

By Yiming Xiao

A BRIEF INTRODUCTION TO

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**THE PRINCIPLES OF MRI**

## WHAT IS IN THIS LECTURE?

- ▶ Some bits of history of MRI
- ▶ How are MR images generated?
  - basic physics, image contrast & k-space
- ▶ What can you do with MRI?

## WHAT IS NOT IN THIS LECTURE?

- ▶ Complicated Quantum Physics
- ▶ Long derivation of equations

# **WHAT IS MRI?**

## **- A FIRST LOOK**

# MRI = MAGNETIC RESONANCE IMAGING



## FOR YOUR SAFETY...

Never wear metal inside the scan room!

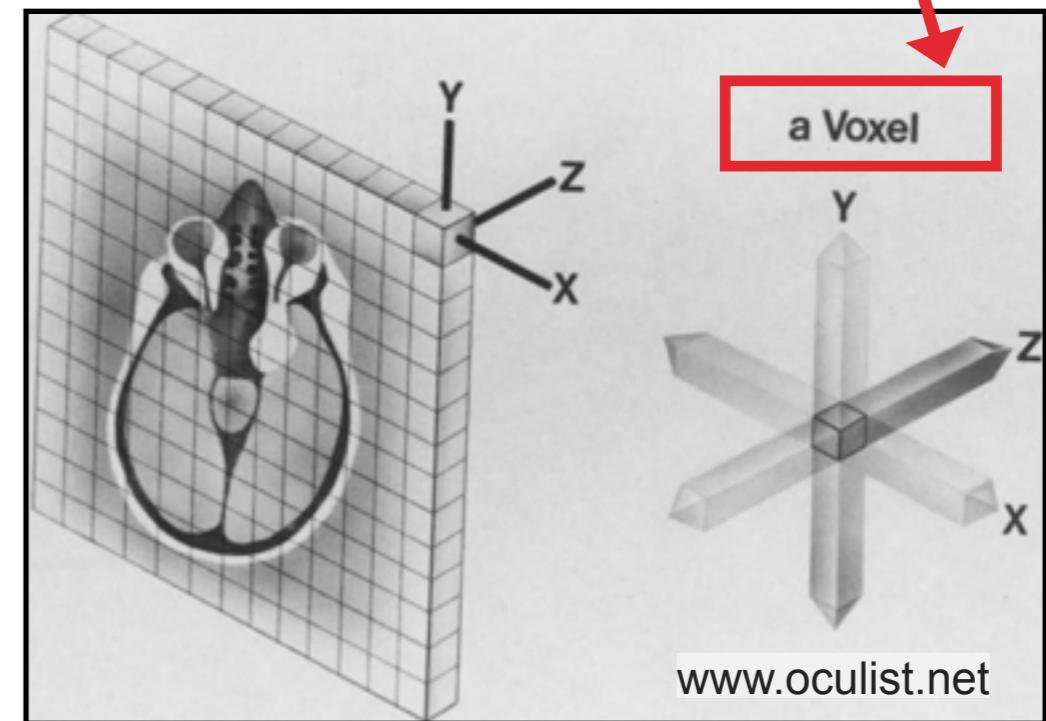
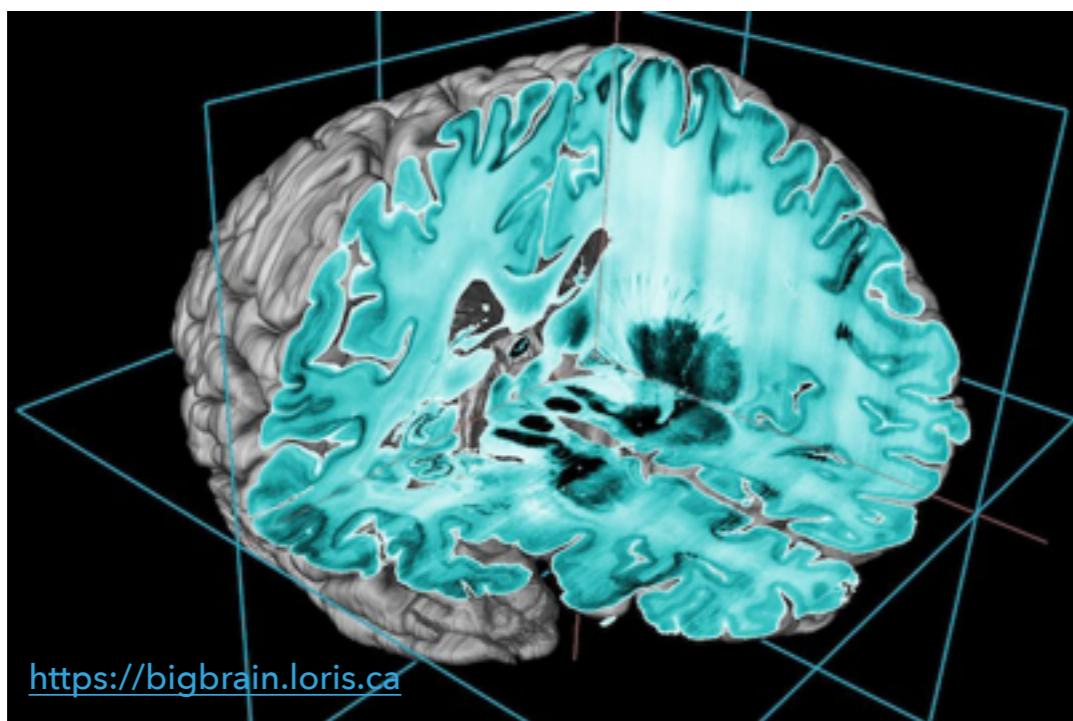


# WHY USE MRI?

- Non-invasive investigation of the anatomy

## WHY USE MRI?

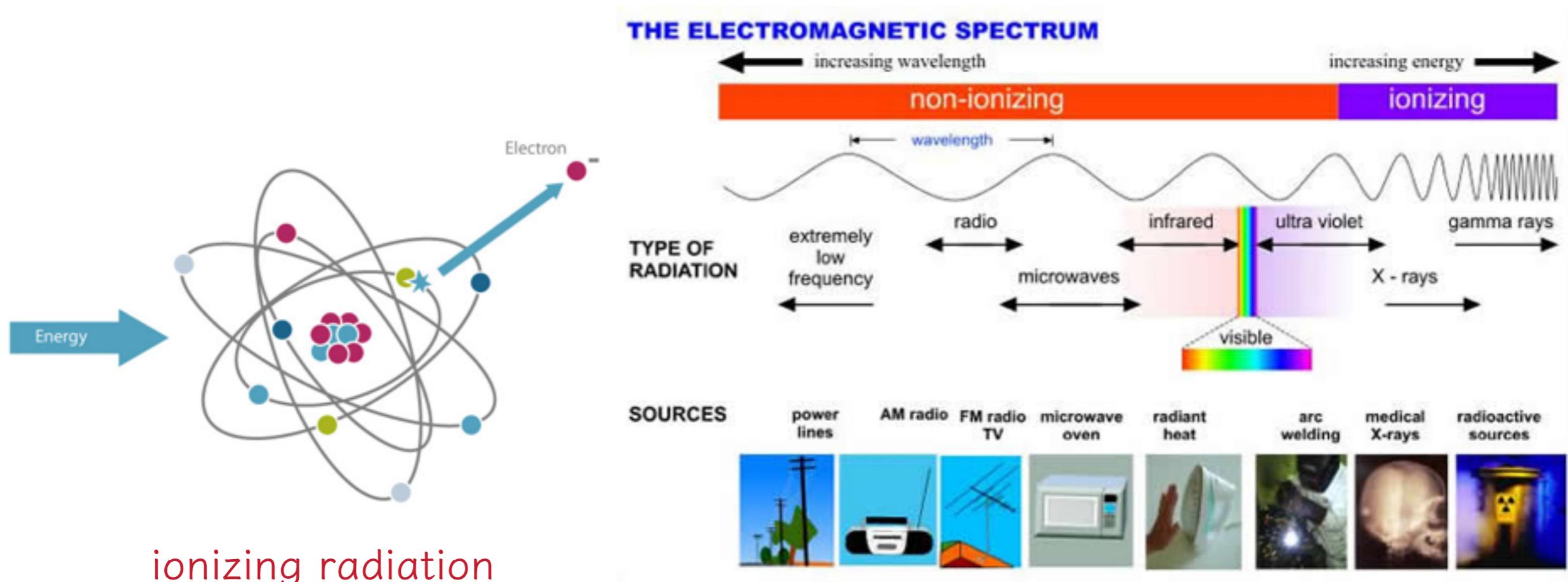
- Non-invasive investigation of the anatomy
- 3D volumetric imaging



More intuitive & capability to quantify volumes

## WHY USE MRI?

- Non-invasive investigation of the anatomy
- 3D volumetric imaging
- Non-ionizing radiation



# WHY USE MRI?

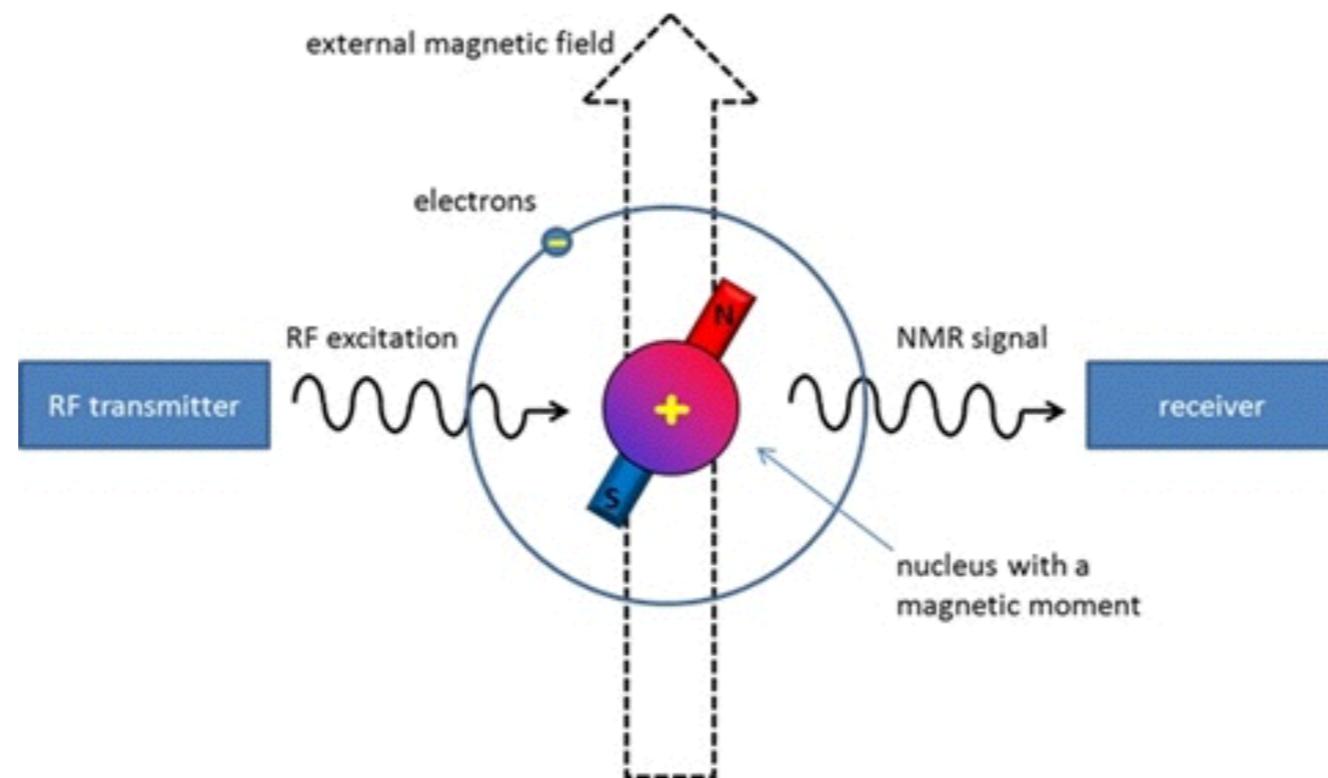
- Non-invasive investigation of the anatomy
- 3D volumetric imaging
- No ionizing radiation
- Great for soft body tissues

For bone or metal materials, CT or X-ray is still recommended..

