# BESIII Physics & Software Meeting Measurement of the CP even fraction $F_+$ in $D^0 \to K^+K^-\pi^+\pi^-$

Martin Tat Guy Wilkinson Sneha Malde Yu Zhang

University of Oxford

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#### Outline

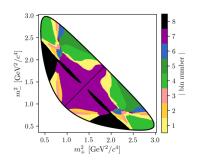
- Introduction and motivation
- 2 Strategy of strong-phase analysis
- Selection
- 4 Fit of single tag yields
- 5 Fit of double tag yields
  - Fit strategy
  - CP tags
  - $K_{S,L}\pi\pi$  tags
- 6 Reweighting of  $KK\pi\pi$  model
- 8 Systematics
- Summary and conclusion

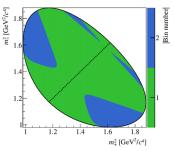
#### Introduction

- Perform strong-phase analysis of  $D^0 \to K^+K^-\pi^+\pi^-$
- This analysis: Phase space integrated analysis
  - $2.93\,\mathrm{fb^{-1}}\ \psi(3770)\ \mathrm{data}\ \mathrm{from}\ 2010\text{-}2011$
  - Measure CP even fraction F<sub>+</sub>
- Future analysis: Binned phase space analysis
  - Expect pprox 20 fb $^{-1}$   $\psi$ (3770) data from 2010-2011 and 2021-2023
  - Measure amplitude-averaged cosine and sine of strong-phase  $c_i$  and  $s_i$
  - Plan to analyse 2021-2022 data initially

#### Introduction to GGSZ analysis of $\gamma$

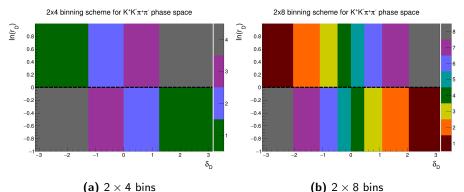
- Main motivation: Measure  $\gamma$  in  $B^\pm \to DK^\pm$  with self-conjugate multi-body D decay
  - Model independent measurement: Bins of D decay phase space
  - External inputs: Measure  $c_i$  and  $s_i$  at BESIII
  - ullet Poor binning reduces statistical sensitivity o No bias!
- ullet J. High Energ. Phys. 2021, 169 (2021):  $B^\pm o D h^\pm$ ,  $D o K_S^0 h^+ h^-$ 
  - Single most precise measurement:  $\gamma = (68.7^{+5.2}_{-5.1})^{\circ}$





#### Introduction to GGSZ analysis of $\gamma$

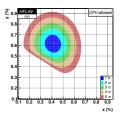
- Our aim: Analyse  $B^\pm \to [K^+K^-\pi^+\pi^-]_D h^\pm$  in bins of phase space
  - Develop binning scheme using LHCb model JHEP 02 (2019) 126
  - ullet Simultaneously analyse  $c_i/s_i$  at BESIII and  $\gamma$  at LHCb
  - Expected precision  $\Delta\gamma \approx 12^\circ$  with LHCb Run 1+2



**Figure 1:** Binning scheme for  $D^0 \to K^+K^-\pi^+\pi^-$ 

#### Introduction to D mixing and CP-violation

- $D o KK\pi\pi$  can also be used to study D-mixing
- Phase space integrated analysis:
  - Physical Review D, 91(9), 2015
  - Measure mixing parameter  $y_{\rm CP}$  and CP-violation parameter  $A_{\Gamma}$  in self-conjugate multi-body decays
- Analysis in bins of phase space:
  - Phys. Rev. Lett. 127, 111801 (2021)
  - Bin-flip analysis of  $D \to K_S \pi \pi$
  - Measure mixing parameters x, y and CP-violation parameters |q/p|,  $\varphi$



