

# Update of $\gamma$ in $B^\pm \rightarrow [K^+ K^- \pi^+ \pi^-]_D h^\pm$ with external strong-phase inputs

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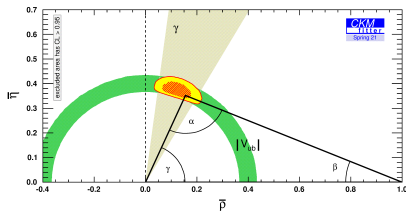
LHCb-UK annual meeting, RAL

8th-10th January 2024

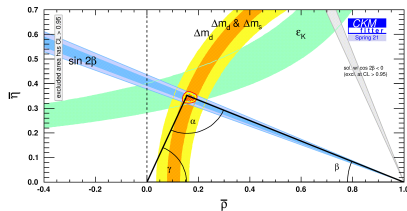


# Introduction to $\gamma$ and $CP$ violation

- CPV in SM is described by the Unitary Triangle, with angles  $\alpha$ ,  $\beta$ ,  $\gamma$
- The angle  $\gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$  is very important:
  - 1 Negligible theoretical uncertainties: Ideal SM benchmark
  - 2 Accessible at tree level: Indirectly probe New Physics that enter loops
  - 3 Compare with a global CKM fit: Is the Unitary Triangle a triangle?



**(a) Tree level:**  $\gamma = (72.1^{+5.4}_{-5.7})^\circ$



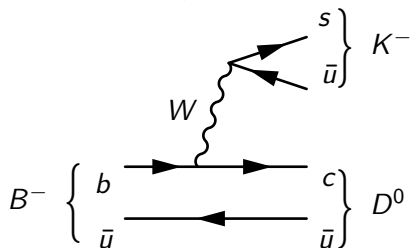
**(b) Loop level:**  $\gamma = (65.5^{+1.1}_{-2.7})^\circ$

CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005), updated results and plots available at:

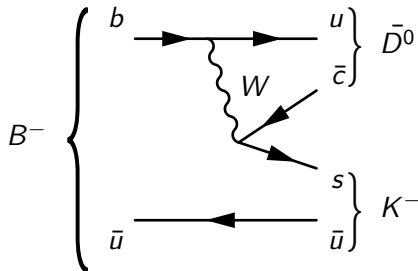
<http://ckmfitter.in2p3.fr>

# Sensitivity through interference

Measure  $\gamma$  through interference effects in  $B^\pm \rightarrow DK^\pm$



Favoured  $B^- \rightarrow D^0 K^-$



Suppressed  $B^- \rightarrow \bar{D}^0 K^-$

- Superposition of  $D^0$  and  $\bar{D}^0$ 
  - Consider  $D^0/\bar{D}^0$  decays to the same final state, such as  $D \rightarrow K^+ K^-$
- $b \rightarrow u\bar{c}s$  and  $b \rightarrow c\bar{u}s$  interference  $\rightarrow$  Sensitivity to  $\gamma$

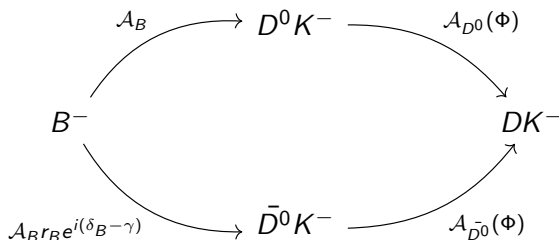
$$\mathcal{A}(B^-) = \mathcal{A}_B \left( \mathcal{A}_{D^0} + r_B e^{i(\delta_B - \gamma)} \mathcal{A}_{\bar{D}^0} \right)$$

$$\mathcal{A}(B^+) = \mathcal{A}_B \left( \mathcal{A}_{\bar{D}^0} + r_B e^{i(\delta_B + \gamma)} \mathcal{A}_{D^0} \right)$$