# WHY USE MRI?

- Non-invasive investigation of the anatomy
- 3D volumetric imaging
- No ionizing radiation
- Great for soft body tissues
- Capability of measuring various chemical/physical/functional properties of organs, and we are still exploring

# WHERE IS SOURCE OF THE SIGNAL ?



Nuclear magnetic resonance (NMR) phenomenon

When placed in a magnetic field, a nucleus can absorb and later emit energy

## WHERE IS SOURCE OF THE SIGNAL ?

- NMR was first experimentally observed in 1945, nearly simultaneously by the research groups of **Felix Bloch** at Stanford University, and **Edward Purcell** at Harvard University.
- Bloch and Purcell were jointly awarded the Nobel Prize in Physics in 1952 for their discovery of Nuclear Magnetic Resonance Spectroscopy.



Felix Bloch



Edward Purcell

## GOING FOR AN NMRI?



**Nuclear Magnetic  
resonance imaging (NMRI)**

OR

**Magnetic Resonance  
Imaging (MRI)**

## GOING FOR AN NMRI?



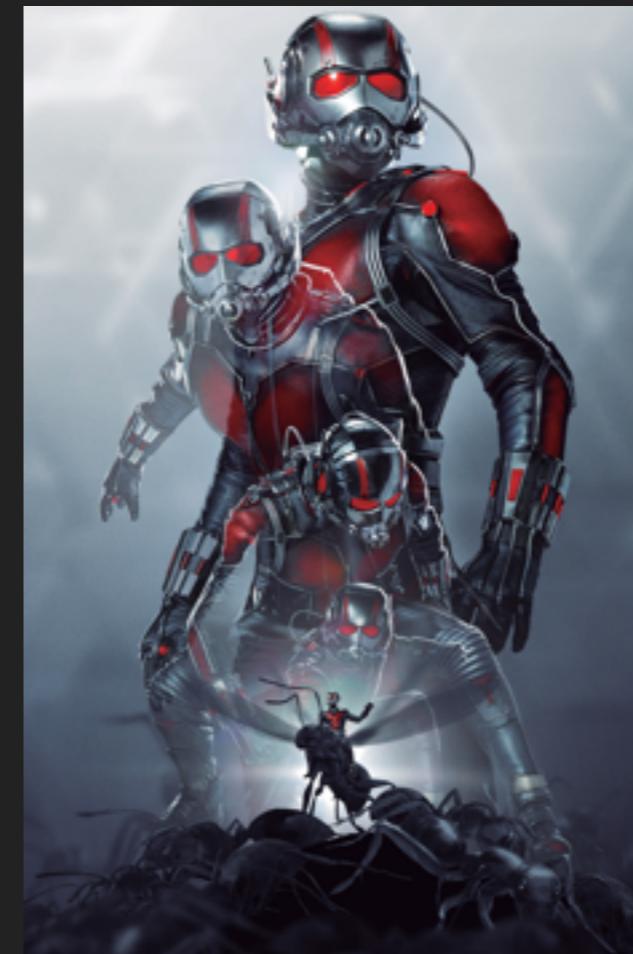
**Nuclear Magnetic  
resonance imaging (NMRI)**

OR

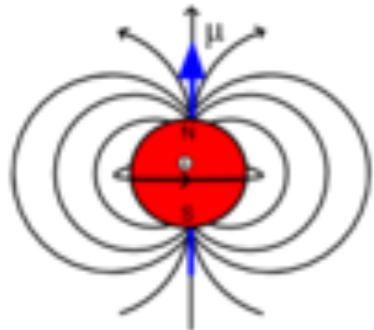
**Magnetic Resonance  
Imaging (MRI)**

Name change in the 1980s

# HOW TO GET AN MR IMAGE?

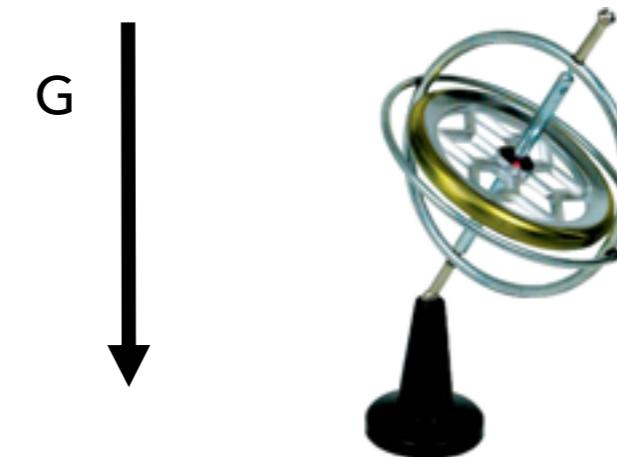
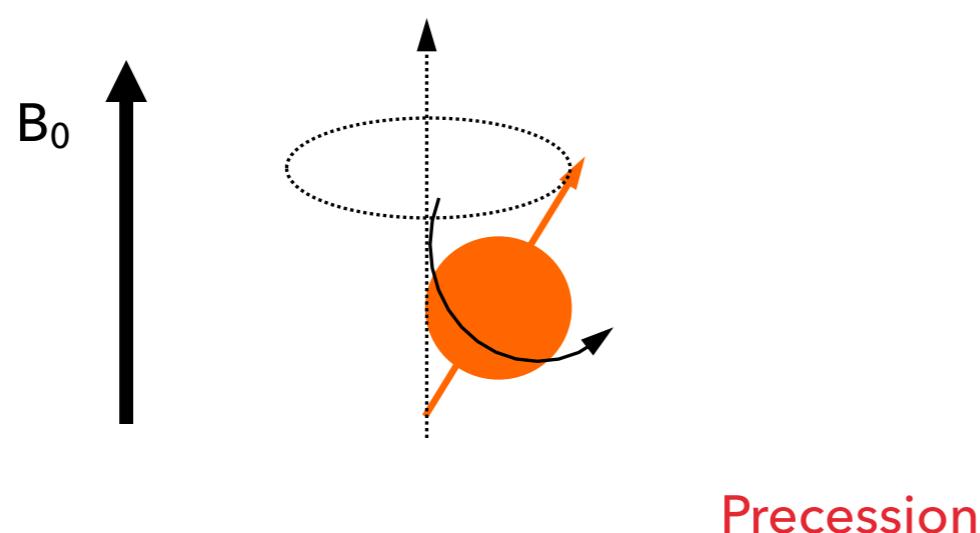


# WHAT IS A SPIN?



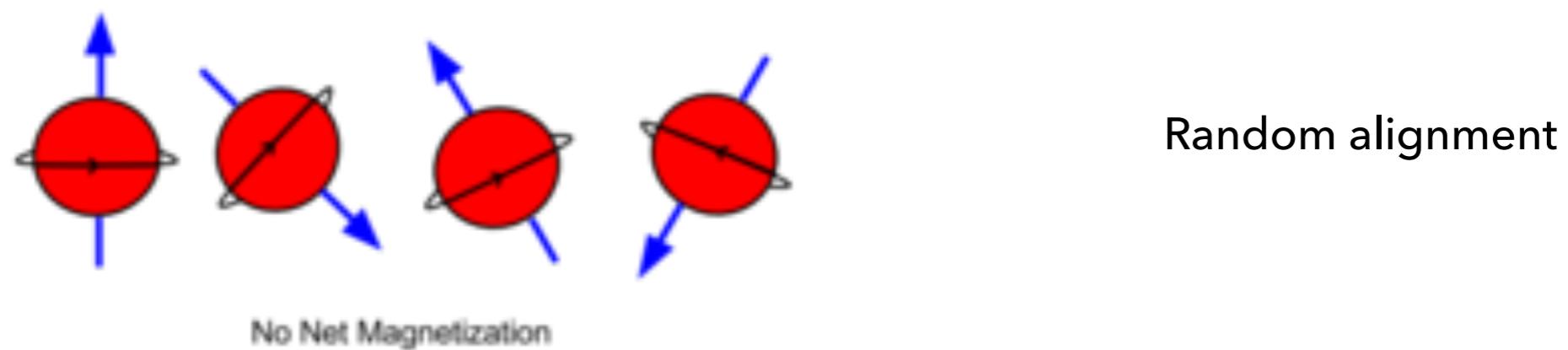
If a nucleus of an atom has an odd number of protons or neutrons, the atom possesses a nonzero spin angular momentum  $S$ , which is called a nuclear spin and is associated with a magnetic dipole moment  $\mu$ .

- For MRIs, we often deal with  $^1\text{H}$  atoms, as 70% of us is  $\text{H}_2\text{O}$ .
- The particle is not actually spinning or rotating.
- *Spin* interacts with electromagnetic fields whereas *classic angular momentum ( $L$ )* interacts with gravitational fields.

