

COURSE "AUTOMATED PLANNING: THEORY AND PRACTICE"

CHAPTER 10: DOMAIN-CONFIGURABLE PLANNING: HIERARCHICAL TASK NETWORKS

Teacher: **Marco Roveri** - marco.roveri@unitn.it
M.S. Course: Artificial Intelligence Systems (LM)
A.A.: 2025-2026
Where: DISI, University of Trento
URL: <https://shorturl.at/A81hf>



Last updated: Monday 27th October, 2025

TERMS OF USE AND COPYRIGHT

USE

This material (including video recording) is intended solely for students of the University of Trento registered to the relevant course for the Academic Year 2025-2026.

SELF-STORAGE

Self-storage is permitted only for the students involved in the relevant courses of the University of Trento and only as long as they are registered students. Upon the completion of the studies or their abandonment, the material has to be deleted from all storage systems of the student.

COPYRIGHT

The copyright of all the material is held by the authors. Copying, editing, translation, storage, processing or forwarding of content in databases or other electronic media and systems without written consent of the copyright holders is forbidden. The selling of (parts) of this material is forbidden. Presentation of the material to students not involved in the course is forbidden. The unauthorised reproduction or distribution of individual content or the entire material is not permitted and is punishable by law.

The material (text, figures) in these slides is authored by Jonas Kvarnström and Marco Roveri.

ASSUMPTIONS

- The fundamental assumptions we considered so far are:
 - We only specify: Objects and state variables
 - We only specify: initial state and goal
 - Physical preconditions and effects of actions



- We only specify what **can** be done!
- The **planner** should decide what **should** be done!

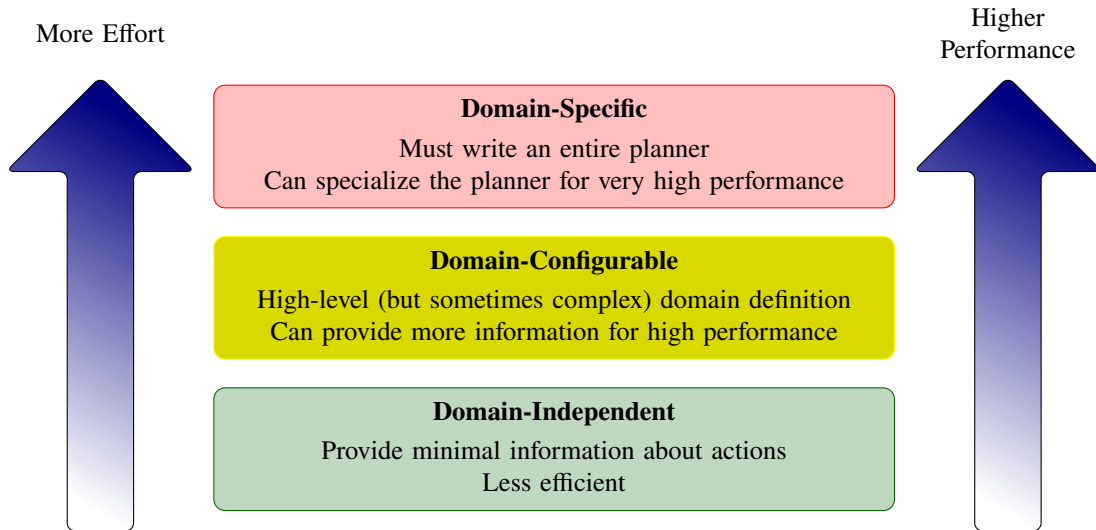


- But... even the most sophisticated heuristics and domain analysis methods lack human intuitions and background knowledge...

DOMAIN-CONFIGURABLE PLANNERS

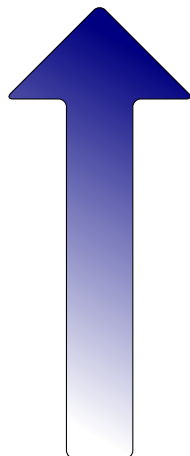
- How can we make a planner take advantage of what we know?
- Planners taking advantage of additional knowledge can be called:
 - Knowledge-rich
 - Domain-Configurable
 - Sometimes incorrectly called "domain-dependent"

COMPARISON



COMPARISON (CONT.)

Larger problem classes
can be handled efficiently



Domain-Configurable

Easier to improve expressivity and efficiency
⇒ Often practically useful for a larger set of domains!

Domain-independent

Should be useful for a wide range of domains

Domain-Specific

Only works in a single domain

HIERARCHICAL-TASK NETWORKS: INTUITION

CLASSICAL PLANNING

- Objective is to **achieve a goal**

```
{ (at TimeSqaure) }
{ (on A B), (on C D) }
...
```



HIERARCHICAL TASK NETWORKS

- Objective is to **perform a task**

```
{ (travel-to TimeSqaure) }
{ (place-blocks-correctly) }
...
```



- **Find** any sequence of actions that achieves the goal

- Use "templates" to incrementally **refine** the task until *primitive* actions are reached!

```
(travel-to TimeSqaure)
  ↓
(taxi-to airport);
(fly-to JFK); ...
```

Provides **guidance** but still requires **planning**!

TERMINOLOGY: PRIMITIVE TASK

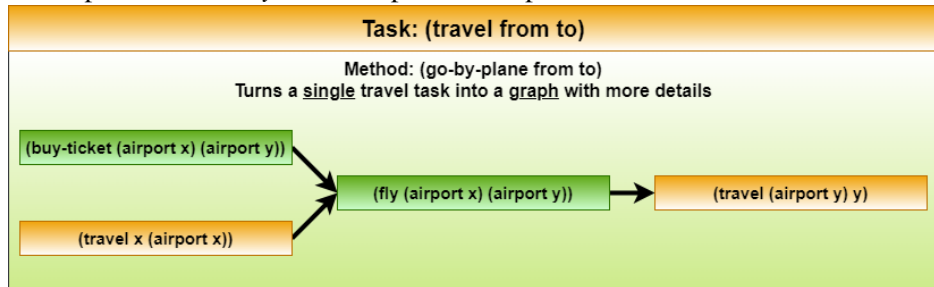
- A **primitive task** corresponds **directly** to an **action**
 - As in classical planning, **what is primitive** depends on:
 - The **execution system**!
 - **How detailed** you want your plans to be!
 - Example:
 - For you the `(fly from to)` may be a primitive task
 - For the pilot, it may be further decomposed into many other smaller steps!
 - **Tasks** can be *ground* or *non-ground*: `(stack A ?x)`
 - No separate terminology, as in *operator/action*