(a) Source: HFLAV



(b) Source: LHCb outreach

#### Motivation for $F_+$ measurement

- ullet  $F_+$  describes the CP content of a self-conjugate multi-body decay
  - $F_+ = 1$  (0) for CP even (odd) final states
- $F_+$  can be measured with current  $3 \, \text{fb}^{-1}$  dataset
  - First model independent measurement of  $F_{\perp}^{KK\pi\pi}!$
  - Useful to test agreement with LHCb model prediction:  $F_+ = 0.736$
- ullet Important input to quasi-GLW analysis of the CKM angle  $\gamma$ 
  - Current GLW modes: KK,  $\pi\pi$ ,  $\pi\pi\pi\pi$
  - ullet Minimal effort to include  $KK\pi\pi$  in GLW analyses  $\Longrightarrow$  More statistics
- Other  $F_+$  measurements:
  - $D^0 \to \pi^+\pi^-\pi^+\pi^-$  JHEP 01 (2018) 144
  - $D^0 \to K_S \pi^+ \pi^- \pi^0$  JHEP 01 (2018) 82
  - $D^0 \rightarrow h^+ h^- \pi^0$  Physics Letters B 747 (2015)
  - Measurements are from CLEO-c, BESIII analyses ongoing

#### Strategy for strong-phase analysis

- **①** Select double tags of  $KK\pi\pi$  vs flavour, CP and self-conjugate tags
- Normalise double tag yields by the corresponding single tag yields
- Measure flavour tag yields K<sub>i</sub>
- Fit  $c_i$  with CP tags and  $c_i+s_i$  with self-conjugate tags:

#### $c_i/s_i$ analysis: Bins of $KK\pi\pi$ phase space

CP: 
$$M_i \propto (K_i + K_{-i} - 2c_i \sqrt{K_i K_{-i}} (2F_+^{\text{tag}} - 1))$$

Self-conjugate: 
$$M_{ij} \propto \left(K_i K_{-j}' + K_{-i} K_j' - 2 \sqrt{K_i K_{-i} K_j' K_{-j}'} (c_i c_j' + s_i s_{-j}')\right)$$

#### $F_+$ analysis: Sum over all $KK\pi\pi$ phase space bins

CP: 
$$M \propto \left(1 - 2(2F_{+}^{KK\pi\pi} - 1)(2F_{+}^{\text{tag}} - 1)\right)$$

Self-conjugate: 
$$M_j \propto \left(K_j' + K_{-j}' - 2c_j' \sqrt{K_j' K_{-j}'} (2F_+^{KK\pi\pi} - 1)\right)$$

#### Selection

- Selection of charged and neutral particles follow standard track and shower requirements
- Require flight significance > 2 for  $K_S$
- $K_S$  veto for  $KK\pi\pi$  and  $\pi\pi\pi^0$  tags
- $\Delta E$  cut of  $3\sigma$
- ullet  $\Delta E$  fit for 4-body modes allows a non-smooth background at  $\Delta E=0$

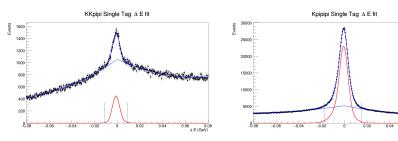
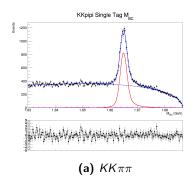
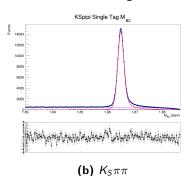


Figure 3: Double Gaussian signal and Chebychev polynomial background

#### Single tag fits

- Fit strategy: Fit  $m_{
  m BC}$
- Fit model:
  - Signal: PDF from signal MC, convoluted with single or double Gaussian
  - Flat background: Argus PDF
  - Peaking background shape and yield fixed
    - Fit shape to dedicated MC samples
    - Calculate yield from ratios of efficiencies and branching fractions