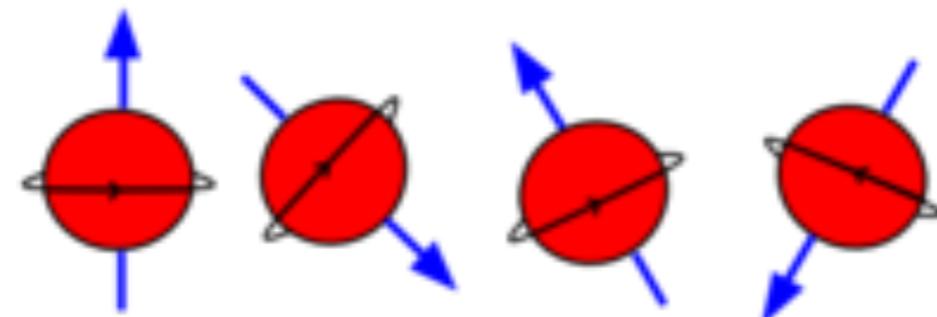


Precession

## MAGNETIZATION $M = \Sigma \mu$

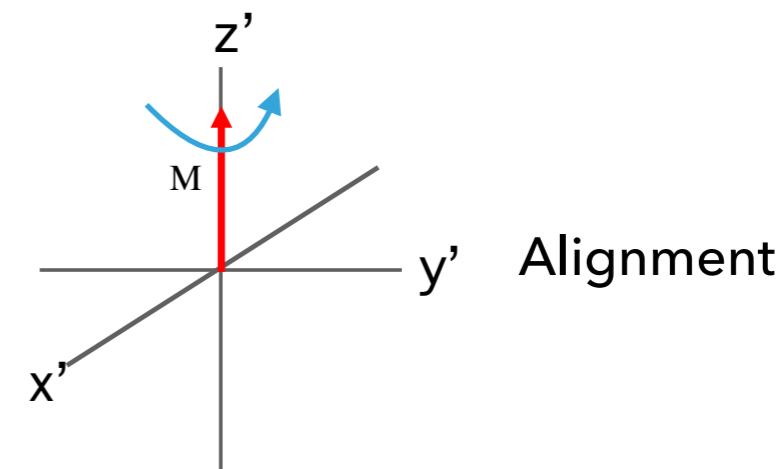
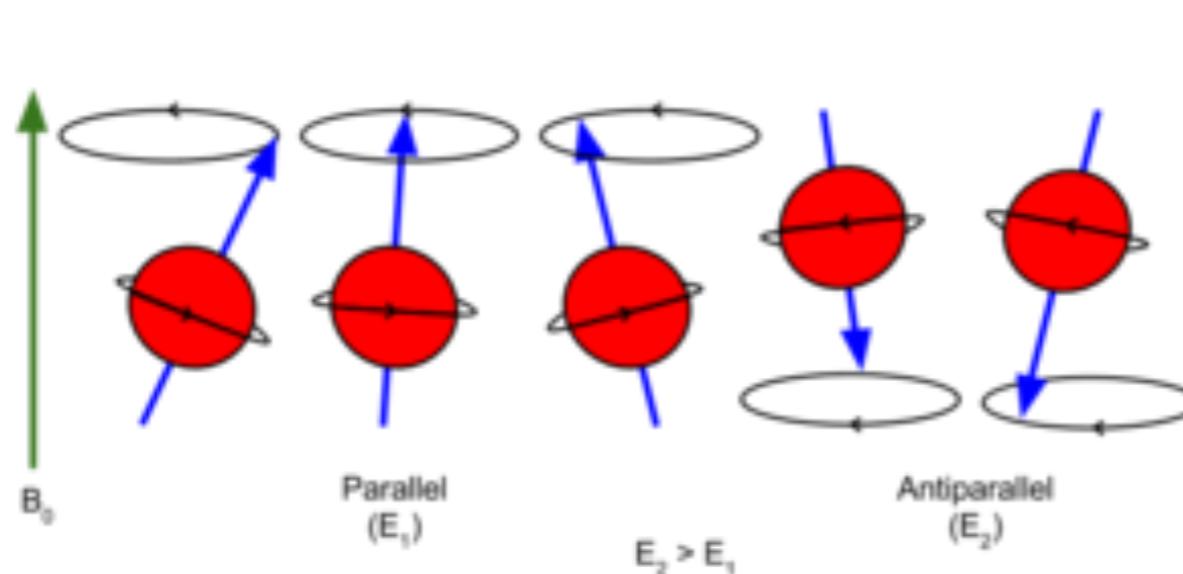


## MAGNETIZATION $M = \sum \mu$



Random alignment

No Net Magnetization

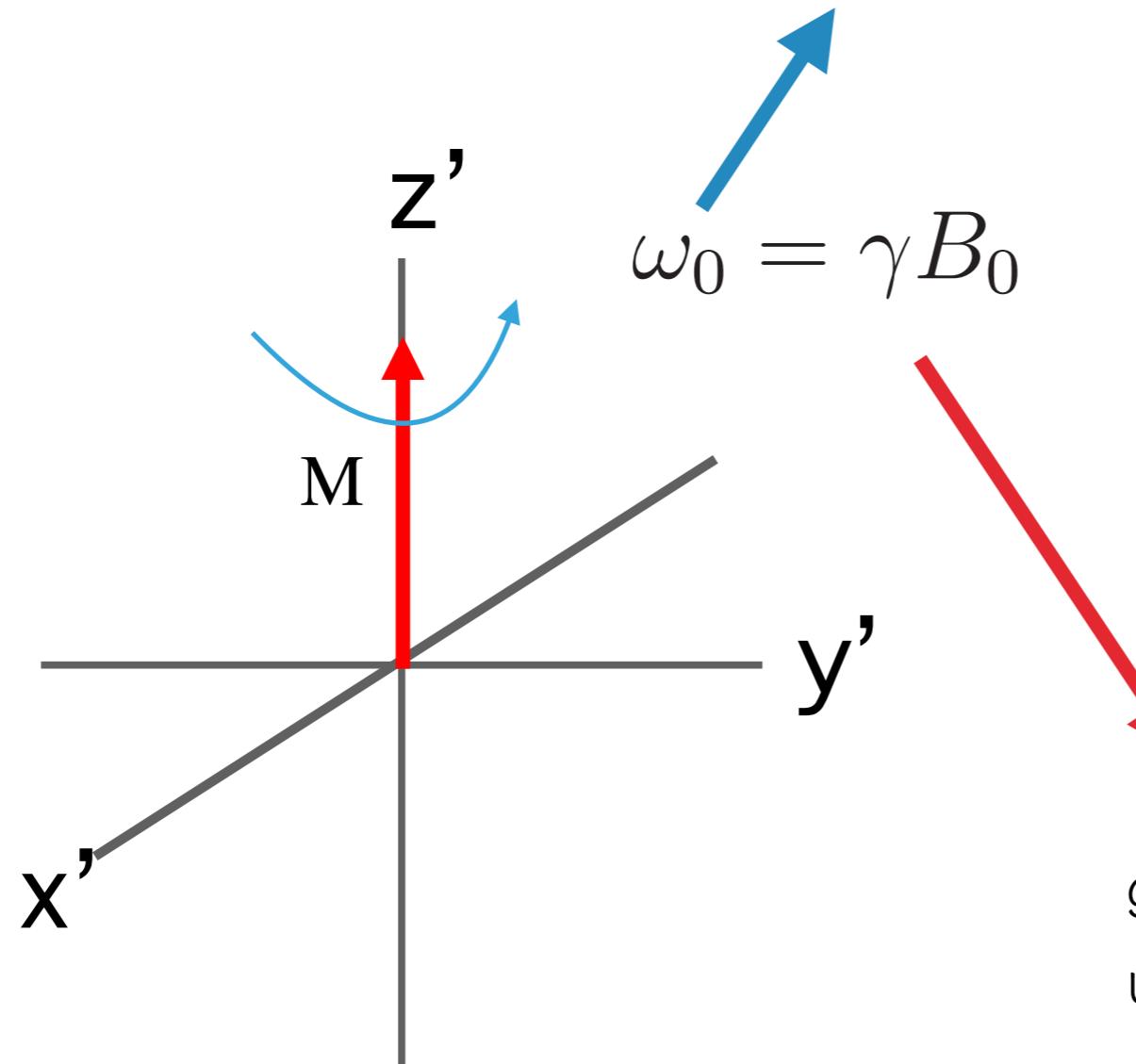


Alignment

The population ratio of two states obeys the Boltzmann distribution

## MAGNETIZATION

$$\mathbf{M} = \Sigma \mu$$

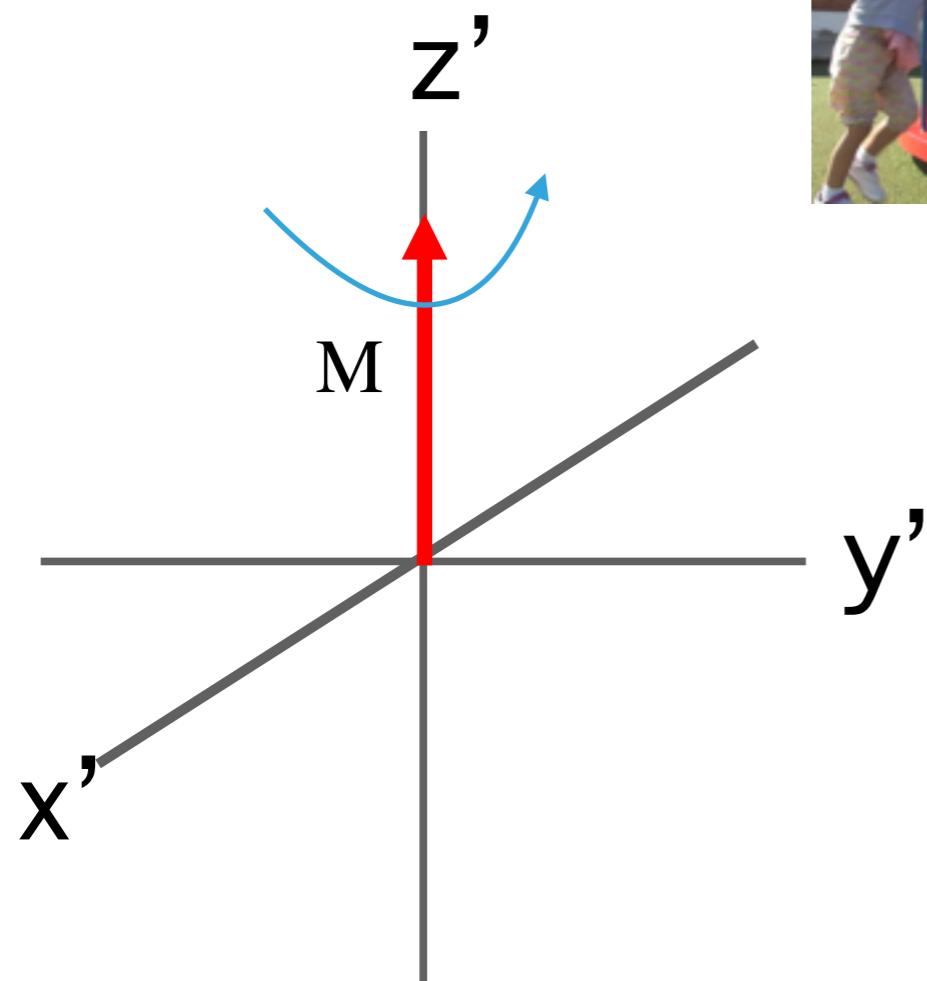


Larmor frequency

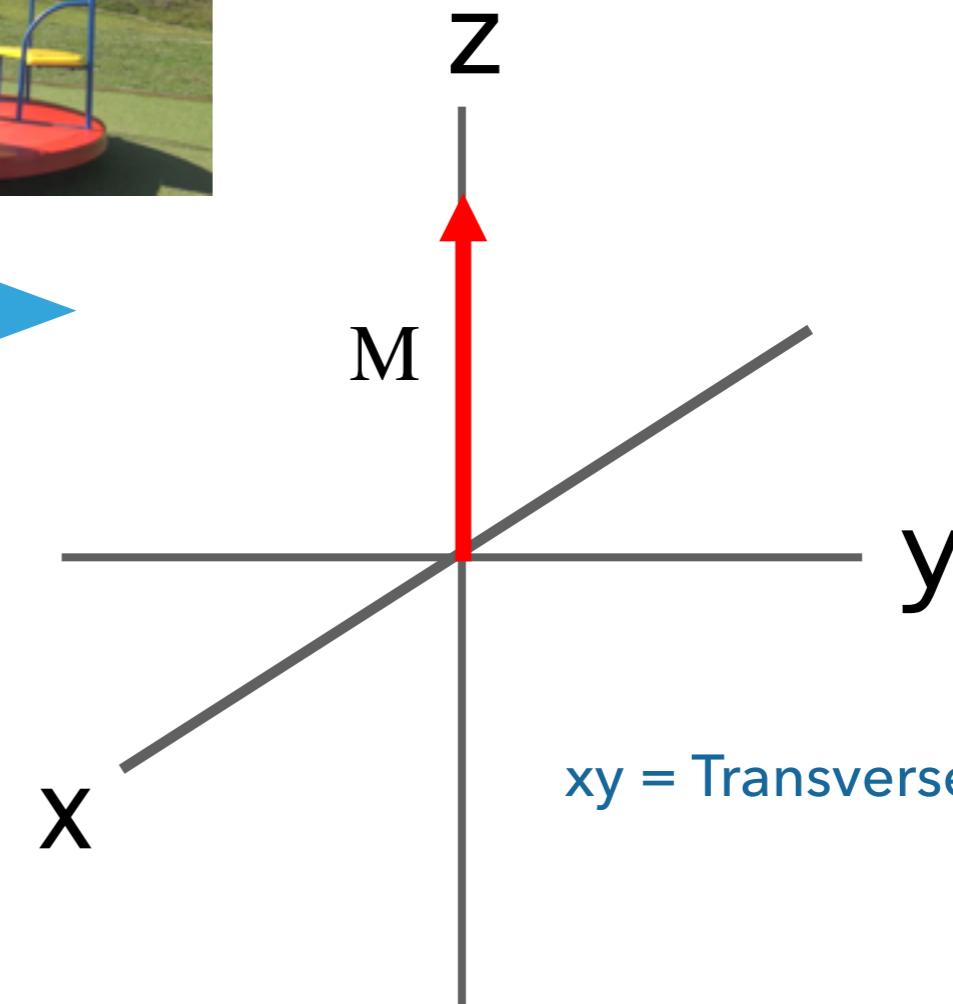
gyromagnetic ratio,  
unique to different atoms

