

# Dependable Hybrid Systems Design: a Refinement Approach

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Nov, 2020

# Where were we?

- ▶ Overview of hybrid system
- ▶ Review of calculus
- ▶ Review of Event-B
- ▶ Develop theories in Event-B

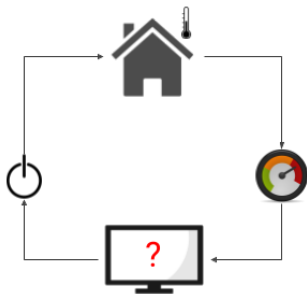
# Outlines

## Design Hybrid Systems in Event-B

Smart Heating System

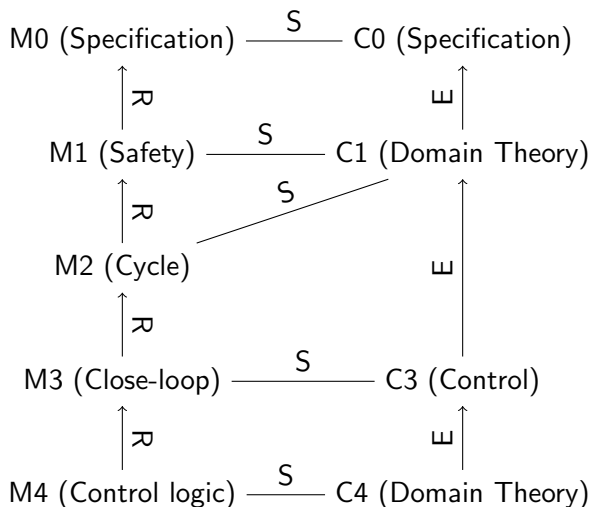
Refinement Strategy for Hybrid System Design

# Smart Heating System



- ▶ 2 modes: ON/OFF
- ▶ Simple dynamics:  $\dot{T}=1/-1$
- ▶ Sample at  $\delta$  s
- ▶ Switch mode costs  $t_{act}$  s  
( $t_{act} < \delta$ )
- ▶ Safety:  $T_{min} \leq T \leq T_{max}$

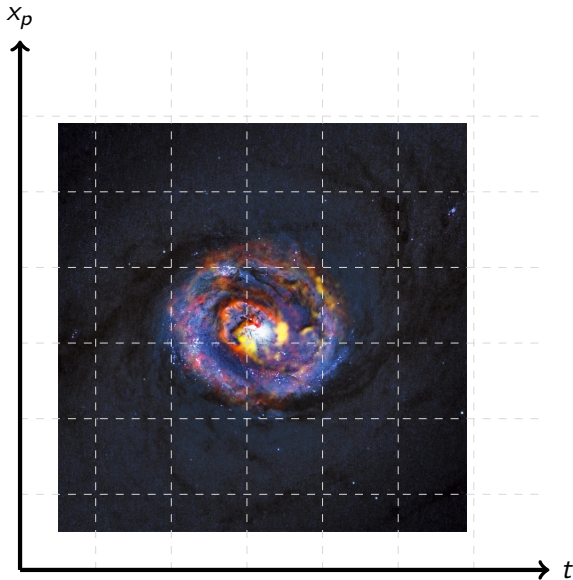
# Refinement Strategy for Hybrid System Design



# Lab Material

- ▶ [https://github.com/veriat1/LORIA\\_WEEK2](https://github.com/veriat1/LORIA_WEEK2)
- ▶ Import **theory-axiom-real** to Rodin, and deploy this theory
- ▶ Import **ex-heating-maintainer-event** to Rodin

# Smart Heating System (Specification M0)



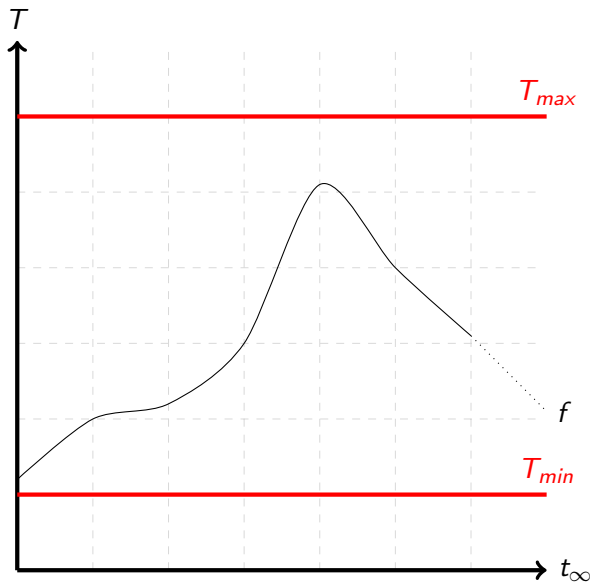
# Smart Heating System (Specification M0)