#### Single tag fits

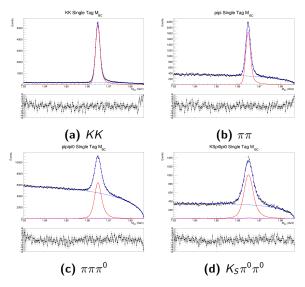


Figure 5: Single tag fits of CP even tags

#### Single tag fits

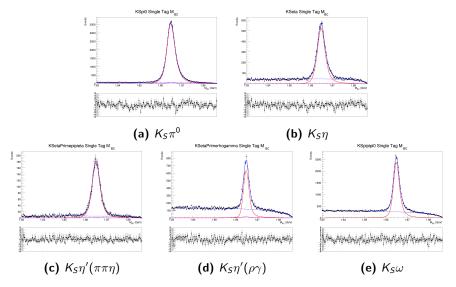


Figure 6: Single tag fits of CP odd tags

### Single tag yields and efficiencies

Tag mode	Single tag yield	Single tag efficiency (%)
$K^+K^-\pi^+\pi^-$	$10642\pm156$	$19.02 \pm 0.09$
K <sup>+</sup> K <sup>-</sup>	$56303 \pm 262$	$63.41 \pm 0.11$
$\pi^+\pi^-$	$20386\pm179$	$67.41 \pm 0.10$
$K_S\pi^0$	$67876\pm278$	$38.18 \pm 0.11$
$K_S\pi^0\pi^0$	$22392 \pm 229$	$14.35\pm0.08$
$K_L\pi^0$	$47595\pm1653$	$27.83 \pm 0.23$
$K_{S}\eta$	$9308\pm113$	$31.78 \pm 0.10$
$K_{\mathcal{S}}\eta'_{\pi\pi\eta}$	$3213 \pm 62$	$12.81\pm0.07$
$K_S \eta'_{ ho\gamma}$	$8283 \pm 116$	$20.80 \pm 0.09$
$\pi^+\pi^-\pi^0$	$107504 \pm 602$	$36.65 \pm 0.11$
$K_S\omega$	$22068 \pm 217$	$14.50\pm0.08$
$K_S\pi^+\pi^-$	$161914 \pm 440$	$36.40 \pm 0.11$
$K_S \pi^+ \pi^-$ part. reco.	$161914 \pm 440$	$\textbf{36.40} \pm \textbf{0.11}$
$K_L \pi^+ \pi^-$	$223141\pm2146$	$46.1\pm0.3$

- Fit strategy:
  - ullet Fully reconstructed tags: Only fit signal  $\emph{m}_{
    m BC}$  because of low statistics
  - ullet Partially reconstructed tags: Fit missing mass squared  $m_{
    m miss}^2$
- Fit model:
  - Signal: PDF from signal MC, convoluted with single Gaussian
  - Background: Argus PDF
  - Peaking backgrounds fixed, with quantum correlation accounted for
  - Simple sideband subtraction for correct signal but wrong tag event
- For tags with multiple bins, perform a simultaneous fit of all bins
  - Shape is floated and shared across all bins
  - Yield of signal and combinatorial background is floated in each bin

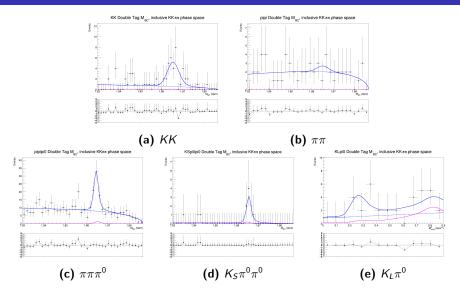


Figure 7: Double tag fits of CP even tags

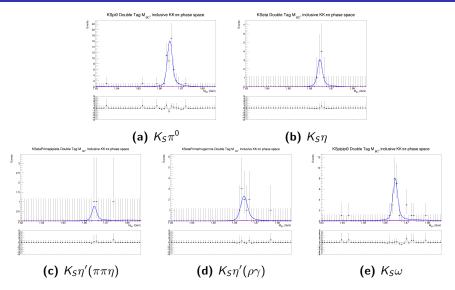


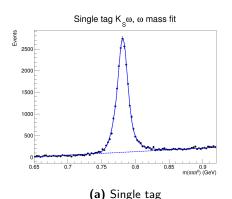
Figure 8: Double tag fits of CP odd tags

