

## Probability and Reward table:

S	а	S'	P(S' a,S')	R(S,a,S')
Cool	Fast	Warm	0,5	2
Cool	Fast	Cool	0,5	2
Cool	Slow	Cool	1	1
Warm	Slow	Warm	0,5	1
Warm	Slow	Cool	0,5	1
Warm	Fast	Overheated	1	-10

## **Optimal Value Table**

	Cool	Warm	Overheated
V0	0,0	0,0	0,0
V1	2,0	1,0	-10,0
V2	3,5	2,5	-10,0
V3	5,0	4,0	-10,0

In the first iteration, all values are 0. For overheated state, all values will remain -10 starting iteration 1, it will not change because it can change from state.

For the second Iteration:

Cool State:

$$\begin{split} Q_1(C,F) &= T(C,F,C)[R(C,F,C) + \gamma V_0(C)] + T(C,F,W)[R(C,F,W) + \gamma V_0(W)] \\ Q_1 &= 0.5[2+1*0] + 0.5[2+1*0] = 2 \\ Q_2(C,S) &= T(C,S,C)[R(C,S,C) + \gamma V_0(C)] \\ Q_2 &= 1[1+1*0] = 1 \\ V_1(C) &= \max \bigl(Q_1(C,F),Q_2(C,S)\bigr) = 2 \end{split}$$

Warm State:

$$\begin{split} Q_1(W,F) &= T(W,F,O)[R(E,F,O) + \gamma V_0(O)] \\ Q_1 &= 1[-10+1*0] = -10 \\ \\ Q_2(W,S) &= T(W,S,C)[R(W,S,C) + \gamma V_0(C)] + T(W,S,W)[R(W,S,W) + \gamma V_0(W)] \\ Q_2 &= 0.5[1+1*0] + 0.5[1+1*0] = 1 \\ \\ V_1(W) &= \max \bigl(Q_1(W,F),Q_2(W,S)\bigr) = 1 \end{split}$$

For the second iteration:

Cool State:

$$\begin{aligned} Q_1(C,F) &= T(C,F,C)[R(C,F,C) + \gamma V_1(C)] + T(C,F,W)[R(C,F,W) + \gamma V_1(W)] \\ Q_1 &= 0.5[2+1*2] + 0.5[2+1*1] = 3.5 \\ Q_2(C,S) &= T(C,S,C)[R(C,S,C) + \gamma V_1(C)] \\ Q_2 &= 1[1+1*2] = 3 \\ V_2(C) &= \max(Q_1(C,F),Q_2(C,S)) = 3.5 \end{aligned}$$

Warm State:

$$\begin{split} Q_1(W,F) &= T(W,F,O)[R(E,F,O) + \gamma V_1(O)] \\ Q_1 &= 1[-10+1*-10] = -20 \\ Q_2(W,S) &= T(W,S,C)[R(W,S,C) + \gamma V_1(C)] + T(W,S,W)[R(W,S,W) + \gamma V_1(W)] \\ Q_2 &= 0.5[1+1*2] + 0.5[1+1*1] = 2.5 \\ V_2(W) &= \max \bigl(Q_1(W,F),Q_2(W,S)\bigr) = 2.5 \end{split}$$

For the third iteration:

Cool State:

$$\begin{aligned} Q_1(C,F) &= T(C,F,C)[R(C,F,C) + \gamma V_2(C)] + T(C,F,W)[R(C,F,W) + \gamma V_2(W)] \\ Q_1 &= 0.5[2+1*3.5] + 0.5[2+1*2.5] = 5 \\ Q_2(C,S) &= T(C,S,C)[R(C,S,C) + \gamma V_1(C)] \\ Q_2 &= 1[1+1*3.5] = 4.5 \\ V_3(C) &= \max \left(Q_1(C,F),Q_2(C,S)\right) = 5 \end{aligned}$$

Warm State:

$$Q_{1}(W,F) = T(W,F,O)[R(E,F,O) + \gamma V_{2}(O)]$$

$$Q_{1} = 1[-10 + 1 * -10] = -20$$

$$Q_{2}(W,S) = T(W,S,C)[R(W,S,C) + \gamma V_{1}(C)] + T(W,S,W)[R(W,S,W) + \gamma V_{1}(W)]$$

$$Q_{2} = 0.5[1 + 1 * 3.5] + 0.5[1 + 1 * 2.5] = 4$$

$$V_{3}(W) = \max(Q_{1}(W,F),Q_{2}(W,S)) = 4$$