

# BESIII Charm Meeting

## Phase-space binned analysis of strong-phase parameters in $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

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# Outline

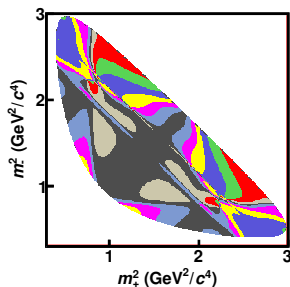
- 1 Introduction
- 2 Binning scheme
- 3 Formalism and measurement strategy
- 4 Selection
- 5 Fit of double tag yields
- 6 Likelihood fit
- 7 Input-output checks
- 8 Fit results
- 9 Bonus measurements
- 10 Summary and conclusion

# Introduction

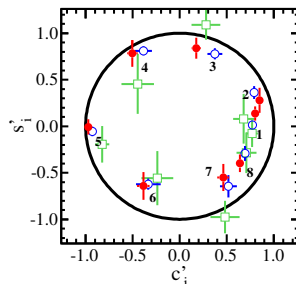
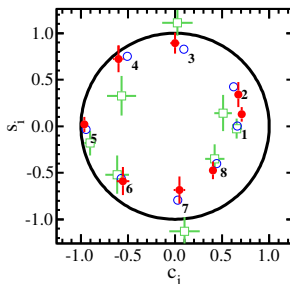
- Aim of analysis: Measure the strong-phase difference between  $D^0$  and  $\bar{D}^0 \rightarrow K^+ K^- \pi^+ \pi^-$  using the  $8 \text{ fb}^{-1} \psi(3770)$  dataset
- Important input to:
  - ① Measurement of the CKM angle  $\gamma$
  - ② Studies of charm mixing and CPV
  - ③ Strong-phase measurements of other decay modes
- Phase-space integrated measurement: [Phys. Rev. D \*\*107\*\* 032009](#)
- Strong phases are diluted when integrated over the 5D phase space  
 $\implies$  Perform analysis in bins
- Binned model-dependent analysis of  $\gamma$  has already been performed at LHCb: [arXiv:2301.10328](#)

# Introduction - Previous strong-phase analyses

- Golden mode for strong-phase analysis:  $D^0 \rightarrow K_{S,L}^0 \pi^+ \pi^-$
- Measurements of  $c_i$  and  $s_i$  performed in  $2 \times 8$  bins:
  - CLEO: [Phys. Rev. D \*\*82\*\* 112006](#)
  - BESIII: [Phys. Rev. D \*\*101\*\* 112002](#)



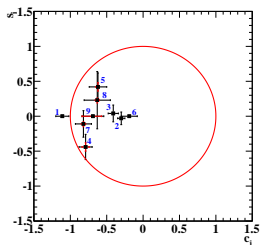
(a) Equal  $\delta$  binning scheme



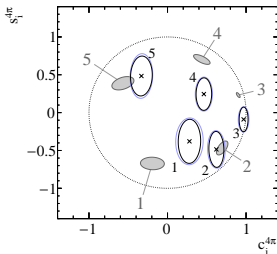
(b)  $c_i$  and  $s_i$  for (left)  $K_S \pi \pi$  and (right)  $K_L \pi \pi$

# Introduction - Previous strong-phase analyses

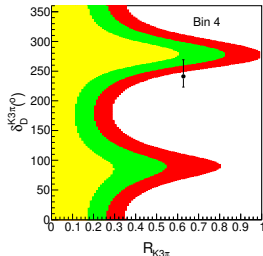
- Four-body decays have a 5D phase space, but their binning scheme may be defined analogously
- Many different strategies for 5D binning schemes:
  - $D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$ : [JHEP 2018 82 \(2018\)](#)
  - $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : [JHEP 2018 144 \(2018\)](#)
  - $D \rightarrow K^- \pi^+ \pi^- \pi^+$ : [JHEP 2021 164 \(2021\)](#)



(a)  $K_S \pi \pi \pi^0$



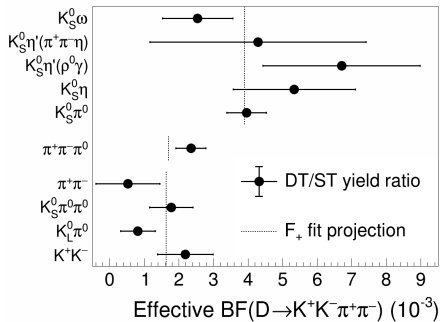
(b)  $4\pi$



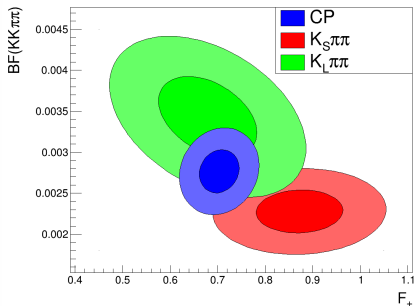
(c)  $K \pi \pi \pi$

# Introduction - Previous strong-phase analyses

- The phase-space integrated strong phase of  $D \rightarrow K^+ K^- \pi^+ \pi^-$  was previously measured: [Phys. Rev. D \*\*107\*\* 032009](#)
- The asymmetry in the branching fraction measured using CP even and CP odd tags is sensitive to the CP-even fraction  $F_+$ 
  - $c_i = 2F_+ - 1$  is the amplitude-average cosine of the strong phase



(a) BF asymmetry



(b)  $F_+$  combination

## Strong phases are determined from yield asymmetries

- When integrating over a phase-space region, variations in strong phases dilute the asymmetries
- We require a binning scheme to minimise the dilution and enhance asymmetry effects

## How to bin a 5-dimensional phase space?

- Generate C++ code for LHCb amplitude model using AmpGen<sup>1</sup>
- For each  $D$  event, calculate

