

COURSE "AUTOMATED PLANNING: THEORY AND PRACTICE"

CHAPTER 10: DOMAIN-CONFIGURABLE PLANNING: HIERARCHICAL TASK NETWORKS

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ASSUMPTIONS

- The fundamental assumptions we considered so far are:

- We only specify: Objects and state variables
- We only specify: initial state and goal
- Physical preconditions and effects of actions



- We only specify what **can** be done!
- The **planner** should decide what **should** be done!



- But... even the most sophisticated heuristics and domain analysis methods lack human intuitions and background knowledge...

DOMAIN-CONFIGURABLE PLANNERS

- How can we make a **planner** take advantage of what **we** know?
- Planners taking advantage of additional knowledge can be called:
 - **Knowledge-rich**
 - **Domain-Configurable**
 - Sometimes **incorrectly** called "**domain-dependent**"

COMPARISON

More Effort

Higher Performance

Domain-Specific

Must write an entire planner
Can specialize the planner for very high performance

Domain-Configurable

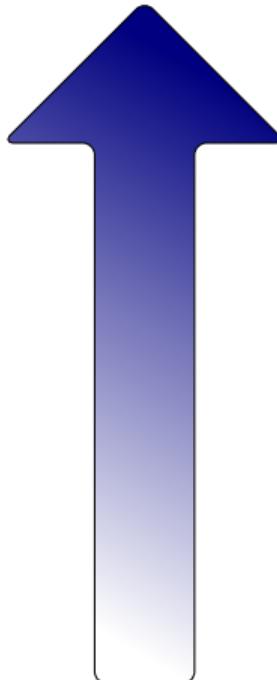
High-level (but sometimes complex) domain definition
Can provide more information for high performance

Domain-Independent

Provide minimal information about actions
Less efficient

COMPARISON (CONT.)

Larger problem classes
can be handled efficiently



Domain-Configurable

Easier to improve expressivity and efficiency
⇒ Often practically useful for a larger set of domains!

Domain-independent

Should be useful for a wide range of domains

Domain-Specific

Only works in a single domain

HIERARCHICAL-TASK NETWORKS: INTUITION

CLASSICAL PLANNING

- Objective is to **achieve a goal**

```
{(at TimeSqaure)}  
{(on A B), (on C D)}  
...
```

- **Find** any sequence of actions that achieves the goal



HIERARCHICAL TASK NETWORKS

- Objective is to **perform a task**

```
{(travel-to TimeSqaure)}  
{(place-blocks-correctly)}  
...
```



- Use "templates" to incrementally **refine** the task until *primitive* actions are reached!

```
(travel-to TimeSqaure)  
    ↓  
    (taxi-to airport);  
    (fly-to JFK); ...
```

Provides **guidance** but still requires **planning**!

TERMINOLOGY: PRIMITIVE TASK

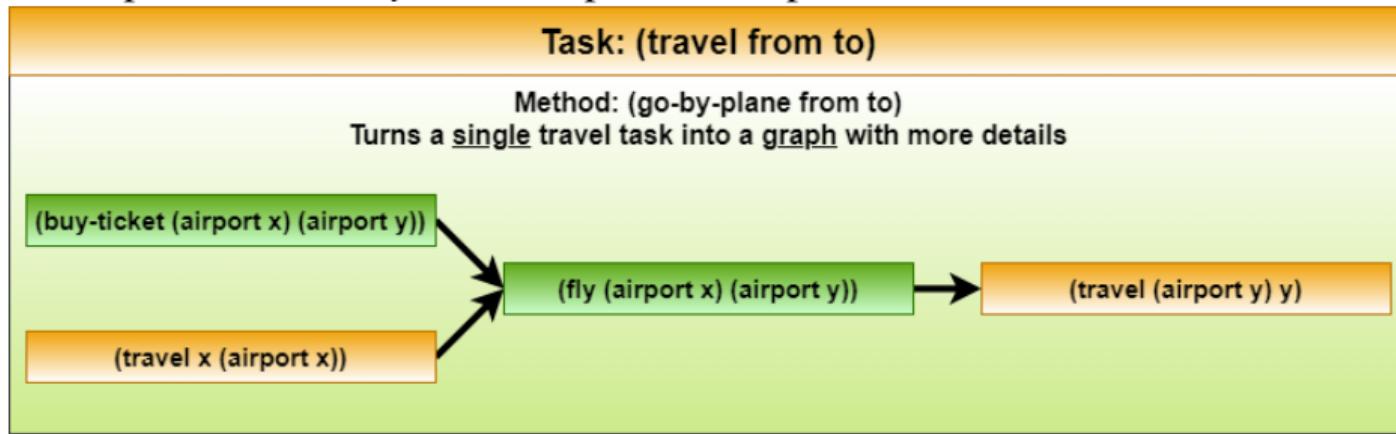
- A **primitive task** corresponds **directly** to an **action**
 - As in classical planning, **what is primitive** depends on:
 - The **execution system!**
 - **How detailed** you want your plans to be!
 - Example:
 - For you the (fly from to) may be a primitive task
 - For the pilot, it may be further decomposed into many other smaller steps!
 - **Tasks** can be *ground* or *non-ground*: (stack A ?x)
 - No separate terminology, as in *operator/action*

TERMINOLOGY: Non-Primitive Task

- A **non-primitive task**
 - Cannot be directly executed
 - Must be **decomposed** into 1 or more **sub-tasks**
- Example:
 - (put-all-blocks-in-place)
 - (make-tower A B C D E)
 - (move-stack-of-blocks x y)

TERMINOLOGY: METHOD

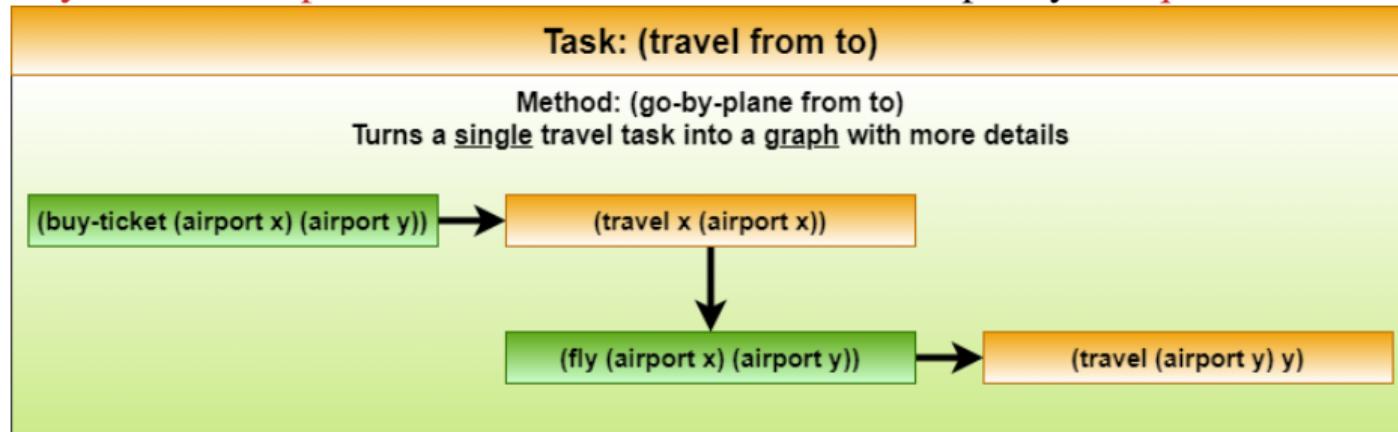
- A **method** specifies *one way* to decompose a non-primitive task into sub-tasks.



- The decomposition is a **graph** $\langle N, E \rangle$
 - Nodes in N correspond to **sub-tasks** to perform
 - Can be primitive or not!
 - Edges in E correspond to **ordering relations**

TOTALLY ORDERED SIMPLE TASK NETWORKS

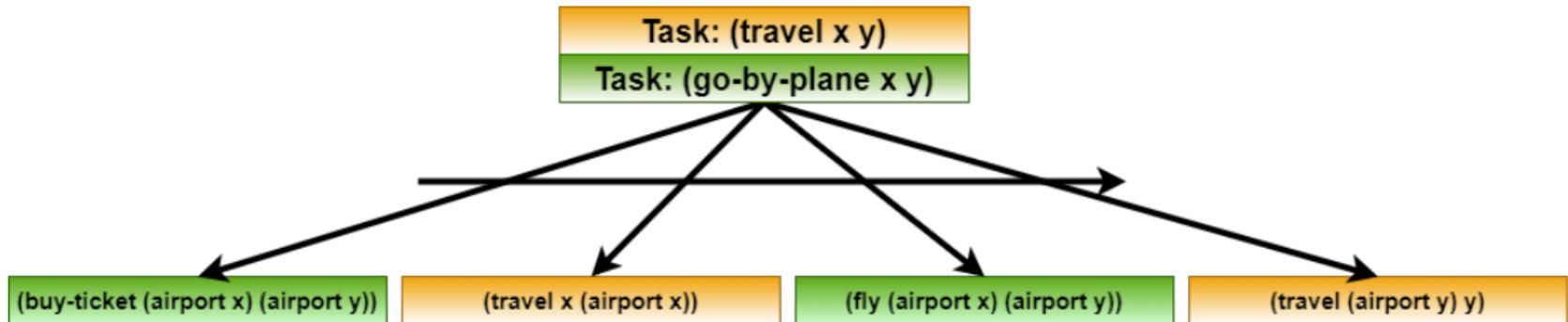
- In **totally ordered simple task networks** each method must specify a **sequence** of sub-tasks!



