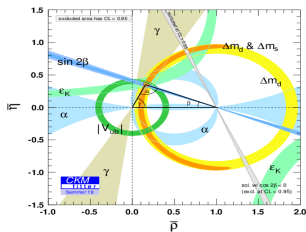


# CKM angle $\gamma$ determination in $B^\pm \rightarrow DK^\pm$ , $D \rightarrow K^+ K^- \pi^+ \pi^-$ decays

Martin Tat

Oxford LHCb

22nd June 2021



# Outline

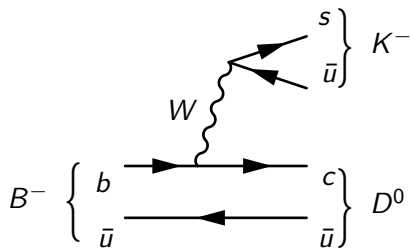
- 1  $\gamma$  and the unitary triangle
- 2 Motivation for the  $D \rightarrow K^+ K^- \pi^+ \pi^-$  decay mode
- 3 Binning scheme and binned fit of  $D \rightarrow K^+ K^- \pi^+ \pi^-$
- 4 Global mass fit
- 5 Binned CP fit
- 6 Strong-phase inputs from quantum-correlated  $D^0 \bar{D}^0$  pairs
- 7 Summary and next steps

# $\gamma$ and the unitary triangle

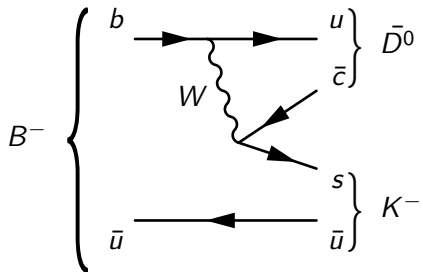
How to measure  $\gamma$ ?



# How to measure $\gamma$ ?



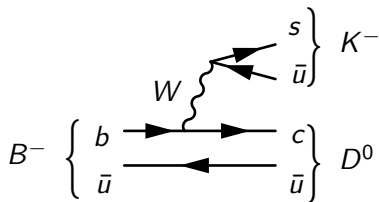
(a)  $B^- \rightarrow D^0 K^-$



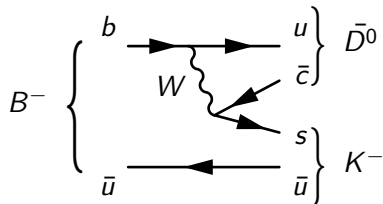
(b)  $B^- \rightarrow \bar{D}^0 K^-$  (colour suppressed)

- Need  $b \rightarrow c\bar{u}s$  and  $b \rightarrow u\bar{c}s$  interference, such as  $B^\pm \rightarrow DK^\pm$ 
  - $D$ : Superposition of  $D^0$  and  $\bar{D}^0$
- Interference when  $D^0$  and  $\bar{D}^0$  decay into a common final state
- Single most precise measurement ( $D \rightarrow K_S^0 h^+ h^-$ ):  $\gamma = (68.7^{+5.2}_{-5.1})^\circ$   
[JHEP 02 \(2021\) 169](#)

# Simplified $\gamma$ measurement



(a)  $B^- \rightarrow D^0 K^-$



(b)  $B^- \rightarrow \bar{D}^0 K^-$  (colour suppressed)

- Decay amplitudes:

- $\mathcal{A}(B^- \rightarrow DK^-) = \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D}^0)$
- $\mathcal{A}(B^+ \rightarrow DK^+) = \mathcal{A}(\bar{D}^0) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0)$

- $\mathcal{A}(D^0)$ - $\mathcal{A}(\bar{D}^0)$  strong phase difference varies throughout phase space

- Two approaches:

- 1 Predict  $\mathcal{A}(D)$  using an amplitude model
- 2 Split phase space into bins and use external strong-phase inputs