## MAGNETIZATION

$$\mathbf{M} = \sum \mu$$



Absolute Frame



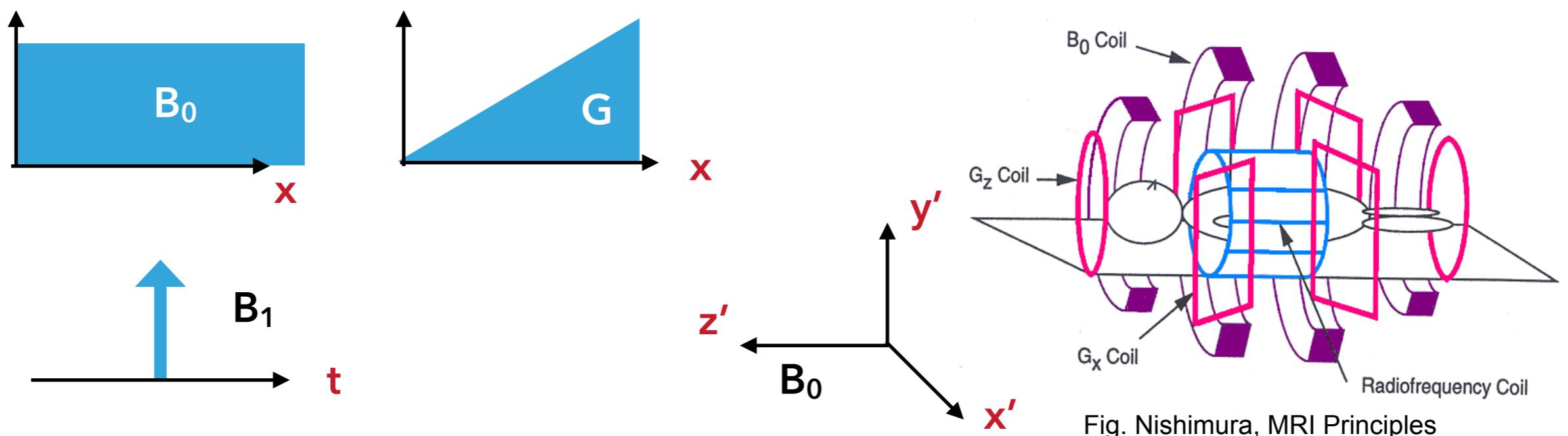
Rotating Frame

$z$  = Longitudinal direction

$xy$  = Transverse plane

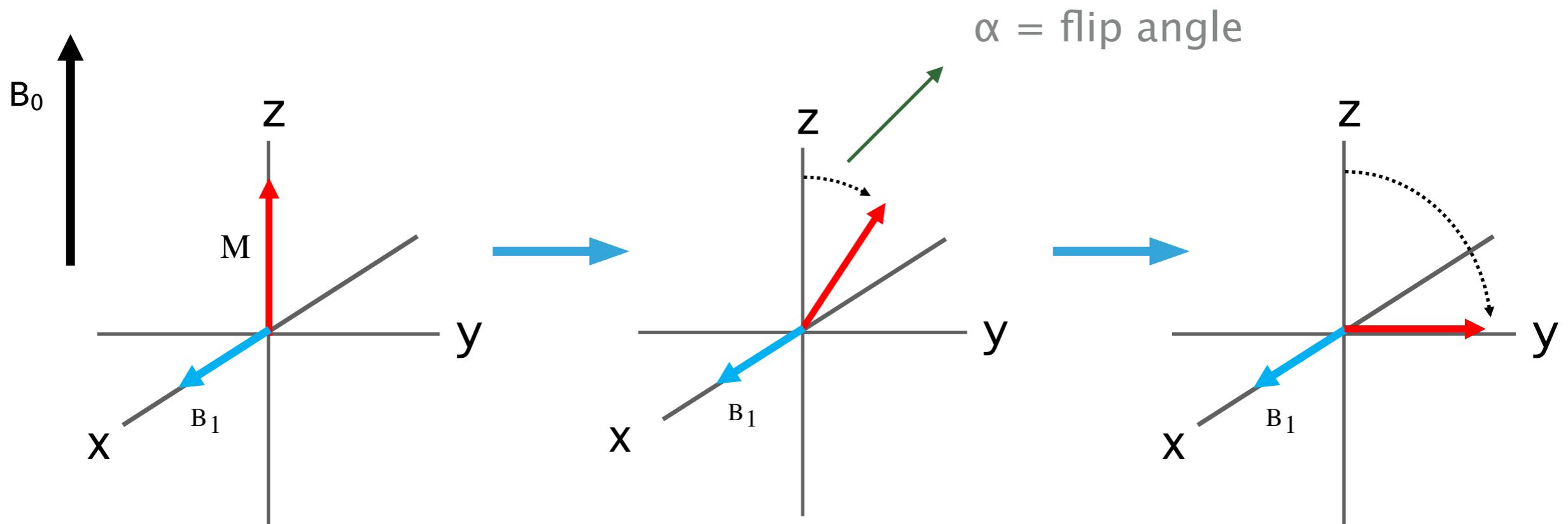
## THE 3 MAGNETIC FIELDS IN MRI

- $B_0$  field: the main field in an MRI scanner (0.5T, 1.5T, 3T, 7T & 9.4T)
- $B_1$  field: small ( $\sim 1/10,000$ T) radio frequency pulse to tip the spin out of equilibrium to produce the signals that determine the image intensity
- $G$  field: the spatially varying gradient field that helps encode spatial information to MRI signals



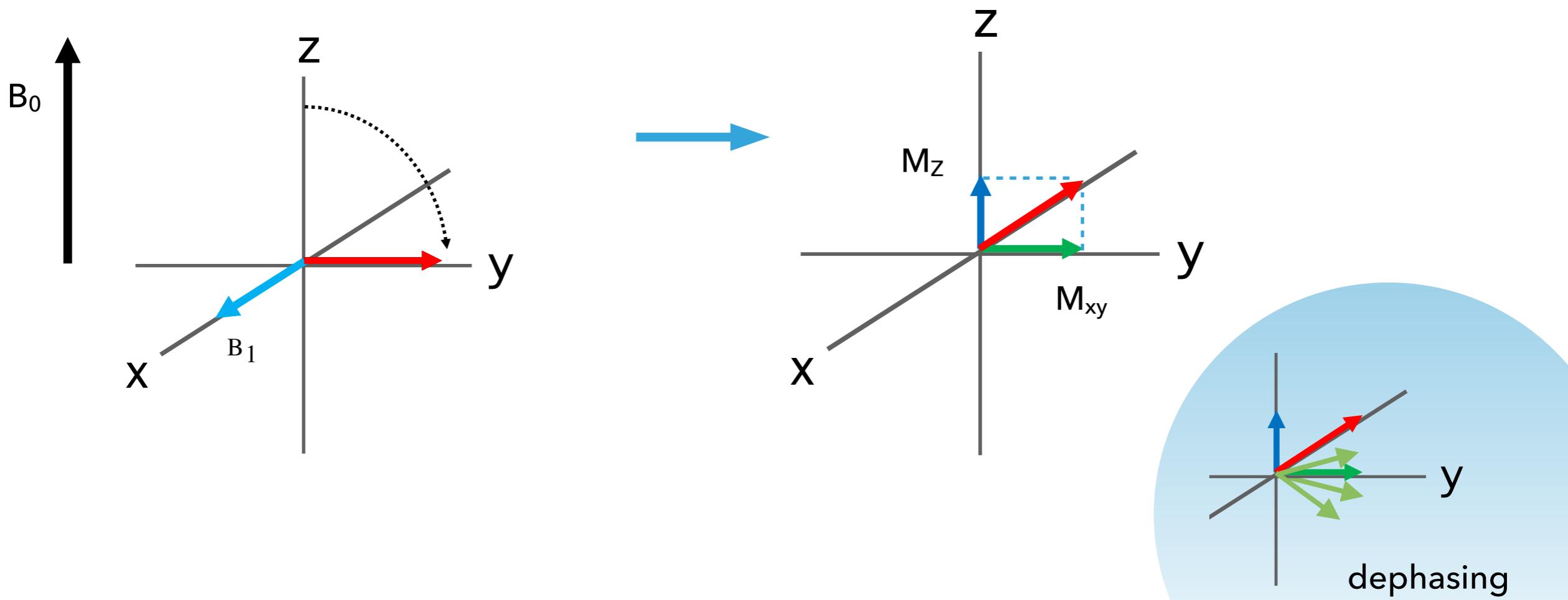
## EXCITATION & RELAXATION

- **Excite** nuclei = tip the magnetization away from the z-direction by  $B_1$ .
- The angle depends on the duration and magnitude of  $B_1$ .
- $B_1$  is tuned to the Larmor frequency to induce magnetic resonance.
- Energy is absorbed.



## EXCITATION & RELAXATION

- **Relaxation** : the process of returning to the magnetization's equilibrium state
- $T_1$  relaxation: the longitudinal component  $\mathbf{M}_z$  grows back
- $T_2$  relaxation: the transverse component  $\mathbf{M}_{xy}$  diminishes