- Alternatively: A sequence $\langle t_1, \dots, t_k \rangle$
 - $\langle (\text{buy-ticket (airport x) (airport y)}),$
 $(\text{travel x (airport x)}),$
 $(\text{fly (airport x) (airport y)}),$
 $(\text{travel (airport y) y}) \rangle$

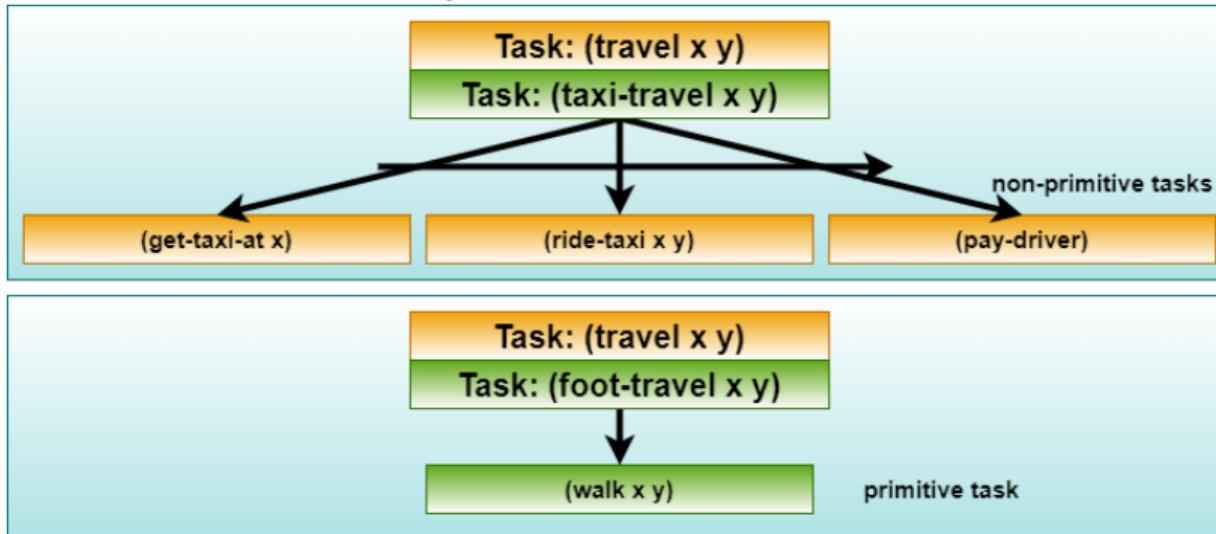
TOTALLY ORDERED SIMPLE TASK NETWORKS

- We illustrate the entire decomposition using an horizontal arrow \longrightarrow to represent the sequence!



MULTIPLE METHODS

- A non-primitive task can have many methods

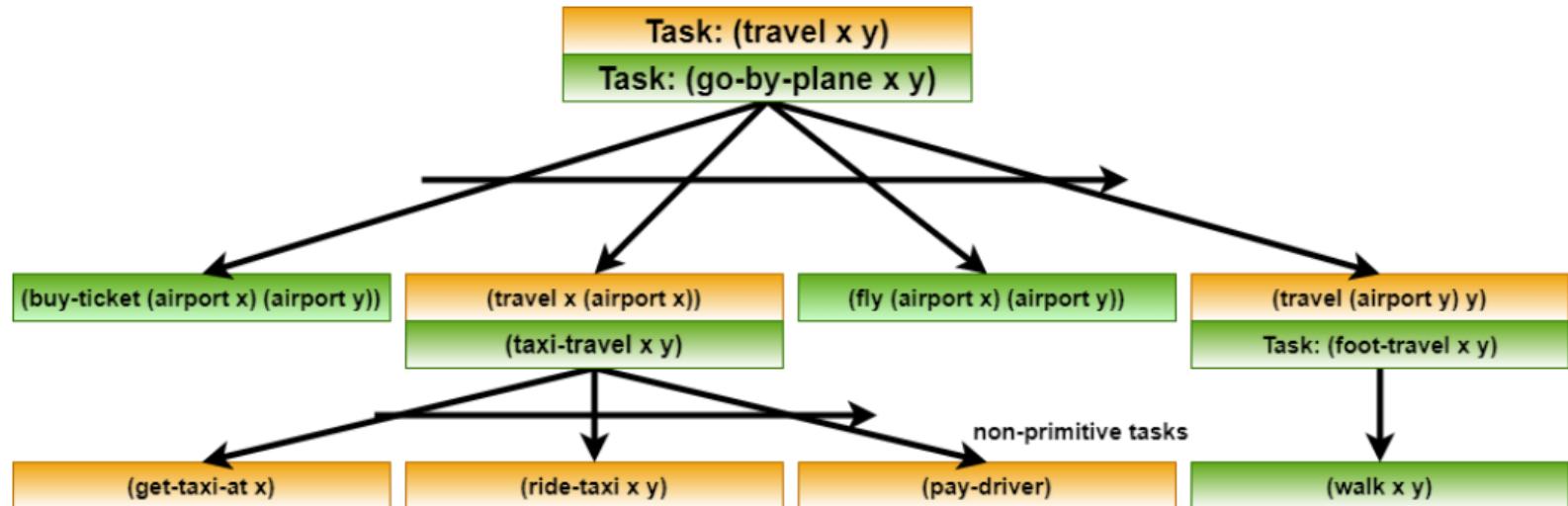


- \Rightarrow You still need to **search** to determine which method to use!
- \Rightarrow ... and to determine the *parameters* (discussed later)!

COMPOSITION

- A Hierarchical Task Network plan:

- Hierarchical
- Consists of **tasks**
- Based on graphs \approx **networks**



DOMAINS, PROBLEMS, SOLUTIONS

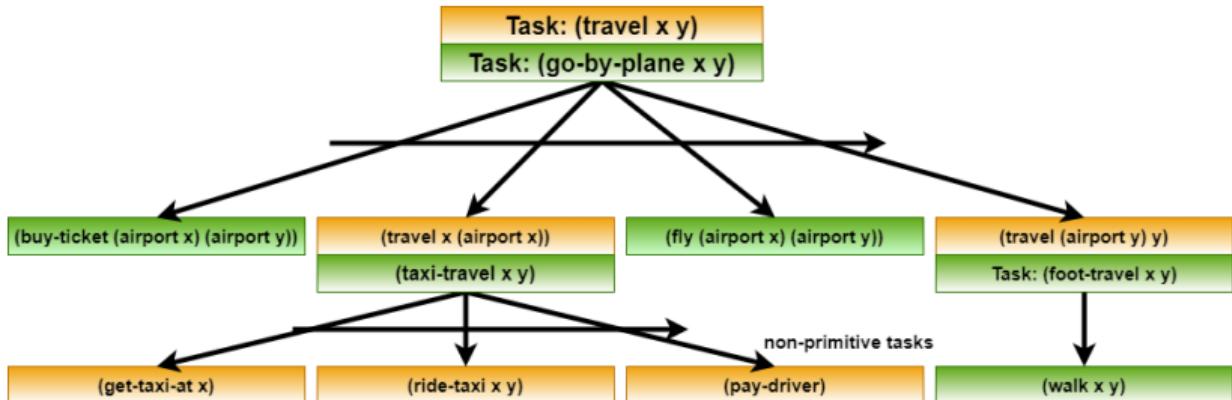
- A Simple Task Network **planning domain** specifies:
 - A set of **tasks**
 - A set of **operators** used as primitive tasks
 - A set of **methods**
- A Simple Task Network **problem instance** specifies:
 - A Simple Task Network planning domain
 - An **initial state**
 - An **initial task network** which shall be ground (no variables)
 - A total order Simple Task Network example:
 $\langle (\text{travel home work}), (\text{do-work}), (\text{travel work home}) \rangle$

General Hierarchical Task Networks can have additional constraints to be enforced!

DOMAINS, PROBLEMS, SOLUTIONS (CONT.)

- Suppose you:

- Start with the **initial task network**
- Recursively apply **methods** to non-primitive tasks expanding them
- Continue until **all non-primitive tasks are expanded**



- Totally ordered \Rightarrow yields an action **sequence**
 - If this is executable: A **solution**
 - No goals to check – they are implicit in the method structure!

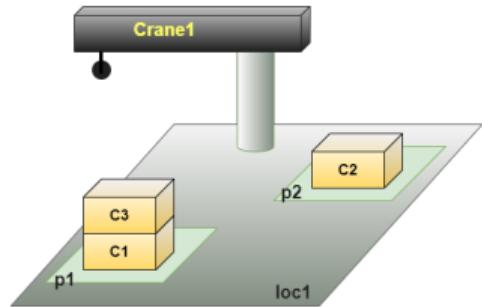
DOMAINS, PROBLEMS, SOLUTIONS (CONT.)

- Hierarchical Task Network planning uses **only** the methods specified for a given task
 - Will **not** try arbitrary actions...
 - For this to be useful, you must **have** useful "*recipes*" for all tasks!

DOCK WORKER ROBOTS

- Example tasks:

- Primitive – All the DWR actions we considered so far
- Move the **topmost** container between piles
- Move the **entire stack** from one pile to another
- Move a stack, but keep it in the **same order**
- Move **several stacks** in the same order
- ...