TERMINOLOGY: NON-PRIMITIVE TASK

- A non-primitive task
 - Cannot be directly executed
 - Must be decomposed into 1 or more sub-tasks
- Example:
 - `(put-all-blocks-in-place)`
 - `(make-tower A B C D E)`
 - `(move-stack-of-blocks x y)`

TERMINOLOGY: METHOD

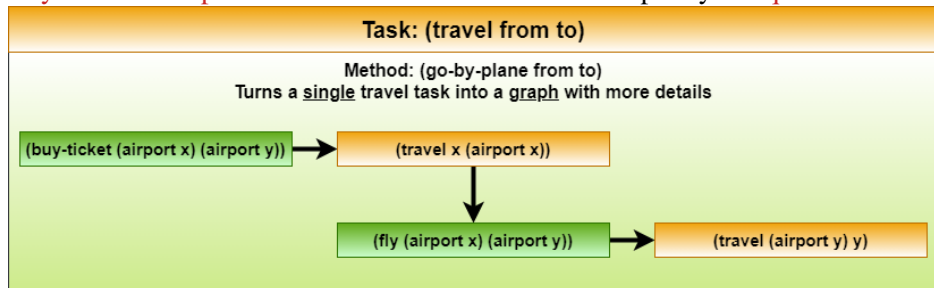
- A **method** specifies *one* way to decompose a non-primitive task into sub-tasks.



- The decomposition is a **graph** $\langle N, E \rangle$
 - Nodes in N correspond to **sub-tasks to perform**
 - Can be primitive or not!
 - Edges in E correspond to **ordering relations**

TOTALLY ORDERED SIMPLE TASK NETWORKS

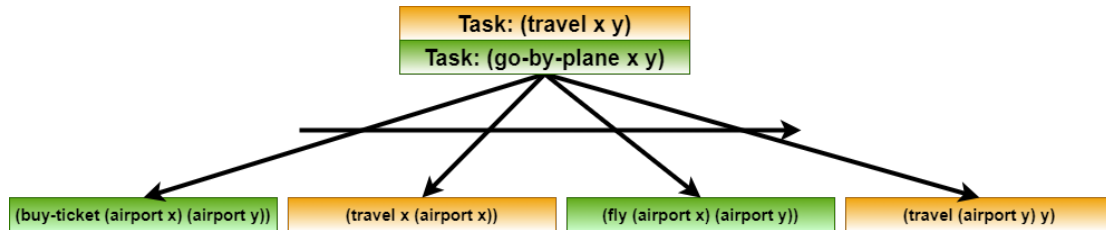
- In **totally ordered simple task networks** each method must specify a **sequence** of sub-tasks!



- Alternatively: A sequence $\langle t_1, \dots, t_k \rangle$
 - \langle (buy-ticket (airport x) (airport y)),
 (travel x (airport x)),
 (fly (airport x) (airport y)),
 (travel (airport y) y) \rangle

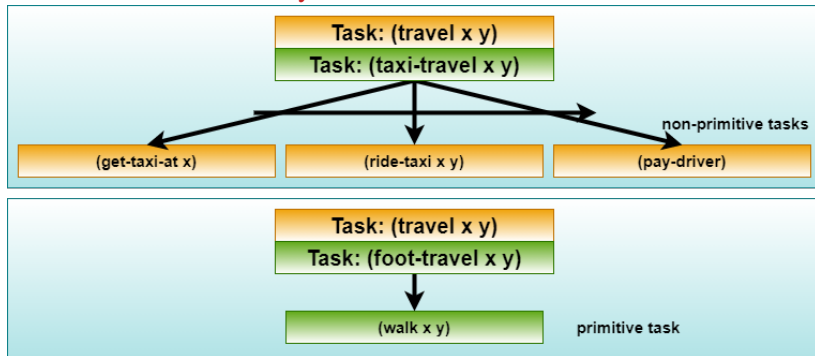
TOTALLY ORDERED SIMPLE TASK NETWORKS

- We illustrate the entire decomposition using an horizontal arrow \longrightarrow to represent the sequence!



MULTIPLE METHODS

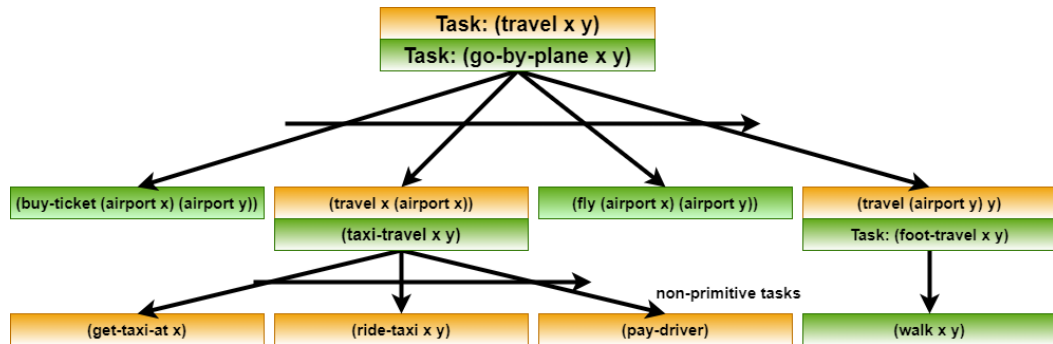
- A non-primitive task can have **many methods**



- \implies You still need to **search** to determine which method to use!
- \implies ... and to determine the *parameters* (discussed later)!

COMPOSITION

- A Hierarchical Task Network plan:
 - Hierarchical
 - Consists of **tasks**
 - Based on graphs \approx **networks**



DOMAINS, PROBLEMS, SOLUTIONS

- A Simple Task Network **planning domain** specifies:
 - A set of **tasks**
 - A set of **operators** used as primitive tasks
 - A set of **methods**

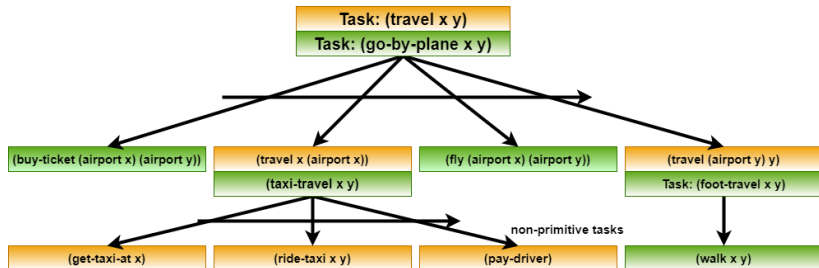
- A Simple Task Network **problem instance** specifies:
 - A Simple Task Network planning domain
 - An **initial state**
 - An **initial task network** which shall be ground (no variables)
 - A total order Simple Task Network example:


```
⟨(travel home work), (do-work), (travel work home)⟩
```

General Hierarchical Task Networks can have additional constraints to be enforced!