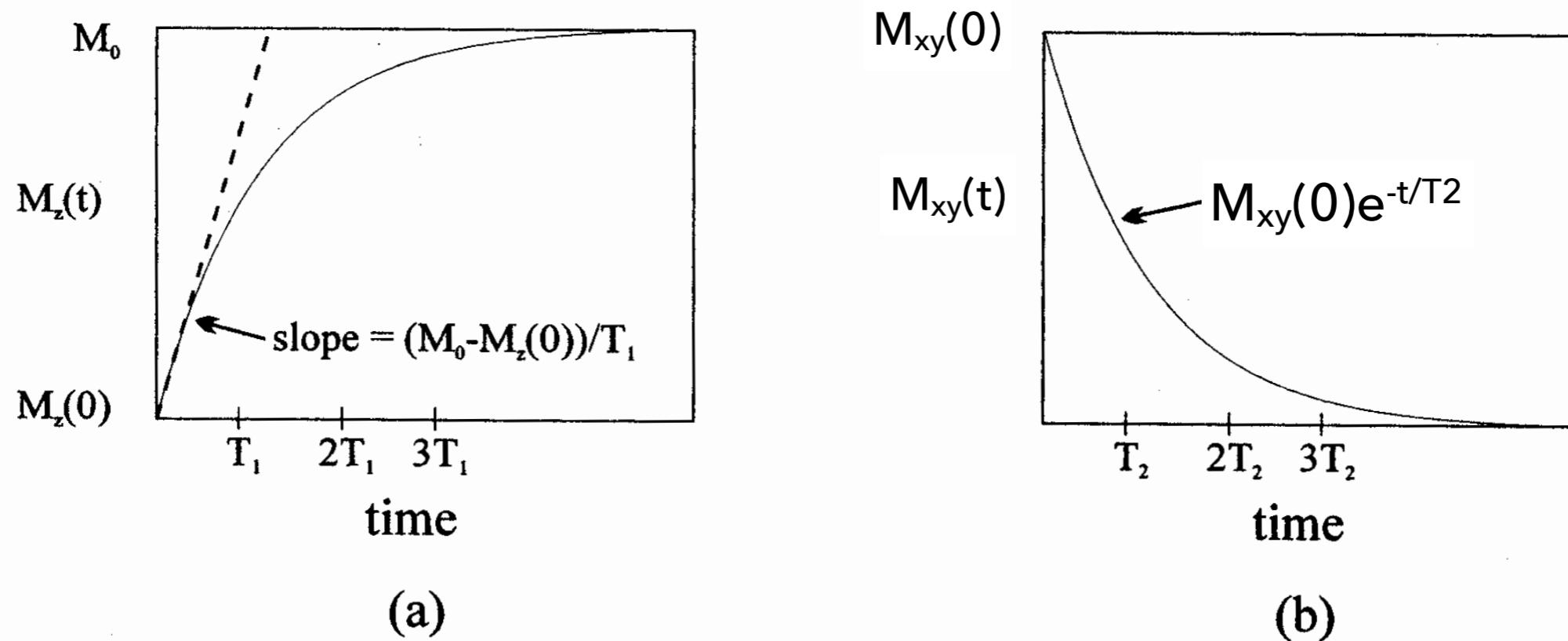


Fig. 4.1: (a) The regrowth of the longitudinal component of magnetization from the initial value  $M_z(0)$  to the equilibrium value  $M_0$ . (b) The decay of the magnitude of the transverse magnetization from an initial value.

Tissue	$T_1$ (ms)	$T_2$ (ms)
gray matter (GM)	950	100
white matter (WM)	600	80
muscle	900	50
cerebrospinal fluid (CSF)	4500	2200
fat	250	60
blood	1200	$100-200^3$

## BLOCH EQUATION

$$\frac{d\mathbf{M}}{dt} = \mathbf{M} \times \gamma \mathbf{B} - \frac{M_x \mathbf{i} + M_y \mathbf{j}}{T_2} - \frac{(M_z - M_0) \mathbf{k}}{T_1}$$

Precession due to  
the Main field, the torque



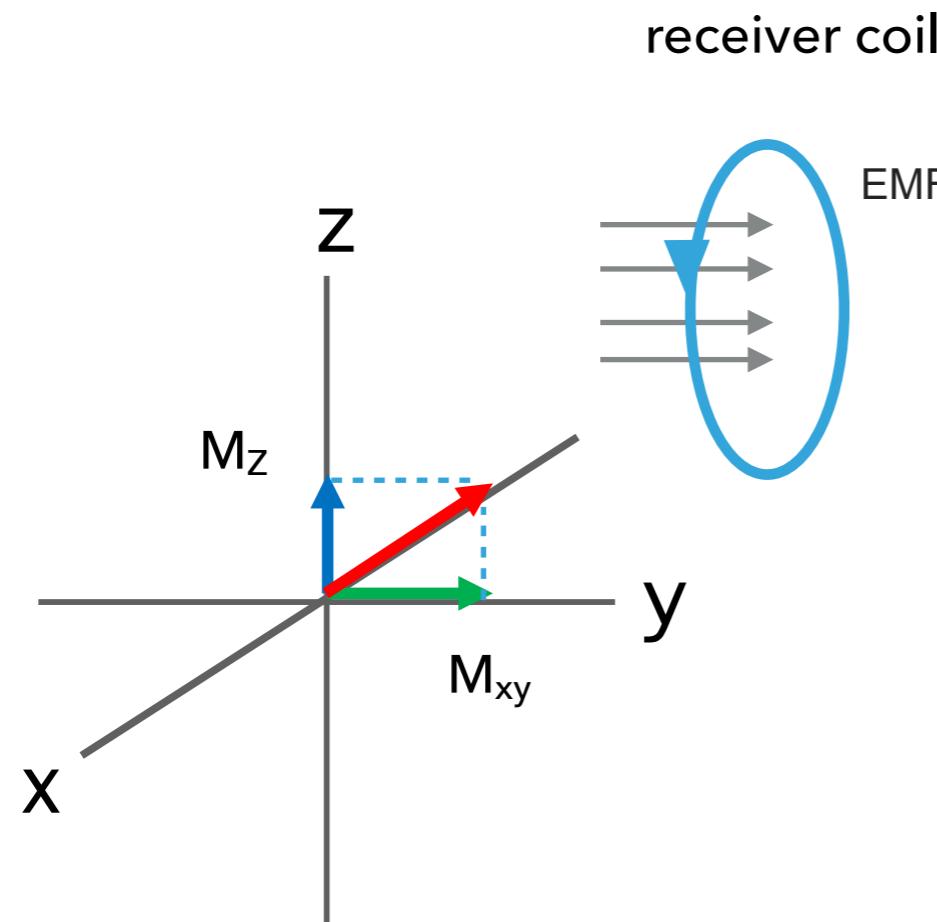
Evolution of M  
in transverse plane



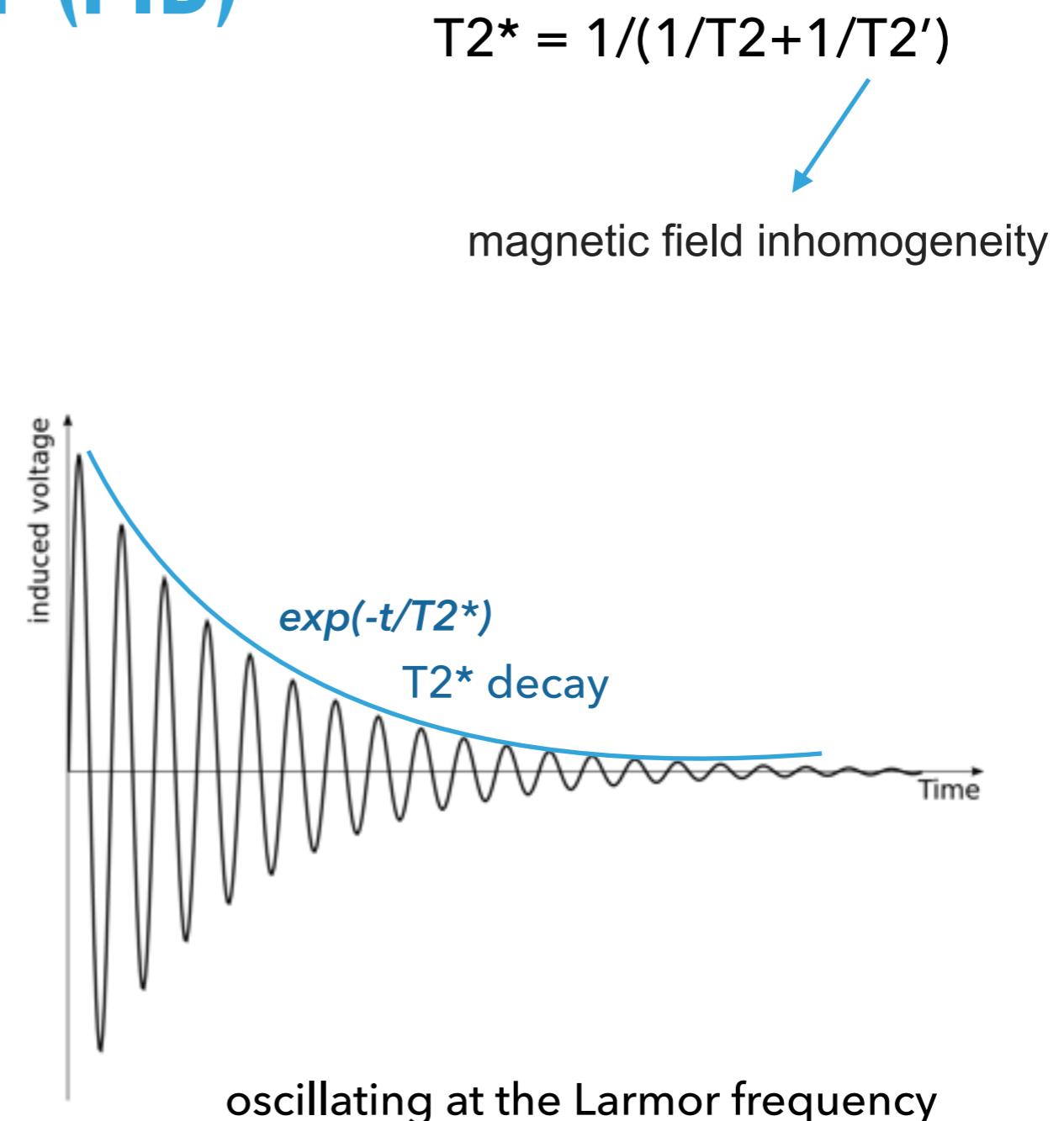
Evolution of M  
in longitudinal direction



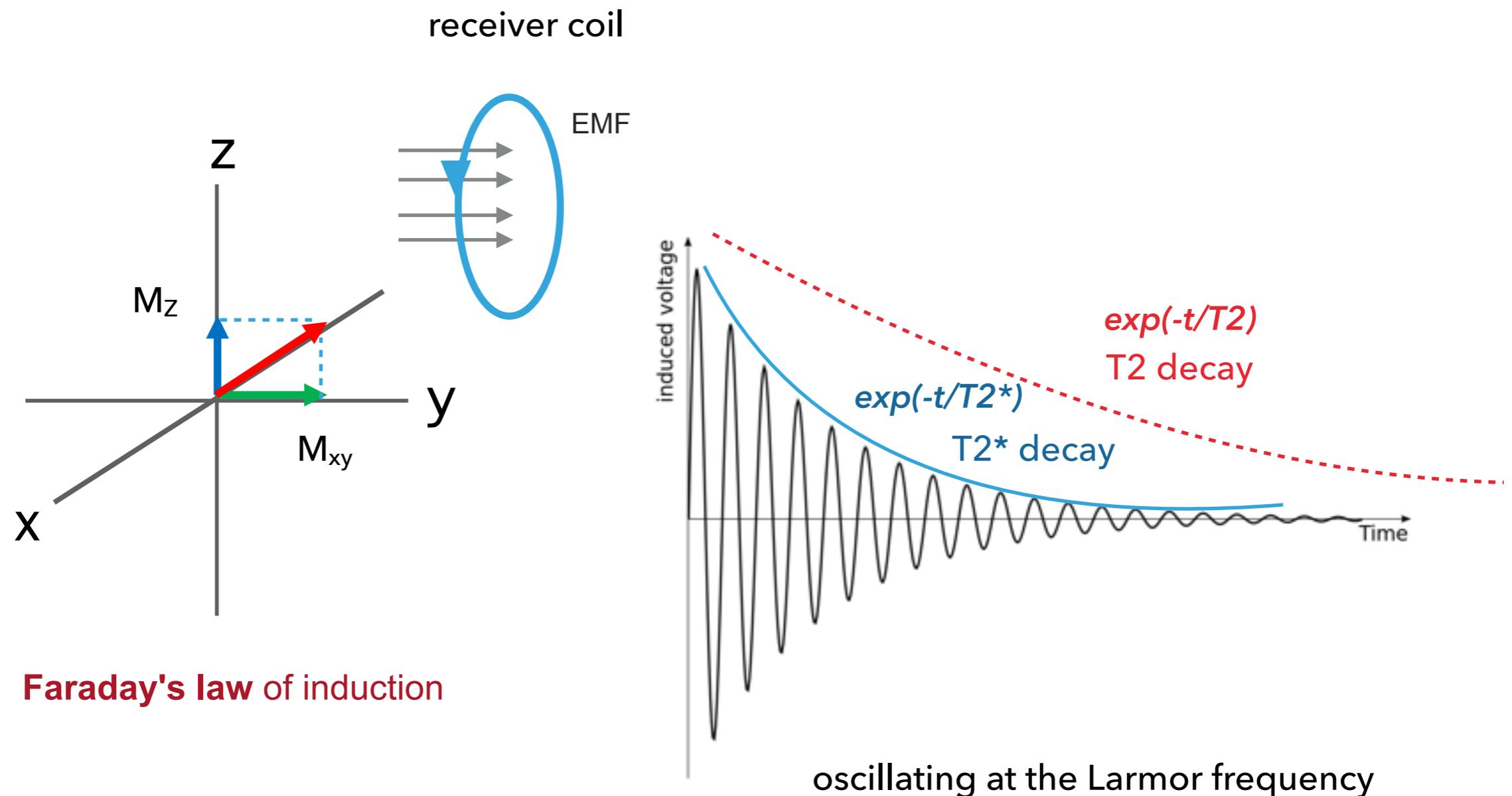
# FREE INDUCTION DECAY (FID)