METHODS

- To move top most container from one pile to another

- **task**

(move-topmost-container pile1 pile2)

The *task* has parameters
given from above

- **method**

(take-and-put cont crane loc
 pile1 pile2 c1 c2)

A *method* can have additional
parameters, whose values are
chosen by the planner
– as in classical planning!

- **precond:** (attached pile1 loc)

(attached pile2 loc)

(belong crane loc) (top cont pile1)

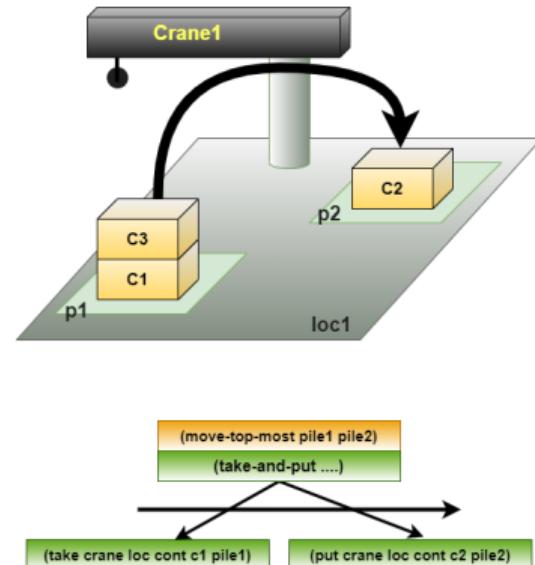
(on cont c1) (top c2 pile2)

The *precond* adds constraints:
crane must be *some* crane in
the same loc as the piles, cont
must be the top most container of
pile1, ...

Interpretation: If you're asked to (move-topmost-container pile1 pile2), check all possible values for cont, crane, loc, c1, c2 where the preconditions are satisfied!

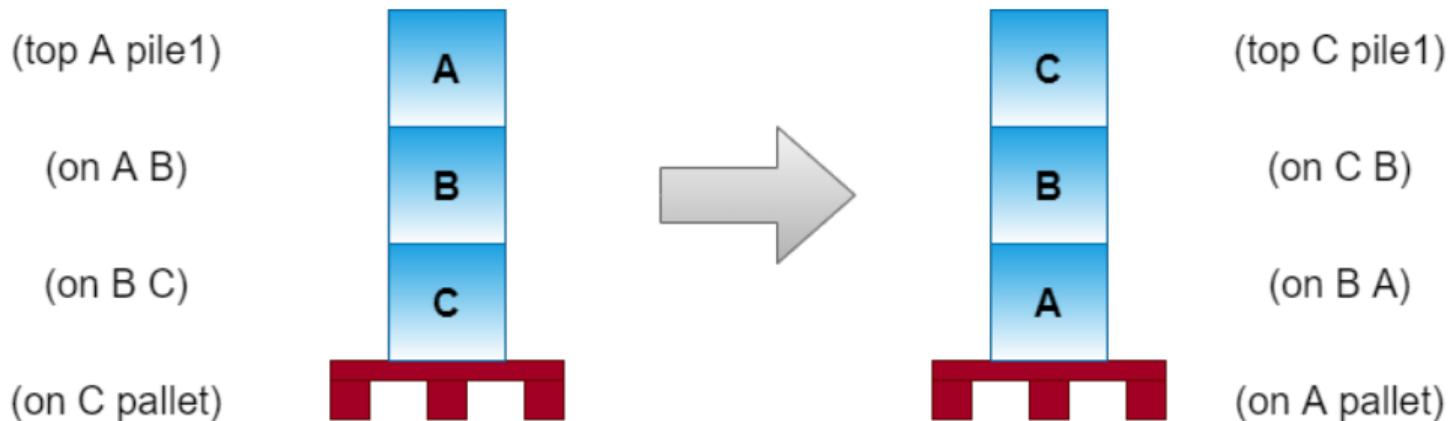
METHODS

- To move top most container from one pile to another
 - task**
 $(move\text{-}topmost\text{-}container \ pile1 \ pile2)$
 - method**
 $(take\text{-}and\text{-}put \ cont \ crane \ loc \ pile1 \ pile2 \ c1 \ c2)$
 - precond:** $(attached \ pile1 \ loc)$
 $(attached \ pile2 \ loc)$
 $(belong \ crane \ loc) \ (top \ cont \ pile1)$
 $(on \ cont \ c1) \ (top \ c2 \ pile2)$
 - subtasks:** $\langle (take \ crane \ loc \ cont \ c1 \ pile1),$
 $\qquad (put \ crane \ loc \ cont \ c2 \ pile2) \rangle$



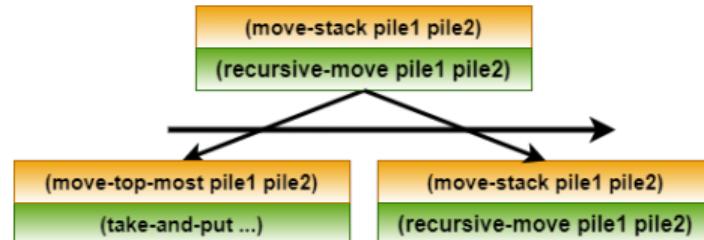
MOVING A STACK OF CONTAINERS

- How can we implement the (move-stack pile1 pile2)?
 - Should we move **all** containers in a stack?
 - There is no **limit** on how many there might be...



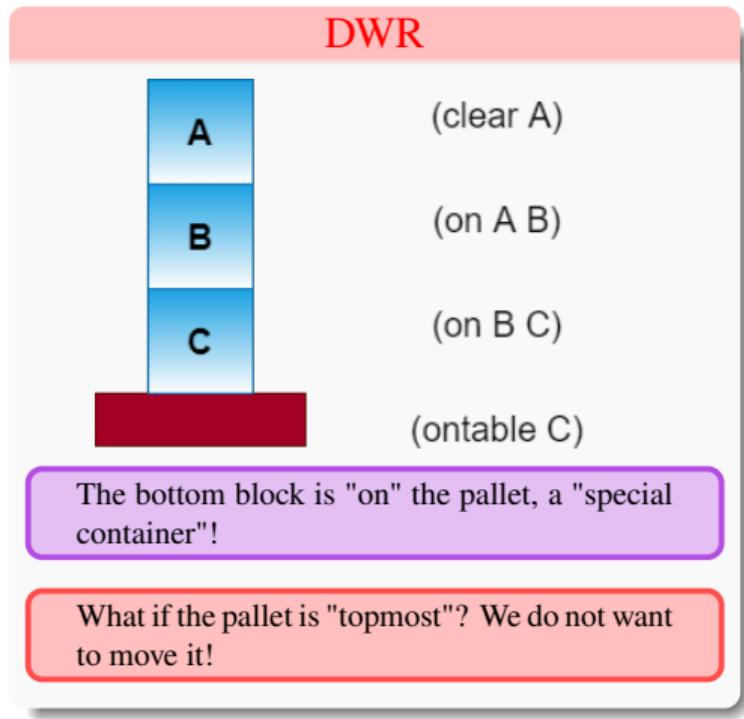
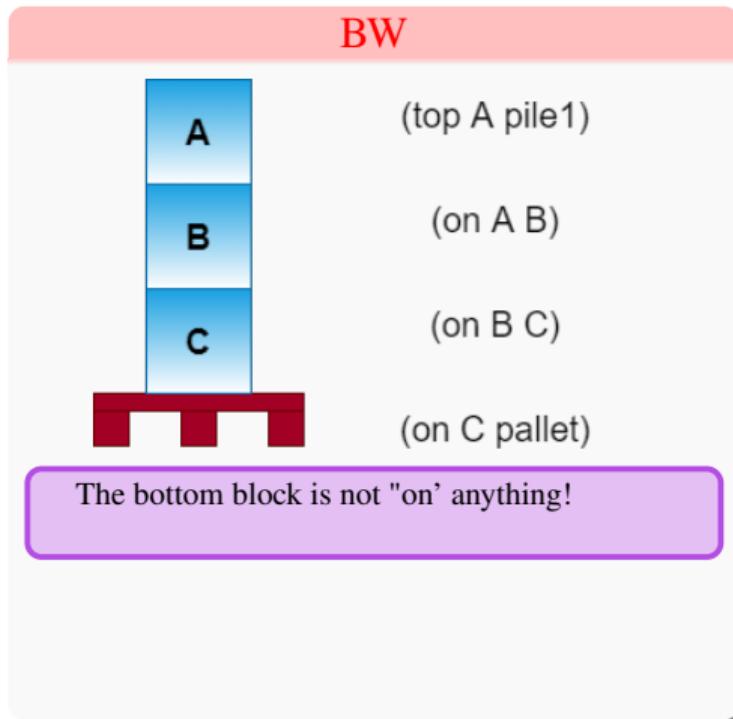
RECURSION

- We need a **loop** with a **termination condition**
 - Hierarchical Task Network planning allows **recursion**
 - Move the **topmost** container (we know how to do that!)
 - Then move the **rest**
 - First attempt:
 - **task:** (move-stack pile1 pile2)
 - **method:** (recursive-move pile1 pile2)
 - **precond:** True
 - **subtasks:** ((move-topmost-container pile1 pile2), (recursive-move pile1 pile2))



RECUSION (CONT.)

- Let's consider the BW and the DWR "pile models"...



RECURSION (CONT.)

