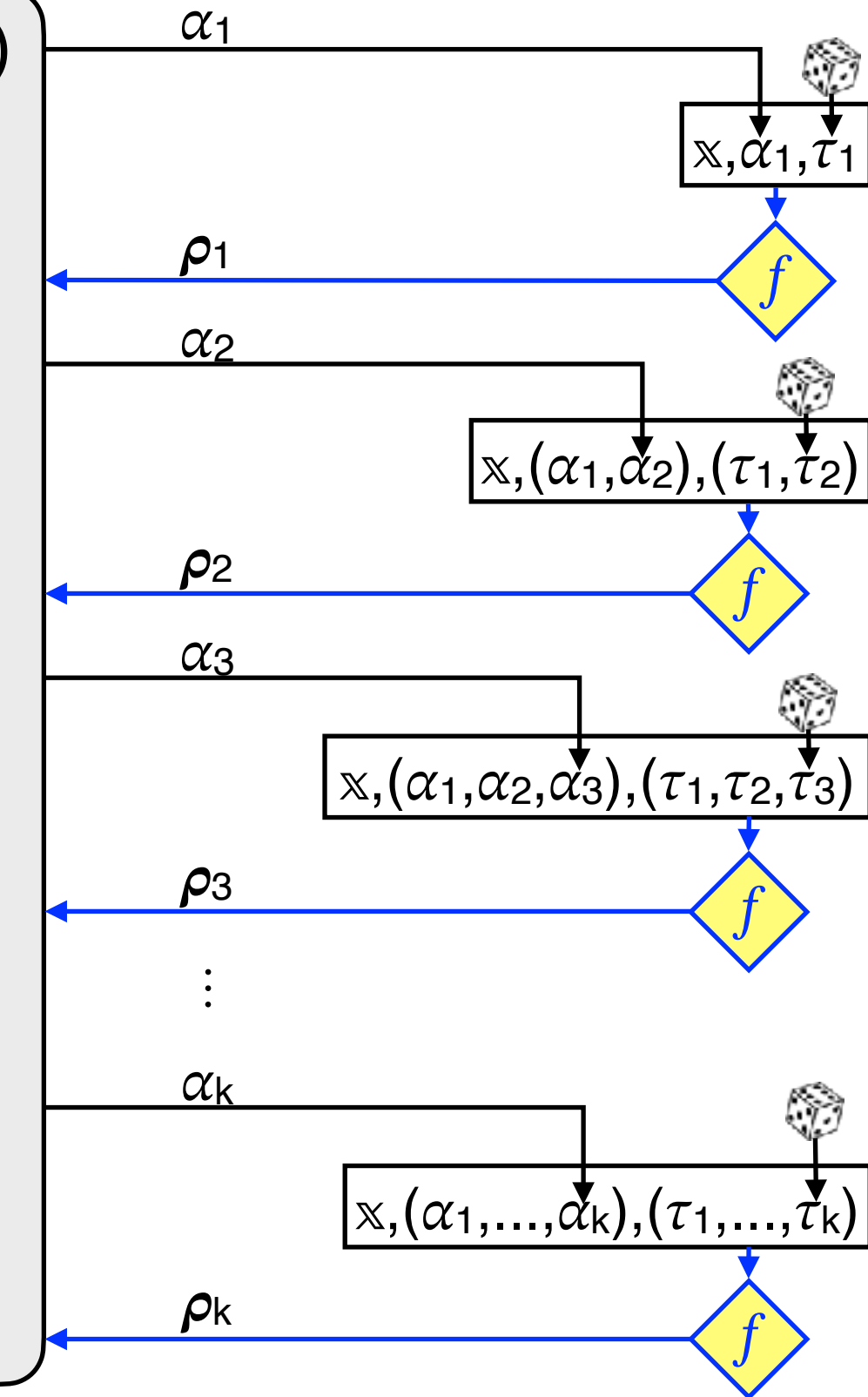
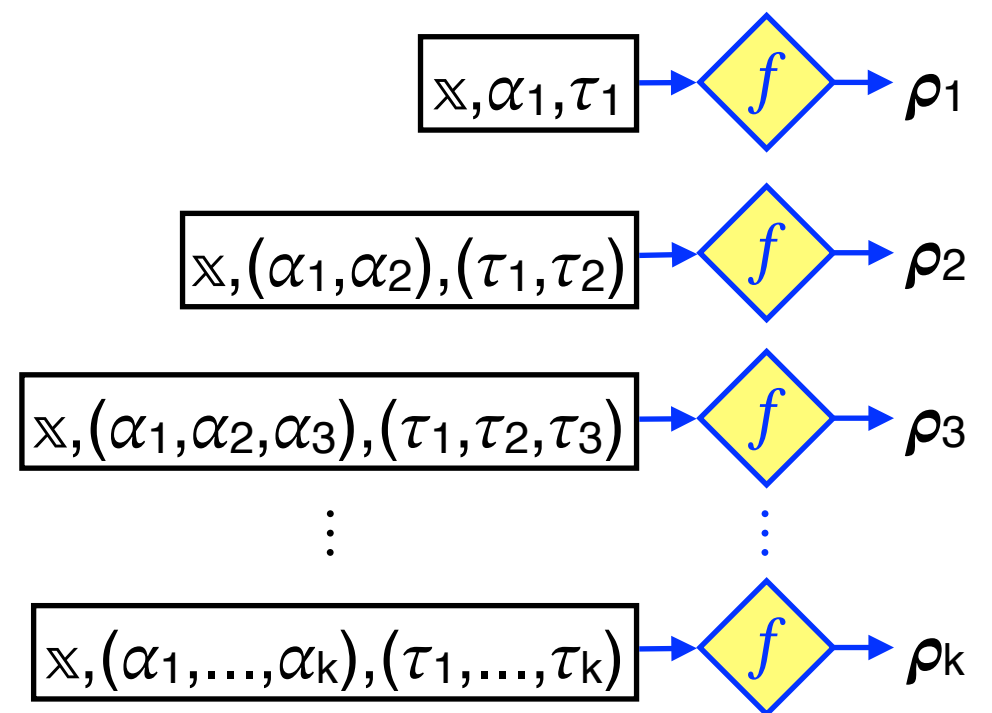


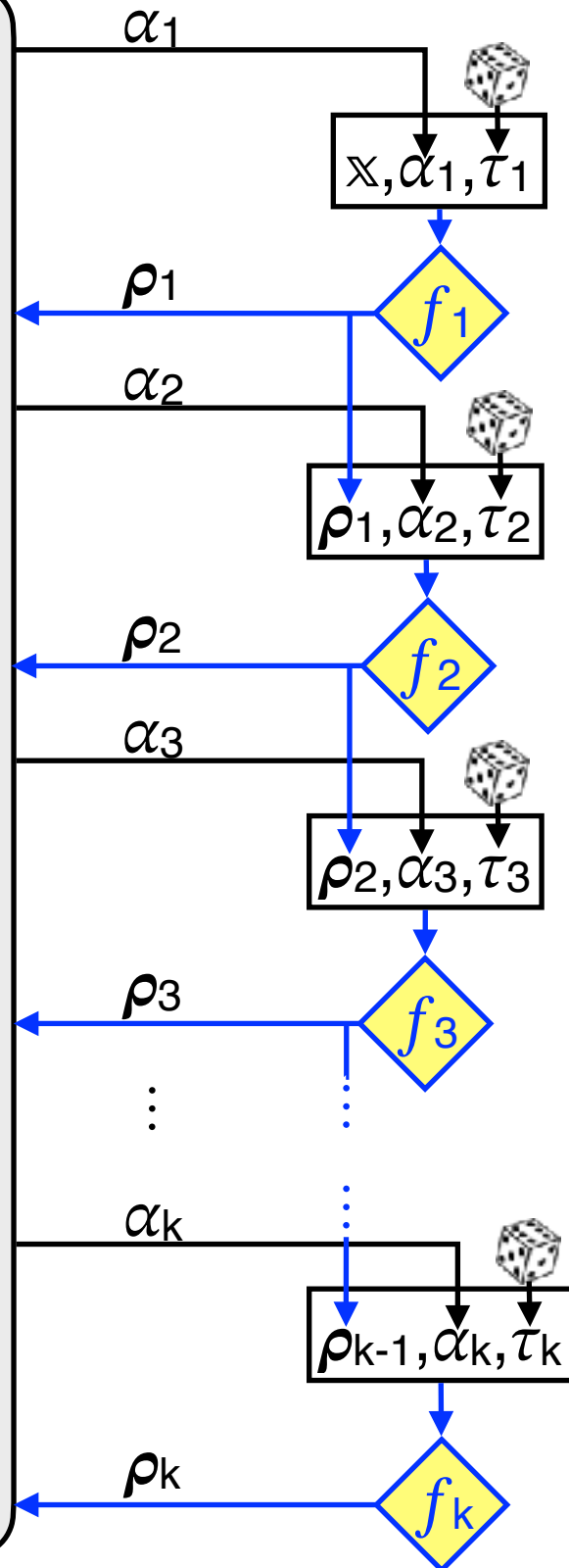
$\mathcal{P}(\mathbb{X}, \mathbb{W})$ 
 $\mathbf{P}_{\text{IP}}(\mathbb{X}, \mathbb{W})$ 