#### CP double tag yields and efficiencies

Daubla tag viold	Double tag officionsy (0/)
	Double tag efficiency (%)
$28\pm10$	$14.52\pm0.06$
$2\pm4$	$15.02\pm0.06$
$48\pm7$	$6.87 \pm 0.04$
$8.0 \pm 2.8$	$2.873 \pm 0.026$
$7\pm5$	$5.29 \pm 0.04$
$8.9 \pm 3.0$	$5.72 \pm 0.04$
$2.2\pm1.6$	$2.024 \pm 0.021$
$8.7 \pm 3.0$	$3.295 \pm 0.027$
$53\pm10$	$7.66 \pm 0.04$
9 ± 3	$2.234 \pm 0.022$
	$48 \pm 7$ $8.0 \pm 2.8$ $7 \pm 5$ $8.9 \pm 3.0$ $2.2 \pm 1.6$ $8.7 \pm 3.0$ $53 \pm 10$

#### Non-resonant background in $K_S\omega$

- ullet  $K_S\omega$  has CP-even contamination from non-resonant  $K_S\pi\pi\pi^0$ 
  - $F_+(K_S\pi\pi\pi^0) = 0.238 \pm 0.012 \pm 0.012$  from CLEO
- ullet From  $m_{
  m BC}$  fit, subtract flat background using sPlot and fit  $\pi\pi\pi^0$



Double tag  $K_S \omega$ ,  $\omega$  mass fit

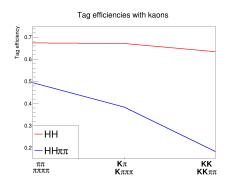
(b) Double tag

#### $F_+$ measurement with $K_{S,L}\pi\pi$ tags

• With  $K_S\pi\pi$ , increase sensitivity through binning of  $K_S\pi\pi$  phase space

$$M_{j} \propto \left(K_{j}^{\prime} + K_{-j}^{\prime} - 2\sqrt{K_{j}^{\prime}K_{-j}^{\prime}}c_{j}^{\prime}(2F_{+}^{KK\pi\pi} - 1)\right)$$

• Problem:  $KK\pi\pi$  reconstruction efficiency is too low  $\to$  Low yields!



ullet Likely explanation: Softer kaons o Kaons get stuck inside tracker

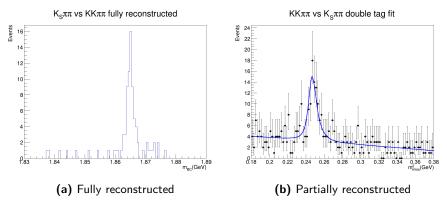
#### $F_+$ measurement with $K_{S,L}\pi\pi$ tags

- Solution: Partially reconstructed  $KK\pi\pi$
- Strategy:
  - **1** Reconstruct  $D \rightarrow K_S \pi \pi$
  - 2 Require 3 remaining good tracks consistent with  $K\pi\pi$
  - Use missing mass to reconstruct missing kaon

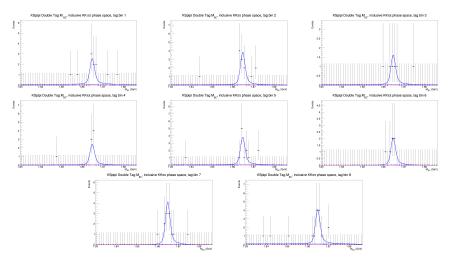
Mode	Inclusive yield	Double tag efficiency
$K_S\pi\pi$ (fully reconstructed)	$69\pm9$	$6.56\pm0.04$
$K_S\pi\pi$ (partially reconstructed)	$91\pm15$	$\textbf{7.01} \pm \textbf{0.04}$
$K_L\pi\pi$ (partially reconstructed)	$158\pm15$	$\textbf{7.25} \pm \textbf{0.04}$