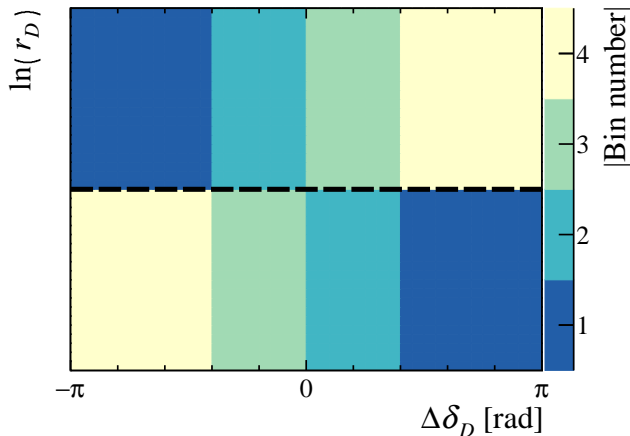
$$\frac{\mathcal{A}(D^0)}{\mathcal{A}(\bar{D}^0)} = r_D e^{i\delta_D}$$

- Bin along  $\delta_D$  and  $r_D$ 
  - Bin boundaries in  $\delta_D$  are moved to maximise sensitivity to  $\gamma$

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<sup>1</sup>AmpGen by Tim Evans

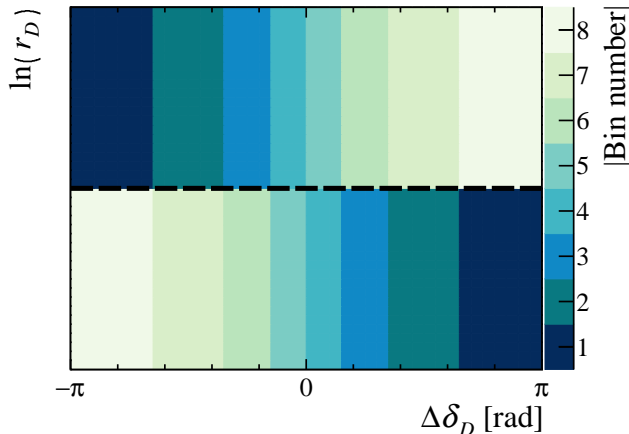
# Binning scheme



Bins  $i < 0$  on top,  $i > 0$  below  
Binning scheme used in this analysis



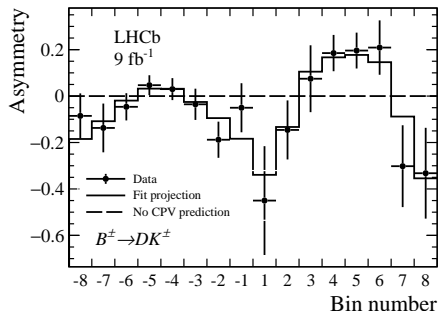
# Binning scheme



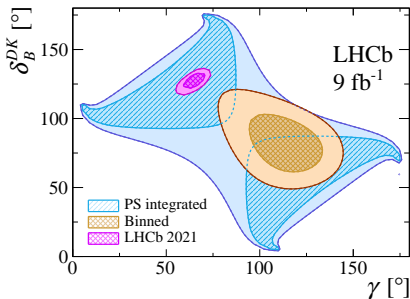
Bins  $i < 0$  on top,  $i > 0$  below

Possible binning scheme for future analysis with  $20 \text{ fb}^{-1}$  dataset

# Model-dependent LHCb measurement



(a) Bin asymmetries in  $B^\pm \rightarrow DK^\pm$



(b) Measurement of  $\gamma$  at LHCb

$$\gamma = (116_{-14}^{+12})^\circ$$

This result is currently model independent, and needs external inputs from BESIII to become a proper model-independent measurement!

$D\bar{D}$  pair from  $\psi(3770)$  is prepared in a  $\mathcal{C} = -1$  state

- $D$  mesons are “quantum correlated”
- The decay of  $D \rightarrow K^+ K^- \pi^+ \pi^-$  is correlated by the  $CP$  content of the tag mode

$$|D\bar{D}\rangle = \frac{1}{\sqrt{2}}(|D^0\rangle|\bar{D}^0\rangle - |\bar{D}^0\rangle|D^0\rangle)$$

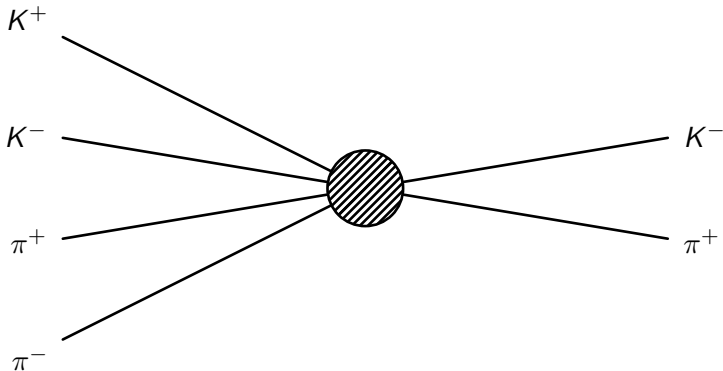
- Equivalently, in terms of  $CP$  eigenstates:

$$|D\bar{D}\rangle = \frac{1}{\sqrt{2}}(|D_-\rangle|D_+\rangle - |D_+\rangle|D_-\rangle)$$

