

# ArrayStack

Open Data Structures



# ArrayStack

Implementing a List using an array



# ArrayStack

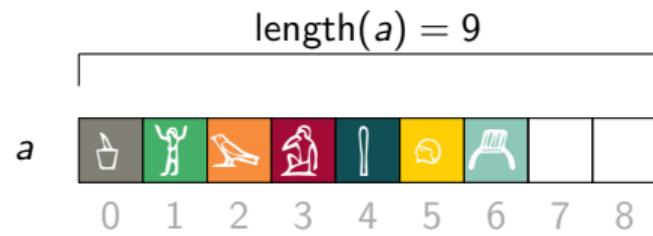
Implementing a List using an array



$$n = 7$$

# ArrayStack

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Implementing a List using an array

get(3)



$$n = 7$$

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Implementing a List using an array

get(3)



$$n = 7$$

# ArrayStack

Implementing a List using an array

$\text{get}(3) \Rightarrow$  



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set(4, )



$$n = 7$$

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set(4, )



$$n = 7$$

# ArrayStack

Implementing a List using an array

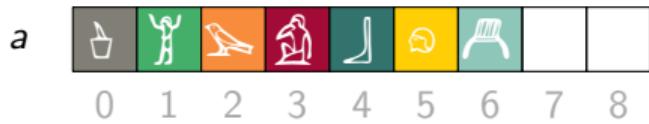
set(4, )



$$n = 7$$

# ArrayStack

Implementing a List using an array



$$n = 7$$

# ArrayStack

Implementing a List using an array

`add(3, )`



$$n = 7$$

# ArrayStack

Implementing a List using an array

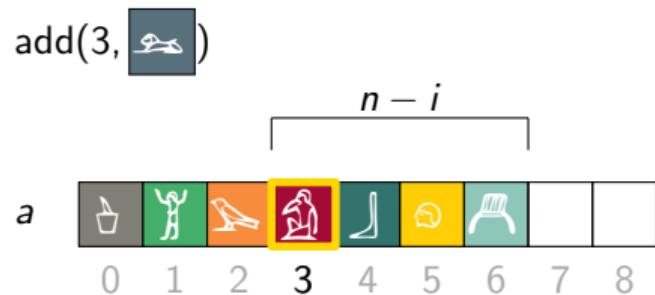
`add(3, )`



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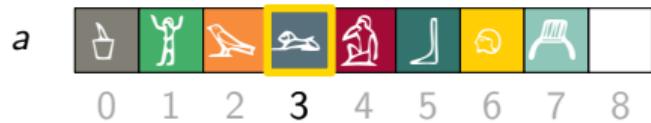


$$n = 7$$

# ArrayStack

Implementing a List using an array

`add(3, )`

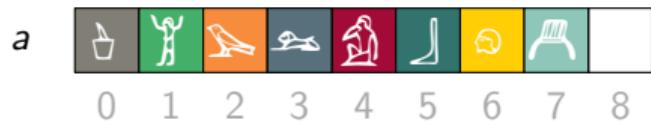


$$n = 7$$

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Implementing a List using an array