#### Partially reconstructed $KK\pi\pi$ vs $K_S\pi\pi$

- Main challenge with partially reconstructed  $KK\pi\pi$ :  $K\pi\pi\pi\pi^0$
- Require no  $\pi^0$  candidates



**Figure 10:**  $KK\pi\pi$  vs  $K_S\pi\pi$ 



**Figure 11:**  $KK\pi\pi$  vs  $K_S\pi\pi$  simultaneous fit

#### Efficiency corrections

- All yields must be corrected for efficiency
- Problem: BESIII simulation uses a very old  $KK\pi\pi$  model in EvtGen
- Solution: Reweight BESIII simulation to look like the LHCb model
  - Use Python hep\_ml Gradient Boosted Reweighter
  - Variables:

    - $2 m^2 (K^+ \pi^-)$
    - $m^2(K^-\pi^+)$
    - $m^2(\pi^+\pi^-)$

    - $m^2(K^+K^-\pi^+)$

#### Naive efficiency correction

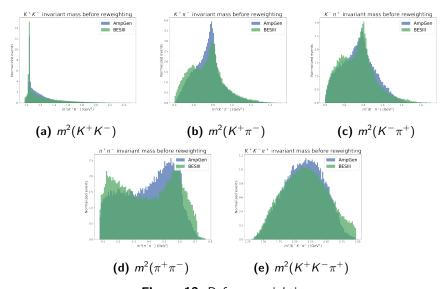


Figure 12: Before reweighting

#### Naive efficiency correction

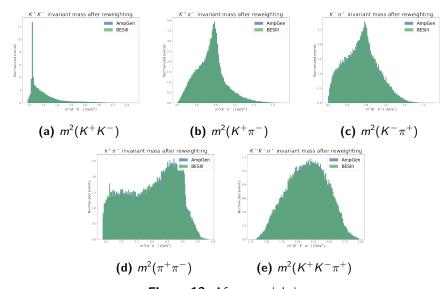
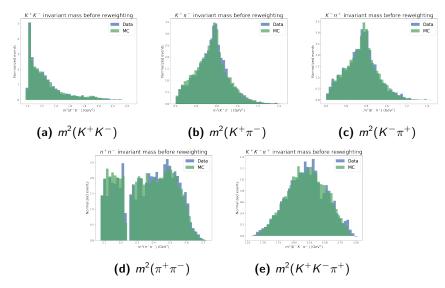


Figure 13: After reweighting

#### Does the naive reweighting work?

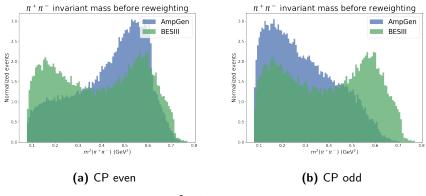


**Figure 14:** Single tag  $D \to KK\pi\pi$  in data and MC after reweighting

#### Quantum correlated LHCb model

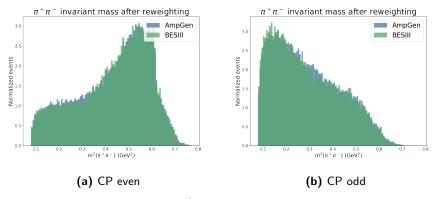
- Problem with naive reweighting:
  - ullet LHCb model assumes a pure  $D^0 o K^+ K^- \pi^+ \pi^-$  decay
  - No quantum correlations
  - Example: If tag is  $D \to KK$ , the  $D \to KK\pi\pi$  decay will be CP odd!
  - ullet Quantum correlations will affect phase space distribution  $\Longrightarrow$  Efficiencies could change
- Solution: Separate reweighters for CP even/odd  $D o K^+K^-\pi^+\pi^-$ 
  - CP even tags: Use efficiencies after reweighting to CP odd model
  - CP odd tags: Use efficiencies after reweighting to CP even model
  - $K_{S,L}\pi\pi$  tags: Do a weighted average of the two efficiencies