 $\pi := ((\alpha_1, \dots, \alpha_k), (\tau_1, \dots, \tau_k))$ 
 $\pi$ 
 $\mathcal{V}(\mathbb{X}, \pi)$ 

- parse  $\pi$  as  $((\alpha_1, \dots, \alpha_k), (\tau_1, \dots, \tau_k))$
- derive IP randomness



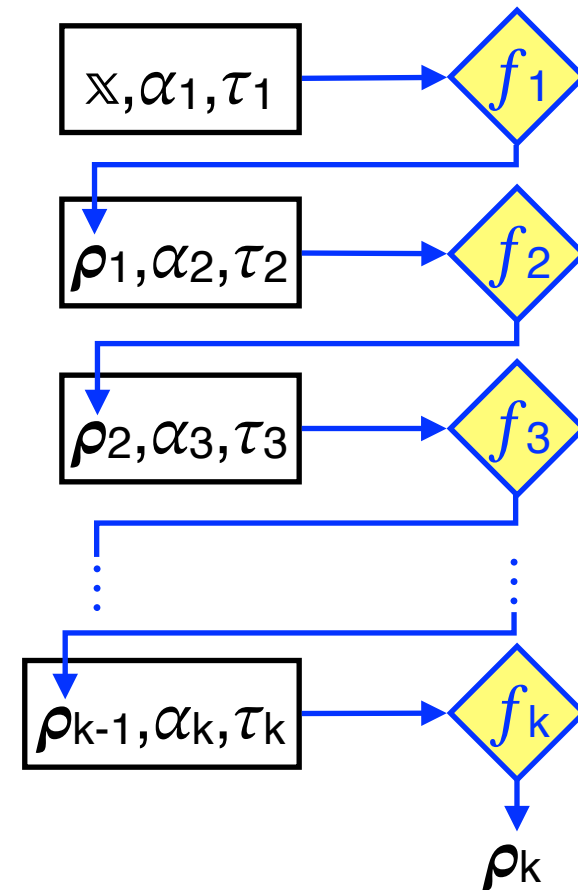
- check IP decision

 $\mathbf{V}_{\text{IP}}(\mathbb{X}, (\alpha_1, \dots, \alpha_k), (\rho_1, \dots, \rho_k))$

$\mathcal{P}(\mathbb{X}, \mathbb{W})$ 
 $\mathbf{P}_{\text{IP}}(\mathbb{X}, \mathbb{W})$ 

 $\pi := ((\alpha_1, \dots, \alpha_k), (\tau_1, \dots, \tau_k))$ 
 $\pi$ 
 $\mathcal{V}(\mathbb{X}, \pi)$ 

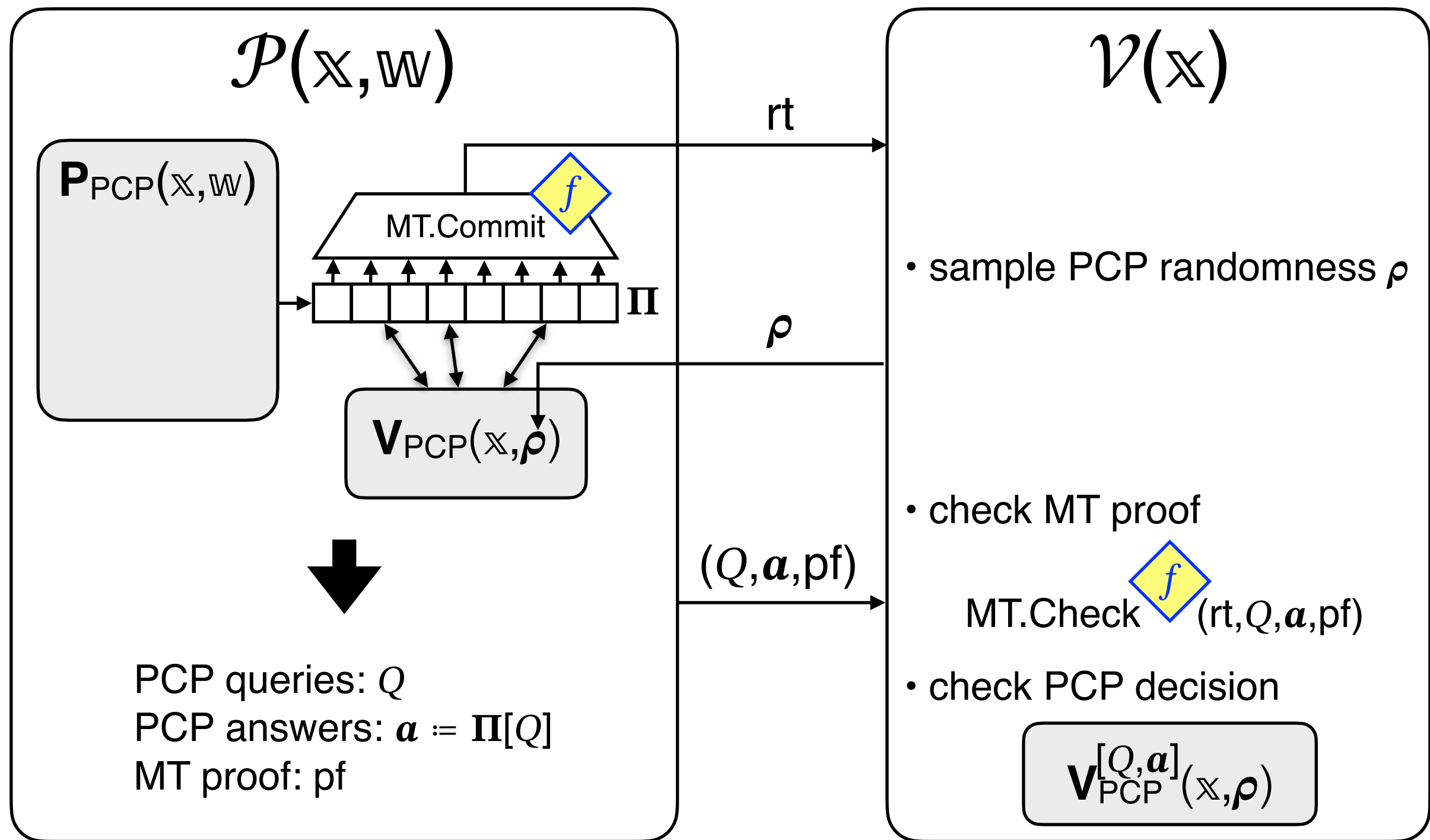
- parse  $\pi$  as  $((\alpha_1, \dots, \alpha_k), (\tau_1, \dots, \tau_k))$