# Motivation for the $D \rightarrow K^+ K^- \pi^+ \pi^-$ decay mode

The need for an efficient binning scheme

# Motivation for the $D \rightarrow K^+ K^- \pi^+ \pi^-$ decay mode

- Proposed by G. Wilkinson, J. Rademacker [Phys. Lett. B, 647\(2007\)](#)
  - Estimated  $\gamma$  precision:  $14^\circ$  with 1000 events
- Why this mode, and why now?
  - 1 Estimate 2000 candidates from LHCb Run 1+2
  - 2 Model-independent analysis reduces systematic uncertainties
  - 3 Much more data from BESIII during 2022-2023 for strong-phase inputs
  - 4 Estimate 2000 candidates from LHCb Run 1+2
  - 5 New LHCb amplitude model [JHEP 02 \(2019\) 126](#)
  - 6 New era of 4-body  $\gamma$  measurements
    - $D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$  by Belle [JHEP 10 \(2019\) 178](#)
    - Ongoing analysis of  $D \rightarrow K^+ \pi^- \pi^+ \pi^-$  at LHCb



# Binned fit of $D \rightarrow K^+ K^- \pi^+ \pi^-$

- Decay amplitudes:

- $\mathcal{A}(B^- \rightarrow DK^-) = \mathcal{A}(D^0) + r_B e^{i(\delta_B - \gamma)} \mathcal{A}(\bar{D}^0)$

- $\mathcal{A}(B^+ \rightarrow DK^+) = \mathcal{A}(\bar{D}^0) + r_B e^{i(\delta_B + \gamma)} \mathcal{A}(D^0)$

- Split into bins  $-i, \dots, -1, +1, \dots, +i$  and integrate over phase space:

- $N_i^- = h_{B^-} \left( K_i + (x_-^2 + y_-^2) \bar{K}_i + 2\sqrt{K_i \bar{K}_i} (x_- c_i + y_- s_i) \right)$

- $N_{-i}^+ = h_{B^+} \left( K_i + (x_+^2 + y_+^2) \bar{K}_i + 2\sqrt{K_i \bar{K}_i} (x_+ c_i + y_+ s_i) \right)$

- Fit to extract  $x_{\pm}$  and  $y_{\pm} \implies$  Interpret in terms of  $\gamma$ ,  $r_B$ ,  $\delta_B$

## CP-violating observables

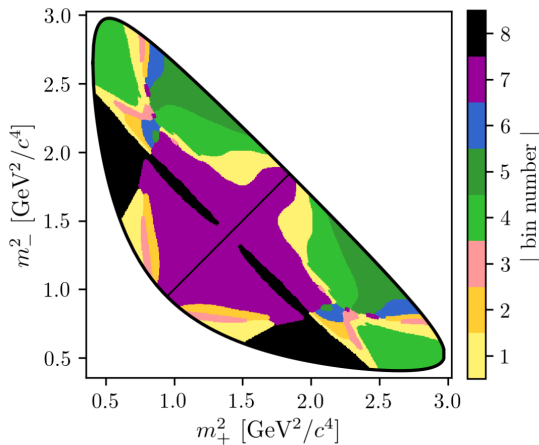
$$x_{\pm} = r_B \cos(\delta_B \pm \gamma), \quad y_{\pm} = r_B \sin(\delta_B \pm \gamma)$$

## External strong-phase input

$c_i, s_i$ : Amplitude-averaged strong phase difference of  $D$  decay

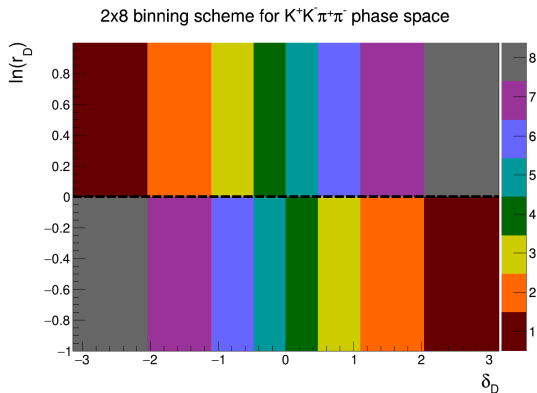
# Binning scheme

- Aim: Maximize interference  $\implies$  Enhance  $x_{\pm}$  and  $y_{\pm}$  sensitivity
- Analogy:  $K_S\pi^+\pi^-$  Dalitz analysis



