

# Model-independent measurement of the CKM angle $\gamma$ with $B^\pm \rightarrow [K^+ K^- \pi^+ \pi^-]_D K^\pm$ at LHCb and BESIII

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IOP Joint APP and HEPP Conference

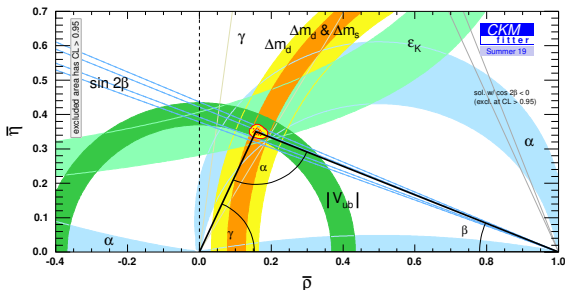
3rd-5th April 2023



## Introduction to $\gamma$ and $CP$ violation

# Introduction to $\gamma$ and $CP$ violation

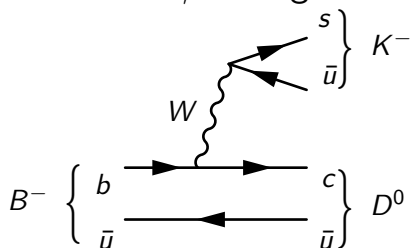
- CPV in SM is described by the Unitary Triangle, with angles  $\alpha$ ,  $\beta$ ,  $\gamma$
- The angle  $\gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$  is very important:
  - 1 Negligible theoretical uncertainties: Ideal SM benchmark
  - 2 Accessible at tree level: Indirectly probe New Physics that enter loops
  - 3 Compare with  $\alpha$ ,  $\beta$  measurements: Is the Unitary Triangle a triangle?



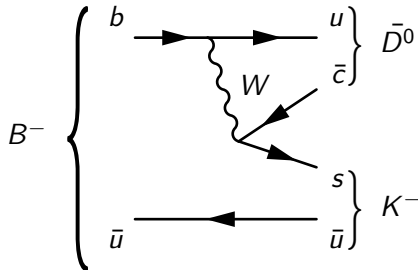
CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005)

# Sensitivity through interference

Measure  $\gamma$  through interference effects in  $B^\pm \rightarrow DK^\pm$



Favoured  $B^- \rightarrow D^0 K^-$



Suppressed  $B^- \rightarrow \bar{D}^0 K^-$

- Superposition of  $D^0$  and  $\bar{D}^0$ 
  - Consider  $D^0/\bar{D}^0$  decays to the same final state, such as  $D \rightarrow K^+ K^-$
- $b \rightarrow u\bar{c}s$  and  $b \rightarrow c\bar{u}s$  interference  $\rightarrow$  Sensitivity to  $\gamma$

$$\mathcal{A}(B^-) = \mathcal{A}_B \left( \mathcal{A}_{D^0} + r_B e^{i(\delta_B - \gamma)} \mathcal{A}_{\bar{D}^0} \right)$$

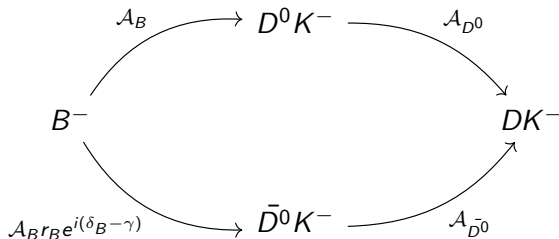
$$\mathcal{A}(B^+) = \mathcal{A}_B \left( \mathcal{A}_{\bar{D}^0} + r_B e^{i(\delta_B + \gamma)} \mathcal{A}_{D^0} \right)$$

- The magnitude of interference effects governed by  $r_B \approx 0.1$

# Sensitivity through interference

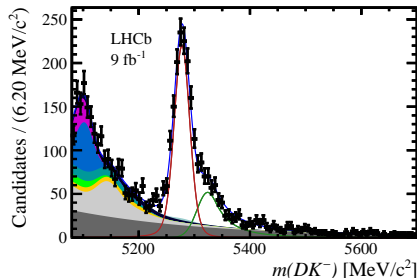
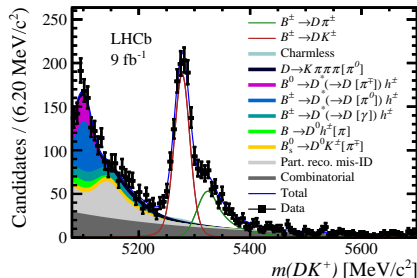
This talk: Focus on multi-body  $D$  decays, where interference effects vary across phase space