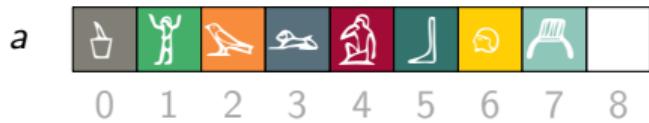
`add(3, )`



$$n = 8$$

# ArrayStack

Implementing a List using an array

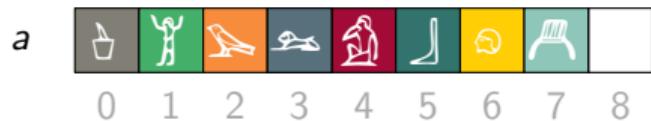


$$n = 8$$

# ArrayStack

Implementing a List using an array

`add(8, )`

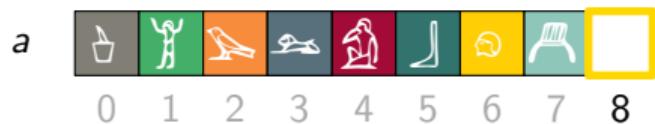


$$n = 8$$

# ArrayStack

Implementing a List using an array

`add(8, )`

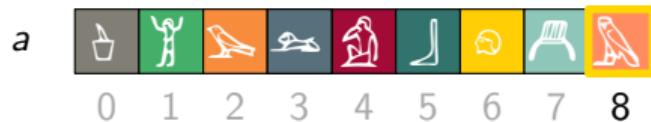


$$n = 8$$

# ArrayStack

Implementing a List using an array

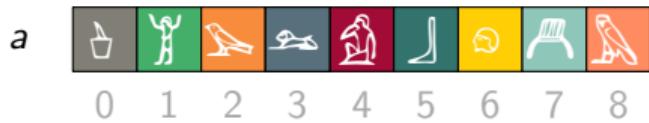
`add(8, )`



$$n = 8$$

# ArrayStack

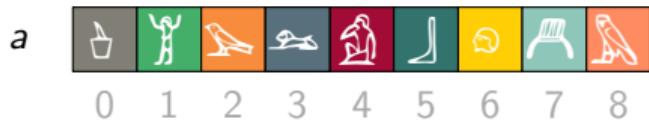
Implementing a List using an array



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# ArrayStack

Implementing a List using an array

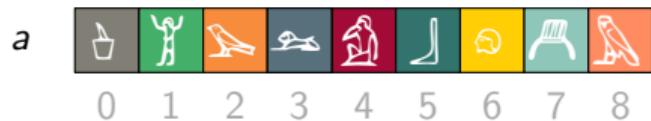


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, `

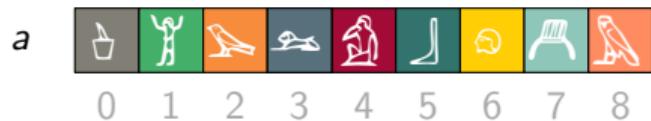


$$n = 9$$

# ArrayStack

Implementing a List using an array

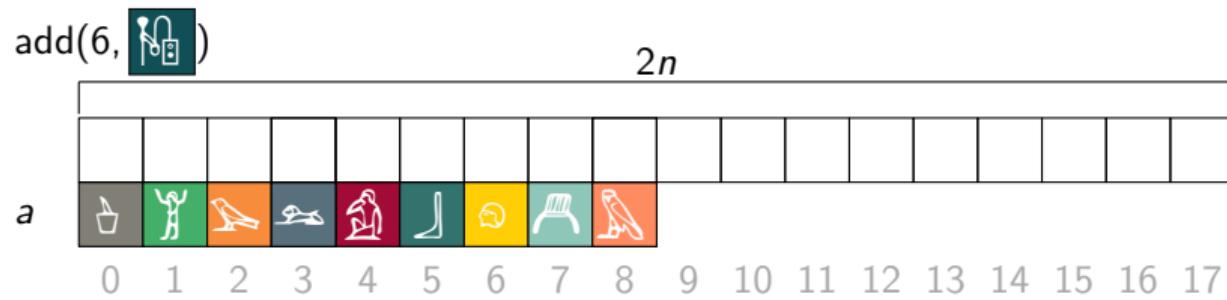
`add(6, `



$n = 9 = \text{length}(a) \Rightarrow \text{resize}()$

# ArrayStack

Implementing a List using an array

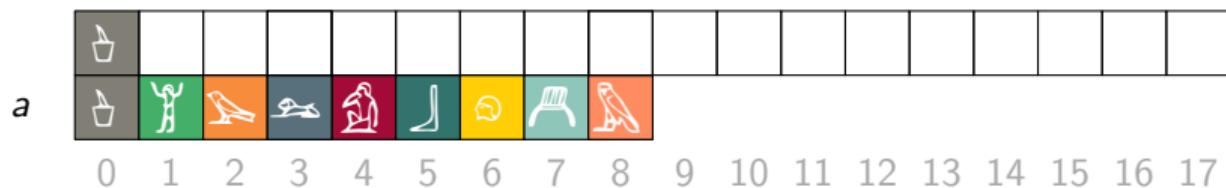


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6,  )`