# Formalism and measurement strategy

- Tag mode can be a flavour tag

- $K\pi$ ,  $K\pi\pi^0$ ,  $K\pi\pi\pi$ ,  $K\ell\nu$

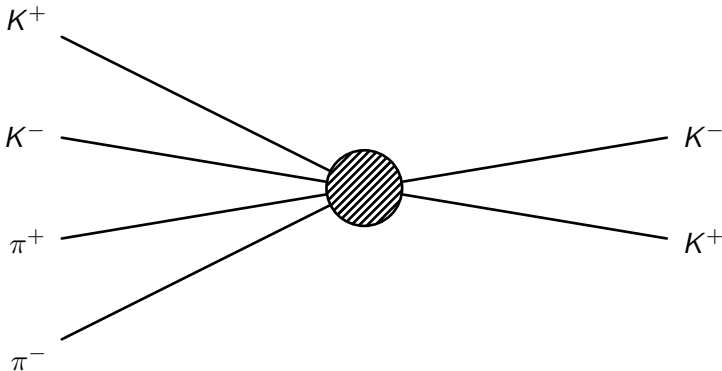


Use flavour tags to measure fraction of  $D^0 \rightarrow KK\pi\pi$  decays in bin  $i$ :

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B} \times K_i$$

# Formalism and measurement strategy

- Tag mode can be a CP even tag
  - $KK$  (fully and part. reco  $KK\pi\pi$ ),  $\pi\pi$ ,  $\pi\pi\pi^0$ ,  $K_S\pi^0\pi^0$ ,  $K_L\pi^0$

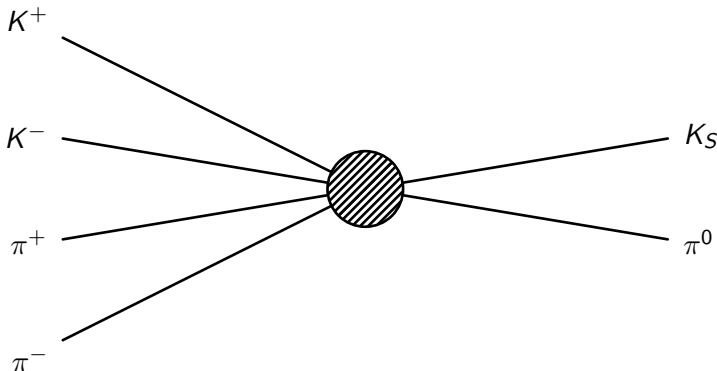


$D \rightarrow K^+K^-$ , which is  $CP$  even, forces  $D \rightarrow K^+K^-\pi^+\pi^-$  to be  $CP$  odd:

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B} \times (K_i + K_{-i} - 2\sqrt{K_i K_{-i}} c_i)$$

# Formalism and measurement strategy

- Tag mode can be a CP odd tag
  - $K_S\pi^0$  (fully and part.reco  $KK\pi\pi$ ),  $K_S\eta$ ,  $K_S\eta'(\pi\pi\eta, \pi\pi\gamma)$ ,  $K_S\pi\pi\pi^0$

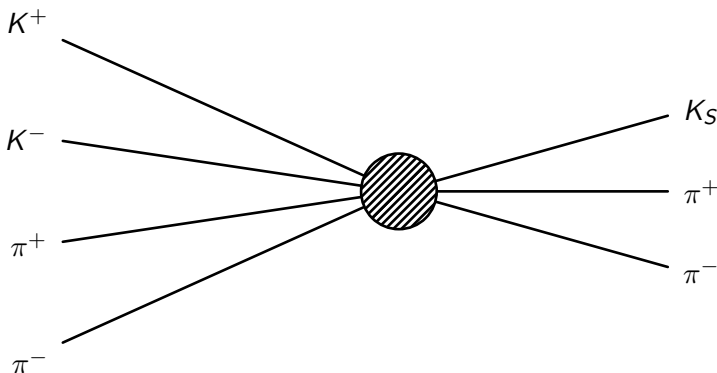


$D \rightarrow K_S^0\pi^0$ , which is  $CP$  odd, forces  $D \rightarrow K^+K^-\pi^+\pi^-$  to be  $CP$  even:

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B} \times (K_i + K_{-i} + 2\sqrt{K_i K_{-i}} c_i)$$

# Formalism and measurement strategy

- Tag mode can be a self-conjugate multi-body tag
  - $K_S\pi\pi$  (fully and part.reco  $KK\pi\pi$ ),  $K_L\pi\pi$

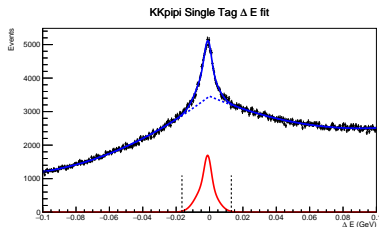


$D \rightarrow K_S^0 \pi^+ \pi^-$  has different strong phases in different bins of phase space:

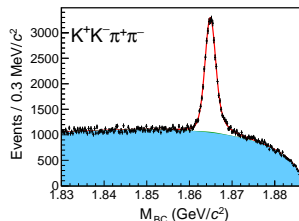
$$\frac{N_{ij}^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B} \times (K_i K'_{-j} + K_{-i} K'_j - 2\sqrt{K_i K_{-i} K'_j K'_{-j}}(c_i c'_j + s_i s'_j))$$

# Selection

- Double-tag analysis: Select  $D \rightarrow KK\pi\pi$  events tagged with flavour,  $CP$  and multi-body tags
- Selection more or less identical to previous double-tag analyses
- $D \rightarrow KK\pi\pi$  selection:
  - 4 good charged tracks
  - $3\sigma$  window around signal peak in  $\Delta E$
  - Asymmetric  $K_S KK$  veto for  $m(\pi^+\pi^-) \in [477, 507] \text{ MeV}$
  - Flight significance cut at 2