- First, consider a phase-space integrated analysis
- Compare yields of  $B^+$  and  $B^-$  and determine the asymmetry
- Interference effects are diluted by  $\kappa$  when integrated over phase space



$$|\mathcal{A}(B^-)|^2 \propto 1 + r_B^2 + 2r_B \kappa \cos(\delta_B - \gamma)$$

# First look at $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D K^\pm$



arXiv:2301.10328

Measuring the  $B^\pm \rightarrow DK^\pm$  asymmetry  $\mathcal{A}$  provide useful constraints on  $\gamma$ , but with some caveats:

- ① Interference effects are diluted by a factor  $\kappa = 0.46 \pm 0.08$ 
  - [Phys. Rev. D \*\*107\*\*, 032009](#)
- ② Four-fold degeneracy:
  - $(\gamma, \delta_B) \rightarrow (\delta_B, \gamma)$
  - $(\gamma, \delta_B) \rightarrow (\pi - \gamma, \pi - \delta_B)$

# Phase-space binned analysis of $B^\pm \rightarrow [K^+ K^- \pi^+ \pi^-]_D K^\pm$

# Phase-space binned analysis of $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D K^\pm$

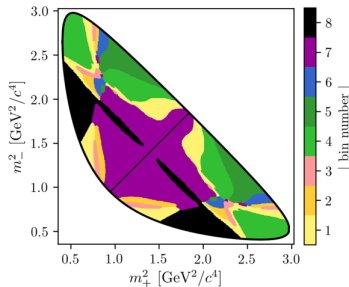
Our aim: First binned model independent measurement of  $\gamma$  in  $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D K^\pm$

- Model dependent measurement first proposed in 2007
  - [Phys. Lett. \*\*B647\*\* \(2007\) 400](#) by J. Rademacker and G. Wilkinson
  - FOCUS amplitude model:  $14^\circ$  precision with 1000 candidates
- State of the art amplitude analysis by LHCb:
  - [JHEP \*\*02\*\* \(2019\) 126](#)
  - Exploits the huge dataset of charm decays collected by LHCb
  - Useful for understanding the 5-dimensional phase space
- Use LHCb model to identify regions with expected large asymmetries
  - Place regions with similar asymmetries together in bins

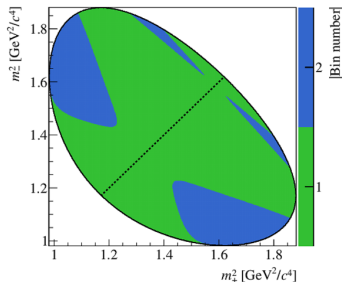


# Phase-space binned analysis of $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D K^\pm$

- Analogous to the decays  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  and  $K_S^0 K^+ K^-$ , where the binning scheme may be visualised on a Dalitz plot



$K_S^0 \pi^+ \pi^-$



$K_S^0 K^+ K^-$

- The strong phase  $\delta_D$  varies across phase space, leading to different asymmetries in each bin
- The amplitude-averaged cosine and sine of  $\delta_D$ ,  $c_i$  and  $s_i$ , are measured directly in bin  $i$  at charm factories, such as BESIII

## Binning scheme

A binning scheme must satisfy the following:

- Minimal dilution of strong phases when integrating over bins
- Enhance interference between  $B^\pm \rightarrow D^0 K^\pm$  and  $B^\pm \rightarrow \bar{D}^0 K^\pm$

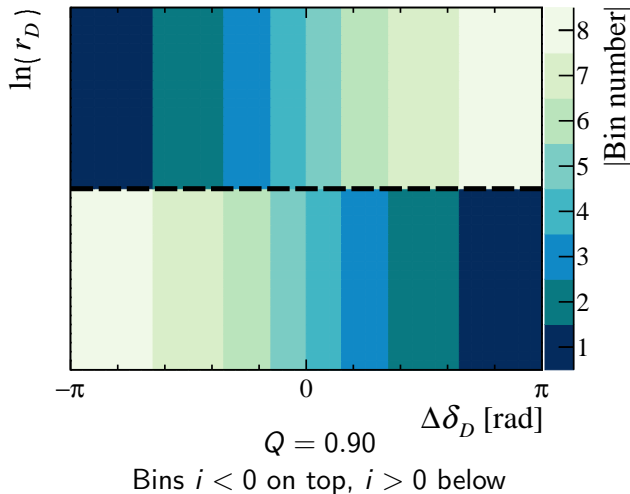
How to bin a 5-dimensional phase space?