DOMAINS, PROBLEMS, SOLUTIONS (CONT.)

- Suppose you:
 - Start with the **initial task network**
 - Recursively apply **methods** to non-primitive tasks expanding them
 - Continue until **all non-primitive tasks are expanded**



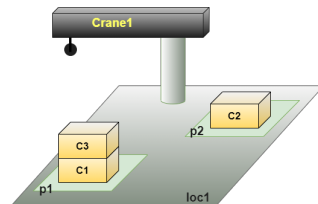
- Totally ordered \implies yields an action **sequence**
 - If this is executable: A **solution**
 - No goals to check – they are implicit in the method structure!

DOMAINS, PROBLEMS, SOLUTIONS (CONT.)

- Hierarchical Task Network planning uses **only** the methods specified for a given task
 - Will **not** try arbitrary actions...
 - For this to be useful, you must **have** useful "*recipes*" for all tasks!

DOCK WORKER ROBOTS

- Example tasks:
 - Primitive – All the DWR actions we considered so far
 - Move the **topmost** container between piles
 - Move the **entire stack** from one pile to another
 - Move a stack, but keep it in the **same order**
 - Move **several stacks** in the same order
 - ...



METHODS

- To **move top most container** from one pile to another

- **task**

`(move-topmost-container pile1 pile2)`

The *task* has parameters
given from above

- **method**

`(take-and-put cont crane loc
pile1 pile2 c1 c2)`

A *method* can have additional
parameters, whose values are
chosen by the planner
– as in classical planning!

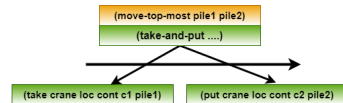
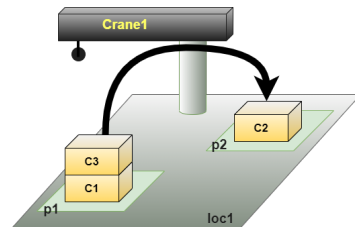
- **precond:** `(attached pile1 loc)`
`(attached pile2 loc)`
`(belong crane loc) (top cont pile1)`
`(on cont c1) (top c2 pile2)`

The *precond* adds constraints:
crane must be *some* crane in
the same loc as the piles, cont
must be the top most container of
pile1, ...

Intepretation: If you're asked to `(move-topmost-container pile1 pile2)`, check all possible values for `cont`, `crane`, `loc`, `c1`, `c2` where the preconditions are satisfied!

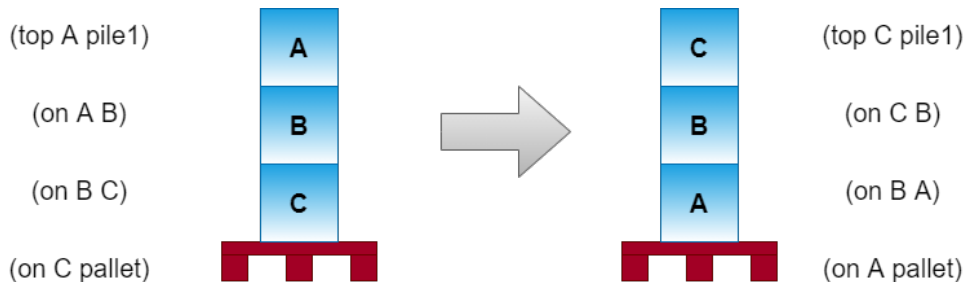
METHODS

- To **move top most container** from one pile to another
 - **task**
`(move-topmost-container pile1 pile2)`
 - **method**
`(take-and-put cont crane loc
 pile1 pile2 c1 c2)`
 - **precond:** `(attached pile1 loc)`
`(attached pile2 loc)`
`(belong crane loc) (top cont pile1)`
`(on cont c1) (top c2 pile2)`
 - **subtasks:** `{ (take crane loc cont c1 pile1),
 (put crane loc cont c2 pile2) }`



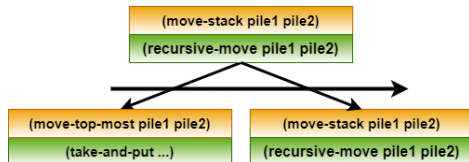
MOVING A STACK OF CONTAINERS

- How can we implement the `(move-stack pile1 pile2)?`
 - Should we move **all** containers in a stack?
 - There is no **limit** on how many there might be...



RECURSION

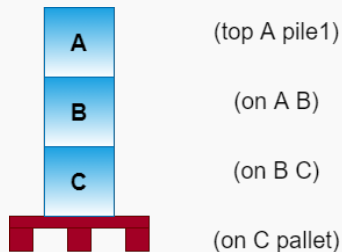
- We need a **loop** with a **termination condition**
 - Hierarchical Task Network planning allows **recursion**
 - Move the **topmost** container (we know how to do that!)
 - Then move the **rest**
- First attempt:
 - **task:** `(move-stack pile1 pile2)`
 - **method:** `(recursive-move pile1 pile2)`
 - **precond:** `True`
 - **subtasks:** `((move-topmost-container pile1 pile2),
(recursive-move pile1 pile2))`



RECURSION (CONT.)

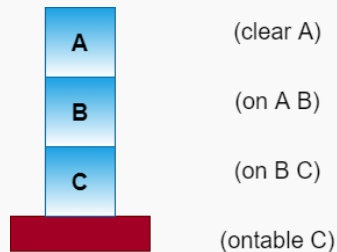
- Let's consider the BW and the DWR "pile models"...

BW



The bottom block is not "on" anything!

DWR



The bottom block is "on" the pallet, a "special container"!

What if the pallet is "topmost"? We do not want to move it!

RECURSION (CONT.)