# Multi-body $D$ decays

This talk: Discuss  $D \rightarrow K^+ K^- \pi^+ \pi^-$ , where interference effects vary across phase space

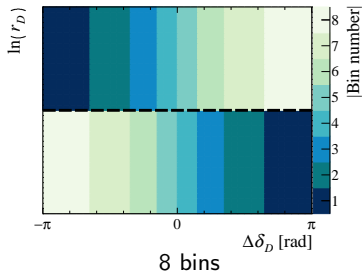
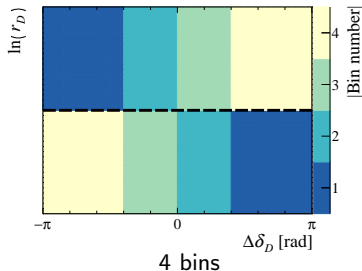
- Strong-phase difference  $\delta_D$  is a function of phase space
- Compare yields of  $B^+$  and  $B^-$  and determine the asymmetry in local phase space regions



$$|\mathcal{A}(B^-)|^2 \propto |\mathcal{A}_{D^0}(\Phi)|^2 + r_B^2 |\mathcal{A}_{\bar{D}^0}(\Phi)|^2 + 2r_B |\mathcal{A}_{D^0}(\Phi)| |\mathcal{A}_{\bar{D}^0}(\Phi)| \cos(\delta_B - \gamma + \delta_D)$$

# Multi-body $D$ decays

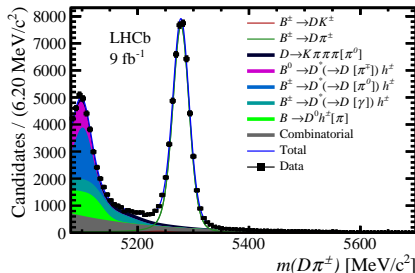
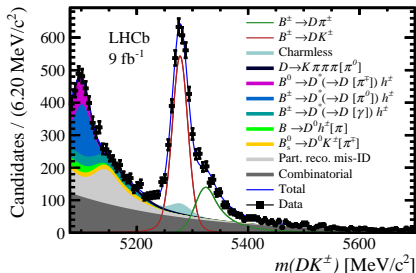
- Interpretation of  $\gamma$  from the multi-body charm decays require external inputs of the charm strong-phase differences
- Measure model-independent strong-phases at a charm factory, such as BESIII, using an optimised binning scheme



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# Phase-space binned $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D K^\pm$

Fully charged final state  $\implies$  Highly suitable for LHCb



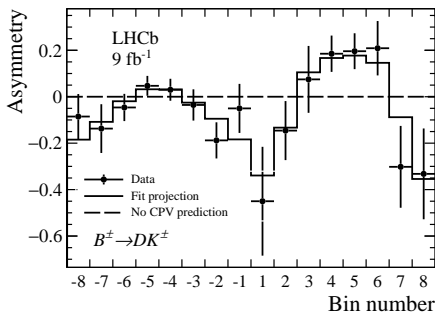
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- $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D h^\pm$  signal yield:
  - $B^\pm \rightarrow DK^\pm$ :  $3026 \pm 38$
  - $B^\pm \rightarrow D\pi^\pm$ :  $44349 \pm 218$

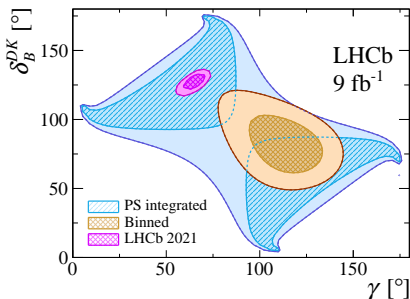
# Phase-space binned $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D K^\pm$

From the phase-space binned asymmetries, we obtain:

$$\gamma = (116^{+12}_{-14})^\circ$$



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How will this evolve with model-independent BESIII inputs?