- To fix this

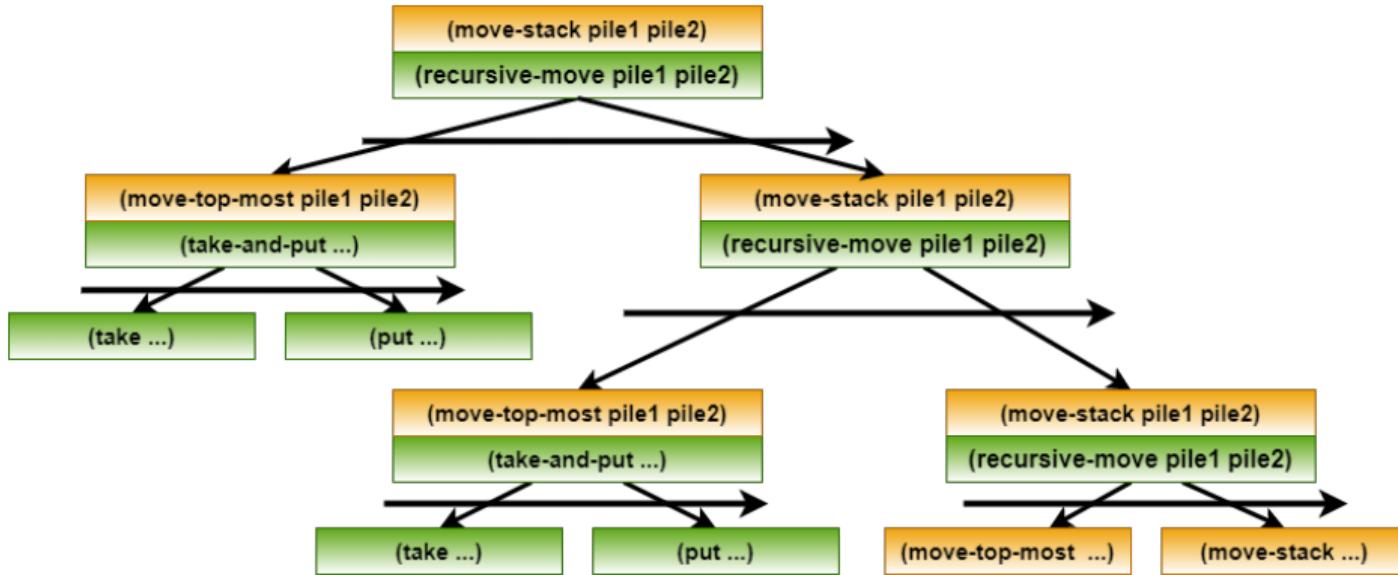
• task:	(move-stack pile1 pile2)
• method:	(recursive-move pile1 pile2 <u>cont</u> x)
• precond:	<u>(top cont pile1) (on cont x)</u>
• subtasks:	$\langle \text{(move-topmost-container pile1 pile2)} \\ \text{(move-stack pile1 pile2)} \rangle$

cont is on top of something (i.e. x), so cont can't be the pallet!

We added two additional method parameters (cont x) – "non-natural", as in "ordinary" planning \Rightarrow does not give the planner a real choice!

RECUSION (CONT.)

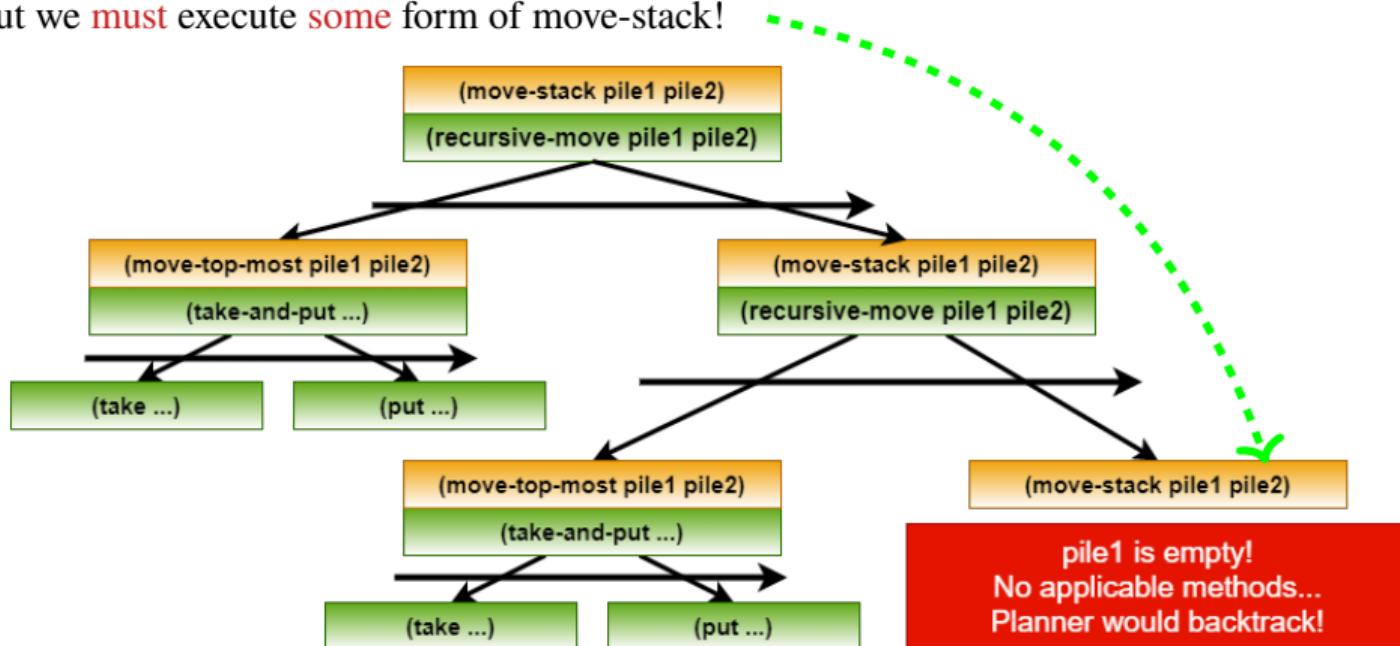
- The planner can create a structure like this...



- ... but when will **the recursion end?**

RECUSION (CONT.)

- At some point, **only the pallet** will be left in the stack
 - The recursive-move will **not be applicable**
 - But we **must** execute **some** form of move-stack!

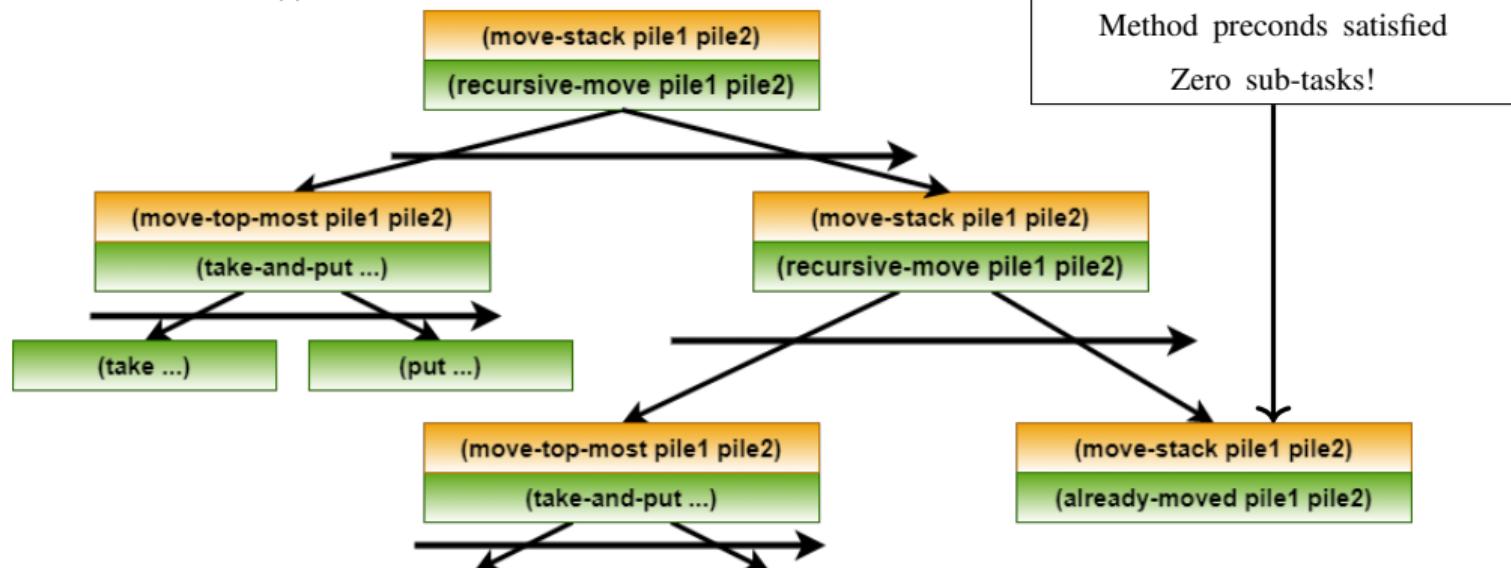


RECUSION (CONT.)