(a)  $\Delta E$  window

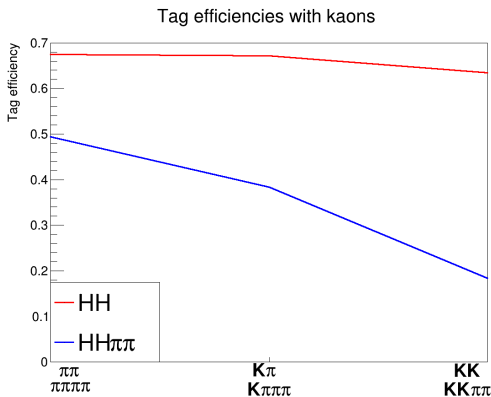


(b) Single tag yield:  $29\,227 \pm 268$



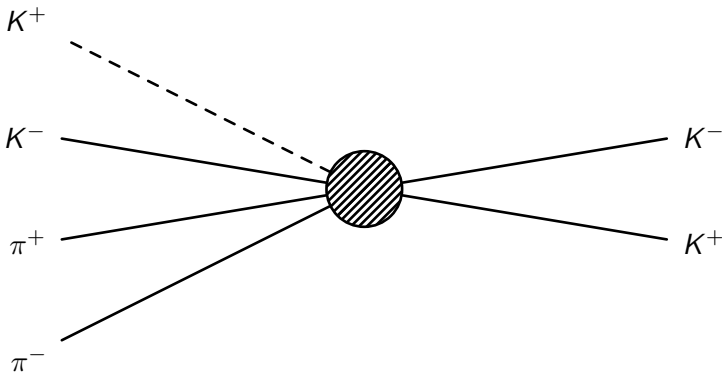
# Partially reconstructed $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

- The reconstruction efficiency of  $D \rightarrow KK\pi\pi$  is less than 20%
- For comparison, the efficiency of  $D \rightarrow \pi\pi\pi\pi$  is around 50%!
- Poor kaon tracking efficiency at low momentum



# Partially reconstructed $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

- Solution: Only reconstruct 3 of the charged  $D$  daughters
  - Presence of missing kaon is inferred from the missing momentum
  - Yields are similar to fully reconstructed sample
  - Large, but non-peaking background from  $D \rightarrow K \pi \pi \pi \pi^0$

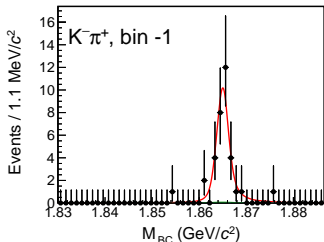


Use this technique with the  $K^+ K^-$ ,  $K_S^0 \pi^0$  and  $K_S^0 \pi^+ \pi^-$  tags

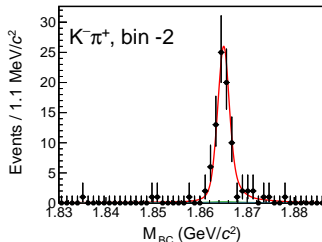
# Double tag fits

- Fit strategy: Only fit signal side  $m_{BC}$  because of low statistics
- Fit model:
  - Signal: PDF from signal MC, convolved with a Gaussian
  - Flatackground: Argus PDF
  - Peaking background: Shape and efficiency from MC, correct for quantum correlation
  - Simple sideband subtraction for correct signal but wrong tag event
- Fit all bins simultaneously
  - Shape is floated and shared across all bins
  - Yield of signal and combinatorial background is floated in each bin

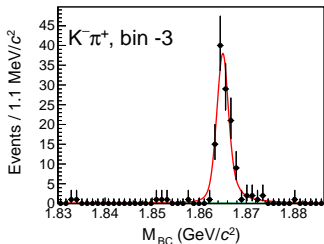
# Double tag fit of $KK\pi\pi$ vs $K\pi$



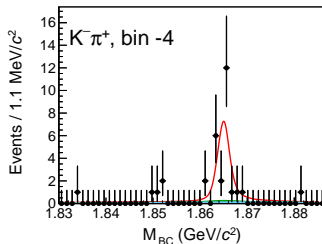
(a) Bin -1 yield:  $32.4^{+6.2}_{-5.5}$



(b) Bin -2 yield:  $82.7^{+9.7}_{-9.0}$

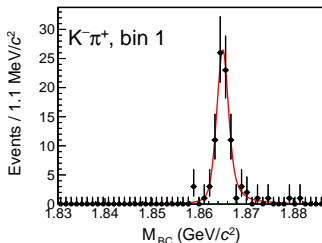


(c) Bin -3 yield:  $120.3^{+11.6}_{-10.9}$

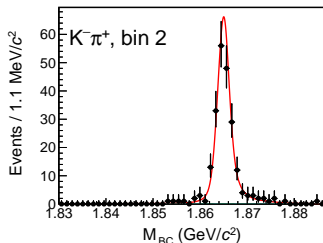


(d) Bin -4 yield:  $22.4^{+5.2}_{-4.6}$

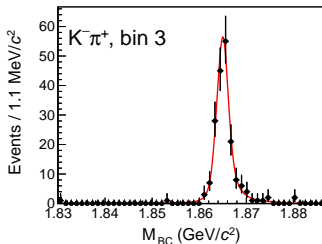
# Double tag fit of $KK\pi\pi$ vs $K\pi$



