### 1 Lastfluss- und Kurzschlussbetrachtung

Das ist jetzt erstellt worden.

a)

$$X_G = x_d \frac{U_2^2}{S_N} = 1.5 \frac{(0.4 \,\text{kV})^2}{400 \,\text{MV A}} = 0.6 \,\text{m}\Omega$$
 (1)

$$R_G = 0\,\Omega\tag{2}$$

$$Z_{T1} = u_k \frac{U_2^2}{S_N} = 0.06 \frac{(0.4 \text{ kV})^2}{5 \text{ MV A}} = 1.92 \text{ m}\Omega$$
 (3)

$$R_{T1} = P_k \frac{U_2^2}{S_N^2} = 0.08 \,\text{MW} \frac{(0.4 \,\text{kV})^2}{(5 \,\text{MV A})^2} = 0.512 \,\text{m}\Omega$$
 (4)

$$X_{T1} = \sqrt{Z_{T1}^2 - R_{T1}^2} = \sqrt{(1.92 \,\mathrm{m}\Omega)^2 - (0.512 \,\mathrm{m}\Omega)^2} = 1.85 \,\mathrm{m}\Omega \tag{5}$$

$$Z_{T2} = u_k \frac{U_2^2}{S_N} = 0.06 \frac{(0.4 \text{ kV})^2}{630 \text{ kV A}} = 15.24 \text{ m}\Omega$$
 (6)

$$R_{T2} = P_k \frac{U_2^2}{S_N^2} = 9 \,\text{kW} \frac{(0.4 \,\text{kV})^2}{(630 \,\text{kV A})^2} = 3,628 \,\text{m}\Omega$$
 (7)

$$X_{T2} = \sqrt{Z_{T2}^2 - R_{T2}^2} = \sqrt{(15,24 \,\mathrm{m}\Omega)^2 - (3,628 \,\mathrm{m}\Omega)^2} = 14,80 \,\mathrm{m}\Omega \tag{8}$$

$$R_{L1} = R' l \left(\frac{U_2}{U_1}\right)^2 = 0.7 \frac{\Omega}{\text{km}} \cdot 6 \text{ km} \cdot \left(\frac{0.4 \text{ kV}}{20 \text{ kV}}\right)^2 = 1,68 \text{ m}\Omega$$
 (9)

$$X_{L1} = X' l \left(\frac{U_2}{U_1}\right)^2 = 0.4 \frac{\Omega}{\text{km}} \cdot 6 \,\text{km} \cdot \left(\frac{0.4 \,\text{kV}}{20 \,\text{kV}}\right)^2 = 0.960 \,\text{m}\Omega$$
 (10)

$$R_{L2} = R'l = 0.3 \frac{\Omega}{\text{km}} \cdot 4 \text{ km} = 60 \text{ m}\Omega$$
(11)

$$X_{L2} = X'l = 0.1 \frac{\Omega}{\text{km}} \cdot 4 \,\text{km} = 20 \,\text{m}\Omega$$
 (12)

b)

$$\underline{Z}_{Ges,V} = (R_{T1} + R_{T2} + R_{L1} + R_{L2}) + j(X_{T1} + X_{T2} + X_{L1} + X_{L2})$$
(13)

$$= (0.512 + 3.628 + 1.68 + 60) \,\mathrm{m}\Omega + \mathrm{j} (1.85 + 14.8 + 0.96 + 20) \,\mathrm{m}\Omega \tag{14}$$

$$= (65,82 + 37,61) \,\mathrm{m}\Omega = 75,81 \cdot \mathrm{e}^{\mathrm{j}0,5191} \mathrm{m}\Omega \tag{15}$$

c) 
$$v_p = 90^{\circ} - 0.517 \cdot \frac{180^{\circ}}{\pi} = 60.26^{\circ}$$
 (16)

d)

$$X_G = x_d'' \frac{U_2^2}{S_N} = 0.25 \frac{(400 \,\text{V})}{400 \,\text{MV A}} = 0.1 \,\text{m}\Omega$$
 (17)

$$\underline{Z}_{k,Ges,V} = \underline{Z}_{Ges,V} + jX_G = (65,82 + 37,71) \,\mathrm{m}\Omega$$
 (18)

$$|\underline{Z}_{k,Ges,V}| = 75,86 \,\mathrm{m}\Omega \tag{19}$$

$$S_k = c \frac{U_2^2}{|Z_{k,Ges,V}|} = 1 \cdot \frac{(400 \text{ V})^2}{75,86 \text{ m}\Omega} = 2,109 \text{ MV A}$$
 (20)

e) 
$$i_{k3p}^{"} = c \frac{U_2}{\sqrt{3} Z_{k,Ges,V}} = 1.1 \cdot \frac{400 \text{ V}}{\sqrt{3} \cdot 75,86 \text{ m}\Omega} = 3,348 \text{ kA}$$
 (21)