- derive IP randomness

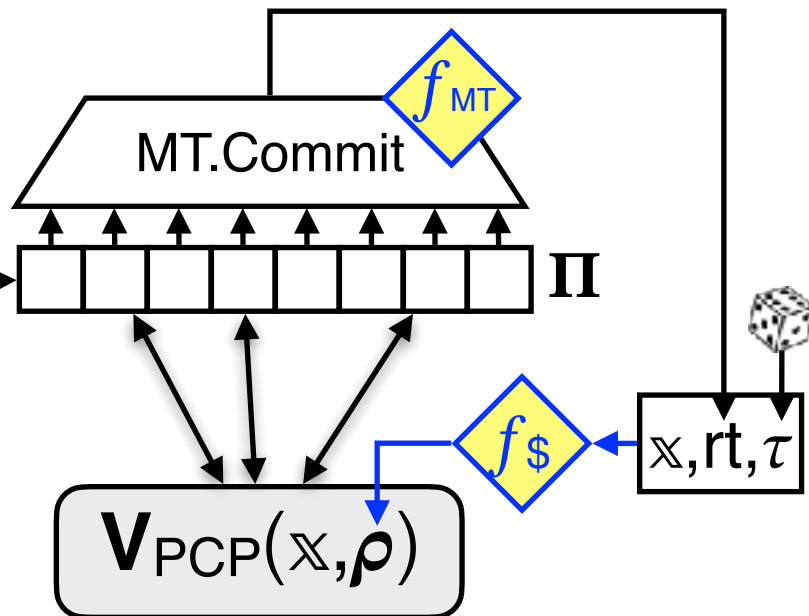


- check IP decision

 $\mathbf{V}_{\text{IP}}(\mathbb{X}, (\alpha_1, \dots, \alpha_k), (\rho_1, \dots, \rho_k))$



$$\mathcal{P}(\mathbb{X}, \mathbb{W})$$

$$\mathbf{P}_{\text{PCP}}(\mathbb{X}, \mathbb{W})$$


PCP queries:  $Q$

PCP answers:  $\mathbf{a} := \Pi[Q]$

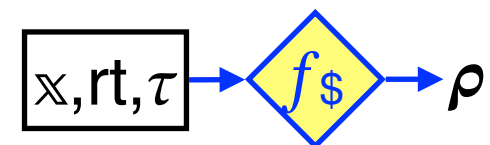
MT proof: pf

$$\pi := (\text{rt}, Q, \mathbf{a}, \text{pf}, \tau)$$

$$\pi$$

$$\mathcal{V}(\mathbb{X}, \pi)$$

- parse  $\pi$  as  $(\text{rt}, Q, \mathbf{a}, \text{pf}, \tau)$
- derive PCP randomness



- check MT proof

MT.Check  $f_{\text{MT}}$   $(\text{rt}, Q, \mathbf{a}, \text{pf})$

- check PCP decision

$$\mathbf{V}_{\text{PCP}}^{[Q, \mathbf{a}]}(\mathbb{X}, \rho)$$



$\mathcal{P}(\mathbb{X}, \mathbb{W})$ 
 $\mathcal{V}(\mathbb{X})$ 
 $\mathbf{P}_{\text{IOP}}(\mathbb{X}, \mathbb{W})$ 

MT.Commit

 $f$ 
 $\Pi_1$ 
 $rt_1$ 
 $\rho_1$ 
 $rt_2$ 
 $\rho_2$ 
 $\vdots$ 
 $rt_k$ 
 $\rho_k$ 

MT.Commit

 $f$ 
 $\Pi_2$ 
 $\vdots$ 

MT.Commit

 $f$ 
 $\Pi_k$ 

- sample IOP randomness  $\rho_1$

- sample IOP randomness  $\rho_2$

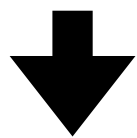
 $\vdots$ 

- sample IOP randomness  $\rho_k$

- check MT proofs

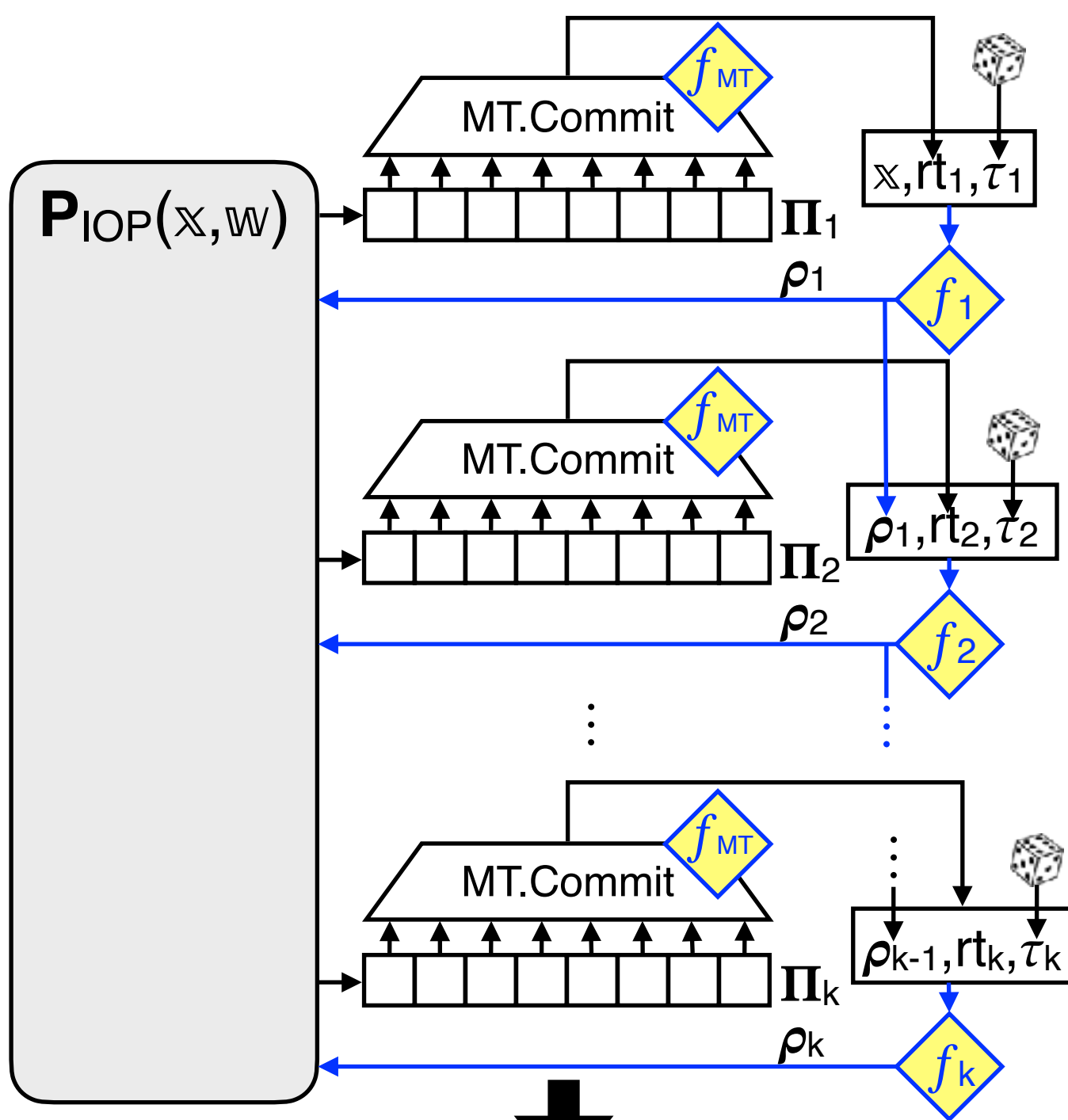
 $\bigwedge_{i \in [k]} \text{MT.Check}^f(rt_i, Q_i, \mathbf{a}_i, \text{pf}_i)$ 

- check IOP decision

 $\mathbf{V}_{\text{IOP}}^{[Q_i, \mathbf{a}_i]_{i \in [k]}}(\mathbb{X}, (\rho_1, \dots, \rho_k))$ 

IOP verifier queries:  $(Q_1, \dots, Q_k)$ 

IOP oracle answers:  $(\mathbf{a}_1, \dots, \mathbf{a}_k)$ 

MT proofs:  $(\text{pf}_1, \dots, \text{pf}_k)$ 
 $((Q_i, \mathbf{a}_i, \text{pf}_i))_{i \in [k]}$