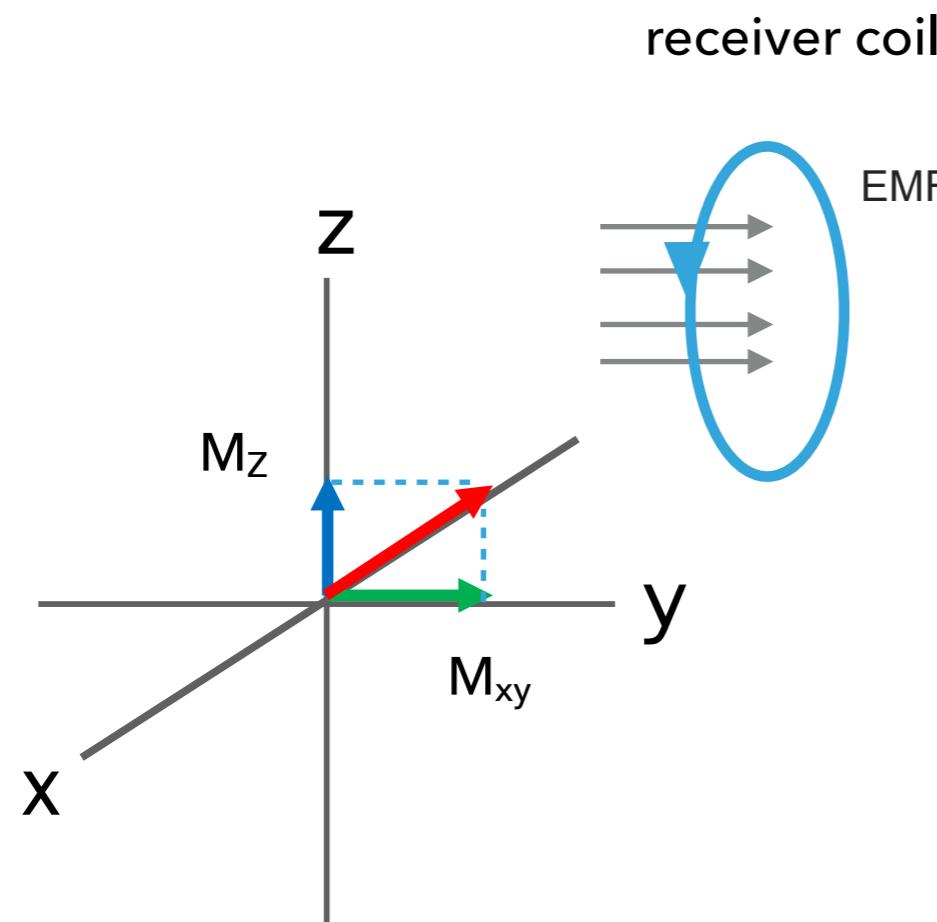
Faraday's law of induction



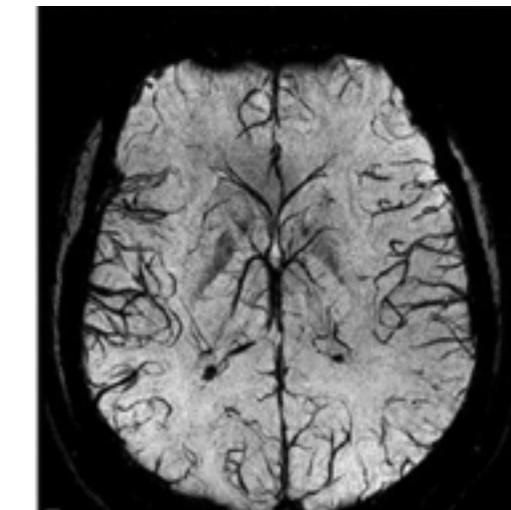
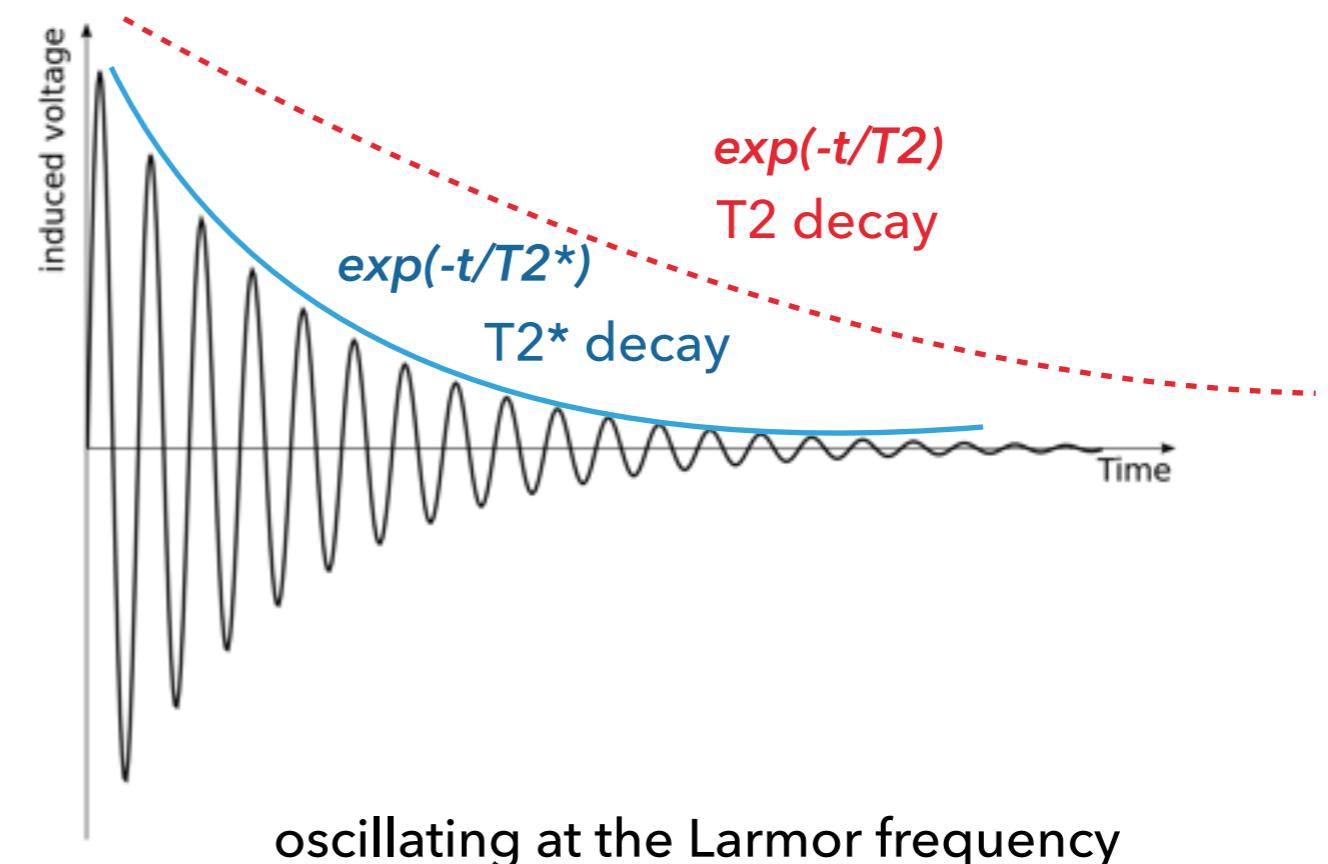
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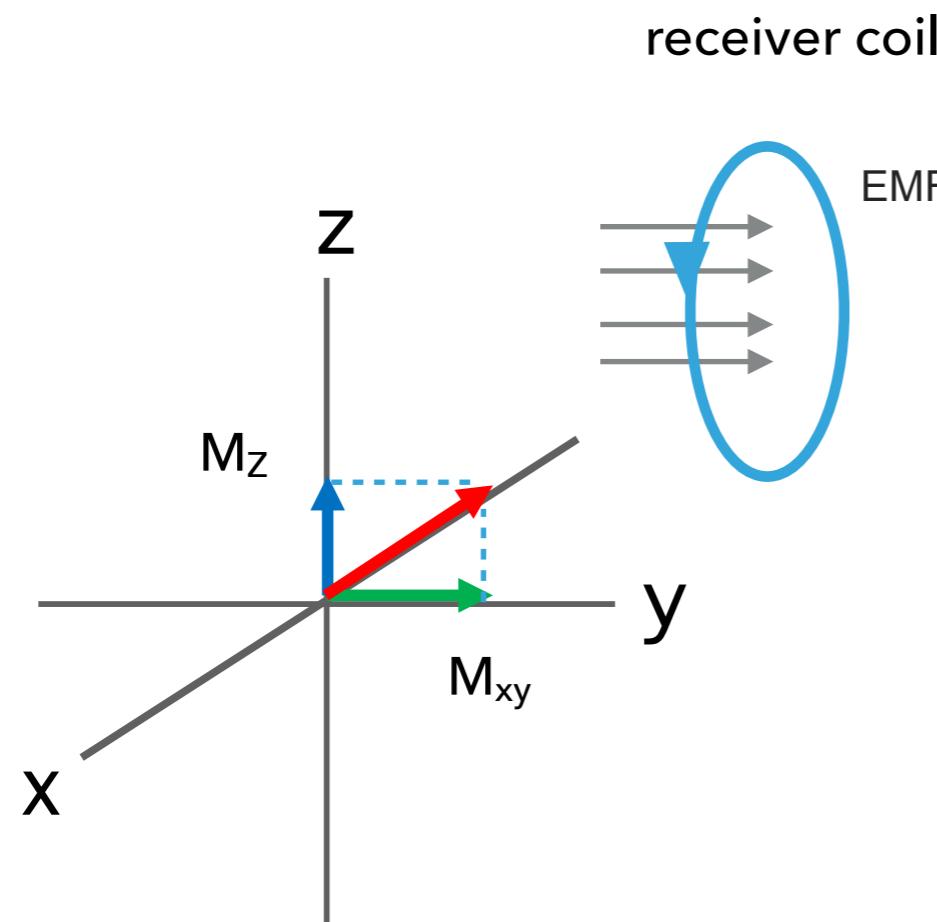
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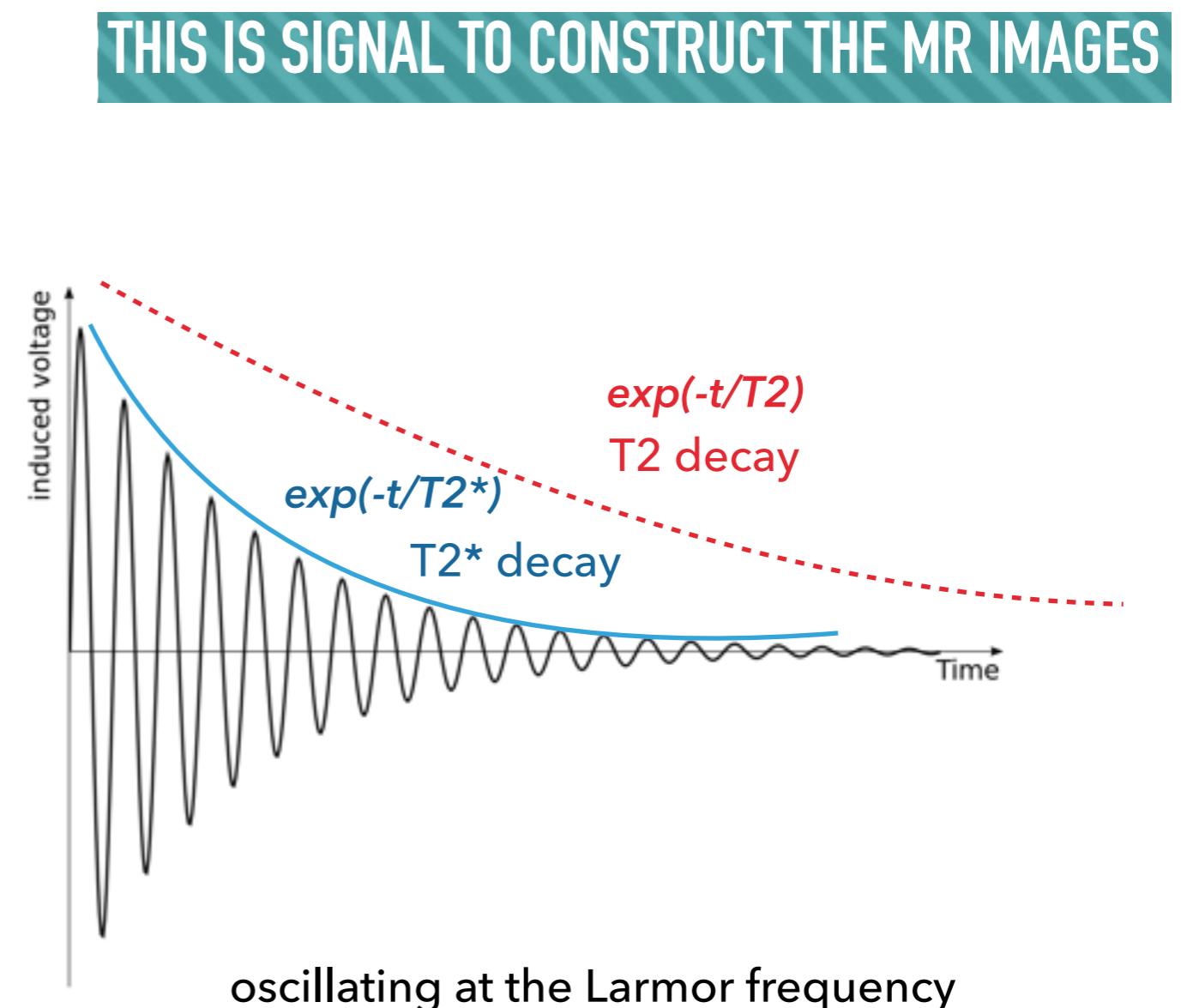
Faraday's law of induction