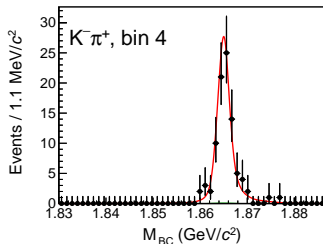
(a) Bin 1 yield:  $84.5^{+9.8}_{-9.1}$



(b) Bin 2 yield:  $211.2^{+15.4}_{-14.8}$

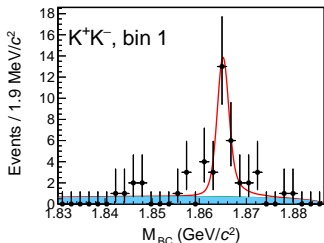


(c) Bin 3 yield:  $181.0^{+14.0}_{-13.3}$

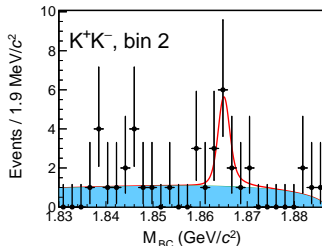


(d) Bin 4 yield:  $88.6^{+9.7}_{-9.0}$

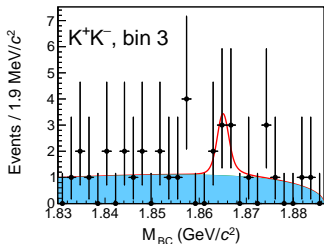
# Double tag fit of $KK\pi\pi$ vs $KK$



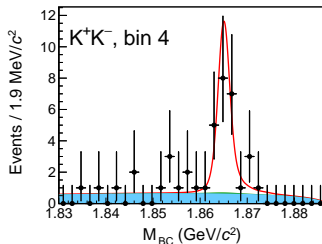
(a) Bin 1 yield:  $25.3^{+6.2}_{-5.5}$



(b) Bin 2 yield:  $8.8^{+4.0}_{-3.3}$

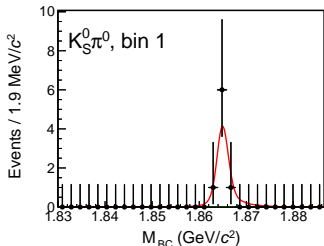


(c) Bin 3 yield:  $4.5^{+3.3}_{-2.6}$

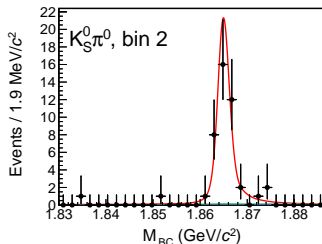


(d) Bin 4 yield:  $21.1^{+5.5}_{-4.8}$

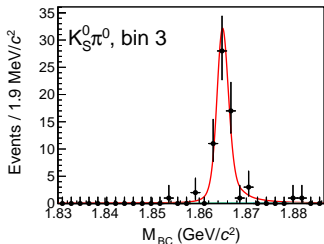
# Double tag fit of $KK\pi\pi$ vs $K_S\pi^0$



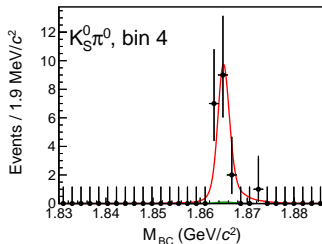
(a) Bin 1 yield:  $7.9^{+3.1}_{-2.5}$



(b) Bin 2 yield:  $40.4^{+6.8}_{-6.3}$

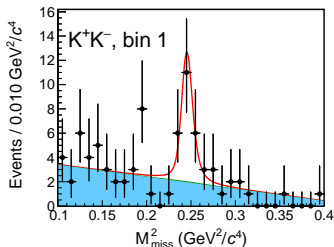


(c) Bin 3 yield:  $61.1^{+8.3}_{-7.8}$

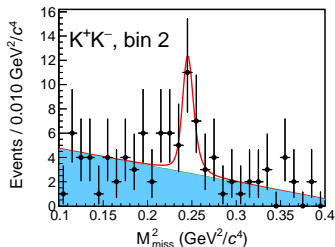


(d) Bin 4 yield:  $18.3^{+4.5}_{-3.9}$

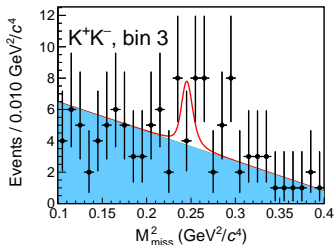
# Double tag fit of partially reconstructed $KK\pi\pi$ vs $KK$



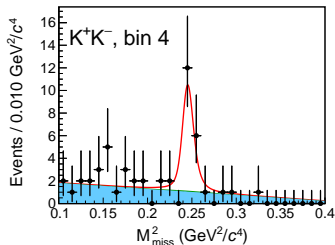
(a) Bin 1 yield:  $19.6^{+5.8}_{-5.1}$



(b) Bin 2 yield:  $17.7^{+6.1}_{-5.3}$



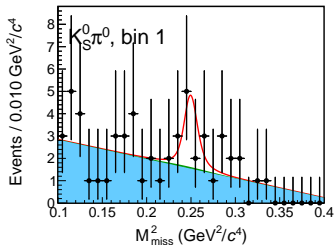
(c) Bin 3 yield:  $7.5^{+6.6}_{-5.7}$



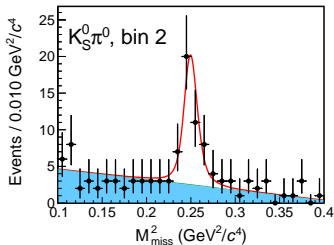
(d) Bin 4 yield:  $17.3^{+5.1}_{-4.4}$



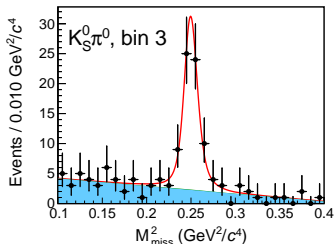
# Double tag fit of partially reconstructed $KK\pi\pi$ vs $K_S\pi^0$



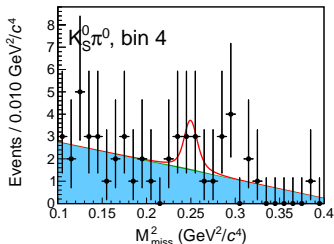
(a) Bin 1 yield:  $7.2^{+4.3}_{-3.5}$



(b) Bin 2 yield:  $39.3^{+8.3}_{-7.3}$



(c) Bin 3 yield:  $64.4^{+9.6}_{-9.0}$



(d) Bin 4 yield:  $4.8^{+3.8}_{-3.0}$

## How to put this all together to determine $c_i$ and $s_i$ ?

- 1 In the past, the strategy has been to measure normalised  $K_i$  first, using flavour tags:

