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$$\sum_{i=1}^m 2^i - 1 = m(m+1) - 1 \quad m > 0$$

Base case

$$m = 1$$

$$m(m+1) - 1 \rightarrow 1(2) - 1 = \underline{1}$$

$$\sum_{i=1}^1 2^i - 1 = 2 \cdot 1 - 1 = \underline{1}$$

True

this implies \forall

$$1 + 3 + \dots + 2k-1 = k(k+1) - 1$$

$$k(k+1) - 1 + 2k+1 \neq (k+1)(k+2) - 1$$

It is not equal, which means
it doesn't hold for all $m > 0$