- 1 For each  $B^\pm$  candidate, use the amplitude model to calculate

$$\frac{\mathcal{A}(D^0)}{\mathcal{A}(\bar{D}^0)} = r_D e^{i\delta_D}$$

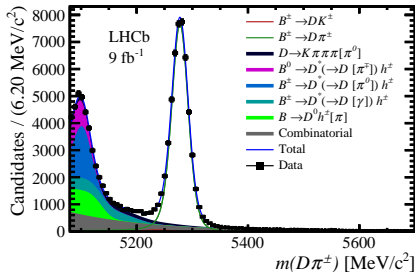
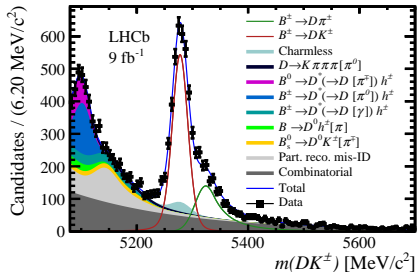
- 2 Split  $\delta_D$  into uniformly spaced bins
- 3 Use the symmetry line  $r_D = 1$  to separate bin  $+i$  from  $-i$
- 4 Optimise the binning scheme by adjusting the bin boundaries in  $\delta_D$

# Binning scheme



# Mass fits, $CP$ fit and $\gamma$

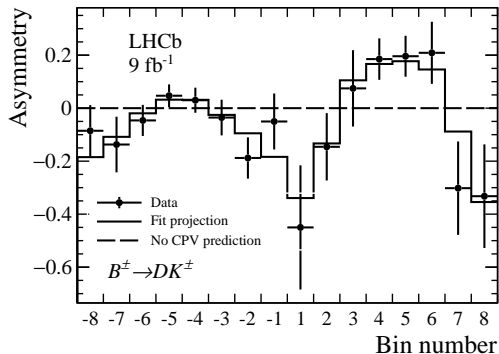
Global invariant mass fit: Fit everything to understand mass shapes and background yields



Signal yield:

$$B^{\pm} \rightarrow DK^{\pm} : 3026 \pm 38$$

$$B^{\pm} \rightarrow D\pi^{\pm} : 44\,349 \pm 218$$



- Clear bin asymmetries are seen, and the non-trivial distribution is driven by the change in strong phases across phase space
- While the interpretation of  $\gamma$  require charm inputs, the observed bin asymmetries are model independent

# Interpretation of $\gamma$

CP fit: Simultaneously fit bin yields and determine physics parameters, using model predictions of  $c_i$  and  $s_i$ :

$$\begin{aligned}\gamma &= (116^{+12}_{-14})^\circ, \\ \delta_B^{DK} &= (81^{+14}_{-13})^\circ, \\ r_B^{DK} &= 0.110^{+0.020}_{-0.020}, \\ \delta_B^{D\pi} &= (298^{+62}_{-118})^\circ, \\ r_B^{D\pi} &= 0.0041^{+0.0054}_{-0.0041},\end{aligned}$$

[arXiv:2301.10328](https://arxiv.org/abs/2301.10328)

However, the latest  $\gamma$  and charm combination result is:

$$\gamma = (63.8^{+3.5}_{-3.7})^\circ$$

Results are compatible at  $3\sigma$ , but could there be some other issue?



CP fit: Simultaneously fit bin yields and determine physics parameters, using model predictions of  $c_i$  and  $s_i$ :

$$\begin{aligned}\gamma &= (116_{-14}^{+12})^\circ, \\ \delta_B^{DK} &= (81_{-13}^{+14})^\circ, \\ r_B^{DK} &= 0.110_{-0.020}^{+0.020}, \\ \delta_B^{D\pi} &= (298_{-118}^{+62})^\circ, \\ r_B^{D\pi} &= 0.0041_{-0.0041}^{+0.0054},\end{aligned}$$

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However, the latest  $\gamma$  and charm combination result is:

$$\gamma = (63.8_{-3.7}^{+3.5})^\circ$$

Do we trust the model predicted  $c_i$  and  $s_i$ , or their uncertainties?