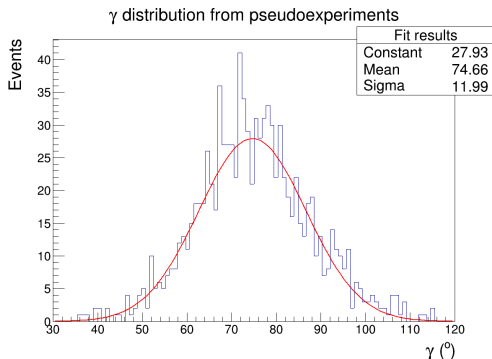
# Binning scheme

- What to do with 5D phase space?
  - Evaluate amplitudes of each event using the LHCb model
  - Calculate  $\mathcal{A}(D^0)/\mathcal{A}(\bar{D}^0) = r_D \exp(i\delta_D)$
  - Effectively reduces 5D  $\rightarrow$  2D



# Pull study

- Generate 1000 toy datasets using LHCb amplitude model
- Fit for  $\gamma$  on each dataset



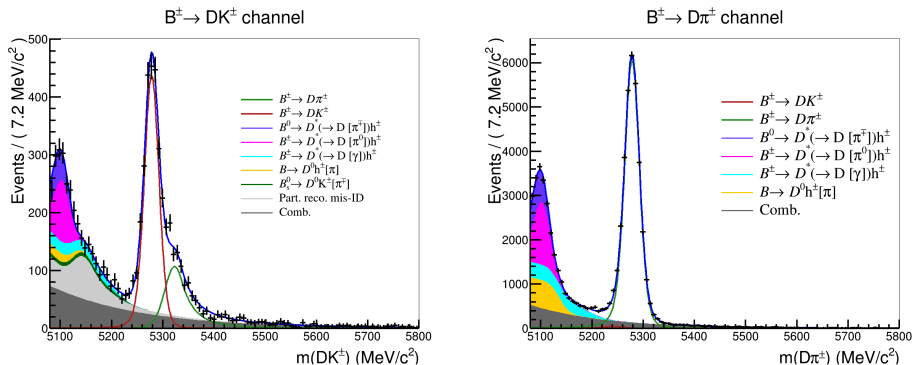
**Figure 3:**  $\gamma$  distribution

Achieved  $\gamma$  precision of  $\sigma(\gamma) = 12^{\circ}$

## Global mass fit

# Global mass fit

- Fit all  $B^\pm \rightarrow (K^+ K^- \pi^+ \pi^-)_D h^\pm$  candidates
- Fix overall signal yield and PDF shape parameters for binned CP fit

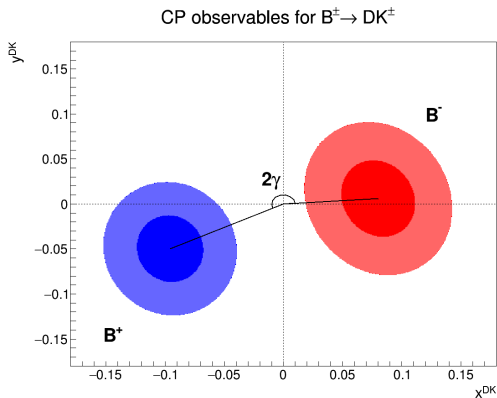


**Figure 4:** Signal yields are  $2290 \pm 59$  (left) and  $33\,113 \pm 211$  (right)

## Binned CP fit

# Global mass fit

- Strong-phase inputs are taken from LHCb amplitude model for now
- Generated 1000 toy datasets  $\implies$  No biases in CP observables!



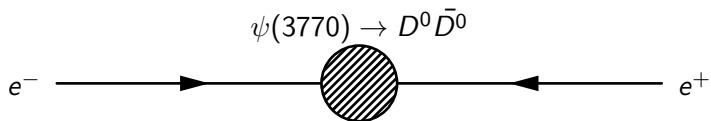
**Figure 5:** Confidence intervals for fitted CP observables  $x_\pm$  and  $y_\pm$