# FREE INDUCTION DECAY (FID)



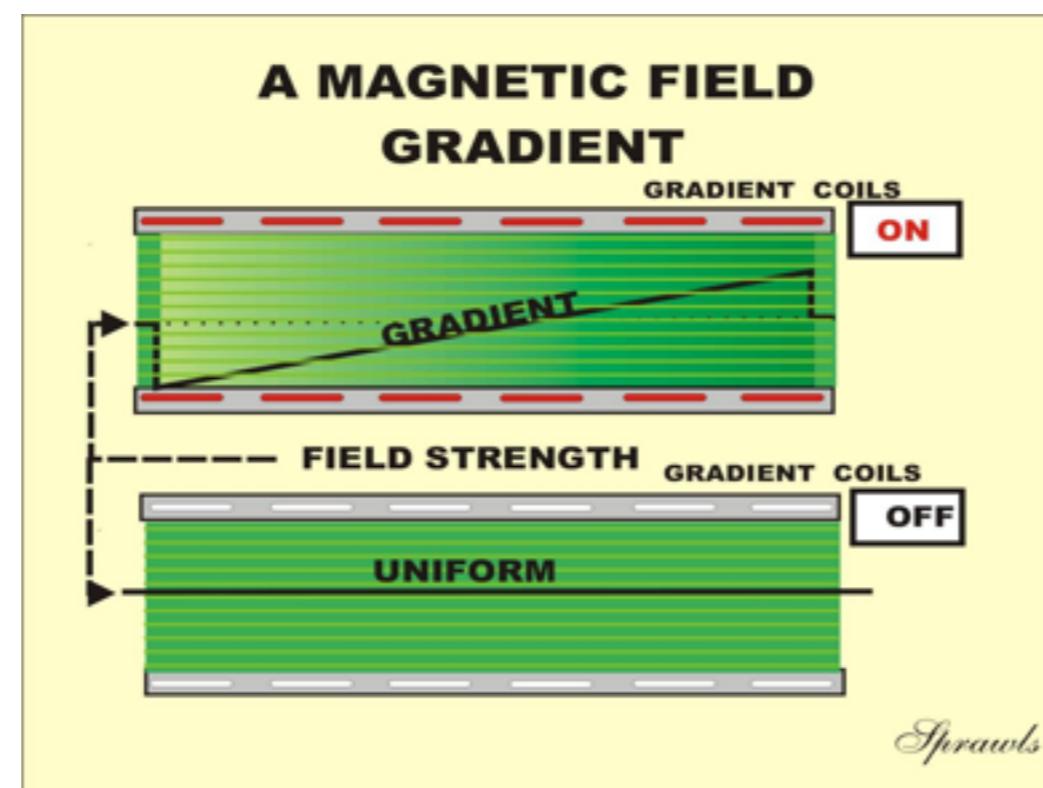
Faraday's law of induction



So what happens to the gradient field ?

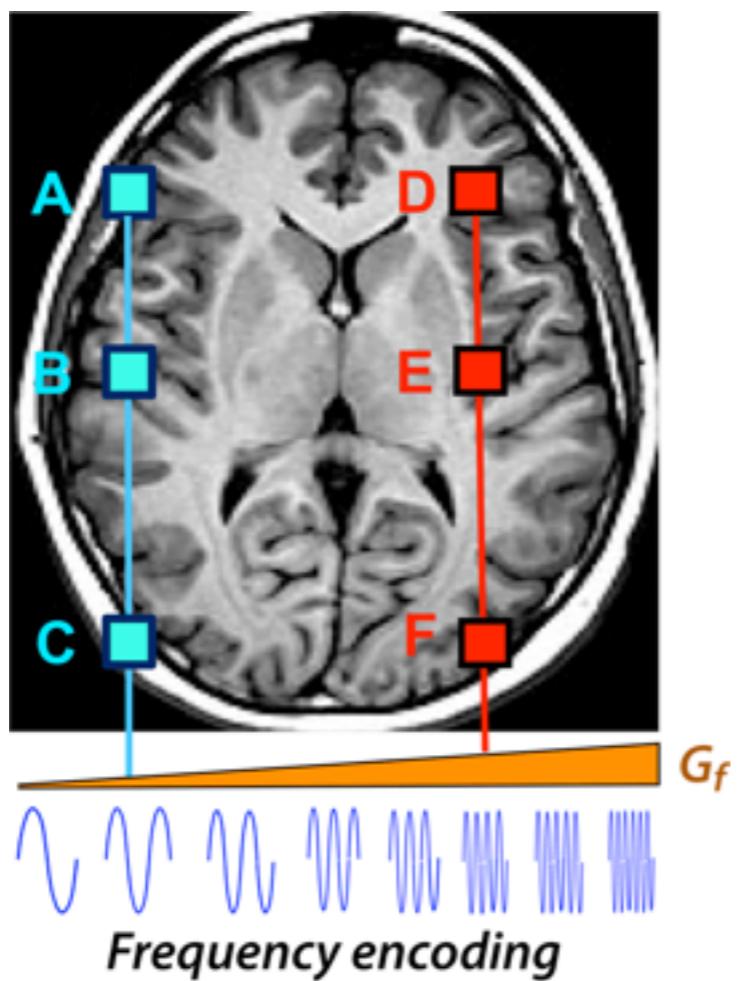
$$\mathbf{G} = (\mathbf{G}_x, \mathbf{G}_y, \mathbf{G}_z)$$