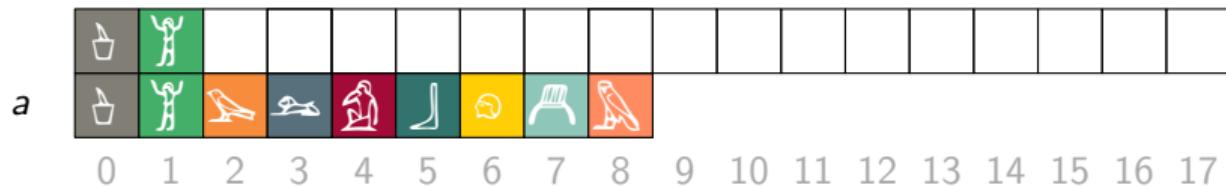


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6,  )`

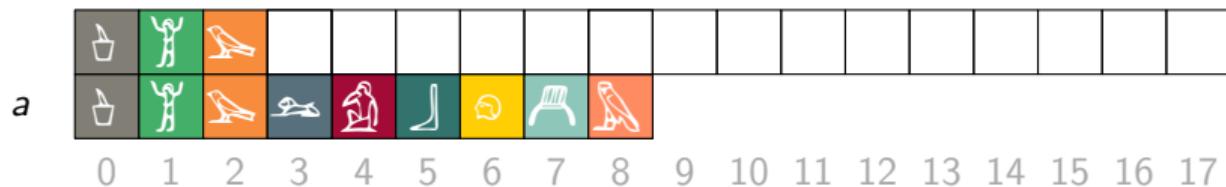


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, 🎵)`

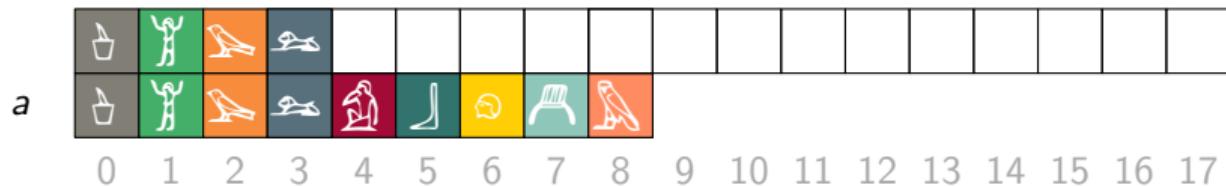


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6,  )`

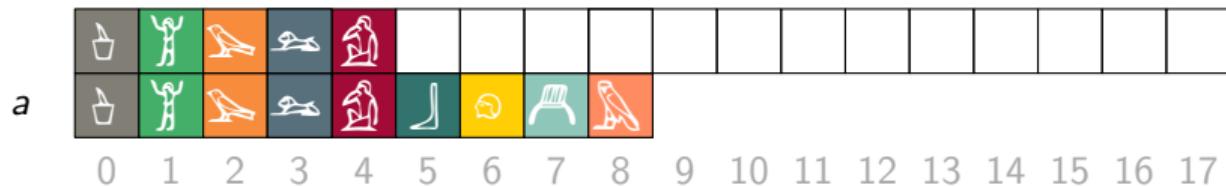


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, `

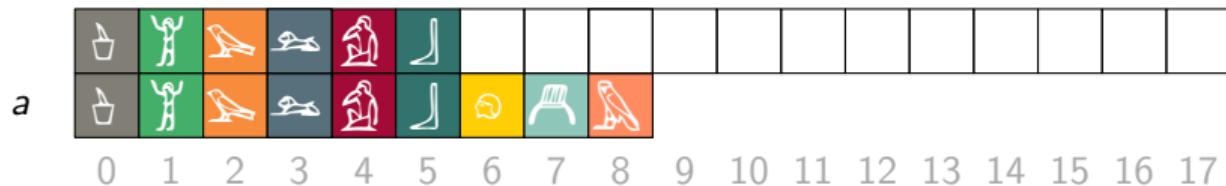


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, `

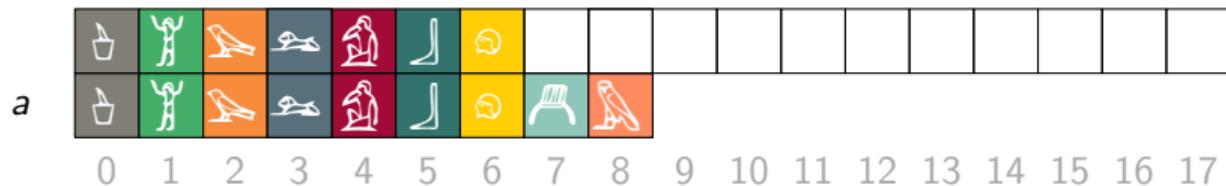


$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, 🎵)`



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Implementing a List using an array

`add(6, 🎵)`



$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, `

																		
<i>a</i>										0	1	2	3	4	5	6	7	8
										9	10	11	12	13	14	15	16	17

$$n = 9$$

# ArrayStack

Implementing a List using an array

`add(6, `

<i>a</i>																		
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17

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Implementing a List using an array

add(6, )



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Implementing a List using an array