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} \propto K_i, \quad \sum_i K_i = 1$$

- 2 However, the  $K_i$  must be corrected for efficiencies and bin migrations, in addition to Doubly Cabbibo Suppressed decays:

$$f_i = \left( 1 + r_D^2 \frac{K_{-i}}{K_i} - 2\sqrt{\frac{K_{-i}}{K_i}} (c_i \cos(\delta_D) + s_i \sin(\delta_D)) \right)^{-1}$$

- 3 Finally, with the  $K_i$  fixed,  $c_i$  and  $s_i$  are determined from CP and multi-body tags:

$$\begin{aligned} \frac{N_i^{\text{DT}}}{N^{\text{ST}}} &\propto K_i + K_{-i} \mp 2\sqrt{K_i K_{-i}} c_i \\ \frac{N_{ij}^{\text{DT}}}{N^{\text{ST}}} &\propto K_i K'_{-j} + K_{-i} K'_j - 2\sqrt{K_i K_{-i} K'_j K'_{-j}} (c_i c'_j + s_i s'_j) \end{aligned}$$

We propose a simpler, but more powerful strategy:

- 1 Treat all  $K_i$ ,  $c_i$  and  $s_i$  as free parameters
- 2 Include the  $D \rightarrow KK\pi\pi$  branching fraction  $\mathcal{B}$  as a free parameter
- 3 Fit flavour,  $CP$  and multi-body tags simultaneously

Master equations:

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B} \epsilon_{ij} \left( K_{-j} + K_j - 2\sqrt{K_j K_{-j}} (c_j \cos(\delta_D) + s_j \sin(\delta_D)) \right)$$

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B} \epsilon_{ij} (K_j + K_{-j} \mp 2\sqrt{K_j K_{-j}} c_j)$$

$$\hat{N}_{ij}^{\text{DT}} = N^{\text{ST}} \mathcal{B} \epsilon_{ijkl} (K_k K'_{-l} + K_{-k} K'_l - 2\sqrt{K_k K_{-k} K'_l K'_{-l}} (c_k c'_l + s_k s'_l))$$

$\epsilon_{ij}$  are combined efficiency and bin migration matrices

The master equations use the free parameters  $\mathcal{B}$ ,  $K_i$ ,  $c_i$  and  $s_i$  to make a prediction  $\hat{N}^{\text{DT}}$  to the measured double tag yields  $N^{\text{DT}}$

## Master equations

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ij} \left( K_{-j} + K_j - 2\sqrt{K_j K_{-j}} (c_j \cos(\delta_D) + s_j \sin(\delta_D)) \right)$$

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ij} (K_j + K_{-j} \mp 2\sqrt{K_j K_{-j}} c_j)$$

$$\hat{N}_{ij}^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ijkl} (K_k K'_{-l} + K_{-k} K'_l - 2\sqrt{K_k K_{-k} K'_l K'_{-l}} (c_k c'_l + s_k s'_l))$$

Ordinarily, we would construct a Gaussian (log)likelihood function  $\Rightarrow$   
Obtain  $\mathcal{B}$ ,  $K_i$ ,  $c_i$  and  $s_i$  by minimising the following function:

$$-\ln(\mathcal{L}) = \frac{1}{2} \sum_{\text{Tag}} \sum_{ij} (V^{-1})_{ij} (N_i^{\text{DT}} - \hat{N}_i^{\text{DT}}) (N_j^{\text{DT}} - \hat{N}_j^{\text{DT}})$$

$$V_{ij} = \rho_{ij} \sigma_i \sigma_j$$

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<sup>1</sup> $\rho$  are correlation coefficients

## Master equations

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ij} \left( K_{-j} + K_j - 2\sqrt{K_j K_{-j}} (c_j \cos(\delta_D) + s_j \sin(\delta_D)) \right)$$

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ij} (K_j + K_{-j} \mp 2\sqrt{K_j K_{-j}} c_j)$$

$$\hat{N}_{ij}^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ijkl} (K_k K'_{-l} + K_{-k} K'_l - 2\sqrt{K_k K_{-k} K'_l K'_{-l}} (c_k c'_l + s_k s'_l))$$

Our DT yields are very small, so their uncertainties are asymmetric  $\implies$   
 Approximate covariance matrix from the asymmetric uncertainties<sup>2</sup>:

$$-\ln(\mathcal{L}) = \frac{1}{2} \sum_{\text{Tag}} \sum_{ij} (V^{-1})_{ij} (N_i^{\text{DT}} - \hat{N}_i^{\text{DT}}) (N_j^{\text{DT}} - \hat{N}_j^{\text{DT}})$$

$$V_{ij} = \rho_{ij} \sigma_i \sigma_j, \quad \sigma = \sqrt{\sigma_- \sigma_+ - (\sigma_+ - \sigma_-)(N^{\text{DT}} - \hat{N}^{\text{DT}})}$$

<sup>2</sup>[arXiv:physics/0406120](https://arxiv.org/abs/physics/0406120)

$$-\ln(\mathcal{L}) = \frac{1}{2} \sum_{\text{Tag}} \sum_{ij} (V^{-1})_{ij} (N_i^{\text{DT}} - \hat{N}_i^{\text{DT}})(N_j^{\text{DT}} - \hat{N}_j^{\text{DT}})$$

$$V_{ij} = \rho_{ij} \sigma_i \sigma_j, \quad \sigma = \sqrt{\sigma_- \sigma_+ - (\sigma_+ - \sigma_-)(N^{\text{DT}} - \hat{N}^{\text{DT}})}$$