- We need a method that **terminates** the recursion

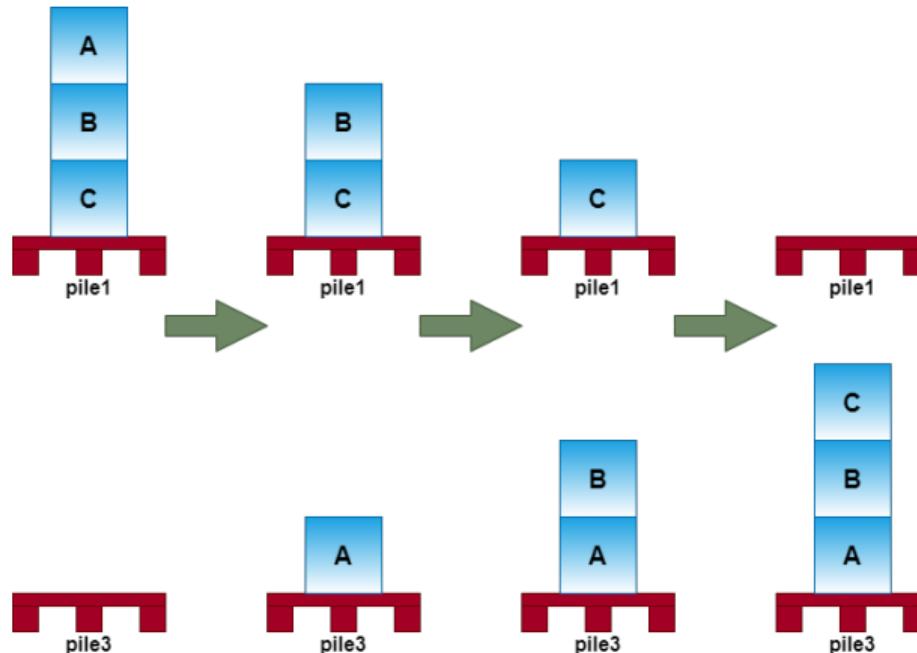
- task:** (move-stack pile1 pile2)
- method:** (already-moved pile1 pile2)
- precond:** (top pallet pile1)
- subtasks:** ()

Unique pallet object
not a variable



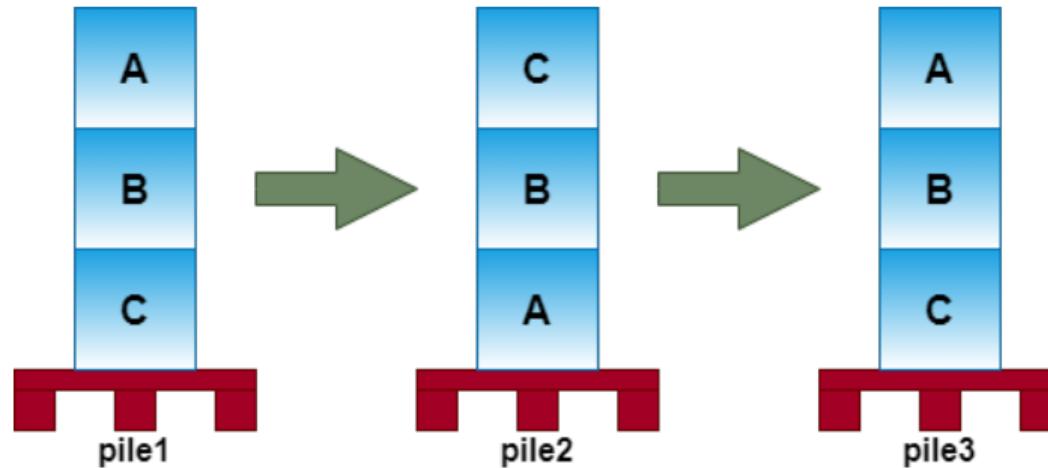
ORDERING

- Using move-stack inverts a stack!



ORDERING (CONT.)

- To avoid this: use intermediate pile



ORDERING (CONT.)

- Example

- **task:** (move-stack-same-order pile1 pile2)
- **method:** (move-each-twice pile1 pileX pile2 loc)
- **precond:**
 - (top pallet pileX)
 - (!= pile1 pileX)
 - (!= pile2 pileX)
 - (!= pile1 pile2)
 - (attached ...) // all in the same loc
 - ...

- **subtasks:** ⟨ (move-stack pile1 pileX) ,
 (move-stack pileX pile2) ⟩

Unlike classical planning,
 someone *specifies* the task!,
 pile1 and pile2

The planner must choose
 a matching **method** ("im-
 plementation") to use

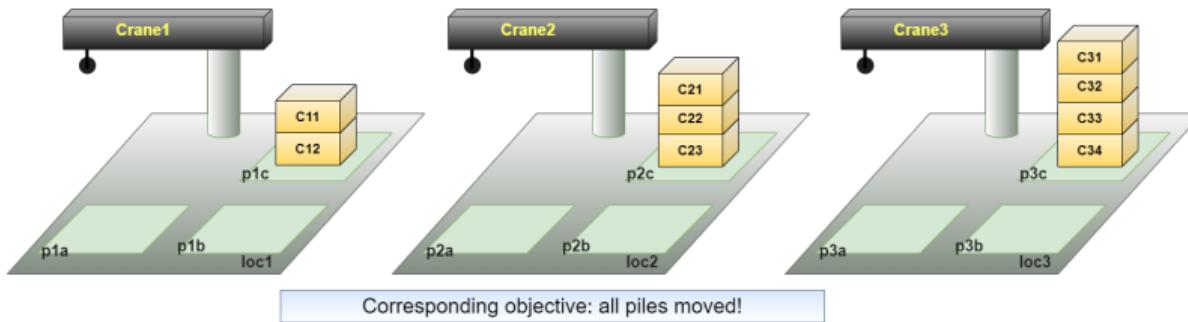
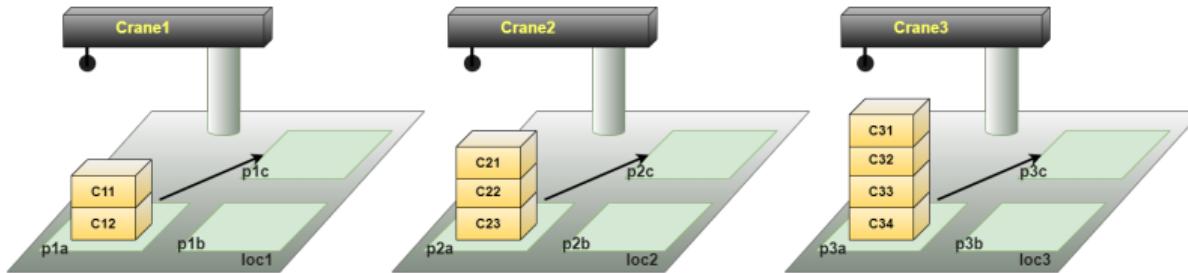
The planner must choose
 added method params pileX
loc to satisfy the precond!

Why does pileX have to be empty initially?

Because the second move-stack moves **all** containers from the intermediate pileX to destination pile2!

OVERALL OBJECTIVE

- Moving three entire stacks of containers preserving order!



OVERALL OBJECTIVE: DEFINING A TASK

- Define a **task** for this objective!

- task:** (move-three-stacks)
- method:** (move-each-twice)
- precond:** // no preconditions apart from the sub-tasks'
- subtasks:** ⟨ (move-stack-same-order p1a p1c),
 (move-stack-same-order p2a p2c),
 (move-stack-same-order p3a p3c) ⟩

- Use this task as the *initial task network*



GOAL PREDICATES IN HIERARCHICAL-TASK NETWORKS

- Here the entire objective is encoded in the initial network
(move-three-stacks)

- $\Rightarrow \langle (\text{move-stack-same-order } p1a\ p1c),$
 $(\text{move-stack-same-order } p2a\ p2c),$
 $(\text{move-stack-same-order } p3a\ p3c) \rangle$

- To avoid this:

- New predicate (`should-move-same-order pile pile`) encoding the goal!
 - task:** `(move-as-necessary)`
 - method:** `(move-and-repeat pile1 pile2)`
 - precond:** `(should-move-same-order pile1 pile2)`
 - subtasks:** `$\langle (\text{move-stack-same-order } pile1\ pile2), ; \text{ makes should-move-... false}$`
 `$(\text{move-as-necessary}) \rangle$`
 - task:** `(move-as-necessary)`
 - method:** `(all-done)`
 - precond:** `(not (exists pile1 pile2`
`[(should-move-same-order pile1 pile2)]))`
 - subtasks:** `$\langle \rangle$`

UNINFORMED PLANNING IN HIERARCHICAL-TASK NETWORKS

- Can even do uninformed unguided planning

- Doing *something, anything*:

- Task (do-something) \Rightarrow operator (pickup x)
- Task (do-something) \Rightarrow operator (putdown x)
- Task (do-something) \Rightarrow operator (stack x y)
- Task (do-something) \Rightarrow operator (unstack x y)

Planner chooses
all parameters!

- Repeating

- Task (achieve-goals) \Rightarrow ⟨ (do-something), (achieve-goals) ⟩

- Ending

- Task (achieve-goals) \Rightarrow ⟨ ⟩, with precond: entire goal is satisfied!

Or combine **aspects** of this model with **other aspects** of "standard" HTN models!

DELIVERY: FIRST VARIATION

- Delivery:
 - A single truck
 - Pick-up a package, drive to destination, unload

- **task:** (deliver package dest)
- **method:** (move-by-truck package packageloc dest)
- **precond:** (at package packageloc)
- **subtasks:** { (driveto packageloc), (load package),
 (driveto dest), (unload package) }

What if the truck is already at the package location?

First driveto is unnecessary!