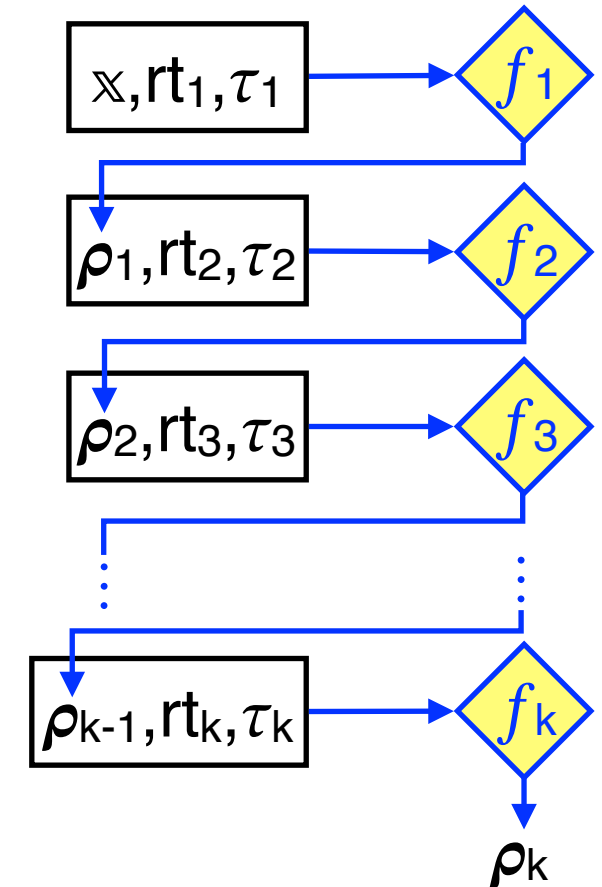
$\mathcal{P}(\mathbb{X}, \mathbb{W})$ 


IOP verifier queries:  $(Q_1, \dots, Q_k)$   
 IOP oracle answers:  $(\mathbf{a}_1, \dots, \mathbf{a}_k)$   
 MT proofs:  $(\text{pf}_1, \dots, \text{pf}_k)$   
 $\pi := ((rt_i, Q_i, \mathbf{a}_i, \text{pf}_i, \tau_i))_{i \in [k]}$

 $\mathcal{V}(\mathbb{X}, \pi)$ 

- parse  $\pi$  as  $((rt_i, Q_i, \mathbf{a}_i, \text{pf}_i, \tau_i))_{i \in [k]}$