There are several reasons why amplitude models cannot be trusted

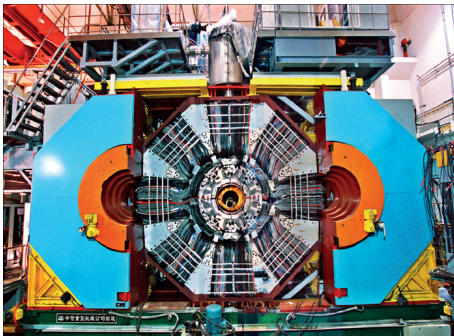
- ① Amplitude models are just models, which may not reflect reality
- ② In fact, the model is fitted to data that knows nothing about  $\delta_D$
- ③ It is impossible to assign an objective error to a model!

We wish to do a model independent measurement  
Let's go and measure  $c_i$  and  $s_i$  at BESIII!

## Strong phase analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ at BESIII

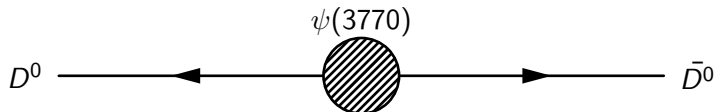
# Strong phase analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ at BESIII

- BESIII: Beijing Spectrometer III, a detector at the Beijing Electron-Positron Collider II, located at IHEP
- $e^+e^-$  collider at the  $\psi(3770) \rightarrow D^0 \bar{D}^0$  threshold
  - 2010-2011:  $3 \text{ fb}^{-1}$
  - 2021-2022:  $5 \text{ fb}^{-1}$
  - 2023-:  $4 \text{ fb}^{-1}$
  - Expect  $20 \text{ fb}^{-1}$  in total by end of 2024

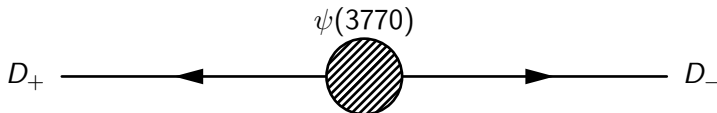


# Strong phase analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ at BESIII

- Double-tag analysis: Reconstruct signal ( $KK\pi\pi$ ) and tag mode
- $D^0 \bar{D}^0$  pair is quantum correlated



- Equivalently, we can consider  $D_+ D_-$ 
  - $D_{\pm} = \frac{1}{\sqrt{2}}(D^0 \pm \bar{D}^0)$  are CP eigenstates

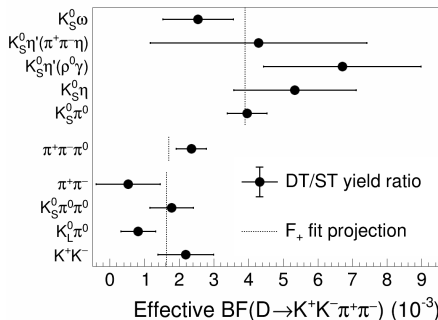


The  $DD$  pair is quantum correlated, spooky action at a distance!

# Strong phase analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ at BESIII

Quantum correlation: The  $CP$  content of the tag can modify the effective branching fraction:

$$\frac{N^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi\pi)(1 \pm c_1)$$



Phys. Rev. D **107**, 032009

$c_1$  is the cosine of the strong phase, averaged over the whole phase space

# Strong phase analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ at BESIII

Our next task is to change the phase-space integrated analysis,

$$\frac{N^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi\pi) \quad (\text{flavour tag})$$

$$\frac{N^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi\pi)(1 \pm c_1) \quad (\text{CP tag})$$

into a binned phase space analysis:

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi\pi)F_i \quad (\text{flavour tag})$$

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi\pi)(F_i + \bar{F}_i \pm 2\sqrt{F_i \bar{F}_i} c_i) \quad (\text{CP tag})$$

- 1  $F_i$ : Measure using flavour tags
- 2  $c_i$ : Determine from asymmetry of  $CP$  even and odd tags
- 3  $s_i$ : Analogous to  $c_i$ , but requires binning of tag mode