## Checklist:

- ▶ Generic hybrid system state trajectory
- ▶ Generic safety property
- ▶ Big-step semantics



# Smart Heating System (Safety M1)

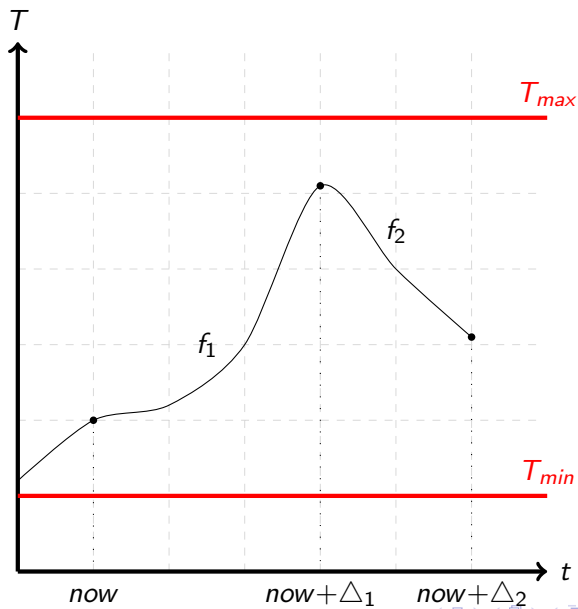


# Smart Heating System (Safety M1)

## Checklist:

- ▶ Concrete system state trajectory
- ▶ Concrete safety property
- ▶ Big-step semantics refined
- ▶ Important proof obligations: guard preservation

## Smart Heating System (Cycle M2)

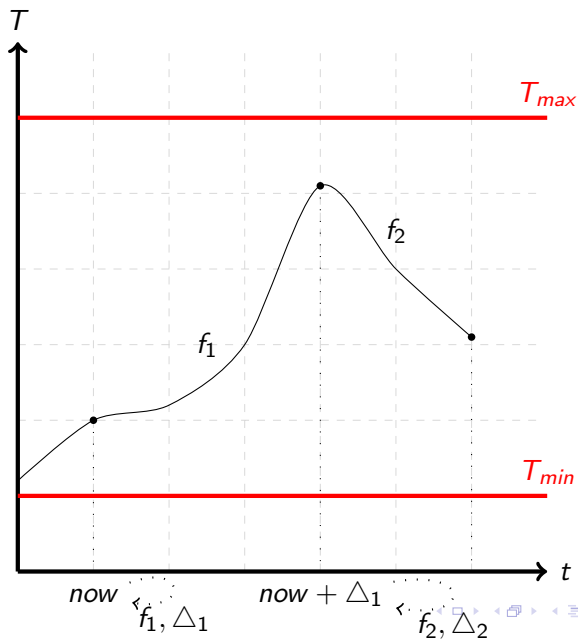


# Smart Heating System (Cycle M2)

## Checklist:

- ▶ Time pointer
- ▶ Refined system state trajectory
- ▶ Refined safety property
- ▶ Small-step semantics
- ▶ Important proof obligations: invariant preservation

# Smart Heating System (Close-loop M3)



# Smart Heating System (Close-loop M3)

## Checklist:

- ▶ Variable for close-loop mode control
- ▶ Prediction (Controller)
- ▶ Progression (Plant)

# Smart Heating System (Control Logic M4)

## Event-triggered

### Checklist:

- ▶ Event-triggered design (when certain events are detected what actions that system should take)
- ▶ Specification of time-triggered design

# Smart Heating System (Control Logic M4)

## Time-triggered

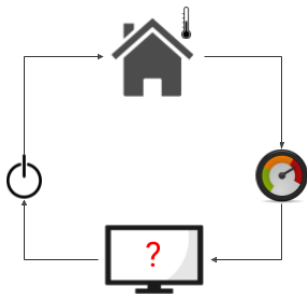
### Checklist:

- ▶ Revisit the description of heating system
- ▶ Time-triggered design(the controller takes action only every once in a while)

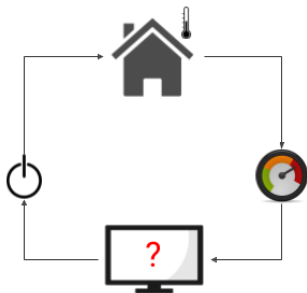


# Smart Heating System (Revisit)

- ▶ 2 modes: ON/OFF
- the only actuation we can do

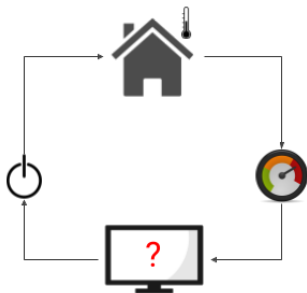


# Smart Heating System (Revisit)



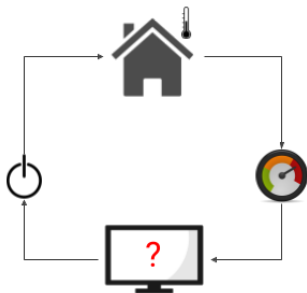
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- the only actuation we can do
- ▶ Simple dynamics:  $\dot{T}=1/-1$
- monotonicity