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$$n = 9$$

# ArrayStack

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$$n = 10$$

# ArrayStack

Implementing a List using an array

remove(5)



$$n = 10$$

# ArrayStack

Implementing a List using an array

remove(5)



$$n = 10$$

# ArrayStack

Implementing a List using an array

remove(5)

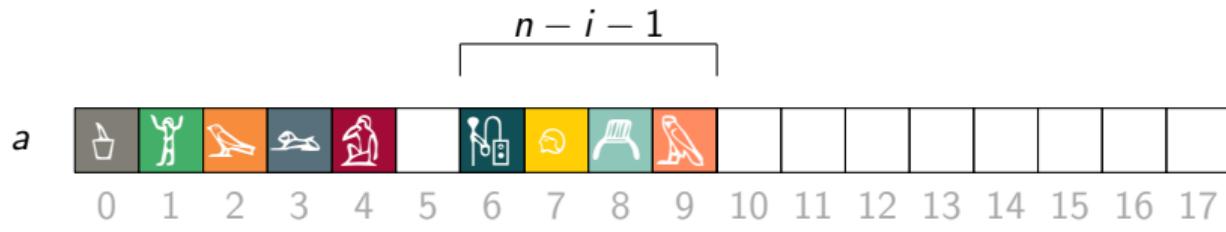


$$n = 10$$

# ArrayStack

Implementing a List using an array

remove(5)



$$n = 10$$

# ArrayStack

Implementing a List using an array

remove(5)



$$n = 10$$

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Implementing a List using an array

remove(5)



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Implementing a List using an array

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Implementing a List using an array



$$n = 9$$

# ArrayStack

Implementing a List using an array

remove(8)



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Implementing a List using an array

remove(8)



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Implementing a List using an array

remove(8)



$$n = 9$$

# ArrayStack

Implementing a List using an array

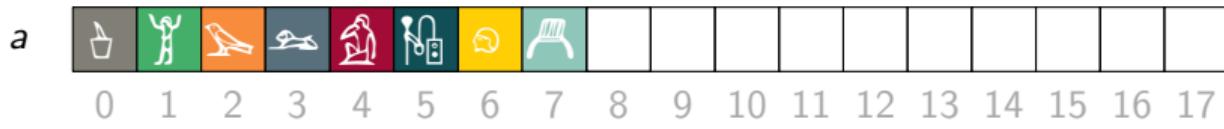
remove(8)



$$n = 8$$

# ArrayStack

Implementing a List using an array



$$n = 8$$

# ArrayStack

Implementing a List using an array

remove(7) ... remove(6) ... remove(5)



$$n = 8$$

# ArrayStack

Implementing a List using an array

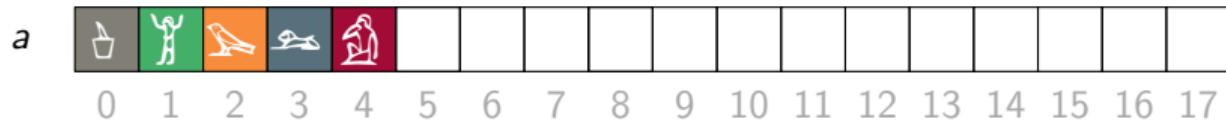
remove(7) ... remove(6) ... remove(5)