- derive IOP randomness

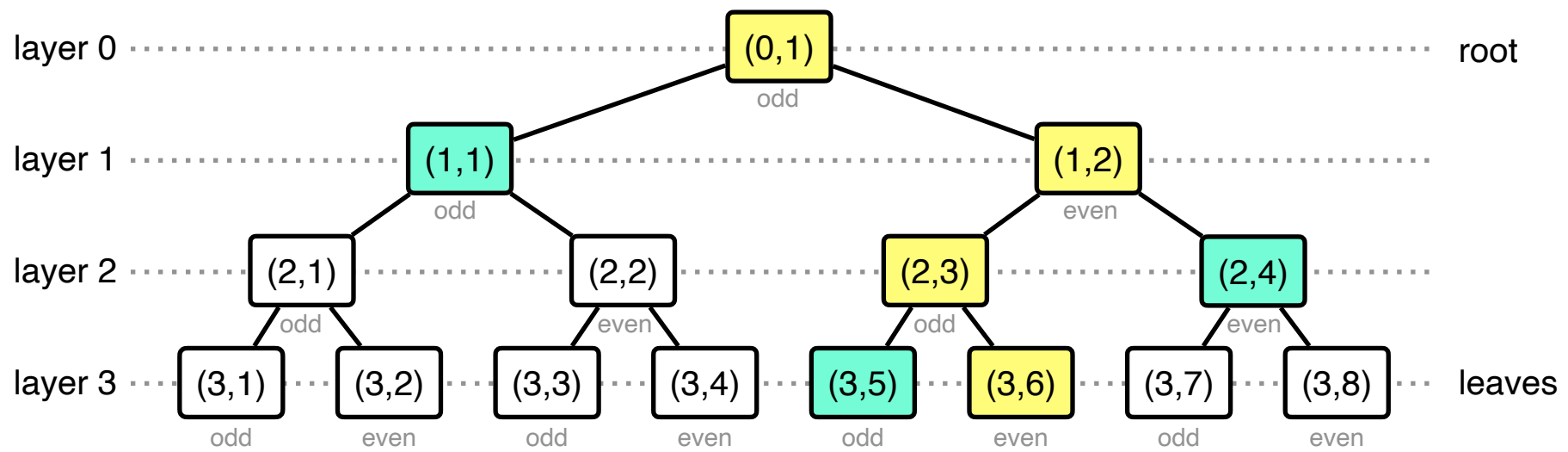


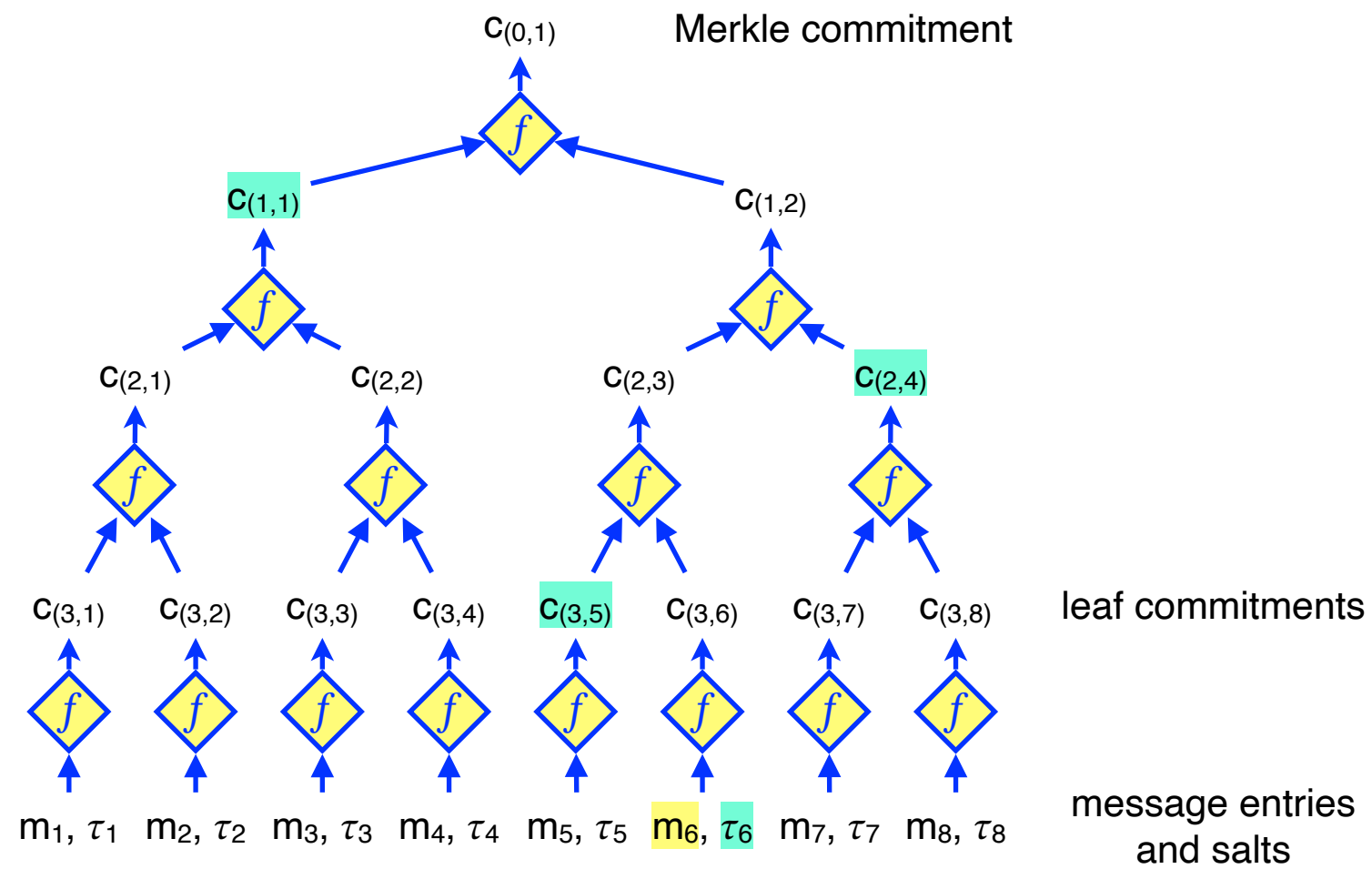
- check MT proofs

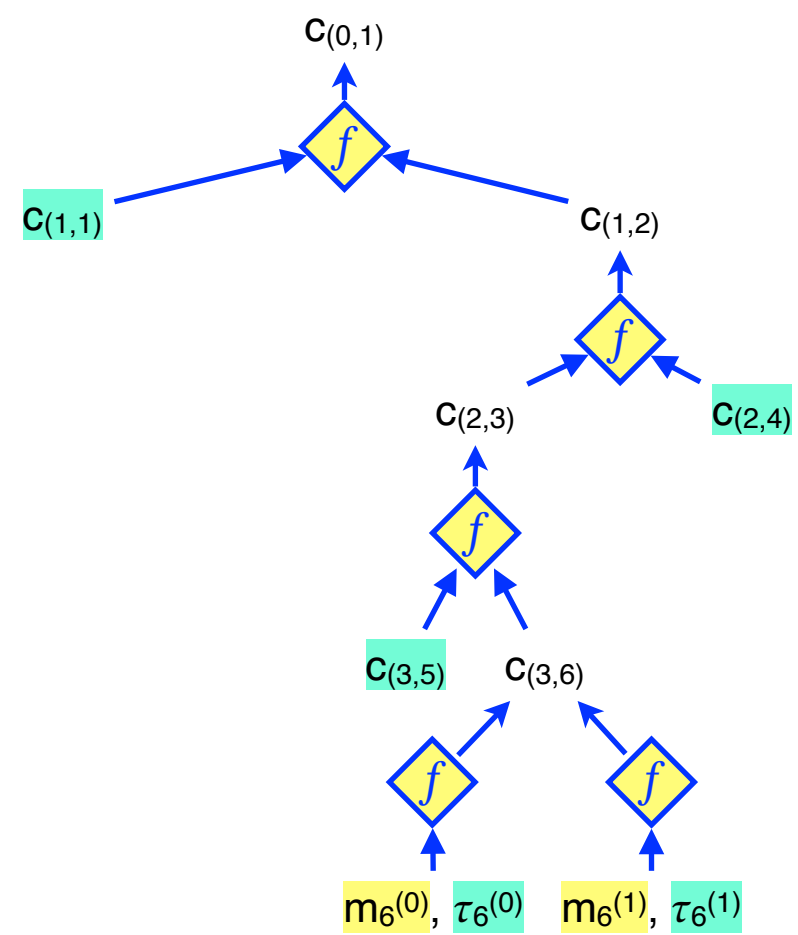
$\bigwedge_{i \in [k]} \text{MT.Check}_{f_{\text{MT}}} (rt_i, Q_i, \mathbf{a}_i, \text{pf}_i)$