- To fix this

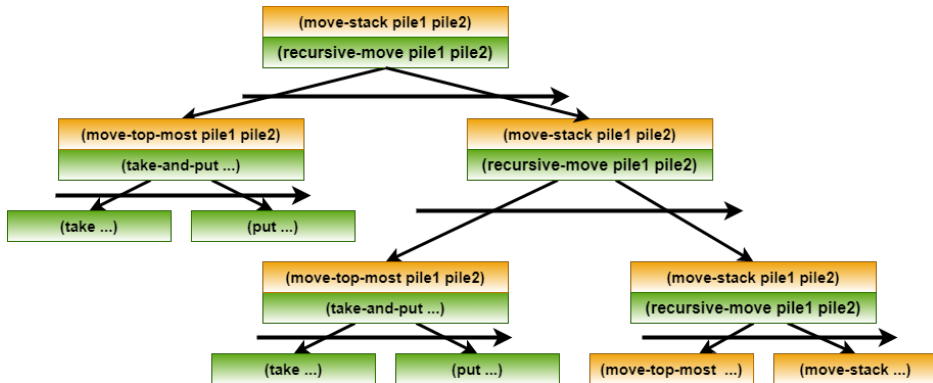
- **task:** `(move-stack pile1 pile2)`
- **method:** `(recursive-move pile1 pile2 cont x)`
- **precond:** `(top cont pile1) (on cont x)`
- **subtasks:** `{ (move-topmost-container pile1 pile2)
 (move-stack pile1 pile2) }`

`cont` is on top of something (i.e. `x`), so `cont` can't be the pallet!

We added two additional method parameters (`cont` `x`) – "non-natural", as in "ordinary" planning \implies does not give the planner a real choice!

RECURSION (CONT.)

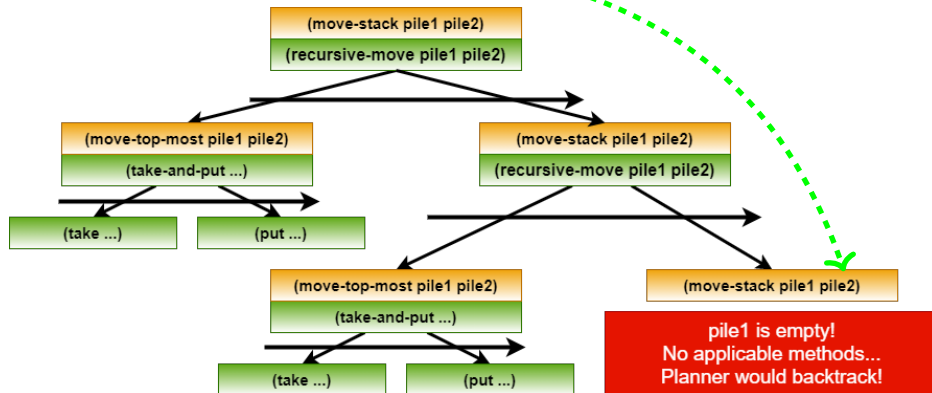
- The planner can create a structure like this...



- ... but when will **the recursion end?**

RECURSION (CONT.)

- At some point, **only the pallet** will be left in the stack
 - The recursive-move will **not be applicable**
 - But we **must** execute **some** form of move-stack!



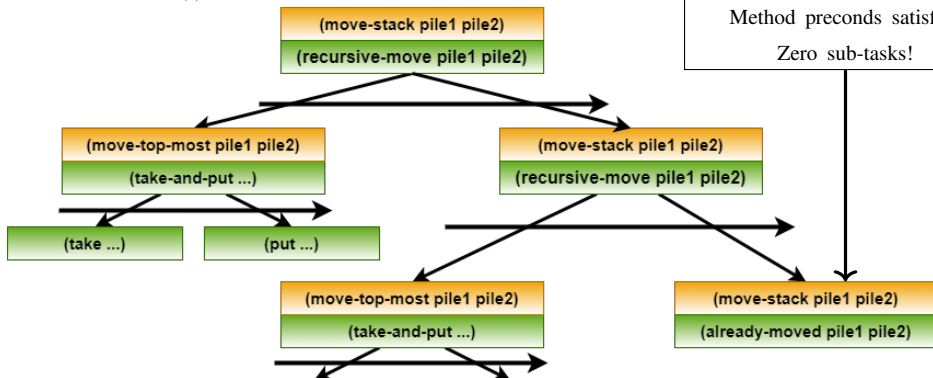
RECURSION (CONT.)

- We need a method that **terminates** the recursion

- task:** `(move-stack pile1 pile2)`
- method:** `(already-moved pile1 pile2)`
- precond:** `(top pallet pile1)`
- subtasks:** `<>`

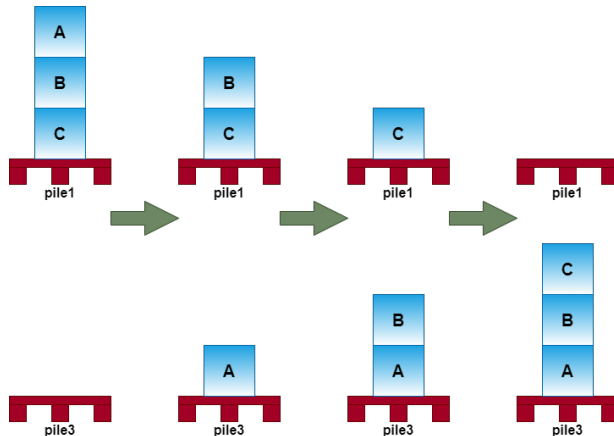
Unique pallet object
not a variable

Method preconds satisfied
Zero sub-tasks!



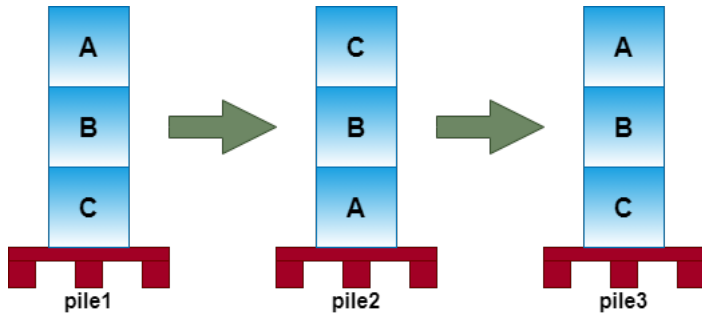
ORDERING

- Using move-stack inverts a stack!



ORDERING (CONT.)

- To avoid this: use intermediate pile



ORDERING (CONT.)

• Example

- **task:** `(move-stack-same-order pile1 pile2)`
- **method:** `(move-each-twice pile1 pileX pile2 loc)`
- **precond:** `(top pallet pileX)`
`(!= pile1 pileX)`
`(!= pile2 pileX)`
`(!= pile1 pile2)`
`(attached ...) // all in the same loc`
`...`
- **subtasks:** `{ (move-stack pile1 pileX),`
`(move-stack pileX pile2) }`

Unlike classical planning,
someone *specifies* the task!,
pile1 and pile2

The planner must choose
a matching **method** ("im-
plementation") to use

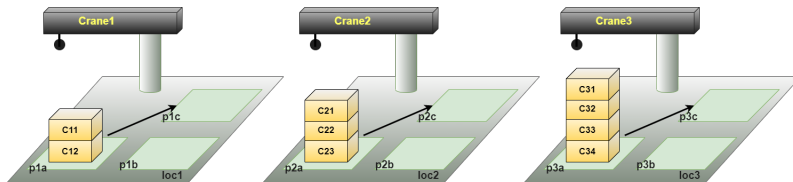
The planner must choose
added method params pileX
loc to satisfy the precondition!

