi^+ \pi^-$
 - CP tags

- $r_D^{K\pi} \sin \delta_D^{K\pi} = -0.010 \pm 0.014$
 - $K_{S,L}^0 \pi^+ \pi^-$

Final result:

- $\delta_D^{K\pi} = (188.7^{+11.2}_{-13.0})^\circ$
- $\delta_D^{K\pi} = (189.8^{+14.3}_{-13.7})^\circ$
from $r_D^{K\pi} \sin \delta_D^{K\pi}$ only



Summary

- Have performed an updated measurement of $\mathcal{A}_{K\pi} = 0.127 \pm 0.012$
- As part of this analysis, BR of three $K_L X$ modes in a manner independent of flavour-tag input were determined
 - These will be valuable inputs for future strong-phase studies
- Have fitted $K^-\pi^+$ vs $K_{S,L}\pi^+\pi^-$ in bins of phase space
 - Gain sensitivity to both $r_D^{K\pi} \cos \delta_D^{K\pi}$ and $r_D^{K\pi} \sin \delta_D^{K\pi}$
- Final result: $\delta_D^{K\pi} = (188.7^{+11.2}_{-13.0})^\circ$
- Precision compares favourably with that from ensemble of charm-mixing data, will improve significantly with increase in data set foreseen at $\psi(3770)$
- MEMO in preparation, and will be circulated in coming week

Thank you!