# Strong-phase inputs from quantum-correlated $D^0\bar{D}^0$ pairs

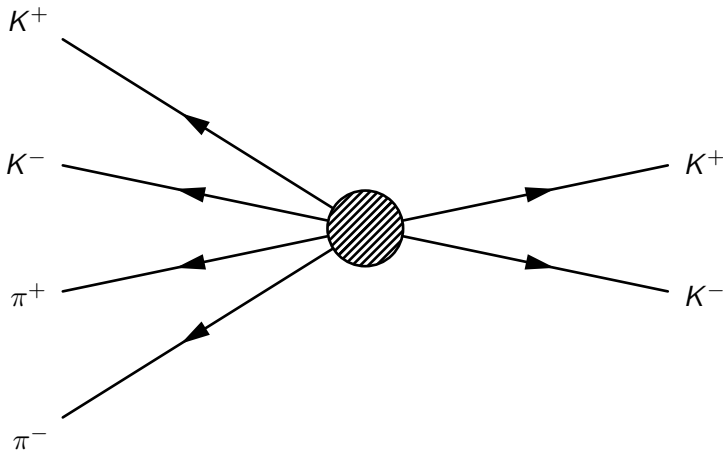
# BESIII double tag analysis

BESIII is a charm factory:  $e^+e^- \rightarrow \psi(3770) \rightarrow D^0\bar{D}^0$



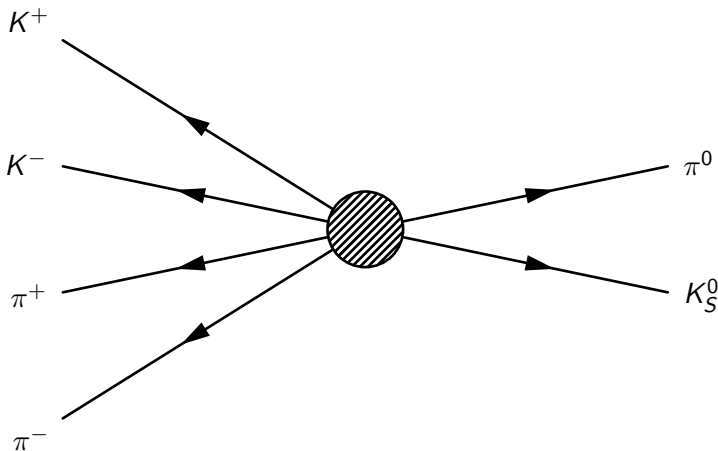
# BESIII double tag analysis

Double tagged signal ( $K^+K^- \pi^+ \pi^-$ ) with known CP even tag ( $K^+K^-$ )



# BESIII double tag analysis

Double tagged signal ( $K^+K^-\pi^+\pi^-$ ) with known CP odd tag ( $K_S^0\pi^0$ )

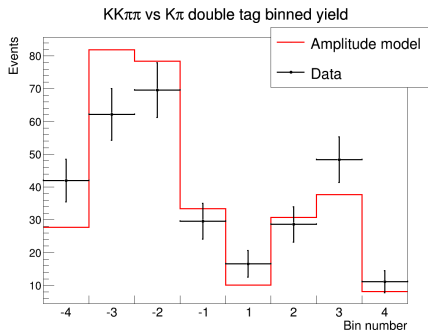


# Double tag method

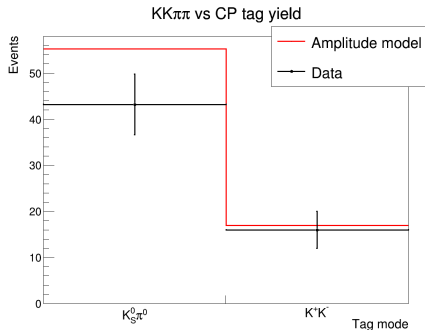
- Signal decay  $D \rightarrow K^+ K^- \pi^+ \pi^-$  is correlated with the tag decay mode
- “Spooky action at a distance”!
- Double-tag yield of CP even tag:
  - $N_i = h(K_i - 2c_i \sqrt{K_i \bar{K}_i} + \bar{K}_i)$
- Double-tag yield of CP odd tag:
  - $N_i = h(K_i + 2c_i \sqrt{K_i \bar{K}_i} + \bar{K}_i)$

# Double tag yields

- Current  $3 \text{ fb}^{-1}$  insufficient, expect  $20 \text{ fb}^{-1}$  by end of 2023
- For now, simply compare double tag yields with expectation from LHCb model



(a) KK $\pi\pi$  vs K $\pi$  (flavour tag)



(b) KK $\pi\pi$  vs KK,  $K_S^0 \pi^0$  (CP tags)

# Summary and next steps

## Summary:

- LHCb: Model-independent binned  $\gamma$  analysis looks promising
- BESIII: Initial double tag yields of BESIII data look consistent

## Next steps:

- LHCb: Ensure peaking backgrounds are under control and study systematic uncertainties
- BESIII: Finalize double tag yield for all tag modes

Thank you!