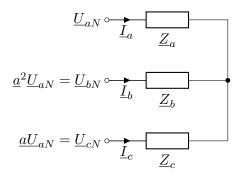
### 2 Drehstromkomponentensystem

a) Messschaltungen von S.49 und S.50 im Skriptum

$$\frac{\underline{I}_a}{\underline{I}_b} = \frac{\underline{Z}_b}{\underline{Z}_a} = \frac{1}{2} \tag{22}$$

$$\underline{Z}_{(0)} = \frac{\underline{U}_{(0)}}{\underline{I}_{(0)}} = \frac{\frac{1}{3} (\underline{U}_{aN} + \underline{U}_{bN} + \underline{U}_{cN})}{\frac{1}{3} (\underline{I}_a + \underline{I}_b + \underline{I}_c)} = \frac{3U_{aN}}{\underline{I}_a (1 + 2 + 2)}$$
(23)

$$=\frac{3\left(\underline{I}_{a}\underline{Z}_{a}+\left(\underline{I}_{a}+\underline{I}_{b}+\underline{I}_{c}\right)\underline{Z}_{N}\right)}{5\underline{I}_{a}}=\frac{3\underline{I}_{a}\left(2\underline{Z}_{b}+5\cdot\frac{1}{5}\underline{Z}_{b}\right)}{5\underline{I}_{a}}=\frac{9}{5}\underline{Z}_{b}\tag{24}$$



$$\underline{Z}_{(1)} = \frac{\underline{U}_{(1)}}{\underline{I}_{(1)}} = \frac{\frac{1}{3} \left( \underline{U}_{aN} + \underline{a}\underline{U}_{bN} + \underline{a}^2\underline{U}_{cN} \right)}{\frac{1}{3} \left( \underline{I}_a + \underline{a}\underline{I}_b + \underline{a}^2\underline{I}_c \right)}$$
(25)

$$\underline{U}_{aN} - \underline{Z}_{a}\underline{I}_{a} = \underline{U}_{bN} - \underline{Z}_{b}\underline{I}_{b} \tag{26}$$

$$\underline{I}_{b} = \frac{\underline{U}_{aN} \left(\underline{a}^{2} - 1\right) + \underline{Z}_{a}\underline{I}_{a}}{\underline{Z}_{b}} \tag{27}$$

$$\underline{U}_{aN} - \underline{Z}_{a}\underline{I}_{a} = \underline{U}_{cN} - \underline{Z}_{c}\underline{I}_{c} \tag{28}$$

$$\underline{I}_{c} = \frac{\underline{U}_{aN} \left(\underline{a} - 1\right) + \underline{Z}_{a} \underline{I}_{a}}{\underline{Z}_{c}} \tag{29}$$

$$\underline{I}_a = -\underline{I}_b - \underline{I}_c = \frac{\underline{U}_{aN}}{\underline{Z}_b} \left( -\underline{a}^2 + 1 - \underline{a} + 1 \right) - 4\underline{I}_a \tag{30}$$

$$5\underline{I}_a = 3\frac{\underline{U}_{aN}}{\underline{Z}_b} \tag{31}$$

$$\underline{I}_a = \frac{3}{5} \frac{\underline{U}_{aN}}{\underline{Z}_b} \tag{32}$$

$$\underline{Z}_{(1)} = \frac{3U_a N}{\underline{I}_a + \frac{\underline{U}_{aN}}{\underline{Z}_b} \underline{a} (\underline{a}^2 - 1) + 2\underline{a}\underline{I}_a + \frac{\underline{U}_{aN}}{\underline{Z}_b} \underline{a}^2 (\underline{a} - 1) + 2\underline{a}^2 \underline{I}_a}$$
(33)

