

1)

P	q	$P \vee q$	$P \downarrow q$
0	0	0	<u>1</u>
0	1	1	<u>0</u>
1	0	1	<u>0</u>
1	1	1	<u>0</u>

2) $P \downarrow P \equiv \neg (P \vee P)$
 $\equiv \neg P \wedge \neg P$ D.M.G
 $\equiv \neg P$

P	$\neg P$	$\neg P \wedge \neg P$
0	1	1
1	0	0

They are logically equivalent

3) $(P \downarrow q) \downarrow (P \downarrow q)$
 $\equiv \neg (\neg (P \vee q) \vee \neg (P \vee q))$
 $\equiv \neg [\neg (P \vee q)] \wedge \neg [\neg (P \vee q)]$ D.M.G
 $\equiv (P \vee q) \wedge (P \vee q)$ Double negation
 $\equiv P \vee q$ As $r \wedge r \equiv r$

$P \vee q \equiv (P \downarrow q) \downarrow (P \downarrow q)$