Why does pileX have to be empty initially?

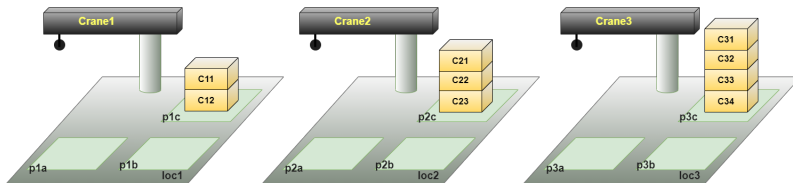
Because the second move-stack moves **all** containers from the intermediate pileX to destination pile2!

OVERALL OBJECTIVE

- Moving three entire stacks of containers preserving order!



Initial state, with three locations, three piles to move



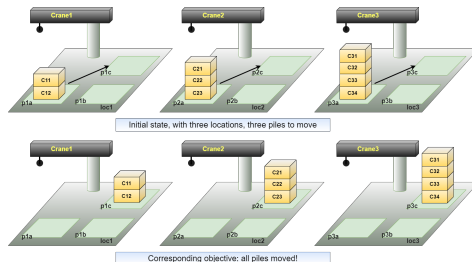
Corresponding objective: all piles moved!

OVERALL OBJECTIVE: DEFINING A TASK

- Define a **task** for this objective!

- task:** (move-three-stacks)
- method:** (move-each-twice)
- precond:** // no preconditions apart from the sub-tasks'
- subtasks:** $\{$ (move-stack-same-order p1a p1c),
 (move-stack-same-order p2a p2c),
 (move-stack-same-order p3a p3c) $\}$

- Use this task as the *initial task network*



GOAL PREDICATES IN HIERARCHICAL-TASK NETWORKS

- Here the entire objective is encoded in the initial network

`(move-three-stacks)`

- \Rightarrow `((move-stack-same-order pla p1c),
 (move-stack-same-order p2a p2c),
 (move-stack-same-order p3a p3c))`

- To avoid this:

- New predicate `(should-move-same-order pile pile)` encoding the goal!

- task:** `(move-as-necessary)`
- method:** `(move-and-repeat pile1 pile2)`
- precond:** `(should-move-same-order pile1 pile2)`
- subtasks:** `((move-stack-same-order pile1 pile2), ; ; makes should-move-... false
 (move-as-necessary))`
- task:** `(move-as-necessary)`
- method:** `(all-done)`
- precond:** `(not (exists pile1 pile2
 [(should-move-same-order pile1 pile2)]))`
- subtasks:** `()`

UNINFORMED PLANNING IN HIERARCHICAL-TASK NETWORKS

- Can even do **uninformed unguided planning**

- Doing *something, anything*:

- Task (do-something) \implies operator (pickup x)
- Task (do-something) \implies operator (putdown x)
- Task (do-something) \implies operator (stack x y)
- Task (do-something) \implies operator (unstack x y)

Planner chooses
all parameters!

- Repeating

- Task (achieve-goals) \implies \langle (do-something), (achieve-goals) \rangle

- Ending

- Task (achieve-goals) \implies $\langle \rangle$, with precondition: entire goal is satisfied!

Or combine **aspects** of this model with **other aspects** of "standard" HTN models!

DELIVERY: FIRST VARIATION

- Delivery:

- A single truck
- Pick-up a package, drive to destination, unload

- **task:** `(deliver package dest)`
- **method:** `(move-by-truck package packageloc dest)`
- **precond:** `(at package packageloc)`
- **subtasks:** `{ (driveto packageloc), (load package),
(driveto dest), (unload package) }`

What if the truck is already at the package location?

First driveto is unnecessary!

DELIVERY: SECOND VARIATION

- Alternative: Two alternative methods deliver

- task:** `(deliver package dest)`
 - method:** `(move-by-truck-1 package packageloc truckloc dest)`
 - precond:** `(at truck truckloc) (at package packageloc) (= truckloc packageloc)`
 - subtasks:** `((load package), (driveto dest), (unload package))`
- task:** `(deliver package dest)`
 - method:** `(move-by-truck-2 package packageloc truckloc dest)`
 - precond:** `(at truck truckloc) (at package packageloc) (!= truckloc packageloc)`
 - subtasks:** `((driveto packageloc), (load package),
(driveto dest), (unload package))`

Do we really have to repeat the entire task?

Many "conditional" sub-tasks \implies combinatorial explosion!

DELIVERY: THIRD VARIATION

- Make the choice in the sub-task instead!

- **task:** `(deliver package dest)`
- **method:** `(move-by-truck-3 package packageloc truckloc dest)`
- **precond:** `(at truck truckloc) (at package packageloc)`
- **subtasks:** `((be-at packageloc), (load package), (be-at dest), (unload package))`

- **task:** `(be-at loc)`
- **method:** `(drive loc)`
- **precond:** `(not (at truck loc))`
- **subtasks:** `((driveto loc))`

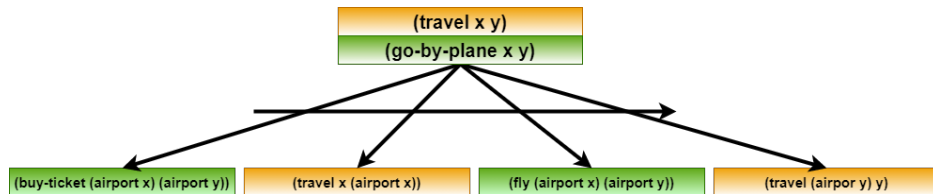
- **task:** `(be-at loc)`
- **method:** `(already-there)`
- **precond:** `(at truck loc)`
- **subtasks:** `()`

SEARCH SPACES

- Need **search space**
 - 1) A **node structure** defining what information is in a node
 - 2) A way of creating an **initial node** from a problems instance
 - 3) A **successor function** / branching rule returning all successors
 - 4) A **solution criterion** detecting if a node corresponds to a solution
 - 5) A **plan extractor** telling us which plan a solution node a corresponds to
- Different alternatives exist!