# Backup: Analytical expressions

- $c_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D}^0)| \cos(\delta_D)}{\sqrt{\int_i d\Phi |\mathcal{A}(D^0)|^2 \int_i d\Phi |\mathcal{A}(\bar{D}^0)|^2}}$
- $s_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)| |\mathcal{A}(\bar{D}^0)| \sin(\delta_D)}{\sqrt{\int_i d\Phi |\mathcal{A}(D^0)|^2 \int_i d\Phi |\mathcal{A}(\bar{D}^0)|^2}}$
- $K_i = \frac{\int_i d\Phi |\mathcal{A}(D^0)|^2}{\sum_j \int_j d\Phi |\mathcal{A}(D^0)|^2}$



## Backup: Optimize bin widths

- Optimize  $x_{\pm}$ ,  $y_{\pm}$  sensitivity
- Vary bin edges, keep symmetric around  $\delta_D = 0$

### Binning $Q$ value

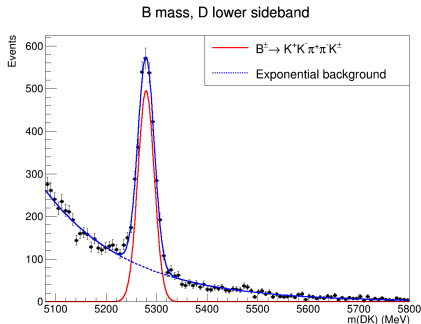
$$Q^2 = 1 - \sum_i \frac{K_i \bar{K}_i (1 - c_i^2 - s_i^2)}{N_i} \bigg/ \sum_i K_i$$

$$Q^2 \approx \sum_i N_i (c_i^2 + s_i^2) \bigg/ \sum_i N_i \text{ if } r_B = 0$$

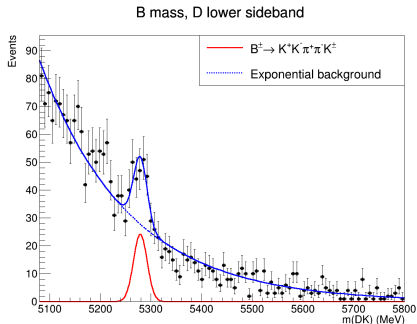
- Can achieve  $Q \approx 0.90$  with 8 bins  $\implies$  expect  $\sigma(\gamma) = 12^\circ$

# Backup: Charmless backgrounds

- Study the  $D$  mass sideband to estimate yield of charmless background



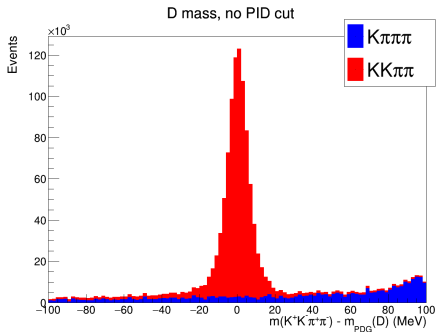
(a) No flight significance cut



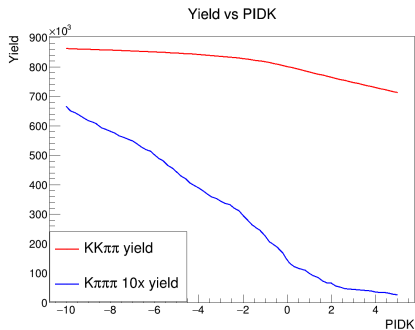
(b) Flight significance cut at 2

# Backup: $K\pi\pi\pi$ background

- Use MC samples to study contamination of  $D \rightarrow K\pi\pi\pi$  under the signal



**(a)**  $D$  mass spectrum of the signal  $KK\pi\pi$  and background  $K\pi\pi\pi$ .



**(b)** Yield of signal  $KK\pi\pi$  and background  $K\pi\pi\pi$  as a function of PID cut.