$$n = 8$$

# ArrayStack

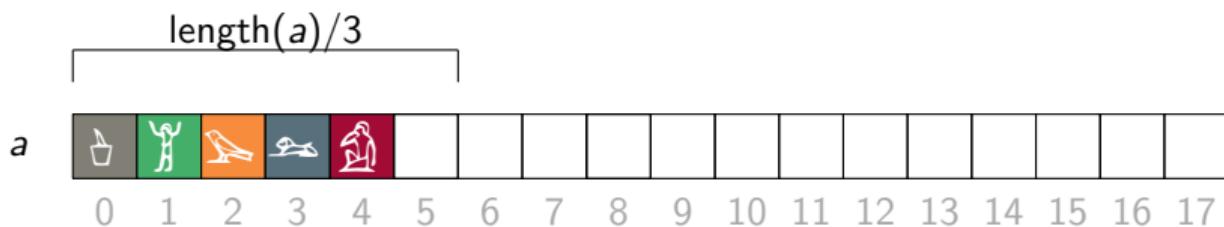
Implementing a List using an array



$$n = 5$$

# ArrayStack

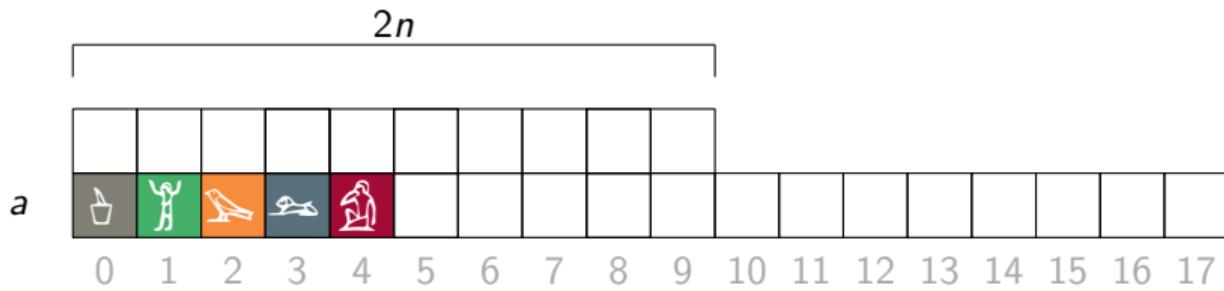
Implementing a List using an array



$n = 5 < \text{length}(a)/3 \Rightarrow \text{resize}()$

# ArrayStack

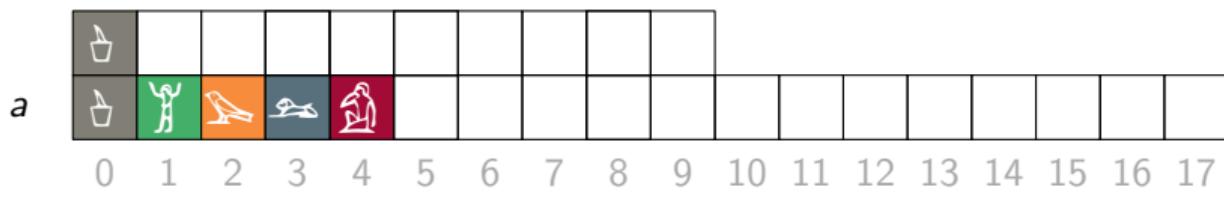
Implementing a List using an array



$$n = 5$$

# ArrayStack

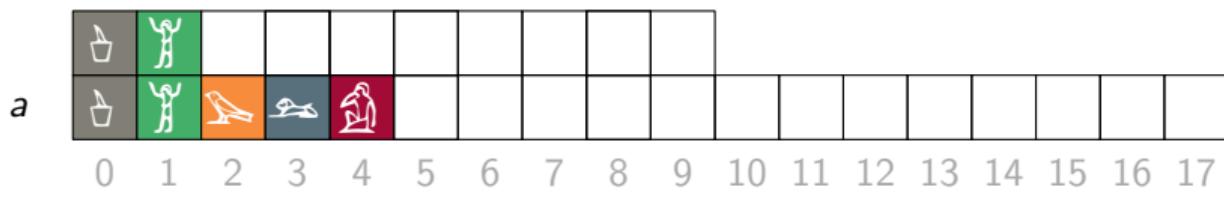
Implementing a List using an array



$$n = 5$$

# ArrayStack

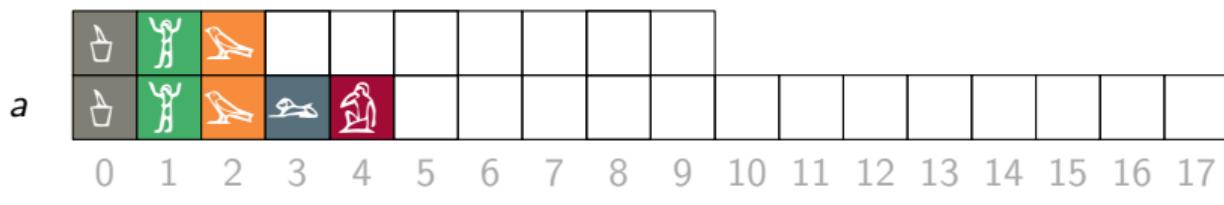
Implementing a List using an array



$$n = 5$$

# ArrayStack

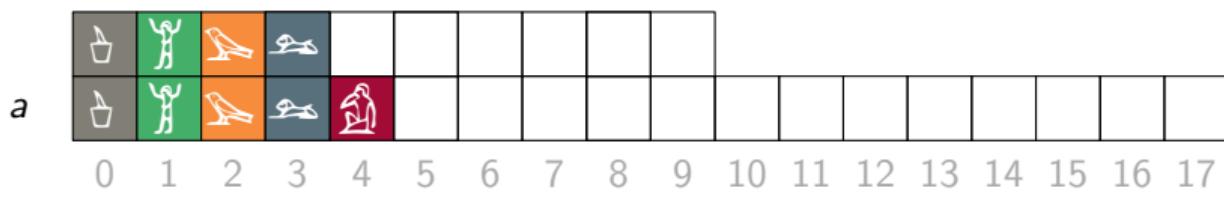
Implementing a List using an array



$$n = 5$$

# ArrayStack

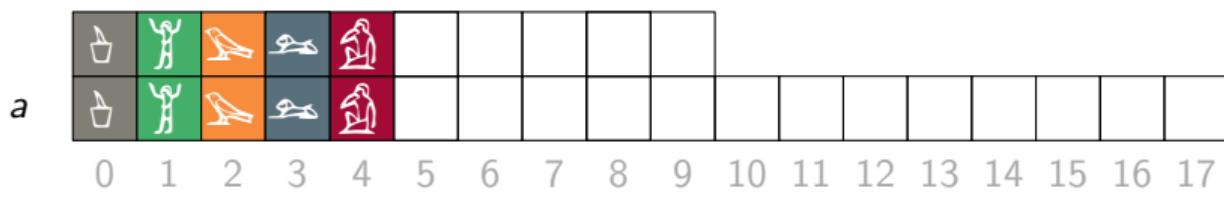
Implementing a List using an array



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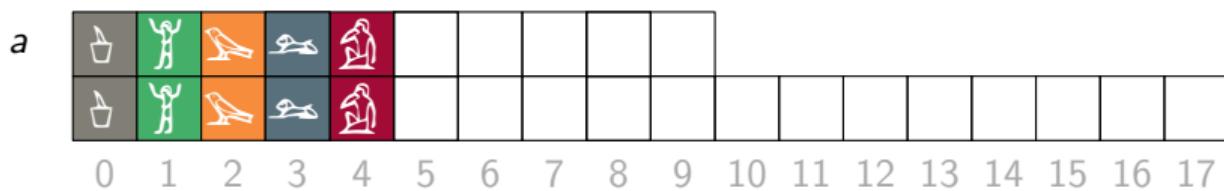
Implementing a List using an array



$$n = 5$$

# ArrayStack

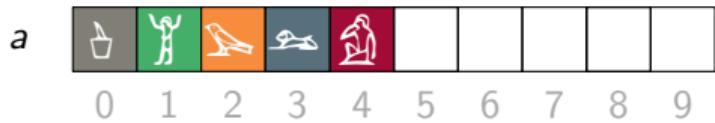
Implementing a List using an array



$$n = 5$$

# ArrayStack

Implementing a List using an array



$$n = 5$$

# ArrayStack

Implementing a List using an array

## Theorem

An ArrayStack implements the List interface.

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Ignoring the time spent in calls to `resize()`,

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- `get(i)` runs in  $O(1)$  time;

