Calcul des séquents intuitionniste (LJ)

Règles

$$\frac{}{\Gamma, A \vdash A}\ \text{ax} \qquad \frac{\Gamma, A, A \vdash B}{\Gamma, A \vdash B}\ \text{cont}$$

$$\frac{\Gamma \vdash A \qquad \Gamma, B \vdash C}{\Gamma, A \Rightarrow B \vdash C}\ \Rightarrow_{\text{left}} \qquad \frac{\Gamma, A \vdash B}{\Gamma \vdash A \Rightarrow B}\ \Rightarrow_{\text{right}}$$

$$\frac{\Gamma \vdash A \qquad \Gamma, B \vdash C}{\Gamma, A \Leftrightarrow B \vdash C}\ \Leftrightarrow_{\text{left1}}$$

$$\frac{\Gamma \vdash B \qquad \Gamma, A \vdash C}{\Gamma, A \Leftrightarrow B \vdash C}\ \Leftrightarrow_{\text{left2}} \qquad \frac{\Gamma, A \vdash B \qquad \Gamma, B \vdash A}{\Gamma \vdash A \Leftrightarrow B}\ \Leftrightarrow_{\text{right}}$$

Calcul des séquents intuitionniste (LJ)

Règles

$$\frac{\Gamma, A, B \vdash C}{\Gamma, A \wedge B \vdash C}\ \wedge_{\text{left}} \qquad \frac{\Gamma \vdash A \qquad \Gamma \vdash B}{\Gamma \vdash A \wedge B}\ \wedge_{\text{right}}$$

$$\frac{\Gamma \vdash A}{\Gamma \vdash A \vee B}\ \vee_{\text{right1}}$$

$$\frac{\Gamma, A \vdash C \qquad \Gamma, B \vdash C}{\Gamma, A \vee B \vdash C}\ \vee_{\text{left}} \qquad \frac{\Gamma \vdash B}{\Gamma \vdash A \vee B}\ \vee_{\text{right2}}$$

$$\frac{\Gamma \vdash A}{\Gamma, \neg A \vdash B}\ \neg_{\text{left}} \qquad \frac{\Gamma, A \vdash \bot}{\Gamma \vdash \neg A}\ \neg_{\text{right}}$$

$$\frac{}{\Gamma, \bot \vdash A}\ \bot_{\text{left}} \qquad \frac{}{\Gamma \vdash \top}\ \top_{\text{right}}$$

Calcul des séquents intuitionniste (LJ)

Règles

$$\frac{\Gamma, A(t) \vdash B}{\Gamma, \forall x.A(x) \vdash B}\ \forall_{\text{left}} \qquad \frac{\Gamma \vdash A(x)}{\Gamma \vdash \forall x.A(x)}\ \forall_{\text{right}},\ x \notin \Gamma$$

$$\frac{\Gamma, A(x) \vdash B}{\Gamma, \exists x.A(x) \vdash B}\ \exists_{\text{left}},\ x \notin \Gamma, B \qquad \frac{\Gamma \vdash A(t)}{\Gamma \vdash \exists x.A(x)}\ \exists_{\text{right}}$$

$$\frac{\Gamma \vdash A \qquad \Gamma, A \vdash B}{\Gamma \vdash B}\ \text{cut}$$

Calcul des séquents classique (LJ_{em})

Règles

$$\frac{\Gamma, A(t) \vdash B}{\Gamma, \forall x.A(x) \vdash B}\ \forall_{\text{left}} \qquad \frac{\Gamma \vdash A(x)}{\Gamma \vdash \forall x.A(x)}\ \forall_{\text{right}},\ x \notin \Gamma$$

$$\frac{\Gamma, A(x) \vdash B}{\Gamma, \exists x.A(x) \vdash B}\ \exists_{\text{left}},\ x \notin \Gamma, B \qquad \frac{\Gamma \vdash A(t)}{\Gamma \vdash \exists x.A(x)}\ \exists_{\text{right}}$$

$$\frac{\Gamma \vdash A \qquad \Gamma, A \vdash B}{\Gamma \vdash B}\ \text{cut} \qquad \frac{\Gamma \vdash \neg\neg A}{\Gamma \vdash A}\ \text{em}$$