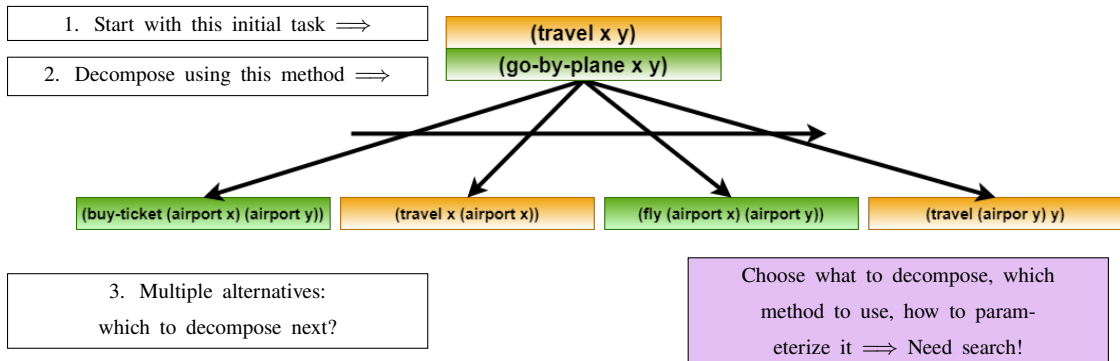
TOTAL ORDER?

- Basic **assumption**: Total Order Simple Task Networks
 - Any **initial task** is totally ordered
 - Any **decomposition method** is totally ordered



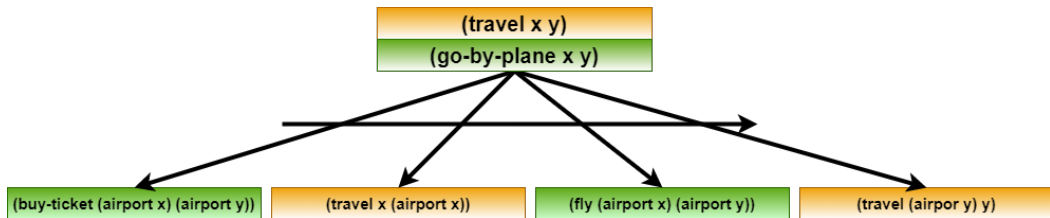
FORWARD DECOMPOSITION?

- Different **decomposition orders** are still possible

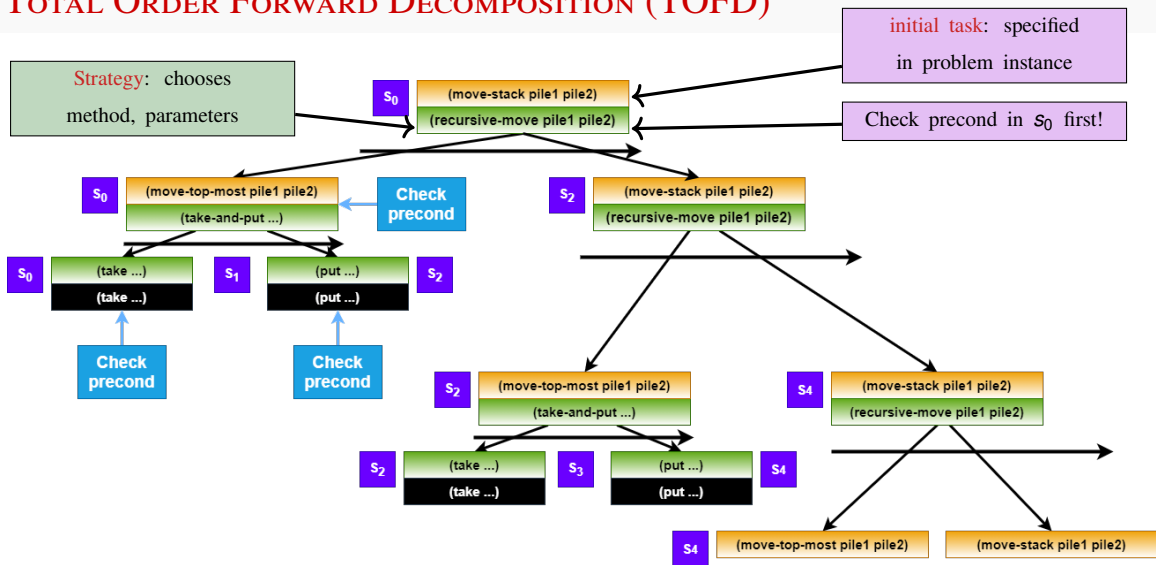


FORWARD DECOMPOSITION!

- **Forward** decomposition: One of many possibilities
 - Go "depth first, left to right"
 - Like forward state space search:
 - Generates actions in the same order in which they will be executed
 - \Rightarrow When we decompose a task, we know the "current" state of the world!



TOTAL ORDER FORWARD DECOMPOSITION (TOFD)



TOFD NODE STRUCTURE

- [1] A **node structure** defining what information is in a node
 - Plan so far
 - Current state - **possible due to forward decomposition**
 - Remaining tasks to expand
- [2] A way of creating an initial search node:



← No actions so far
Current state s_0
Remaining tasks = the initial task from the problem!

- Examples: Nodes visited in the previous slide



TOFD SUCCESSORS

• [3] Successors:

- We know which task to decompose
- Find all applicable methods and apply them



• [4] Solution test

- No more tasks \implies done!

• [5] Solution extraction

- The resulting search node *contains* a sequential plan!

SOLVING TOTAL ORDER STN PROBLEMS

- TOFD takes a search node
 - π - a sequence of actions
 - s - the current state
 - $\langle t_1, \dots, t_k \rangle$ - a list of tasks to be achieved in **the specific order**
- We also assume:
 - O - the available operators (with params, preconds, effects)
 - M - the available methods (with params, preconds, subtasks)
- **Returns**
 - A sequential plan
 - Loses the hierarchical structure of the final plan
 - Simplifies the presentation - but the structure *could* also be kept!

TOFD: BASE CASE

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

$\rightarrow [2]$

open $\leftarrow \{\text{initial-node}\}$

while (open $\neq \emptyset$) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

$\rightarrow [6]$ TOFD uses depth first search

$\rightarrow [4]$ If we have no tasks left to decompose..

if $k = 0$ **then return** π

TOFD: GROUND PRIMITIVE TASKS

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

open $\leftarrow \{\text{initial-node}\}$

while (open $\neq \emptyset$) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

if $k = 0$ **then return** π

if t_1 is primitive **then**

$\text{actions} \leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$

$\text{candidates} \leftarrow \{ a \mid a \in \text{actions} \wedge \text{name}(a) = t_1 \wedge a \text{ applicable in } \mathcal{S} \}$

\rightarrow For simplicity: The case when all tasks to achieve are ground

$\rightarrow [2]$

$\rightarrow [6]$ TOFD uses depth first search

$\rightarrow [4]$ If we have no tasks left to decompose..