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Implementing a List using an array

## Theorem

An ArrayStack implements the List interface.

Ignoring the time spent in calls to `resize()`,

- `get(i)` runs in  $O(1)$  time;
- `set(i, x)` runs in  $O(1)$  time;

# ArrayStack

Implementing a List using an array

## Theorem

An ArrayStack implements the List interface.

Ignoring the time spent in calls to `resize()`,

- `get(i)` runs in  $O(1)$  time;
- `set(i, x)` runs in  $O(1)$  time;
- `add(i, x)` runs in  $O(1 + n - i)$  time; and

# ArrayStack

Implementing a List using an array

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An ArrayStack implements the List interface.

Ignoring the time spent in calls to `resize()`,

- `get(i)` runs in  $O(1)$  time;
- `set(i, x)` runs in  $O(1)$  time;
- `add(i, x)` runs in  $O(1 + n - i)$  time; and
- `remove(i)` runs in  $O(1 + n - i)$  time.

# ArrayStack

Implementing a List using an array

## Theorem

An ArrayStack implements the List interface.

Ignoring the time spent in calls to `resize()`,

- `get(i)` runs in  $O(1)$  time;
- `set(i, x)` runs in  $O(1)$  time;
- `add(i, x)` runs in  $O(1 + n - i)$  time; and
- `remove(i)` runs in  $O(1 + n - i)$  time.

## Question

What about the calls to `resize()`?

# End of Lesson