# Smart Heating System (Revisit)



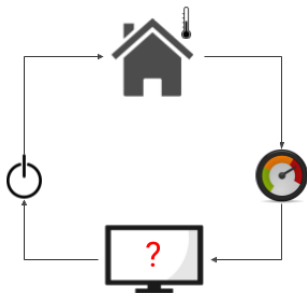
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- ▶ Sample at  $\delta$  s
- Decision at sampling time

# Smart Heating System (Revisit)



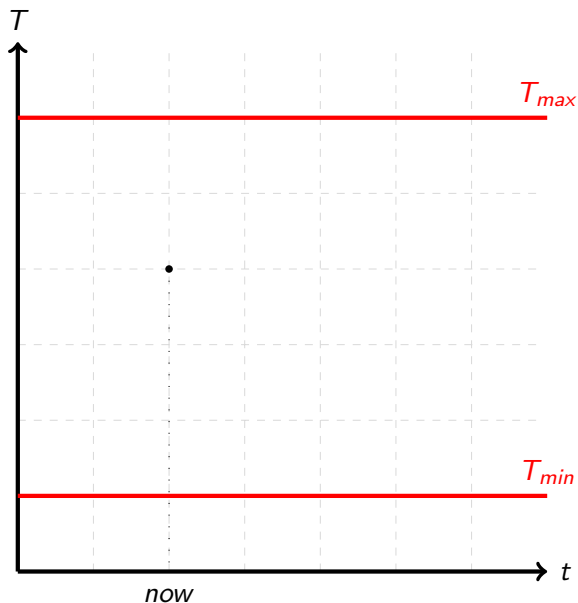
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( $t_{act} < \delta$ )
- Cost of switch mode

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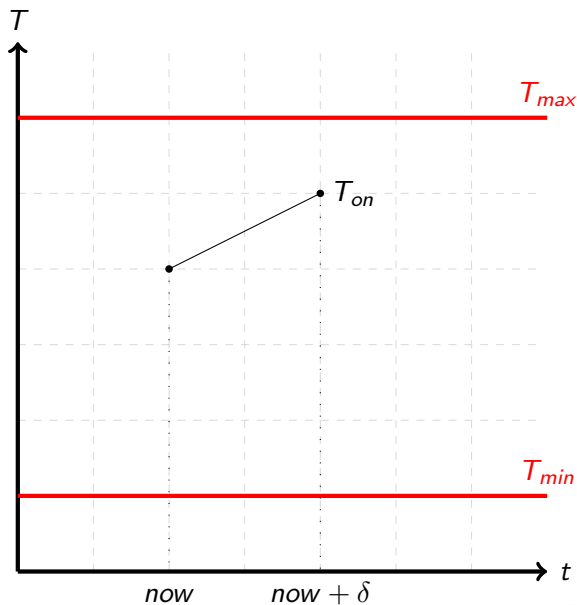


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- ▶ Safety:  $T_{min} \leq T \leq T_{max}$

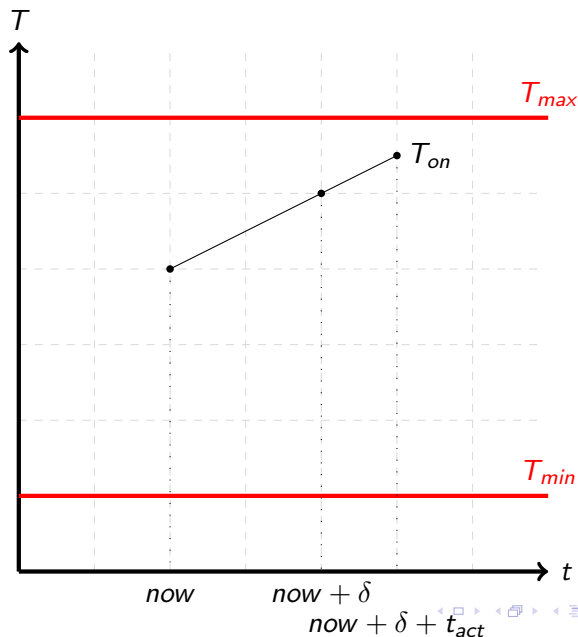
Case 1: ON mode,  $T(now) \leq T_{max}$ , Stay ON



Case 1: ON mode,  $T(now + \delta) \leq T_{max}$ , Stay ON



Case 1: ON mode,  $T(now + \delta + t_{act}) \leq T_{max}$ , Stay ON





## Case 2,3,4: ?