## Key free parameters in the fit:

- $\gamma$  (obviously)
- $r_B, \delta_B$ : Hadronic parameters of  $B^\pm \rightarrow DK^\pm$
- $c_i, s_i$ : Charm strong-phase parameters

$B^\pm \rightarrow DK^\pm$  yield in bin  $i$

$$\hat{N}_{\pm i}^\pm = h_{B^\pm} \left( F_i + r_B^2 F_{+i} + 2r_B \sqrt{F_+ F_{-i}} (\cos(\delta_B \pm \gamma) c_i - \sin(\delta_B \pm \gamma) s_i) \right)$$

In principle straightforward: Fit  $B^\pm$  yields and extract  $\gamma$   
Reduce binning to  $2 \times 4$  bins to accommodate BESIII statistics



## Cross check: Model-dependent fit of $\gamma$

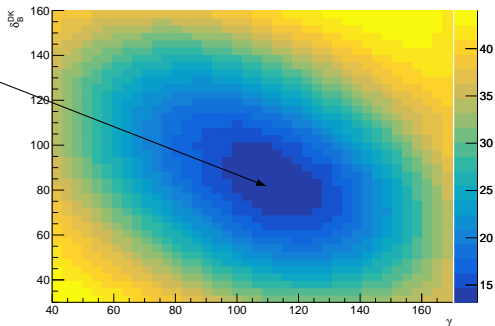
Construct log-likelihood function using  $B^\pm \rightarrow DK^\pm$  yields and model-predicted  $c_i$  and  $s_i$ :

$$\mathcal{L} = \frac{1}{2} \sum_i \left( \frac{N_i - \hat{N}_i}{\sigma_i} \right)^2$$

Simultaneous LHCb and BESIII fit

Fit result:  
 $\gamma = (112 \pm 13)^\circ$

Consistent with  
 $2 \times 8$  bins ✓



To include the effect of  $c_i$  and  $s_i$  from the BESIII measurement, perform a simultaneous fit:

$$\mathcal{L} = \frac{1}{2} \sum_i \left( \frac{N_i - \hat{N}_i}{\sigma_i} \right)^2 + \mathcal{L}_{BESIII}$$

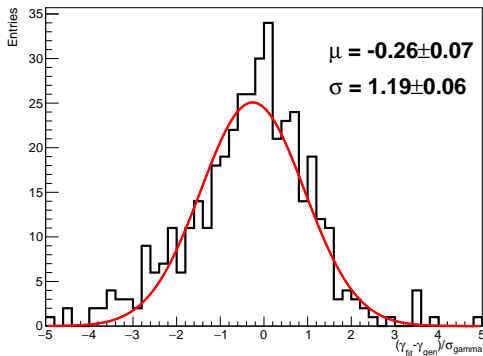
Why not simply assign a systematic uncertainty?

- 1 Contribution of  $\gamma$  uncertainty from BESIII could be large, and may move the central value of  $\gamma$
- 2 Uncertainties of  $s_i$  are expected to be very non-Gaussian, which could propagate into non-Gaussian uncertainties of  $\gamma$

# Simultaneous fit of LHCb and BESIII bin yields

Run toys using expected BESIII yields and bin yields from  
 $B^\pm \rightarrow [K^+ K^- \pi^+ \pi^-]_D h^\pm$  paper:

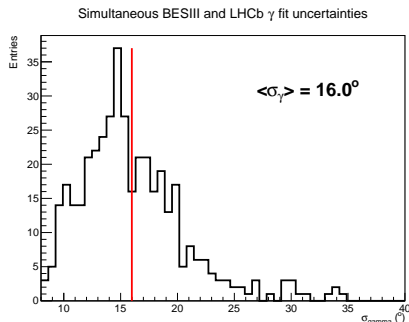
Simultaneous BESIII and LHCb  $\gamma$  fit pulls



Stable fit with minimal bias and small undercoverage

# Simultaneous fit of LHCb and BESIII bin yields

Study expected  $\gamma$  uncertainty, after correcting for coverage:

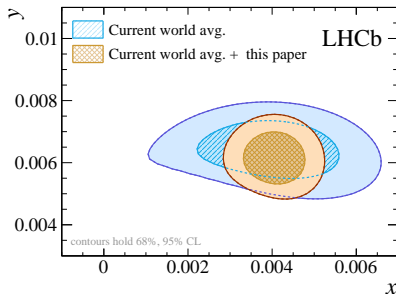
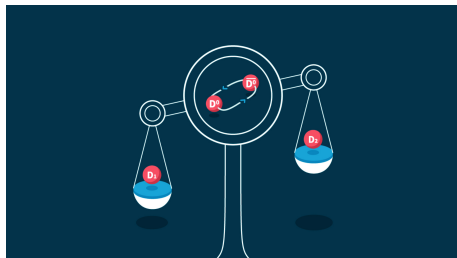


Conclusion from toy studies:

- 1 Well behaved fit, with expected sensitivity of  $\sigma(\gamma) = 16^{\circ}$
- 2 Only small corrections to bias and coverage required
- 3 Will update  $\gamma$  result once BESIII measurement is released

# Charm mixing studies with multi-body decays

The non-zero mass difference between  $D^0$  and  $\bar{D}^0$  was measured using the multi-body decay  $D \rightarrow K_S^0 \pi^+ \pi^-$



Phys. Rev. Lett **127**, 111801 (2021)

Charm strong-phase differences were crucial for this measurement!

# Charm mixing studies with multi-body decays

Mixing equations depend on  $x$  and  $y$ , but also  $c_i$  and  $s_i$ :

## 1. Charm mixing equations

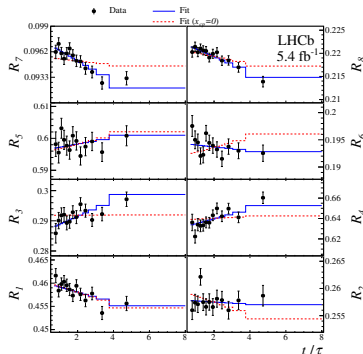
$$N_{D^0}(+i, \langle t \rangle_j) = K_{+i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (yc_i + xs_i)$$

$$N_{D^0}(-i, \langle t \rangle_j) = K_{-i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (yc_i - xs_i)$$

- 1 Fit the mixing equations
- 2 Fit the ratio of mixing equations

## 2. Charm mixing ratio (bin-flip)

$$R_i = \frac{K_{+i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (yc_i + xs_i)}{K_{-i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (yc_i - xs_i)}$$



# Charm mixing studies with multi-body decays

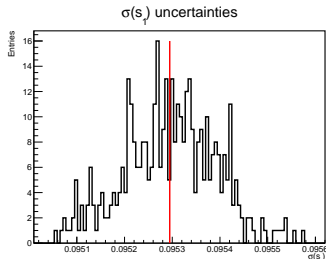
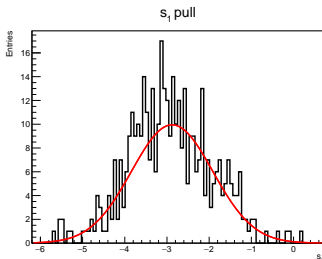
Alternative strategy: Fix  $x$  and  $y$ , and measure  $c_i$  and  $s_i$

## 1. Charm mixing equations

$$N_{D^0}(+i, \langle t \rangle_j) = K_{+i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (yc_i + xs_i)$$

$$N_{D^0}(-i, \langle t \rangle_j) = K_{-i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (yc_i - xs_i)$$

- Two independent equations per bin, two observables per bin
- Similar statistical sensitivity to  $c_i$  and  $s_i$ , in contrast to BESIII