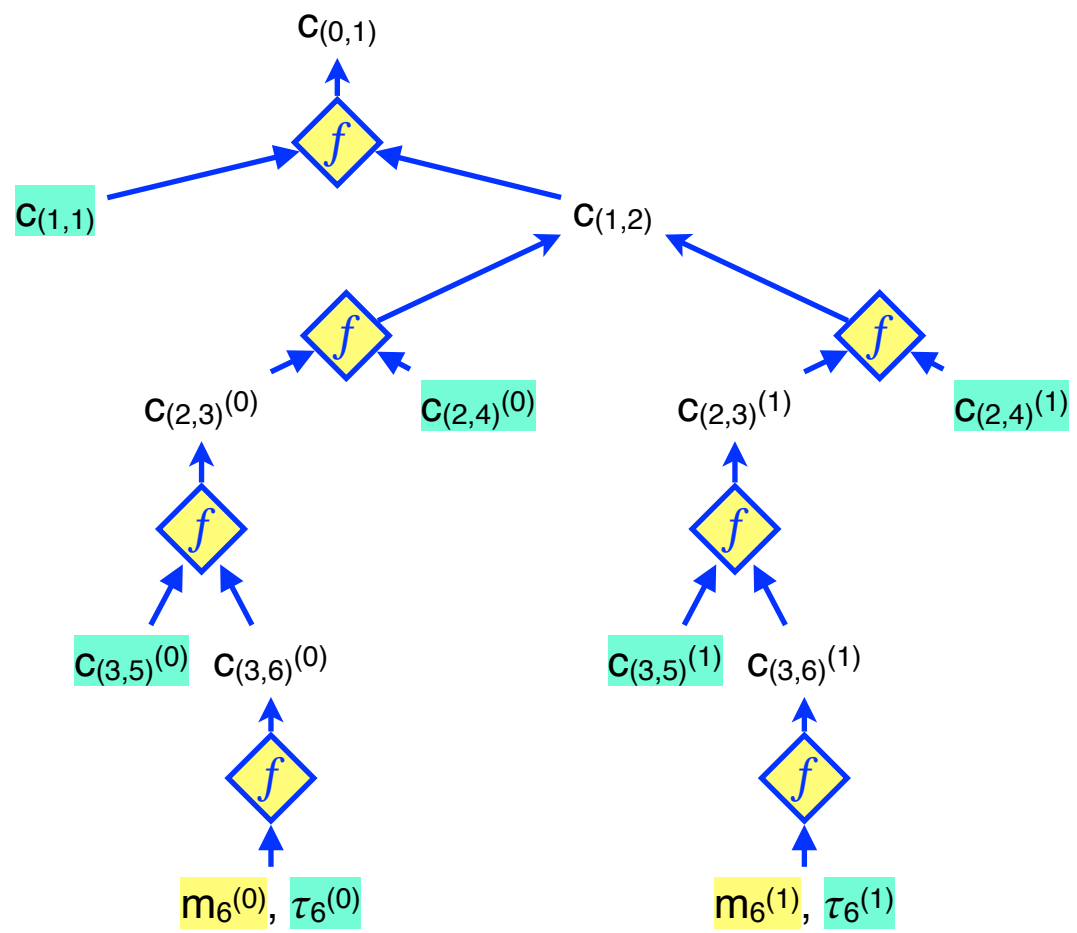
- check IOP decision

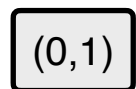
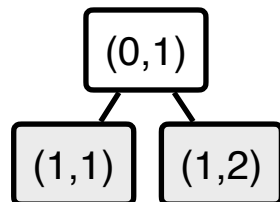
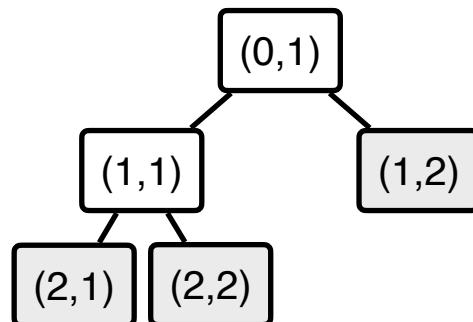
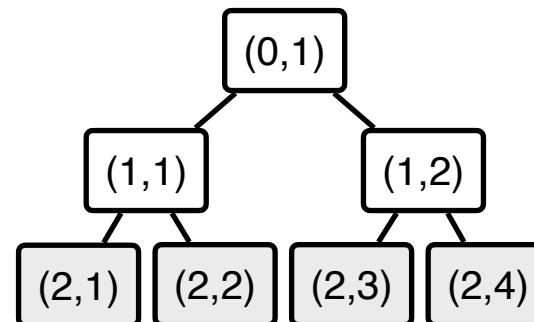
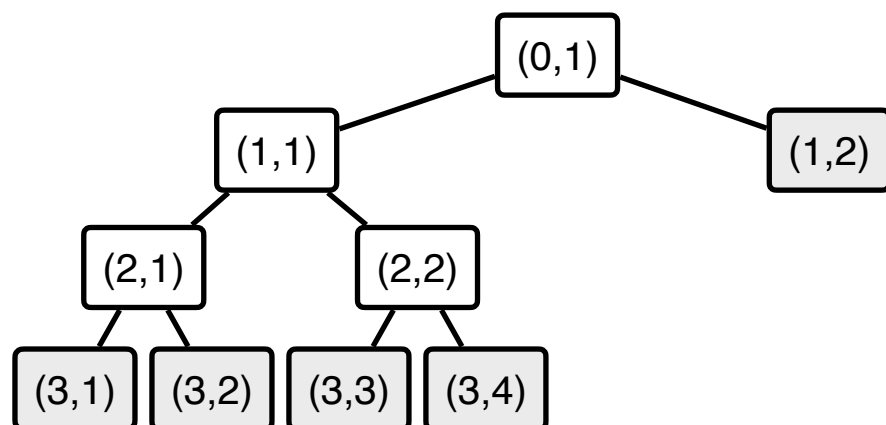
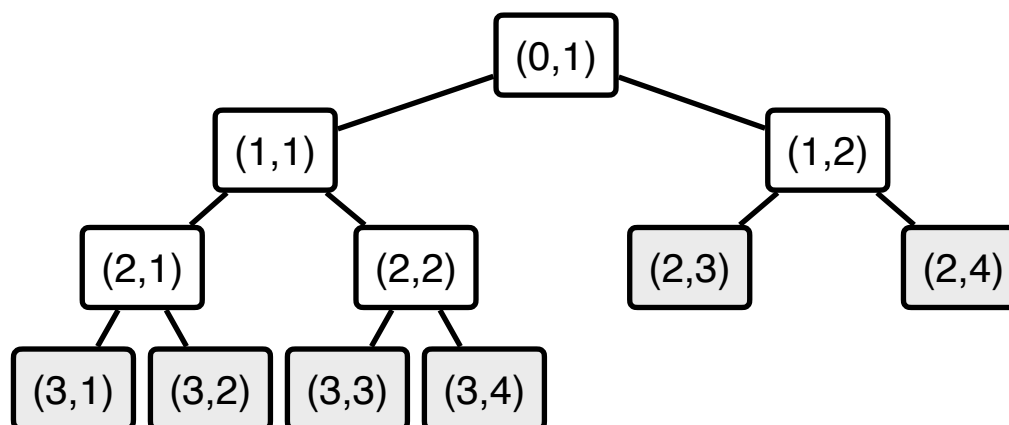
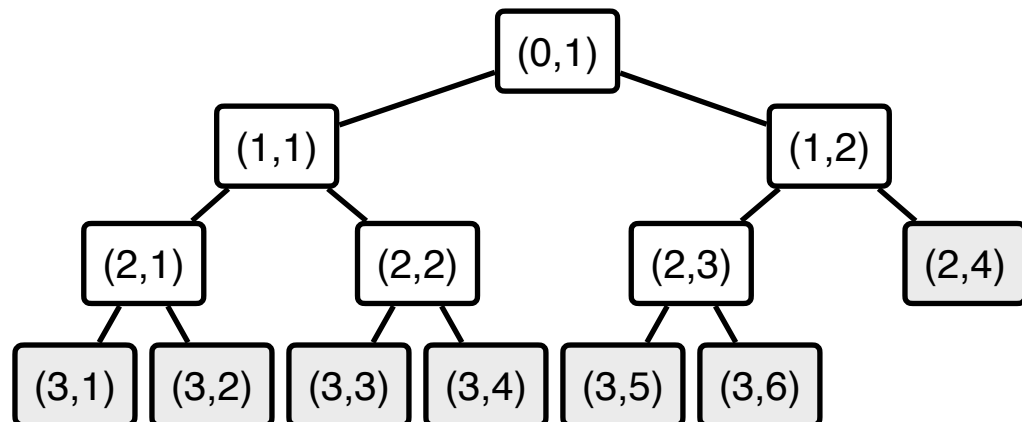
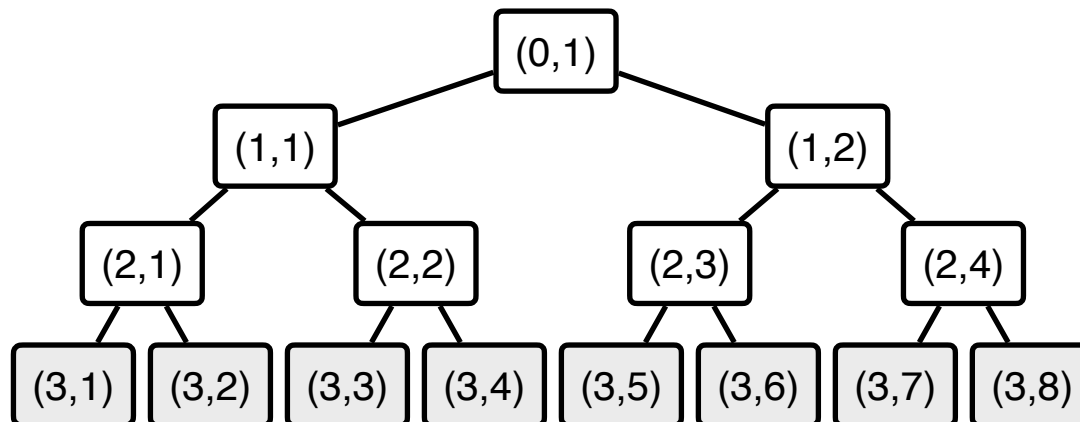
$\mathbf{V}_{\text{IOP}}[Q_i, \mathbf{a}_i]_{i \in [k]} (\mathbb{X}, (\rho_1, \dots, \rho_k))$