DELIVERY: SECOND VARIATION

- Alternative: Two alternative methods deliver

- **task:** (deliver package dest)
 - **method:** (move-by-truck-1 package packageloc truckloc dest)
 - **precond:** (at truck truckloc) (at package packageloc) (= truckloc packageloc)
 - **subtasks:** { (load package), (driveto dest), (unload package) }
-
- **task:** (deliver package dest)
 - **method:** (move-by-truck-2 package packageloc truckloc dest)
 - **precond:** (at truck truckloc) (at package packageloc) (!= truckloc packageloc)
 - **subtasks:** { (driveto packageloc), (load package),
 (driveto dest), (unload package) }

Do we really have to repeat the entire task?

Many "conditional" sub-tasks \implies combinatorial explosion!

DELIVERY: THIRD VARIATION

- Make the choice in the sub-task instead!

- **task:** (deliver package dest)
- **method:** (move-by-truck-3 package packageloc truckloc dest)
- **precond:** (at truck truckloc) (at package packageloc)
- **subtasks:** ⟨ (be-at packageloc), (load package), (be-at dest), (unload package) ⟩

- **task:** (be-at loc)
- **method:** (drive loc)
- **precond:** (not (at truck loc))
- **subtasks:** ⟨ (driveto loc) ⟩

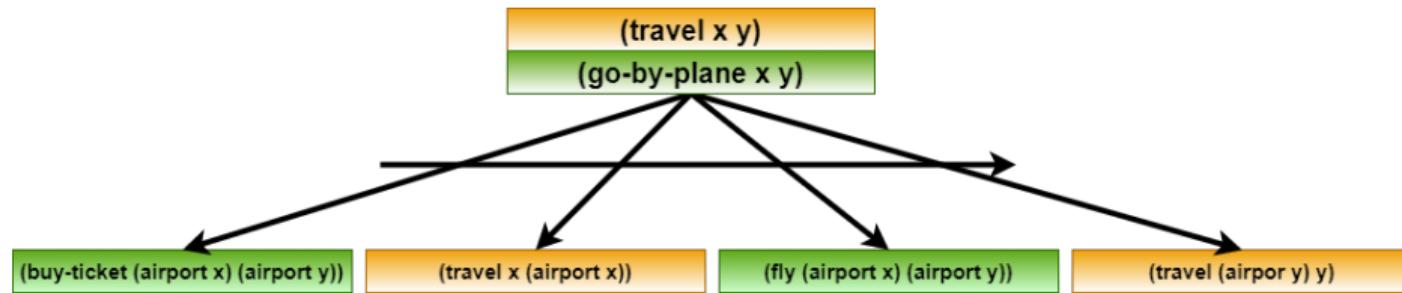
- **task:** (be-at loc)
- **method:** (already-there)
- **precond:** (at truck loc)
- **subtasks:** ⟨ ⟩

SEARCH SPACES

- Need search space
 - 1) A **node structure** defining what information is in a node
 - 2) A way of creating an **initial node** from a problems instance
 - 3) A **successor function** / branching rule returning all successors
 - 4) A **solution criterion** detecting if a node corresponds to a solution
 - 5) A **plan extractor** telling us which plan a solution node corresponds to
- Different alternatives exist!

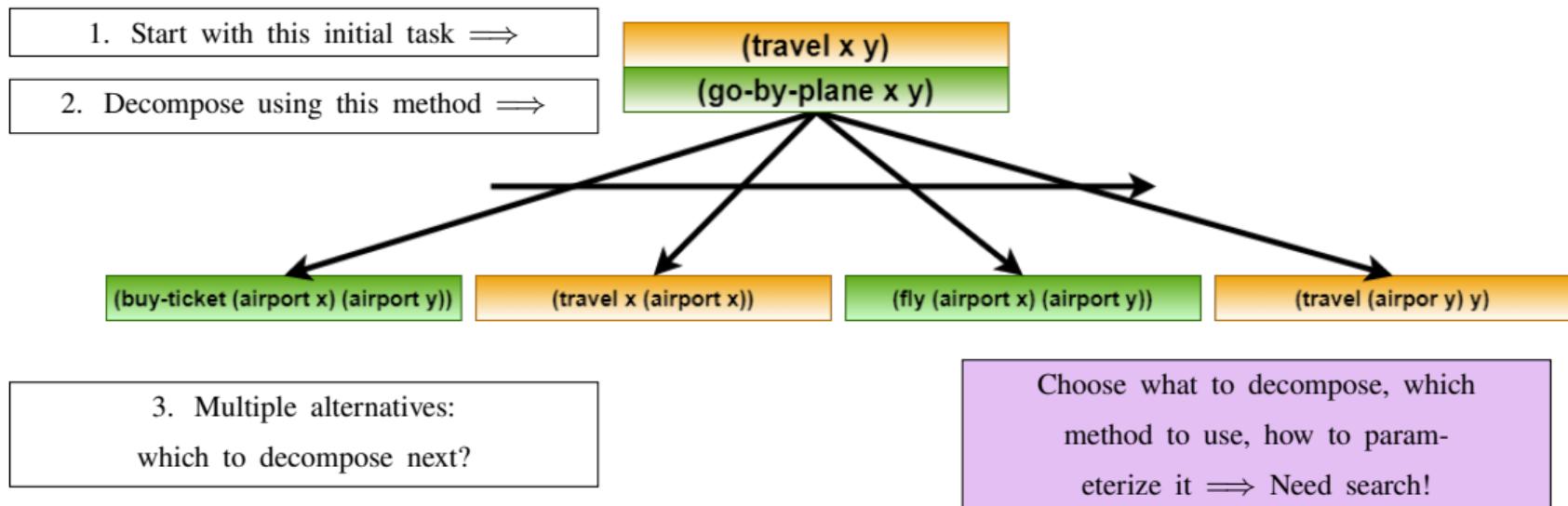
TOTAL ORDER?

- Basic assumption: Total Order Simple Task Networks
 - Any initial task is totally ordered
 - Any decomposition method is totally ordered



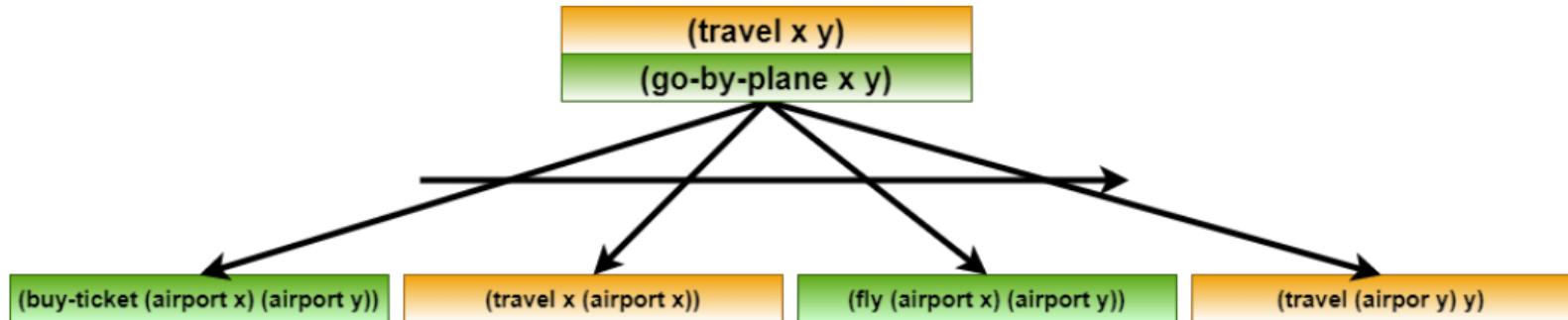
FORWARD DECOMPOSITION?

- Different decomposition orders are still possible



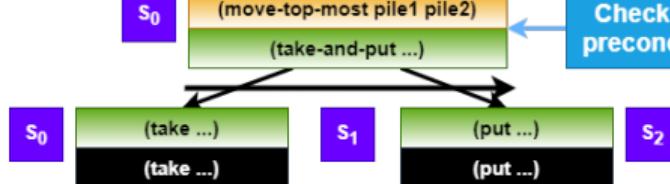
FORWARD DECOMPOSITION!

- Forward decomposition: One of many possibilities
 - Go "depth first, left to right"
 - Like forward state space search:
 - Generates actions in the same order in which they will be executed
 - \Rightarrow When we decompose a task, we know the "current" state of the world!



TOTAL ORDER FORWARD DECOMPOSITION (TOFD)

Strategy: chooses method, parameters



Check precond



initial task: specified in problem instance
Check precond in S_0 first!

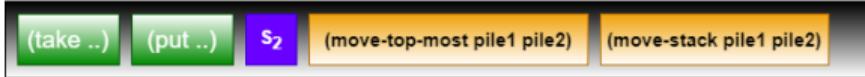


TOFD NODE STRUCTURE

- [1] A node structure defining what information is in a node
 - Plan so far
 - Current state - possible due to forward decomposition
 - Remaining tasks to expand
- [2] A way of creating an initial search node:



- Examples: Nodes visited in the previous slide

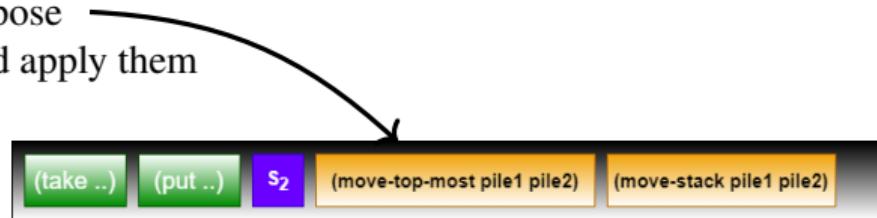


No actions so far
 Current state s_0
 Remaining tasks = the initial task from the problem!