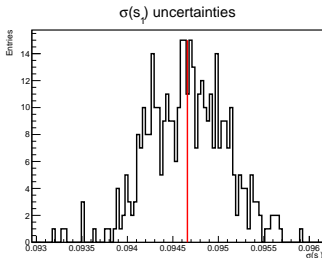
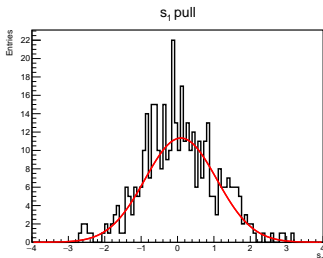
# Charm mixing studies with multi-body decays

Can also use bin-flip method to fit  $s_i$ , but  $c_i$  must be fixed

## 2. Charm mixing ratio (bin-flip)

$$R_i = \frac{K_{+i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (y c_i + x s_i)}{K_{-i} - \sqrt{K_{+i}K_{-i}} \langle t \rangle_j (y c_i - x s_i)}$$

- Only one independent equation per bin
- Sensitivity found to be similar to fitting mixing equations directly

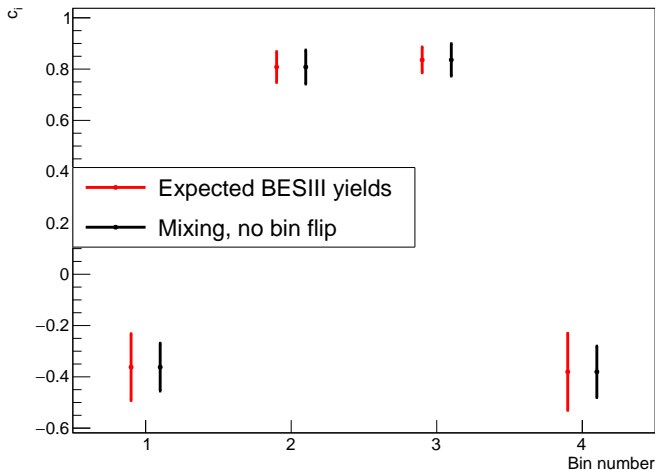




# Charm mixing studies with multi-body decays

Sensitivity to  $c_i$ : Similar between BESIII and charm mixing at LHCb

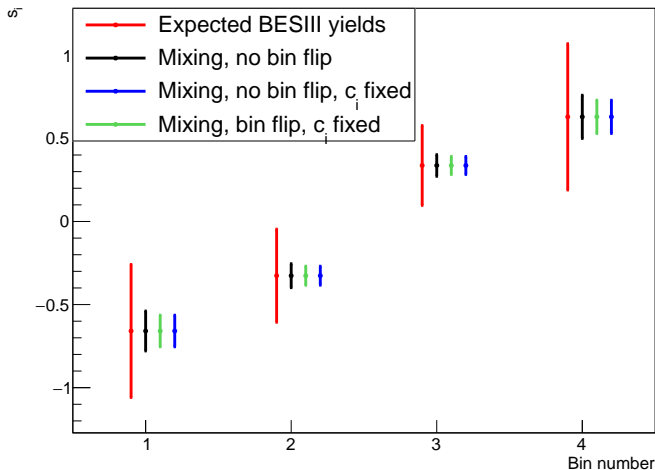
$c_i$  sensitivity studies



# Charm mixing studies with multi-body decays

Sensitivity to  $s_i$ : Significant improvements expected!

$s_i$  sensitivity studies



## Summary:

- 1 Measurement of  $\gamma$  in  $B^\pm \rightarrow [K^+K^-\pi^+\pi^-]_D h^\pm$  is ready to be combined with **model-independent** strong-phase inputs
- 2 BESIII strong-phase inputs can be further constrained using charm-mixing measurements at LHCb, and provide comparable sensitivity to  $s_i$

## Future prospects:

- ① Measurement is still statistically limited, and will be significantly improved with LHCb Upgrade I
- ② Additional BESIII data and charm-mixing measurements from LHCb will bring strong-phase systematics down further
- ③ Can extend this strategy to many more four-body modes
  - Studies of  $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$  show similar results

Thanks for your attention!