# Strong phase analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ at BESIII

Our next task is to change the phase-space integrated analysis,

$$\frac{N^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi\pi) \quad (f')$$

$$\frac{N^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK\pi) \quad (\text{CP tag})$$

into a binned phase analysis:

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0 \rightarrow KK) \quad (\text{flavour tag})$$

$$\frac{N_i^{\text{DT}}}{N^{\text{ST}}} = \mathcal{B}(D^0) (F_i + \bar{F}_i \pm 2\sqrt{F_i \bar{F}_i} c_i) \quad (\text{CP tag})$$

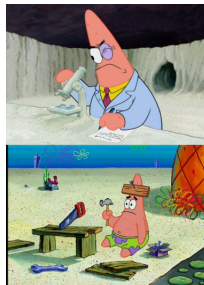
- ①  $F_i$ : Measure using 1. our tags
- ②  $c_i$ : Determine from asymmetry of  $CP$  even and odd tags
- ③  $s_i$ : Analogous to  $c_i$ , but requires binning of tag mode

Work in progress!



# Summary and conclusion

- 1 I have presented the first model-independent measurement of  $\gamma$  using  $B^\pm \rightarrow [K^+ K^- \pi^+ \pi^-]_D K^\pm$
- 2 The optimised binning scheme, developed with an amplitude model, successfully identified regions with large, local  $CP$  asymmetries
- 3 Model predictions of  $\delta_D$  must not be trusted for  $\gamma$  extraction
- 4 LHCb analysis has  $3\sigma$  tension with world average
- 5 External inputs from charm factories, such as BESIII, are crucial to eliminate biases due to modelling



Making binning scheme with amplitude model

Predicting strong phases with amplitude model

Thanks for your attention!

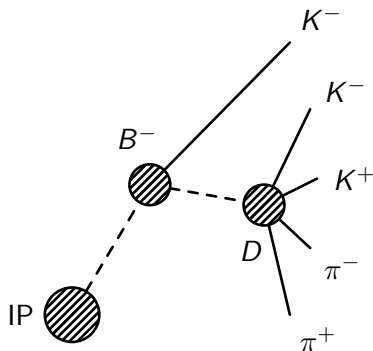
## Backup slides

## Event selection

## Decay topology

Look for:

- 1 5 charged tracks
- 2 Displaced  $B$  vertex
- 3 1 bachelor track with good PID information
- 4 Displaced  $D$  vertex with invariant mass within 25 MeV of the  $D^0$  mass



Offline selection has 3 stages

Initial cuts:

- 1 Invariant  $D$  and  $B$  mass cuts
- 2 Momentum and RICH requirements

Boosted Decision Tree (BDT)

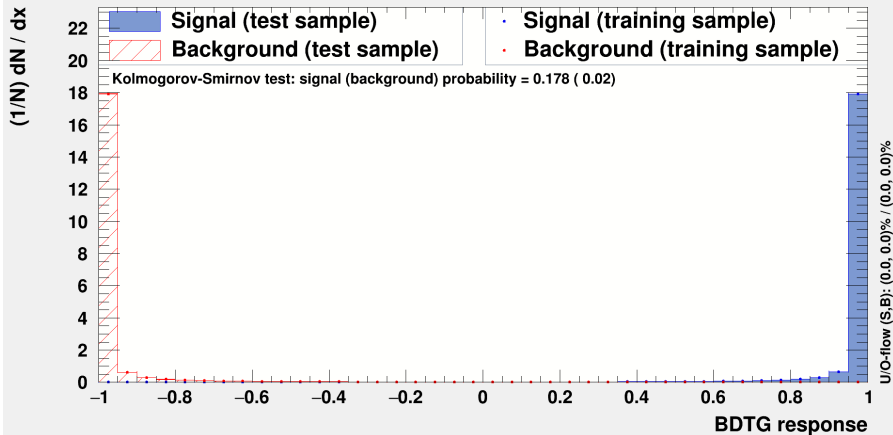
- Signal sample: Simulation samples
- Background sample: Upper  $B$  mass sideband
- 28 variables describing kinematics, impact parameters, vertex quality

Final selection

- 1  $D$  Flight distance
- 2 Particle Identification of bachelor
- 3  $K_S^0$  veto