\rightarrow A primitive task is decomposed into a single action!
Possibly many to choose from!



TOFD: SUCCESSORS

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

open $\leftarrow \{\text{initial-node}\}$

while (open $\neq \emptyset$) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

if $k = 0$ **then return** π

if t_1 is primitive **then**

$\text{actions} \leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$

$\text{candidates} \leftarrow \{ a \mid a \in \text{actions} \wedge \text{name}(a) = t_1 \wedge a \text{ applicable in } \mathcal{S} \}$

for each $a \in \text{candidates}$ **do**

$\pi' \leftarrow \pi + a$

$s' \leftarrow \gamma(\mathcal{S}, a)$

$\text{rest} \leftarrow \langle t_2, \dots, t_k \rangle$

$\text{open} \leftarrow \text{open} \cup \{ \langle \pi', s', \text{rest} \rangle \}$

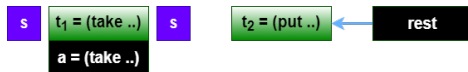
→ *For simplicity: The case when all tasks to achieve are ground*

→ [2]

→ *A primitive task is decomposed into a single action!*
→ *Possibly many to choose from!*

→ *Add action at the end*

→ *Apply the action, find the new state*



TOFD: LIFTED PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$ 
  open  $\leftarrow \{\text{initial-node}\}$ 
  while (open  $\neq \emptyset$ ) do
     $\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
    if  $k = 0$  then return  $\pi$ 
    if  $t_1$  is primitive then
      actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
      candidates  $\leftarrow \{ (a, \sigma) \mid a \in \text{actions} \wedge \text{name}(a) = \sigma(t_1) \wedge a \text{ applicable in } \mathcal{S} \}$ 

```

\rightarrow The case when all tasks to achieve are non-ground. The plan will still be ground

$\rightarrow [2]$

\rightarrow A primitive task is decomposed into a single action!
Possibly many to choose from!

\rightarrow σ is a substitution function! Basically, σ can specify variable bindings for parameters of $t_1 \dots$



TOFD: LIFTED PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$ 
  open  $\leftarrow \{\text{initial-node}\}$ 
  while (open  $\neq \emptyset$ ) do
     $\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
    if  $k = 0$  then return  $\pi$ 
    if  $t_1$  is primitive then
      actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
      candidates  $\leftarrow \{ (a, \sigma) \mid a \in \text{actions} \wedge \text{name}(a) = \sigma(t_1) \wedge a \text{ applicable in } \mathcal{S} \}$ 
      for each  $a, \sigma \in \text{candidates}$  do
         $\pi' \leftarrow \pi + a$ 
         $\mathcal{S}' \leftarrow \gamma(\mathcal{S}, a)$ 
        rest  $\leftarrow \langle \sigma(t_2), \dots, \sigma(t_k) \rangle$ 
        open  $\leftarrow \text{open} \cup \{ \langle \pi', \mathcal{S}', \text{rest} \rangle \}$ 

```

→ The case when all tasks to achieve are non-ground. The plan will still be ground

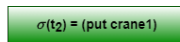
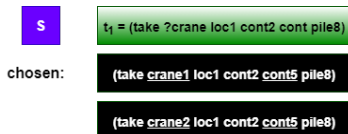
→ [2]

→ A primitive task is decomposed into a single action!
→ Possibly many to choose from!

→ Add action at the end

→ Apply the action, find the new state

→ Must have the same variable bindings!



$\sigma = \{ ?\text{crane} \rightarrow \text{crane1}, ?\text{cont} \rightarrow \text{cont5} \}$

$\sigma = \{ ?\text{crane} \rightarrow \text{crane2}, ?\text{cont} \rightarrow \text{cont5} \}$

TOFD: NON-PRIMITIVE TASKS

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

open $\leftarrow \{\text{initial-node}\}$

while (open $\neq \emptyset$) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

if $k = 0$ **then return** π

if t_1 is primitive **then**

...

else

$\text{ground} \leftarrow \text{GROUND-INSTANCES-OF-METHODS}(M)$

$\text{candidates} \leftarrow \{ (m, \sigma) \mid m \text{ ground} \wedge \text{task}(m) = \sigma(t_1) \wedge m \text{ applicable in } \mathcal{S} \}$

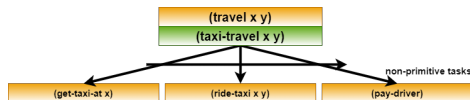
→ The case when all tasks to achieve are non-ground. The plan will still be ground

→ [2]

→ t_1 is e.g. (travel LiU Resecentrum)

→ A non-primitive task is decomposed into a new task-list.

→ May have many methods to choose from!



TOFD: NON-PRIMITIVE TASKS (CONT.)