TOFD SUCCESSORS

- [3] Successors:

- We know which task to decompose
- Find all applicable methods and apply them



- [4] Solution test

- No more tasks \implies done!

- [5] Solution extraction

- The resulting search node *contains* a sequential plan!

SOLVING TOTAL ORDER STN PROBLEMS

- TOFD takes a search node
 - π - a sequence of actions
 - s - the current state
 - $\langle t_1, \dots, t_k \rangle$ - a list of tasks to be achieved in **the specific order**
- We also assume:
 - O - the available operators (with params, preconds, effects)
 - M - the available methods (with params, preconds, subtasks)
- Returns
 - A sequential plan
 - Loses the hierarchical structure of the final plan
 - Simplifies the presentation - but the structure *could* also be kept!

TOFD: BASE CASE

```
function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
    initial-node ← ⟨[], problem.initialstate, problem.initialtask⟩ → [2]
    open ← {initial-node}
    while (open ≠ ∅) do
        ⟨π, s, ⟨t1, ..., tk⟩⟩ ← SEARCH-STRATEGY-REMOVE-FROM(open)
        → [6] TOFD uses depth first search
        → [4] If we have no tasks left to decompose..
        if k = 0 then return π
```

TOFD: GROUND PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
    initial-node  $\leftarrow \langle[], problem.initialstate, problem.initialtask\rangle$ 
    open  $\leftarrow \{\text{initial-node}\}$ 
    while (open  $\neq \emptyset$ ) do
         $\langle\pi, s, \langle t_1, \dots, t_k \rangle\rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(open)$ 

        if  $k = 0$  then return  $\pi$ 
        if  $t_1$  is primitive then
            actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
            candidates  $\leftarrow \{ a | a \in \text{actions} \wedge \text{name}(a) = t_1 \wedge a \text{ applicable in } s \}$ 

```

→ For simplicity: The case when all tasks to achieve are ground
→ [2]

→ [6] TOFD uses depth first search
→ [4] If we have no tasks left to decompose..

→ A primitive task is decomposed into a single action!
→ Possibly many to choose from!



TOFD: SUCCESSORS

```

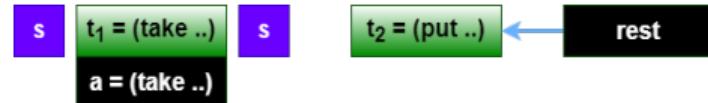
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    initial-node  $\leftarrow \langle[], problem.initialstate, problem.initialtask\rangle$ 
    open  $\leftarrow \{\text{initial-node}\}$ 
    while (open  $\neq \emptyset$ ) do
         $\langle\pi, s, \langle t_1, \dots, t_k \rangle\rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
        if  $k = 0$  then return  $\pi$ 
        if  $t_1$  is primitive then
            actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
            candidates  $\leftarrow \{ a | a \in \text{actions} \wedge \text{name}(a) = t_1 \wedge a \text{ applicable in } s \}$ 
            for each  $a \in \text{candidates}$  do
                 $\pi' \leftarrow \pi + a$ 
                 $s' \leftarrow \gamma(s, a)$ 
                rest  $\leftarrow \langle t_2, \dots, t_k \rangle$ 
                open  $\leftarrow \text{open} \cup \{\langle\pi', s', \text{rest}\rangle\}$ 

```

For simplicity: The case when all tasks to achieve are ground
→ [2]

A primitive task is decomposed into a single action!
→ Possibly many to choose from!

→ Add action at the end
→ Apply the action, find the new state



TOFD: LIFTED PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
    initial-node  $\leftarrow \langle[], problem.initialstate, problem.initialtask\rangle$ 
    open  $\leftarrow \{\text{initial-node}\}$ 
    while (open  $\neq \emptyset$ ) do
         $\langle\pi, s, \langle t_1, \dots, t_k \rangle\rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
        if  $k = 0$  then return  $\pi$ 
        if  $t_1$  is primitive then
            actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
            candidates  $\leftarrow \{ (a, \sigma) | a \in \text{actions} \wedge \text{name}(a) = \sigma(t_1) \wedge a \text{ applicable in } s \}$ 

```

\rightarrow The case when all tasks to achieve are non-ground. The plan will still be ground
 \rightarrow [2]

\rightarrow A primitive task is decomposed into a single action!
 \rightarrow Possibly many to choose from!

\rightarrow σ is a substitution function! Basically, σ can specify variable bindings for parameters of t_1 ...



TOFD: LIFTED PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
    initial-node  $\leftarrow \langle[], problem.initialstate, problem.initialtask\rangle$ 
    open  $\leftarrow \{\text{initial-node}\}$ 
    while (open  $\neq \emptyset$ ) do
         $\langle\pi, s, \langle t_1, \dots, t_k \rangle\rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
        if  $k = 0$  then return  $\pi$ 
        if  $t_1$  is primitive then
            actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
            candidates  $\leftarrow \{ (a, \sigma) | a \in \text{actions} \wedge \text{name}(a) = \sigma(t_1) \wedge a \text{ applicable in } s \}$ 
            for each  $a, \sigma \in \text{candidates}$  do
                 $\pi' \leftarrow \pi + a$ 
                 $s' \leftarrow \gamma(s, a)$ 
                rest  $\leftarrow \langle\sigma(t_2), \dots, \sigma(t_k)\rangle$ 
                open  $\leftarrow \text{open} \cup \{\langle\pi', s', \text{rest}\rangle\}$ 

```

s $t_1 = (\text{take ?crane loc1 cont2 cont pile8})$

chosen:

 $(\text{take crane1 loc1 cont2 cont5 pile8})$ $(\text{take crane2 loc1 cont2 cont5 pile8})$

\rightarrow The case when all tasks to achieve are non-ground. The plan will still be ground
 $\rightarrow [2]$

\rightarrow A primitive task is decomposed into a single action!
 \rightarrow Possibly many to choose from!

\rightarrow Add action at the end
 \rightarrow Apply the action, find the new state
 \rightarrow Must have the same variable bindings!

 $\sigma(t_2) = (\text{put crane1})$ $\sigma = \{ ?\text{crane} \rightarrow \text{crane1}, ?\text{cont} \rightarrow \text{cont5} \}$ $\sigma = \{ ?\text{crane} \rightarrow \text{crane2}, ?\text{cont} \rightarrow \text{cont5} \}$

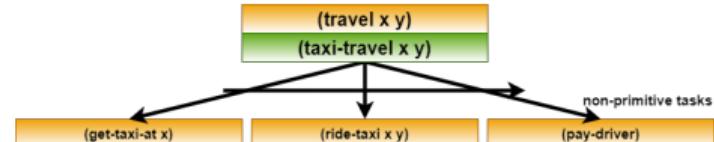
TOFD: Non-Primitive Tasks

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
    initial-node  $\leftarrow \langle[], problem.initialstate, problem.initialtask\rangle$ 
    open  $\leftarrow \{\text{initial-node}\}$ 
    while (open  $\neq \emptyset$ ) do
         $\langle\pi, s, \langle t_1, \dots, t_k \rangle\rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(open)$ 
        if  $k = 0$  then return  $\pi$ 
        if  $t_1$  is primitive then
            ...
        else
             $ground \leftarrow \text{GROUND-INSTANCES-OF-METHODS}(M)$ 
            candidates  $\leftarrow \{ (m, \sigma) | m \text{ ground} \wedge \text{task}(m) = \sigma(t_1) \wedge m \text{ applicable in } s \}$ 
    
```

The case when all tasks to achieve are non-ground. The plan will still be ground
→ [2]

*→ t_1 is e.g. (travel LiU Resecentrum)
A non-primitive task is decomposed into a new task-list.
→ May have many methods to choose from!*



TOFD: Non-Primitive Tasks (cont.)

```

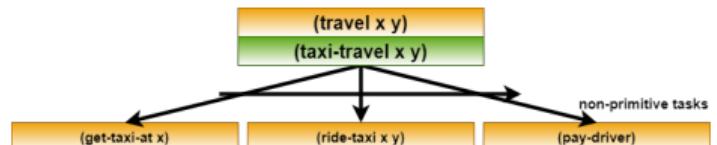
function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
    initial-node  $\leftarrow \langle[], problem.initialstate, problem.initialtask\rangle$ 
    open  $\leftarrow \{\text{initial-node}\}$ 
    while (open  $\neq \emptyset$ ) do
         $\langle\pi, s, \langle t_1, \dots, t_k \rangle\rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(open)$ 
        if  $k = 0$  then return  $\pi$ 
        if  $t_1$  is primitive then
            ...
        else
            ground  $\leftarrow \text{GROUND-INSTANCES-OF-METHODS}(M)$ 
            candidates  $\leftarrow \{ (m, \sigma) | m \text{ ground} \wedge \text{task}(m) = \sigma(t_1) \wedge m \text{ applicable in } s \}$ 
            for each  $(m, \sigma) \in \text{candidates}$  do
                 $\pi' \leftarrow \pi$ 
                 $s' \leftarrow s$ 
                rest  $\leftarrow \langle \text{SUBTASKS}(m) + \sigma(t_2), \dots, \sigma(t_k) \rangle$ 
                open  $\leftarrow \text{open} \cup \{\langle\pi', s', \text{rest}\rangle\}$ 

```

The case when all tasks to achieve are non-ground. The plan will still be ground

$\rightarrow [2]$

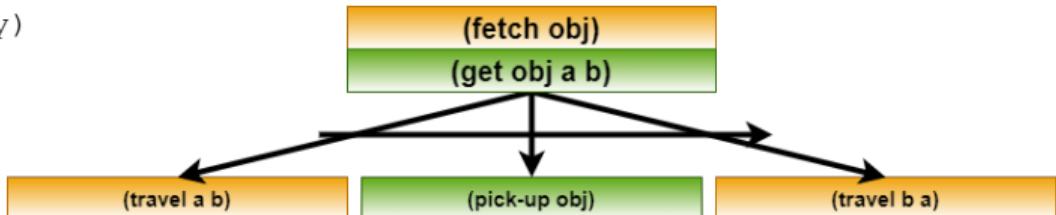
\rightarrow No action needed!
 \rightarrow No state change
 \rightarrow Prepend new list! The "origin" of a task is discarded:
 \rightarrow only the sub-tasks are relevant!