- The above likelihood has good coverage for flavour and  $CP$  tags...
- ... but not for multi-body decays
  - Bins with  $\sigma_- \approx 0$  make the fit unstable
  - Fit convergence was found to be less than 60%
- In multi-body decays, use the full unbinned likelihood directly
  - Fit convergence improves to over 95%
  - Much slower, but much more accurate

## One last technical detail...

- 8  $K_i$  parameters, but  $\sum_i K_i = 1$ , so only 7 are independent
- We could set  $K_4 = 1 - \sum_{i \neq 4} K_i$ , but such a parameterisation is unstable due to strong correlations
- Use a recursive fraction parameterisation ([JHEP 2021 169 \(2021\)](#))
- Recursive fractions  $R_i$  are defined as:

$$R_i \equiv \begin{cases} K_i, & i = -4 \\ K_i / \sum_{j \geq i} K_j, & -4 < i < +4 \\ 1, & i = +4. \end{cases}$$

# Parameterisation of $K_i$

Visualisation of this parameterisation:

## 1. Definition of $c'_1$

$$\underbrace{c_1}_{\equiv c'_1} + \underbrace{c_2 + c_3 + \dots}_{\equiv 1 - c'_1} = 1$$

## 2. Eliminate $c_1$

$$c_2 + c_3 + c_4 + \dots = 1 - c'_1$$

## 3. Definition of $c'_2$

$$\underbrace{\frac{c_2}{1 - c'_1}}_{\equiv c'_2} + \underbrace{\frac{c_3 + c_4 + \dots}{1 - c'_1}}_{\equiv 1 - c'_2} = 1$$

Repeat this procedure until the last coefficient, which is 1



# Input-output checks

Input-output checks are performed by generating toy datasets

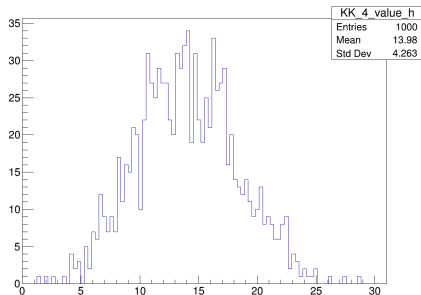
- 1 Check fit convergence
- 2 Check error coverage
- 3 Correct any biases in fitted parameters

Unfortunately, in this analysis we cannot simply generate Poisson-distributed DT yields:

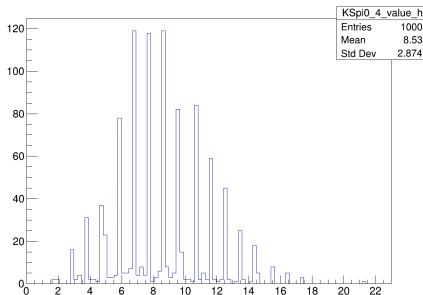
- 1 Asymmetric uncertainties
- 2 Large background-to-signal
- 3 Multi-body tags with low yields require a full unbinned likelihood

Solution: Generate toy datasets for each double tag fit

# Input-output checks



(a) Input yield: 13.9

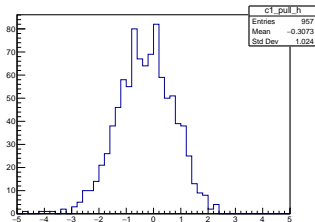


(b) Input yield: 8.6

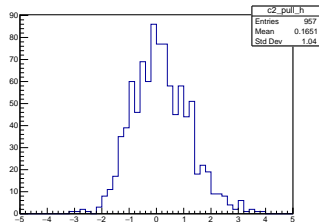
**Figure 12:** Fitted yields in toy datasets for the (left)  $KK$  and (right)  $K_S\pi^0$  tags

- 1 No biases are observed
- 2 Distributions are asymmetric  $\implies$  uncertainties are asymmetric
- 3  $KK$  uncertainty is non-Poisson because of large backgrounds from  $q\bar{q}$
- 4  $K_S\pi^0$  has small backgrounds, so observed yields Poisson distributed

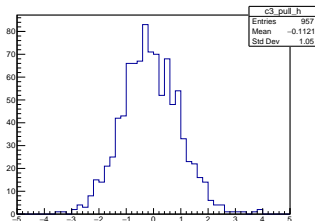
# Input-output checks



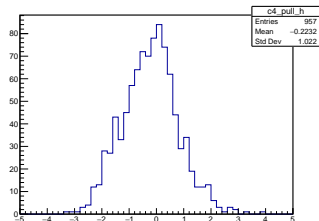
(a)  $c_1$  pulls



(b)  $c_2$  pulls

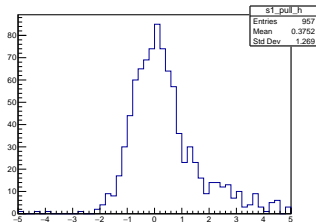


(c)  $c_3$  pulls

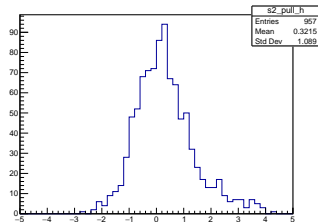


(d)  $c_4$  pulls

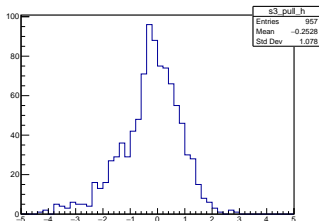
# Input-output checks



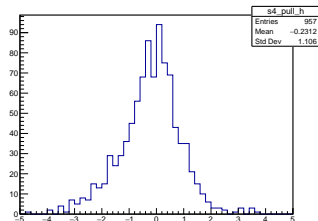
(a)  $s_1$  pulls



(b)  $s_2$  pulls



(c)  $s_3$  pulls



(d)  $s_4$  pulls

## What do the toy fits tell us?

- 1 Both  $c_i$  and  $s_i$  pulls has asymmetric tails
- 2 Effect is small in  $c_i$  and a small bias correction will be sufficient
- 3  $s_i$  has a small overcoverage, but a large tail, so special care is required