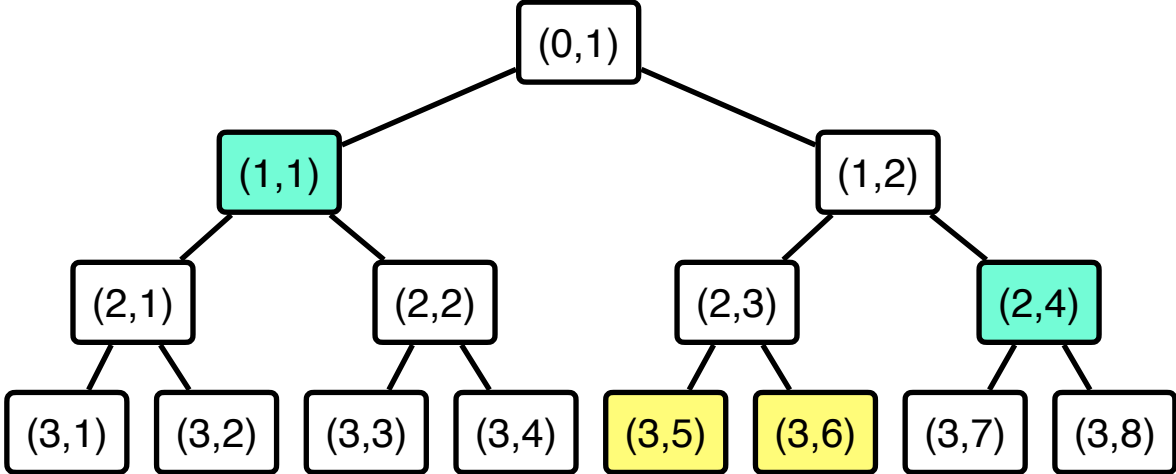




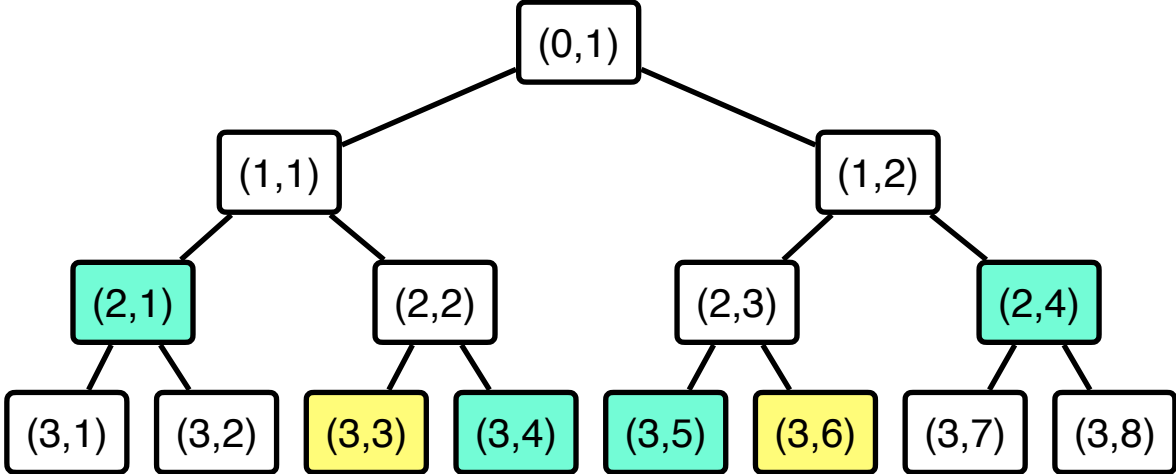


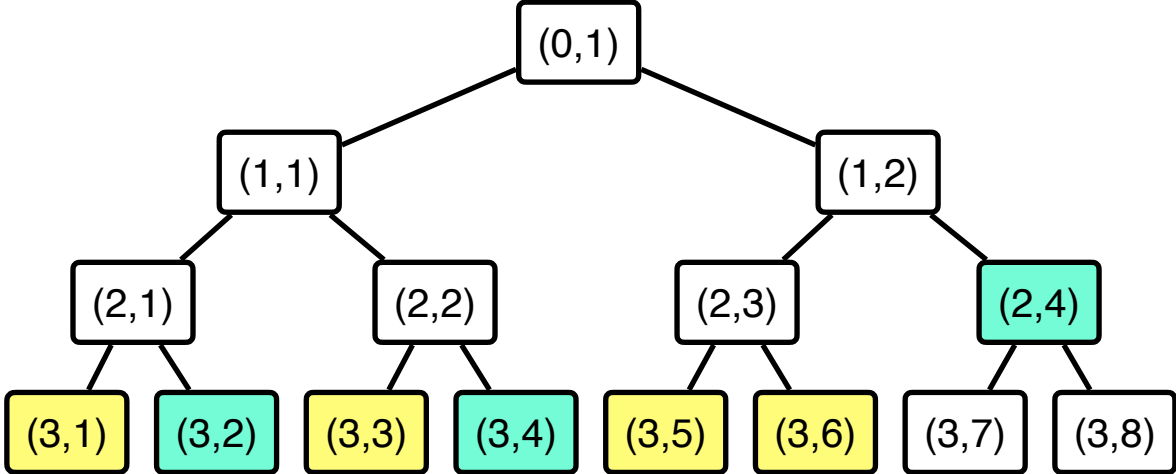


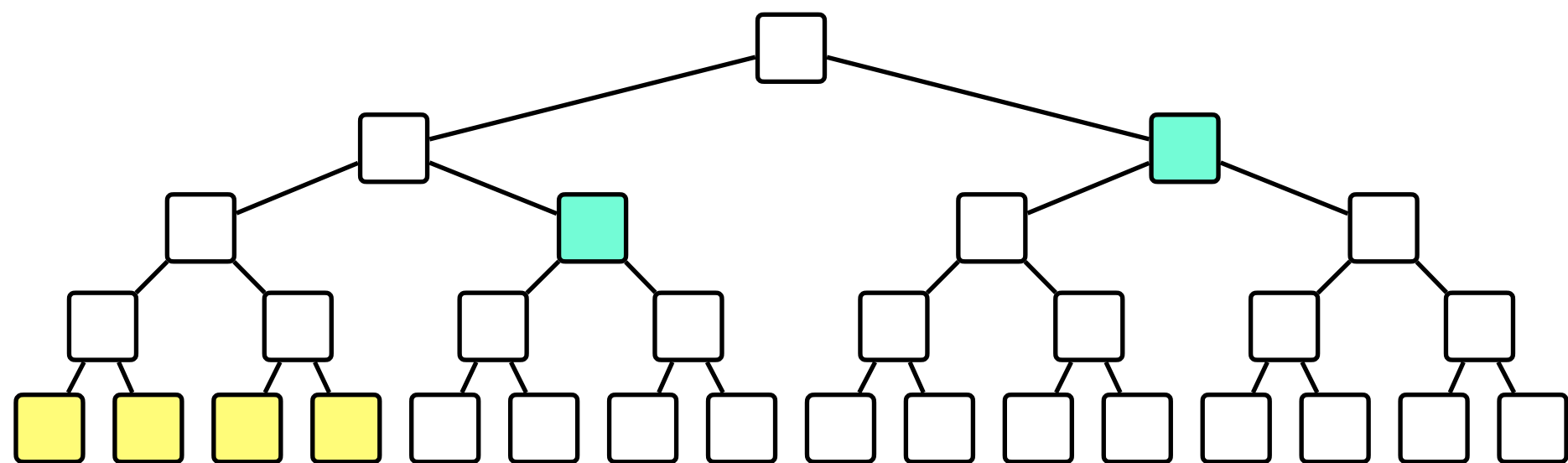
$T_1$  $T_2$  $T_3$  $T_4$  $T_5$  $T_6$  $T_7$  $T_8$ 