LIMITATIONS OF ORDERED-TASK PLANNING

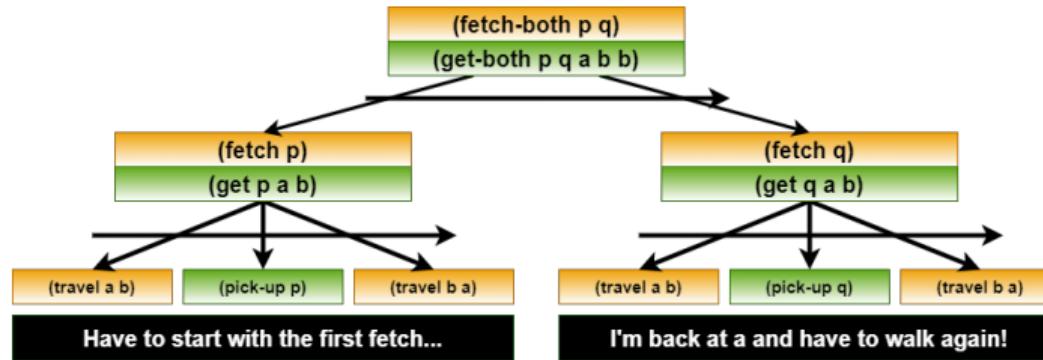
- TOFD requires **totally ordered** methods
 - Can't interleaves sub-tasks of different tasks
- Suppose we want to **fetch one object** somewhere, then return to where we are now
 - **task:** (fetch obj)
 - **method:** (get obj mypos objpos)
 - **precond:** (robotat mypos) (at obj objpos)
 - **subtasks:** { (travel mypos objpos), (pick-up obj), (travel objpos mypos) }

 - **task:** (travel x y)
 - **method:** (walk x y)
 - **method:** (stayat x y)



LIMITATIONS OF ORDERED-TASK PLANNING (CONT.)

- Suppose we want to fetch **two** objects somewhere, then return to where we are now
- One idea: Just "fetch" each object in sequence
 - task:** (fetch-both obj1 obj2)
 - method:** (get-both obj1 obj2 mypos objpos1 objpos2)
 - precond:**
 - subtasks:** { (fetch obj1 mypos objpos1), (fetch obj2 mypos objpos2) }



ALTERNATIVE METHODS

- To generate more efficient plans using total-order STNs:

- Use a different domain model!

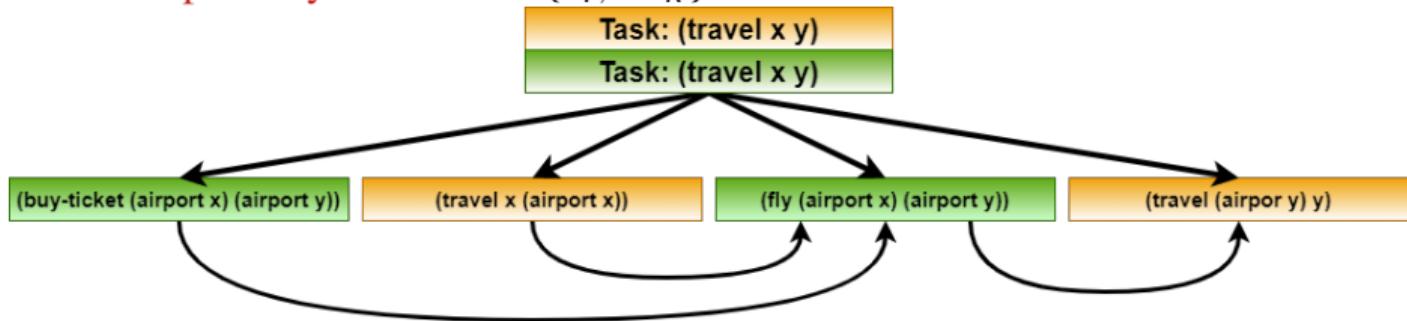
- **task:** (fetch-both obj1 obj2)
 - **method:** (get-both obj1 obj2 mypos objpos1 objpos2)
 - **precond:** (!= objpos1 objpos2) (at obj1 objpos1) (at obj2 objpos2)
 - **subtasks:** { (travel mypos objpos1), (pick-up obj1),
 (travel objpos1 objpos2), (pick-up obj2),
 (travel objpos2 mypos) }

 - **task:** (fetch-both obj1 obj2)
 - **method:** (get-both-in-same-place obj1 obj2 mypos objpos)
 - **precond:** (at obj1 objpos) (at obj2 objpos)
 - **subtasks:** { (travel mypos objpos), (pick-up obj1),
 (pick-up obj2), (travel objpos mypos) }

Or: Load-all; drive-truck; unload-all

PARTIALLY ORDERED METHODS

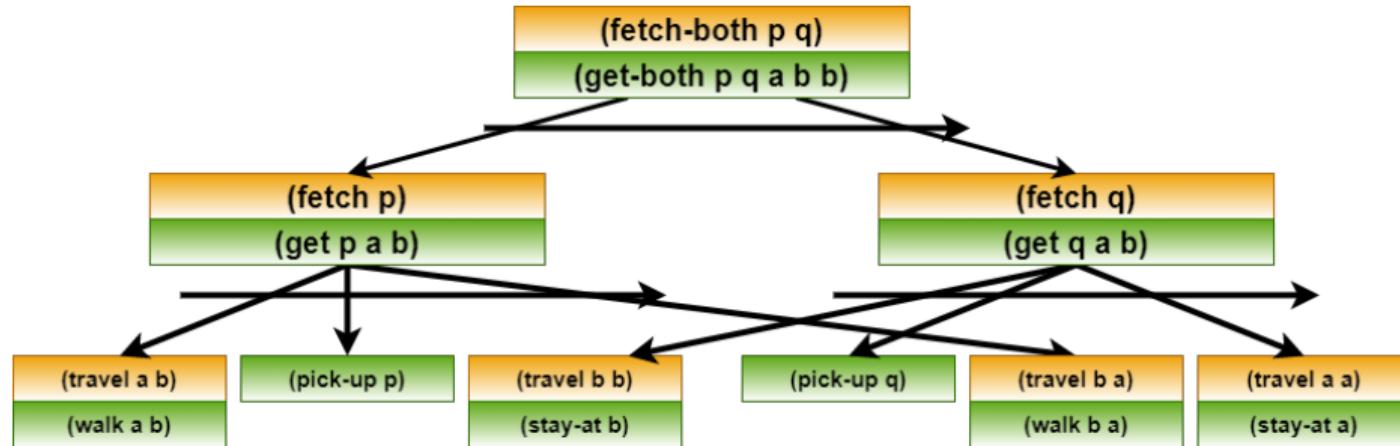
- The sub-tasks are a **partially ordered** set $\{t_1, \dots t_k\}$ – a *network*



- method:** (go-by-plane x y)
 - task:** (travel x y)
 - precond:** (long-distance x y)
 - network:**
 $u_1 = (\text{buy-ticket (airport x) (airport y)})$
 $u_2 = (\text{travel x (airport x)})$
 $u_3 = (\text{fly (airport x) (airport y)})$
 $u_4 = (\text{travel (airport y) y})$
 $\{ (u_1, u_3), (u_2, u_3), (u_3, u_4) \}$

PARTIALLY ORDERED METHODS

- With partially ordered methods sub-tasks can be interleaved



- Requires a more complicated planning algorithm: POFD
- SHOP2: implementation of POFD-like algorithm + generalizations

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- [1] Hector Geffner and Blai Bonet. *A Concise Introduction to Models and Methods for Automated Planning*. Synthesis Lectures on Artificial Intelligence and Machine Learning. Morgan & Claypool Publishers, 2013. ISBN 9781608459698. doi: 10.2200/S00513ED1V01Y201306AIM022. URL <https://doi.org/10.2200/S00513ED1V01Y201306AIM022>.
- [2] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated planning - theory and practice*. Elsevier, 2004. ISBN 978-1-55860-856-6.
- [3] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated Planning and Acting*. Cambridge University Press, 2016. ISBN 978-1-107-03727-4. URL <http://www.cambridge.org/de/academic/subjects/computer-science/artificial-intelligence-and-natural-language-processing/automated-planning-and-acting?format=HB>.
- [4] Patrik Haslum, Nir Lipovetzky, Daniele Magazzeni, and Christian Muise. *An Introduction to the Planning Domain Definition Language*. Synthesis Lectures on Artificial Intelligence and Machine Learning. Morgan & Claypool Publishers, 2019. doi: 10.2200/S00900ED2V01Y201902AIM042. URL <https://doi.org/10.2200/S00900ED2V01Y201902AIM042>.