#### Before weighting to CP even/odd models



**Figure 15:**  $m^2(\pi^+\pi^-)$  before reweighting

#### After weighting to CP even/odd models

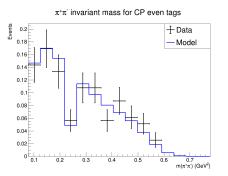


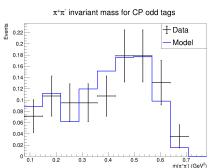
**Figure 16:**  $m^2(\pi^+\pi^-)$  after reweighting

No reweighting	Naive reweighting	CP even model	CP odd model
18.0%	19.0%	18.1%	21.9%

#### Agreement between quantum correlated data and model

- Note: LHCb model knows nothing about quantum correlations
- $D^0/\bar{D^0}$  amplitudes simply combined to obtain CP even/odd models
- Important question: Can the model describe quantum correlated double tag data at all? Answer: Yes!



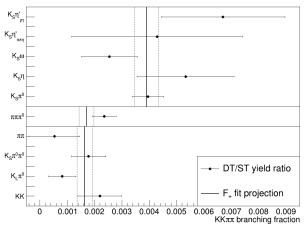


- (a) Double tags of  $KK\pi\pi$  vs CP even
- **(b)** Double tags of  $KK\pi\pi$  vs CP odd

Figure 17:  $m^2(\pi^+\pi^-)$  in double tags, compared with CP even/odd LHCb models

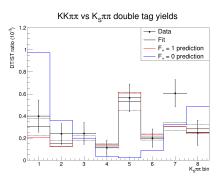
#### $F_+$ measurement with CP tags

#### $D^0 \rightarrow KK\pi\pi$ BF asymmetry

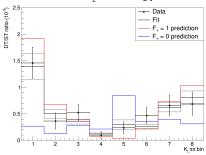


**Figure 18:**  $F_+$  combination of CP tags Fit result:  $F_+ = 0.703 \pm 0.042$ ,  $\chi^2 = 1.4$ 

#### $F_+$ measurement with $K_{S,L}\pi\pi$ tags



#### $KK\pi\pi$ vs $K_1\pi\pi$ double tag yields



(a) Result:  $F_+ = 0.872 \pm 0.091$ ,  $\chi^2 = 1.3$  (b) Result:  $F_+ = 0.679 \pm 0.103$ ,  $\chi^2 = 0.8$ 

**Figure 19:**  $F_+$  combination of  $K_S\pi\pi$  (left) and  $K_L\pi\pi$  (right)

#### $F_+$ combination

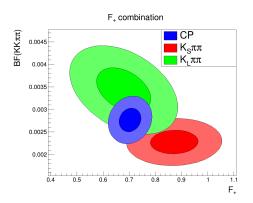


Figure 20:  $F_+$  combination

- Observe large anti-correlation in  $K_L\pi\pi$  because  $F_+^{K_L\pi\pi} \approx 0.354$ 
  - Yield of  $K_L\pi\pi$  is twice as large as that of  $K_S\pi\pi$
  - ullet Fractional bin yields and total yield contains information about  $F_+$
  - When  $K_L\pi\pi$  BF is available, combine all tags!