$$=\frac{3\underline{U}_{aN}}{-\underline{I}_a+3\frac{\underline{U}_{aN}}{\underline{Z}_b}}=\frac{3\underline{U}_{aN}}{-\frac{3}{5}\frac{\underline{U}_{aN}}{\underline{Z}_b}+3\frac{\underline{U}_{aN}}{\underline{Z}_b}}=\frac{5}{4}\underline{Z}_b \tag{34}$$

$$\underline{Z}_{(2)} = \frac{\underline{U}_{(2)}}{\underline{I}_{(2)}} = \frac{\frac{1}{3} \left( \underline{U}_{aN} + \underline{a}^2 \underline{U}_{bN} + \underline{a} \underline{U}_{cN} \right)}{\frac{1}{3} \left( \underline{I}_a + \underline{a}^2 \underline{I}_b + \underline{a} \underline{I}_c \right)} = \frac{U_{aN}}{\underline{I}_a + \underline{a}^2 \underline{I}_b + \underline{a} \underline{I}_c}$$
(35)

Wenn man  $\underline{I}_b$  und  $\underline{I}_c$  miteinander vertauscht, was man machen darf, weil  $\underline{Z}_b = \underline{Z}_c$ , dann hat man die selbe Gleichung wie für  $\underline{Z}_{(1)}$ , woraus folgt  $\underline{Z}_{(2)} = \underline{Z}_{(1)}$ .

b)

$$\underline{I}_{(0)} = \frac{1}{3} \left( k I_{ph} + \underline{a}^2 I_{ph} + \underline{a} I_{ph} \right) = \frac{1}{3} \left( k - 1 \right) I_{ph}$$

$$\tag{36}$$

$$\underline{I}_{(1)} = \frac{1}{3} (kI_{ph} + I_{ph} + I_{ph}) = \frac{1}{3} (k+2) I_{ph}$$
(37)

$$\underline{I}_{(2)} = \frac{1}{3} \left( k I_{ph} + \underline{a} I_{ph} + \underline{a}^2 I_{ph} \right) = \frac{1}{3} (k - 1) I_{ph}$$
(38)

c)

$$\underline{U}_{(0)} = \underline{Z}_{(0)}\underline{I}_{(0)} = \frac{9}{5}\underline{Z}_b \frac{1}{3} (k-1) I_p h = \frac{3}{5} (k-1) \underline{Z}_b I_{ph}$$
(39)

$$\underline{U}_{(1)} = \underline{Z}_{(1)}\underline{I}_{(1)} = \frac{5}{4}\underline{Z}_b\frac{1}{3}(k+2)I_ph = \frac{5}{12}(k+2)\underline{Z}_bI_{ph}$$

$$\tag{40}$$

$$\underline{U}_{(2)} = \underline{Z}_{(2)}\underline{I}_{(2)} = \frac{5}{4}\underline{Z}_b \frac{1}{3} (k-1) I_p h = \frac{5}{12} (k-1) \underline{Z}_b I_{ph}$$
(41)

d)

$$\underline{U}_{a} = \underline{U}_{(0)} + \underline{U}_{(1)} + \underline{U}_{(2)} = \left(\frac{3}{5}\left(k-1\right) + \frac{5}{12}\left(k+2\right) + \frac{5}{12}\left(k-1\right)\right)\underline{Z}_{b}I_{ph} \tag{42}$$

$$= \left(\frac{43}{30}k - \frac{11}{60}\right)\underline{Z}_b I_{ph} \tag{43}$$

e) 
$$\underline{U}_{a} = \left(\frac{43}{30} \cdot 0.619 - \frac{11}{60}\right) (15 + j5) \Omega \cdot 13.05 A = (137.8 + j45.93) V \tag{44}$$