# Fit results

$$c_1 = -0.40 \pm 0.13$$

$$s_1 = -0.18 \pm 0.32$$

$$c_2 = 0.79 \pm 0.06$$

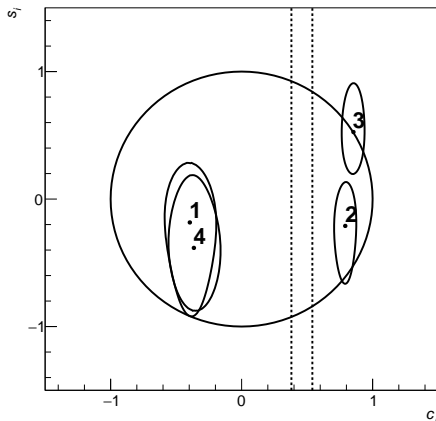
$$s_2 = -0.21 \pm 0.24$$

$$c_3 = 0.85 \pm 0.06$$

$$s_3 = 0.53 \pm 0.24$$

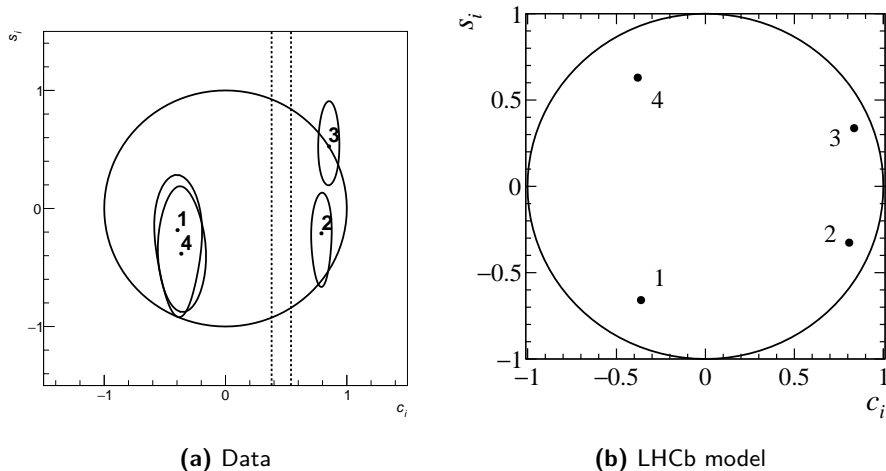
$$c_4 = -0.36 \pm 0.13$$

$$s_4 = -0.38 \pm 0.31$$



**Figure 15:** Contours of  $c_i$  vs  $s_i$ , corresponding to  $\Delta \log(\mathcal{L}) = 2.30$ , or 68% confidence level. Dashed lines show  $F_+$  measurement.

# Fit results



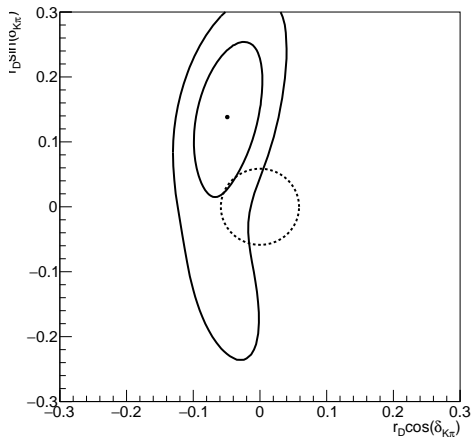
**Figure 16:** Comparison between model and model-independent measurements

- $K_i$ , which is constrained by flavour tags, are free parameters in the fit
- Corrections for DCS decays, which depend on the strong phases  $\delta_D$ , are part of the fit
- We could instead treat  $\delta_D$  as a free parameter, and make a simultaneous measurement
- In this analysis we can measure  $\delta_{K\pi}$  with negligible reduction in sensitivity to  $c_i$  and  $s_i$

$$\hat{N}_i^{\text{DT}} = N^{\text{ST}} \mathcal{B}_{\epsilon ij} \left( K_{-j} + K_j - 2\sqrt{K_j K_{-j}} (c_j \cos(\delta_D) + s_j \sin(\delta_D)) \right)$$

- Free parameters:  $r_D \cos(\delta_{K\pi})$  and  $r_D \sin(\delta_{K\pi})$





**Figure 17:** Contours of  $r_D \cos(\delta_{K\pi})$  vs  $r_D \sin(\delta_{K\pi})$ , corresponding to  $\Delta \log(\mathcal{L}) = 2.30$  and  $6.18$ , or 68% and 95% confidence level. Dashed line indicates measured value of  $r_D$ .

# Branching fraction measurement

In addition, we have another nuisance parameter: The  $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$  branching fraction

Current PDG value:

$$\mathcal{B} = (2.47 \pm 0.11) \times 10^{-3}$$

Fit result:

$$\mathcal{B} = (2.765 \pm 0.046) \times 10^{-3}$$

Much better precision than the current world average!

Do we have the necessary estimates of tracking and PID systematics to also publish this measurement?

# Summary

- A phase-space binned measurement of the  $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$  strong-phases has been performed
  - Analysis uses a  $2 \times 4$  binning scheme
  - Measurement will improve significantly with full  $20 \text{ fb}^{-1}$  dataset
  - New strategy: Treat  $c_i$ ,  $s_i$  and  $K_i$  on an equal footing
  - Additionally,  $\delta_D^{K\pi}$  can also be determined
  - The  $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$  branching fraction more than 2 times more precise than the current PDG value
- Next steps:
  - 1 Perform systematics studies
  - 2 Write up MEMO

Thank you!