# Event selection

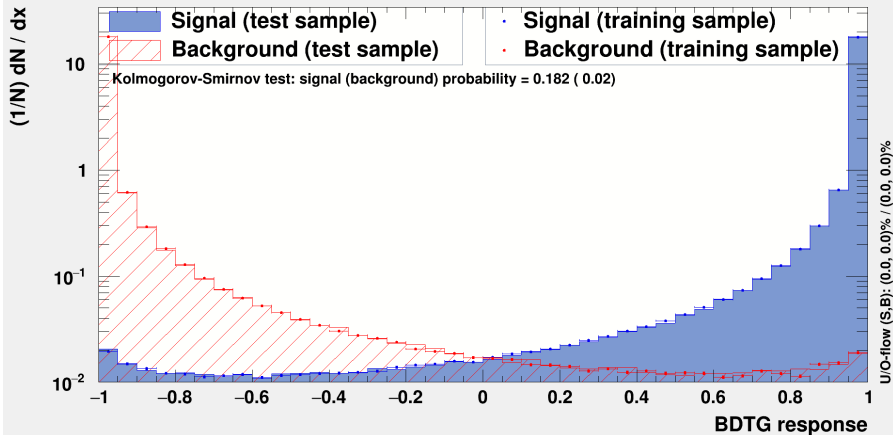
## TMVA overtraining check for classifier: BDTG



BDT is highly efficient at rejecting combinatorial background

# Event selection

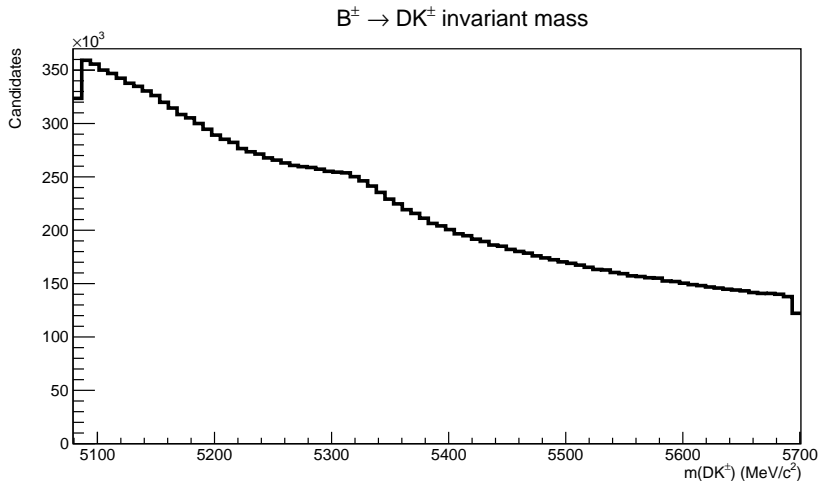
## TMVA overtraining check for classifier: BDTG



Very important, combinatorial background is large in multi-body decays



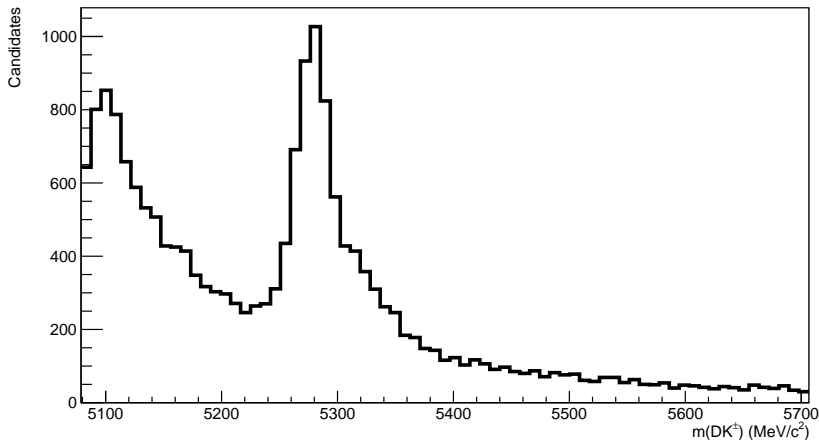
# Event selection



The invariant  $B$  mass, after online selection, show no visible signal...

# Event selection

$B^\pm \rightarrow DK^\pm$  invariant mass



... but the BDT does a great job cleaning this up!