#### 3 Pumpspeicherkraftwerk

a)

$$E = \rho V g \Delta h = 1000 \,\frac{\text{kg}}{\text{m}^3} \cdot 0.6 \cdot 70 \cdot 10^6 \,\text{m}^3 \cdot 9.81 \,\frac{\text{m}}{\text{s}^2} \cdot 150 \,\text{m} = 61.8 \cdot 10^{12} \,\text{J} = 61.8 \,\text{TJ} \quad (45)$$

b)

$$P_{el} = \eta_H \eta_T \eta_{el} (1 - \varepsilon) \rho Q_N g \Delta h \tag{46}$$

$$= 0.94 \cdot 0.92 \cdot 0.96 \cdot (1 - 0.02) \cdot 1000 \frac{\text{kg}}{\text{m}^3} \cdot 115 \frac{\text{m}^3}{\text{s}} \cdot 9.81 \frac{\text{m}}{\text{s}^2} \cdot 150 \,\text{m} = 137.68 \,\text{MW} \quad (47)$$

c) 
$$t = \frac{V_{OS} (FS - FS_{min})}{Q_N} = \frac{70 \cdot 10^6 \,\mathrm{m}^3 \cdot (0.6 - 0.4)}{115 \,\frac{\mathrm{m}^3}{\mathrm{s}}} = 121.74 \cdot 10^3 \,\mathrm{s} = 33.82 \,\mathrm{h} \tag{48}$$

d)

$$P_{el} = \frac{\rho Q_{Pump} g \Delta h}{\eta_H \eta_{P} \eta_{el} (1 - \varepsilon)} = \frac{1000 \frac{\text{kg}}{\text{m}^3} \cdot 115 \frac{\text{m}^3}{\text{s}} \cdot 9.81 \frac{\text{m}}{\text{s}^2} \cdot 150 \text{ m}}{0.94 \cdot 0.88 \cdot 0.96 \cdot (1 - 0.02)} = 170.17 \text{ MW}$$
(49)

e) 
$$\eta_{Ges} = \eta_H^2 \eta_T \eta_P \eta_{el}^2 (1 - \varepsilon)^2 = 0.94^2 \cdot 0.92 \cdot 0.88 \cdot 0.96^2 \cdot (1 - 0.02)^2 = 0.6332$$
 (50)

f) 
$$D = \sqrt{2g\Delta h} \frac{p}{2\pi f} = \sqrt{2 \cdot 9.81 \frac{\text{m}}{\text{s}^2} \cdot 150 \,\text{m}} \cdot \frac{12}{2\pi 50 \,\text{Hz}} = 2.072 \,\text{m}$$
 (51)

# 3 Fünf Sicherheitsregeln

Siehe Skriptum S.IX

# 4 Wirtschaftlichkeitsbetrachtung eines Solarkraftwerks

a)

$$T_m = \frac{E}{P} = \frac{1079 \frac{\text{GW h}}{\text{a}}}{377 \text{MW}} = 2862,07 \frac{\text{h}}{\text{a}}$$
 (52)

b)

$$\beta_{-} = \frac{q^{n} - 1}{(q - 1)q^{n}} = \frac{1,05^{25} - 1}{(1,05 - 1)1,05^{25}} = 14,09 \,\mathrm{a}$$
(53)

$$\alpha = \frac{1}{\beta_{-}} \tag{54}$$

$$K = \alpha A + Z = \frac{1}{14.09 \,\mathrm{a}} \cdot 1600 \cdot 10^6 \,\$ + 6 \cdot 10^6 \,\frac{\$}{\mathrm{a}} + 2.2 \cdot 10^6 \,\frac{\$}{\mathrm{a}} = 121.724 \cdot 10^6 \,\frac{\$}{\mathrm{a}} \tag{55}$$

c)

$$\beta_{+} = \frac{(q^{m} - 1) q}{q - 1} = \frac{(1,070^{25} - 1) 1,07}{1,07 - 1} = 67,6765$$
 (56)

$$B_{25} = A_{R,-m}q^m + Z\beta_+ + Z + Z\beta_- + R_nq^{-n}$$
(57)

$$= 600 \cdot 10^{6} \$ \cdot 1,07^{25} + 121,724 \cdot 10^{6} \$ \cdot (67,6765 + 1) = 11,616 \cdot 10^{9} \$$$
 (58)

d)
$$p = \frac{\frac{B_{25} + G}{\beta_{+}}}{E} = \frac{\frac{11,616 \cdot 10^{9} \$ + 3 \cdot 10^{9} \$}{67,6765}}{1079 \cdot 10^{6} \text{ kW h}} = 0,200 \frac{\$}{\text{kW h}}$$
(59)