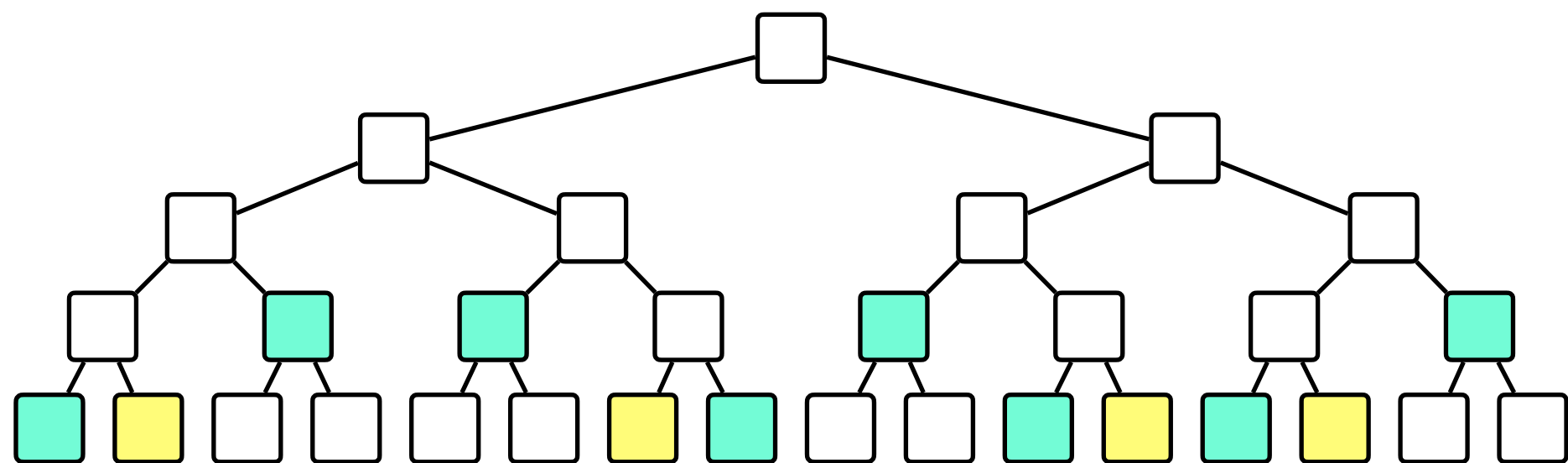


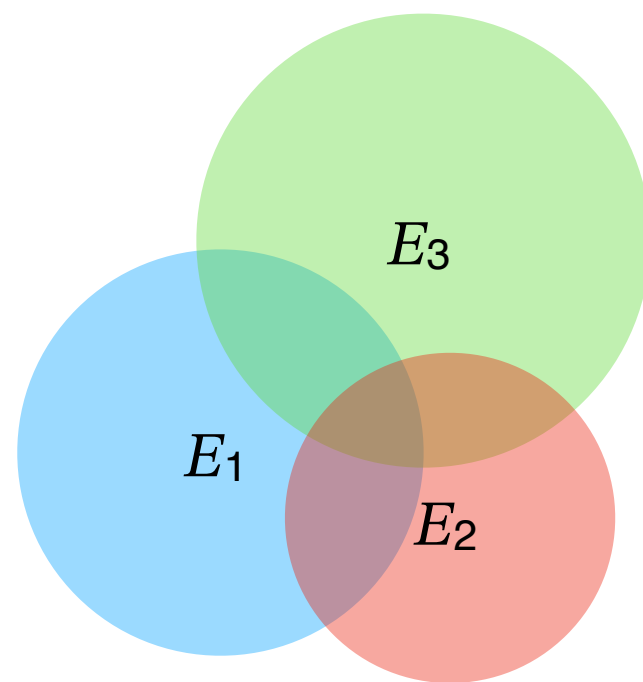


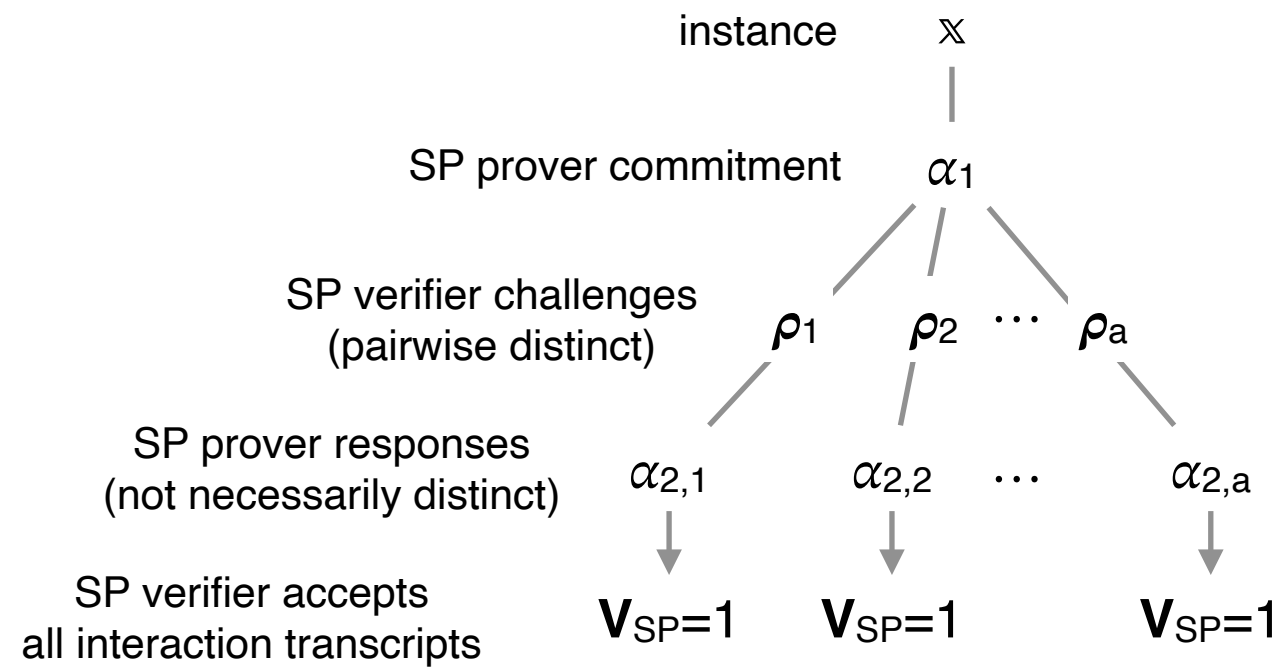


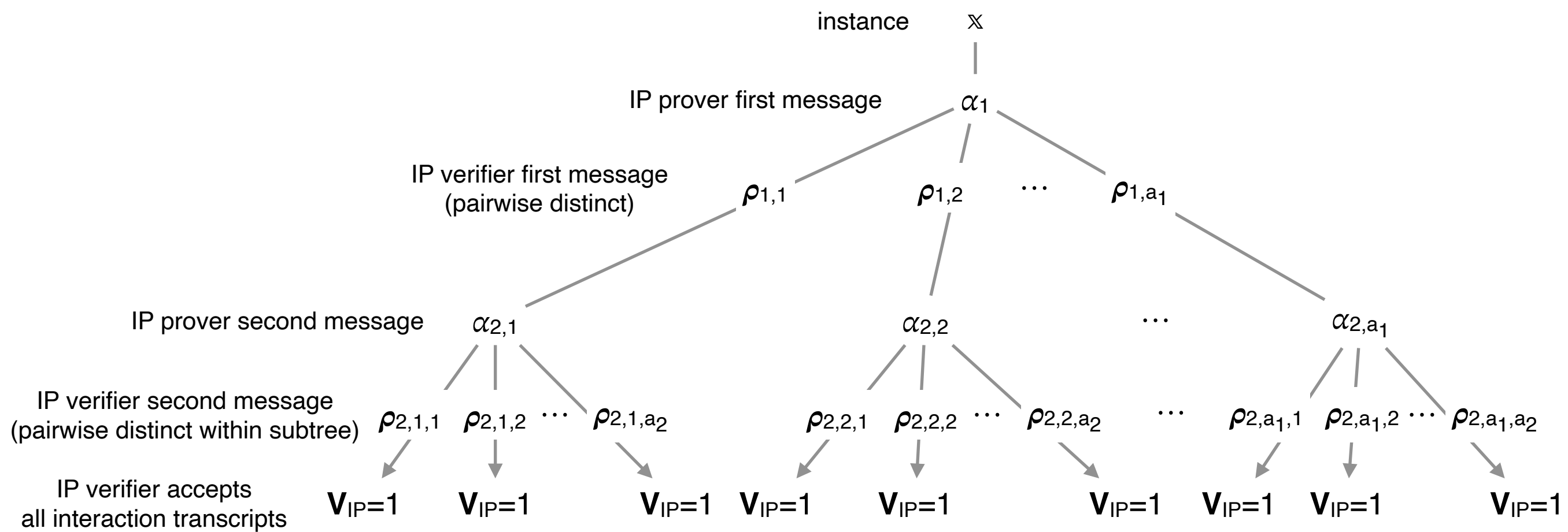


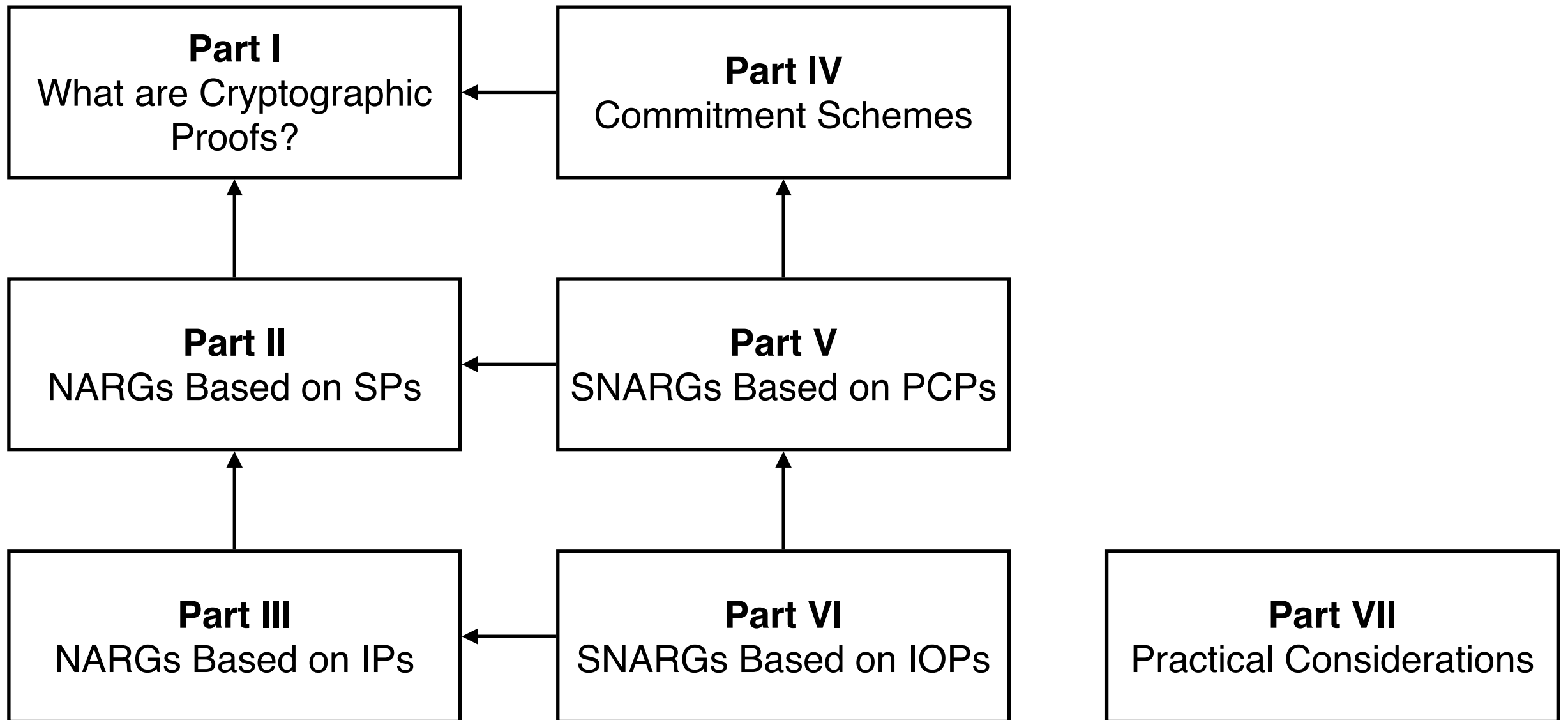














# Building Cryptographic Proofs from Hash Functions

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