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$ 
  open  $\leftarrow \{\text{initial-node}\}$ 
  while (open  $\neq \emptyset$ ) do
     $\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
    if  $k = 0$  then return  $\pi$ 
    if  $t_1$  is primitive then
      ...
    else
      ground  $\leftarrow \text{GROUND-INSTANCES-OF-METHODS}(M)$ 
      candidates  $\leftarrow \{ (m, \sigma) \mid m \text{ ground} \wedge \text{task}(m) = \sigma(t_1) \wedge m \text{ applicable in } \mathcal{S} \}$ 
      for each  $(m, \sigma) \in \text{candidates}$  do
         $\pi' \leftarrow \pi$ 
         $s' \leftarrow s$ 
        rest  $\leftarrow \langle \text{SUBTASKS}(m) + \sigma(t_2), \dots, \sigma(t_k) \rangle$ 
        open  $\leftarrow \text{open} \cup \{ \langle \pi', s', \text{rest} \rangle \}$ 

```

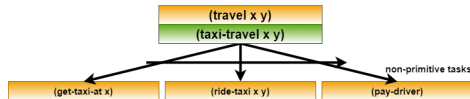
→ The case when all tasks to achieve are non-ground. The plan will still be ground

→ [2]

→ No action needed!

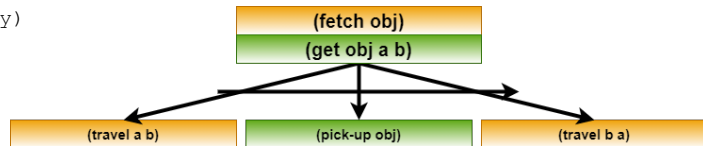
→ No state change

→ Prepend new list! The "origin" of a task is discarded: only the sub-tasks are relevant!



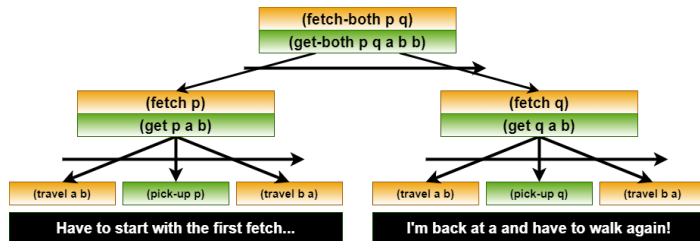
LIMITATIONS OF ORDERED-TASK PLANNING

- TOFD requires **totally ordered** methods
 - Can't interleaves sub-tasks of different tasks
- Suppose we want to **fetch one object** somewhere, then return to where we are now
 - task:** (fetch obj)
 - method:** (get obj mypos objpos)
 - precond:** (robotat mypos) (at obj objpos)
 - subtasks:** { (travel mypos objpos), (pick-up obj), (travel objpos mypos) }
- task:** (travel x y)
- method:** (walk x y)
- method:** (stayat x y)



LIMITATIONS OF ORDERED-TASK PLANNING (CONT.)

- Suppose we want to fetch **two** objects somewhere, then return to where we are now
- One idea: Just "fetch" each object in sequence
 - task:** `(fetch-both obj1 obj2)`
 - method:** `(get-both obj1 obj2 mypos objpos1 objpos2)`
 - precond:**
 - subtasks:** `{ (fetch obj1 mypos objpos1), (fetch obj2 mypos objpos2) }`



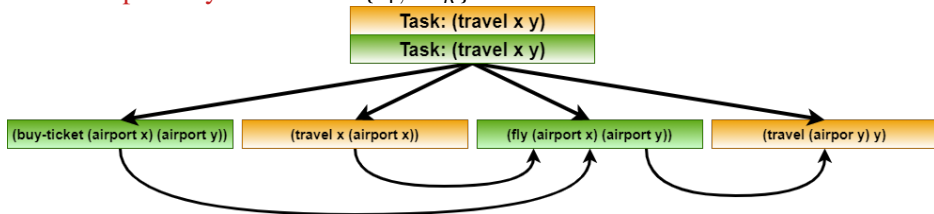
ALTERNATIVE METHODS

- To generate more efficient plans using total-order STNs:
 - Use a different domain model!
 - **task:** `(fetch-both obj1 obj2)`
 - **method:** `(get-both obj1 obj2 mypos objpos1 objpos2)`
 - **precond:** `(!= objpos1 objpos2) (at obj1 objpos1) (at obj2 objpos2)`
 - **subtasks:** `{ (travel mypos objpos1), (pick-up obj1),
 (travel objpos1 objpos2), (pick-up obj2),
 (travel objpos2 mypos) }`
 - **task:** `(fetch-both obj1 obj2)`
 - **method:** `(get-both-in-same-place obj1 obj2 mypos objpos)`
 - **precond:** `(at obj1 objpos) (at obj2 objpos)`
 - **subtasks:** `{ (travel mypos objpos), (pick-up obj1),
 (pick-up obj2), (travel objpos mypos) }`

Or: Load-all; drive-truck; unload-all

PARTIALLY ORDERED METHODS

- The sub-tasks are a **partially ordered** set $\{t_1, \dots, t_k\}$ – a *network*

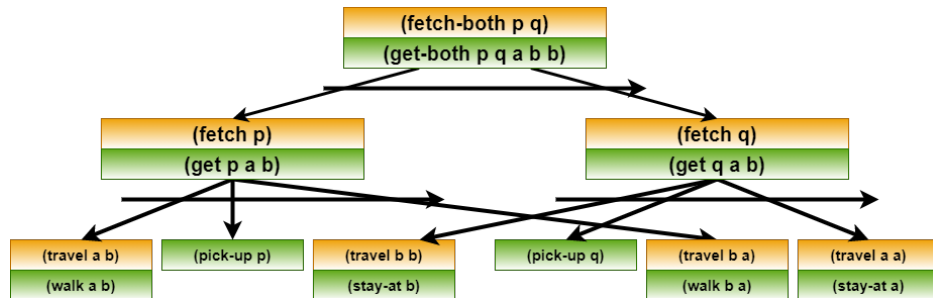


- method:** (go-by-plane x y)
 - task:** (travel x y)
 - precond:** (long-distance x y)
 - network:**

$$\begin{aligned}
 u_1 &= (\text{buy-ticket } (\text{airport } x) (\text{airport } y)) \\
 u_2 &= (\text{travel } x (\text{airport } x)) \\
 u_3 &= (\text{fly } (\text{airport } x) (\text{airport } y)) \\
 u_4 &= (\text{travel } (\text{airport } y) y) \\
 &\{ (u_1, u_3), (u_2, u_3), (u_3, u_4) \}
 \end{aligned}$$

PARTIALLY ORDERED METHODS

- With partially ordered methods **sub-tasks can be interleaved**



- Requires a more complicated planning algorithm: POFD
- SHOP2: implementation of POFD-like algorithm + generalizations

REFERENCES I

- [1] Hector Geffner and Blai Bonet. *A Concise Introduction to Models and Methods for Automated Planning*. Synthesis Lectures on Artificial Intelligence and Machine Learning. Morgan & Claypool Publishers, 2013. ISBN 9781608459698. doi: 10.2200/S00513ED1V01Y201306AIM022. URL <https://doi.org/10.2200/S00513ED1V01Y201306AIM022>.
- [2] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated planning - theory and practice*. Elsevier, 2004. ISBN 978-1-55860-856-6.
- [3] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated Planning and Acting*. Cambridge University Press, 2016. ISBN 978-1-107-03727-4. URL <http://www.cambridge.org/de/academic/subjects/computer-science/artificial-intelligence-and-natural-language-processing/automated-planning-and-acting?format=HB>.
- [4] Patrik Haslum, Nir Lipovetzky, Daniele Magazzeni, and Christian Muise. *An Introduction to the Planning Domain Definition Language*. Synthesis Lectures on Artificial Intelligence and Machine Learning. Morgan & Claypool Publishers, 2019. doi: 10.2200/S00900ED2V01Y201902AIM042. URL <https://doi.org/10.2200/S00900ED2V01Y201902AIM042>.