#### Systematics

Tag-specific systematic uncertainties, in units of  $10^{-2}$ 

Source	CP tags	$K_{S,L}\pi\pi$ tags
Efficiency	0.1	0.4
External inputs	0.3	8.0
Peaking backgrounds	0.2	0.3
$K_L^0\pi^0$ ST yield	2.1	N/A
Efficiency factorisation	0.6	N/A
Total	2.2	0.9

Common systematic uncertainties, in units of  $10^{-2}$ 

Source	Common systematic
Efficiency reweighting	1.5
$K_{\mathcal{S}}^{0}$ veto	0.8

#### Summary

- First model-independent measurement of CP even fraction in  $D^0 \to K^+ K^- \pi^+ \pi^-$ 
  - Analysis is now ready for review
  - $F_{+} = 0.730 \pm 0.040 \pm 0.017$
  - Statistics dominated!
  - Very consistent with model prediction:  $F_+ = 0.736$
- Valuable input to:
  - ullet  $\gamma$  measurement with GLW method
  - D-mixing and CPV analyses
- ullet Future  $\psi(3770)$  data will allow us to perform a binned analysis

## Thank you!

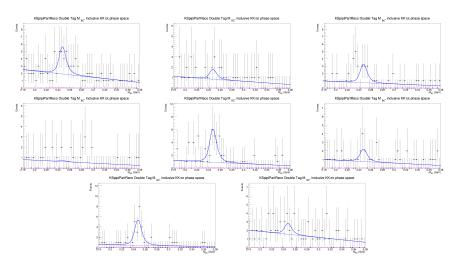
#### Backup

## Backup

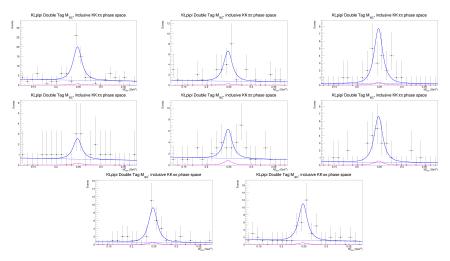
#### Tag modes

- Flavour tags:
  - *K*π, *K*ππ<sup>0</sup>, *K*πππ, *Ke*ν
- CP even tags:
  - KK,  $\pi\pi$ ,  $\pi\pi\pi^0$  (mostly CP even),  $K_S\pi^0\pi^0$ ,  $K_L\pi^0$
- CP odd tags:
  - $K_S\pi^0$ ,  $K_S\eta$ ,  $K_S\omega$ ,  $K_S\eta'_{\pi\pi\eta}$ ,  $K_S\eta'_{\rho\gamma}$
- Self-conjugate tags:
  - K<sub>S</sub>ππ, K<sub>L</sub>ππ

Underlined tags have not been finalized yet



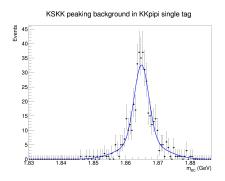
**Figure 21:** Partially reconstructed  $KK\pi\pi$  vs  $K_S\pi\pi$  simultaneous fit



**Figure 22:**  $KK\pi\pi$  vs  $K_L\pi\pi$  simultaneous fit

#### Peaking backgrounds

- Strategy for fixing peaking backgrounds:
  - Generate dedicated MC sample
  - Obtain retention rate of peaking background
  - Fit background with appropriate shape (Gaussian, Crystal Ball, ...)
  - Use BFs from PDG to fix background-to-signal ratio



**Figure 23:** Double Gaussian fit of  $K_SKK$  background in  $KK\pi\pi$  single tag fit

#### Quantum correlation in peaking backgrounds

- Strategy for peaking backgrounds with different CP:
  - Correct using  $F_{+}^{KK\pi\pi}$  from LHCb model
- Strategy for  $K_SKK$  background in  $KK\pi\pi$ 
  - $F_{+}^{K_{S}KK} = 0.524 \pm 0.018$  from Phys. Rev. D **102**, 052008
  - Use dedicated MC to find retention in each  $K_SKK$  bin
  - $K_S$  veto removes more  $K_S\phi$  than  $K_Sa(980)^0 \implies$  Calculate effective  $F_+$  for  $K_SKK$  to  $KK\pi\pi$  background