## TWO EFFECTS



# FREQUENCY ENCODING

mriquestions.com



# COMPUTING THE SIGNAL

solution to the bloch equation



$$s_r(t) = \int M(\mathbf{r}, t)dV = \iiint M(x, y, z, t)dx dy dz$$

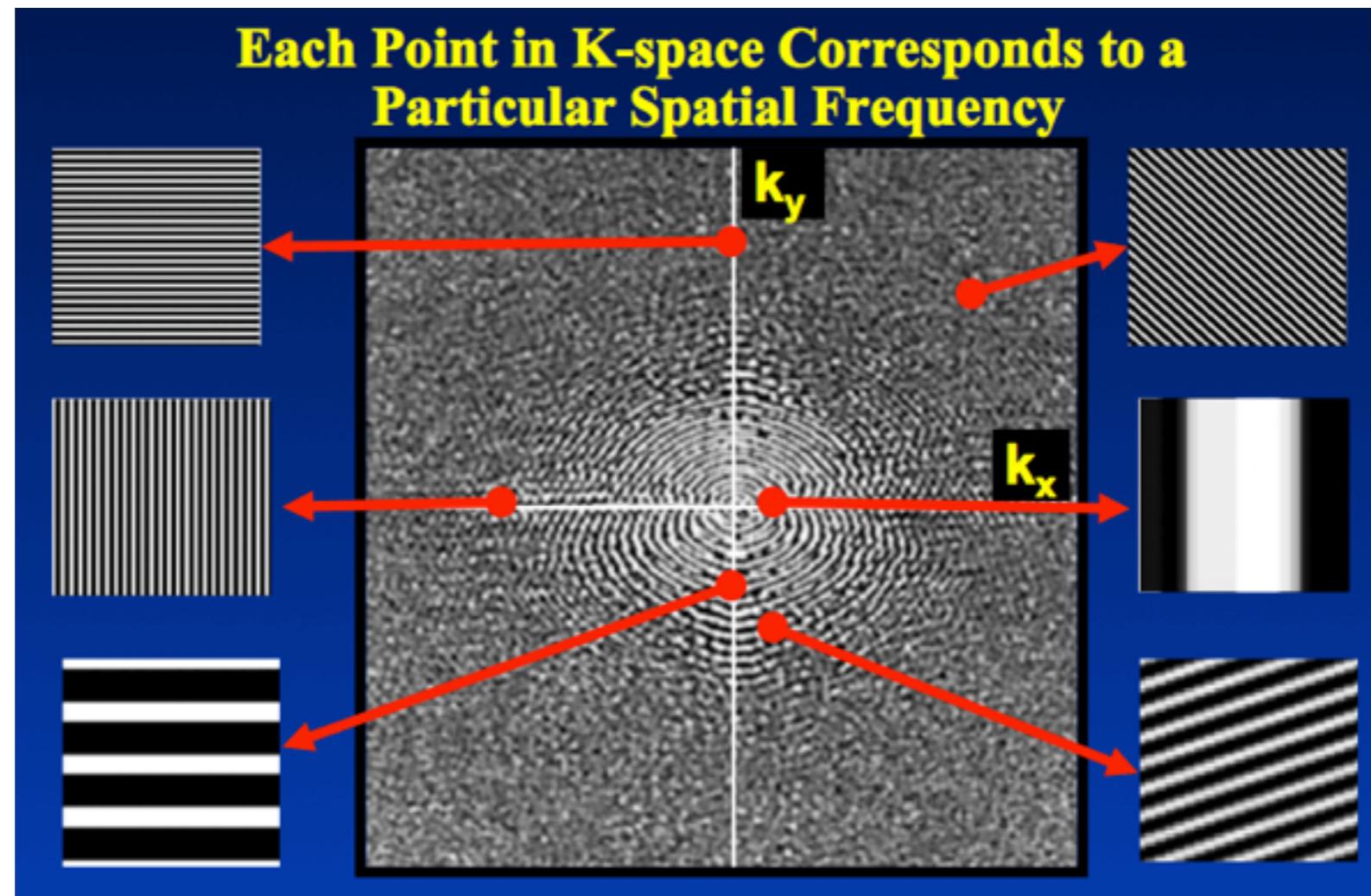


A lot of math later...

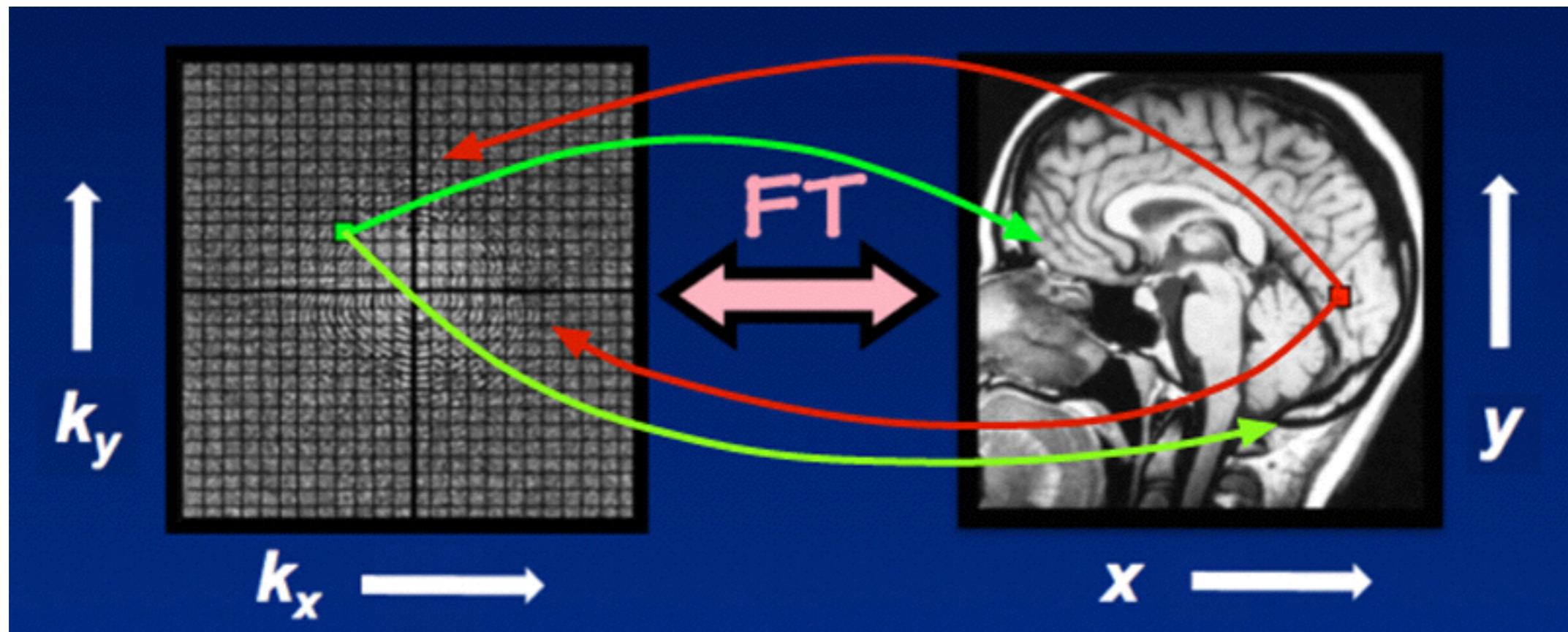
$$s(t) = \iiint m(x, y, z) e^{-i2\pi[k_x(t)x + k_y(t)y + k_z(t)z]} dx dy dz$$

where  $k_x(t) = \frac{\gamma}{2\pi} \int_0^t G_x(\tau) d\tau$ ,  $k_y(t) = \frac{\gamma}{2\pi} \int_0^t G_y(\tau) d\tau$ , and  $k_z(t) = \frac{\gamma}{2\pi} \int_0^t G_z(\tau) d\tau$ .

# K-SPACE



## FROM K-SPACE TO AN IMAGE



## FROM K-SPACE TO AN IMAGE

- The connection between k-space and the Fourier transformation was discovered by Peter Mansfield and Paul C. Lauterbur in the 1970s.
- They shared the Nobel Prize in Physics in 2003 for their works that made volumetric imaging possible with MRI



Peter Mansfield



Paul C. Lauterbur

# SEQUENCE PROGRAMMING & IMAGE CONTRAST

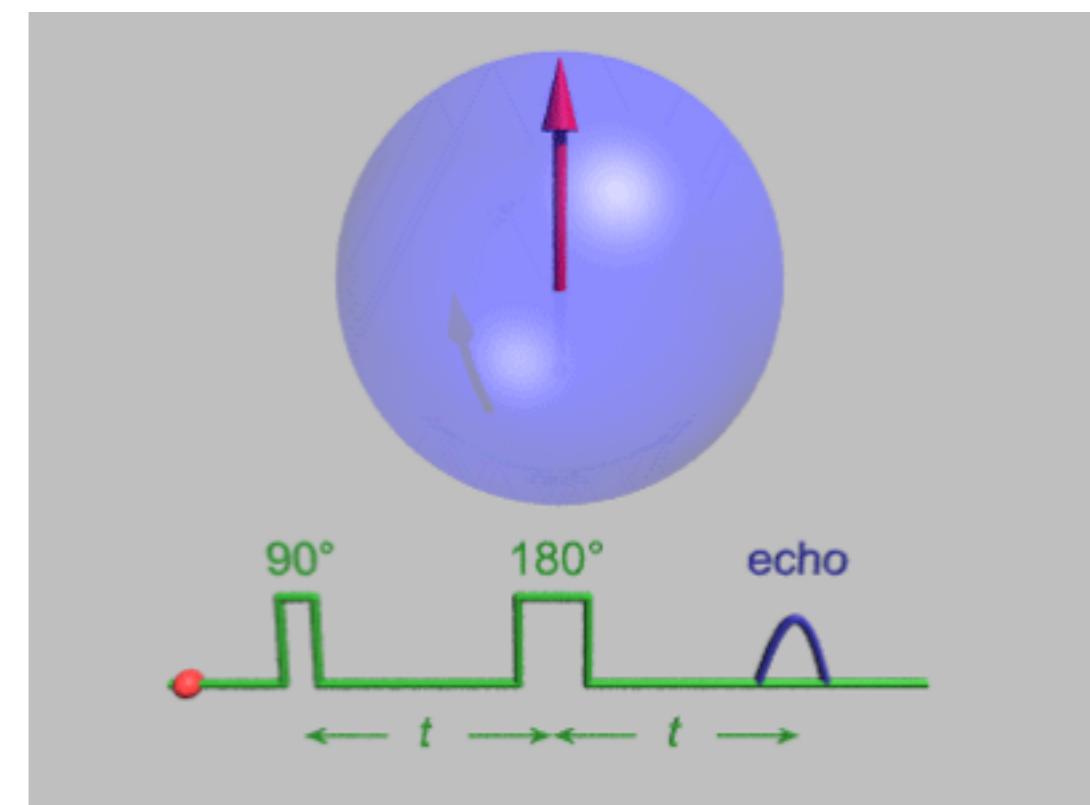
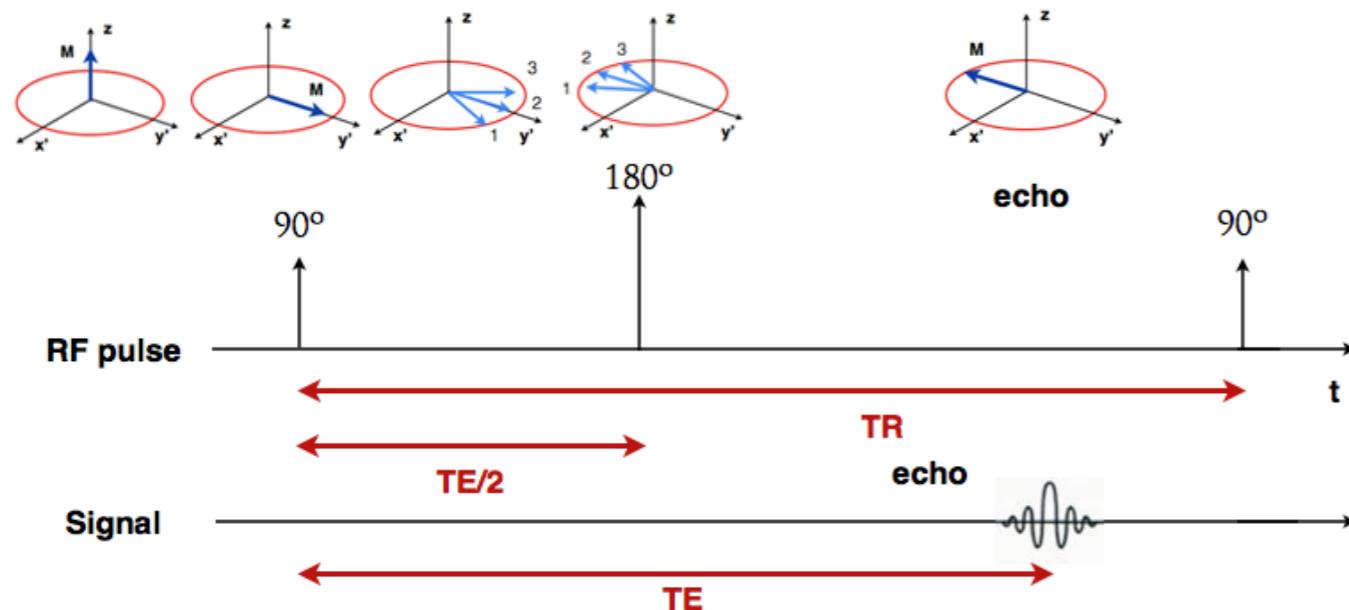
## PULSE SEQUENCE DESIGN

An MRI pulse sequence is a pre-set program on how and when to apply changing gradient fields, RF pulses, and data acquisition events to the scan subject.

### THREE VARIABLES

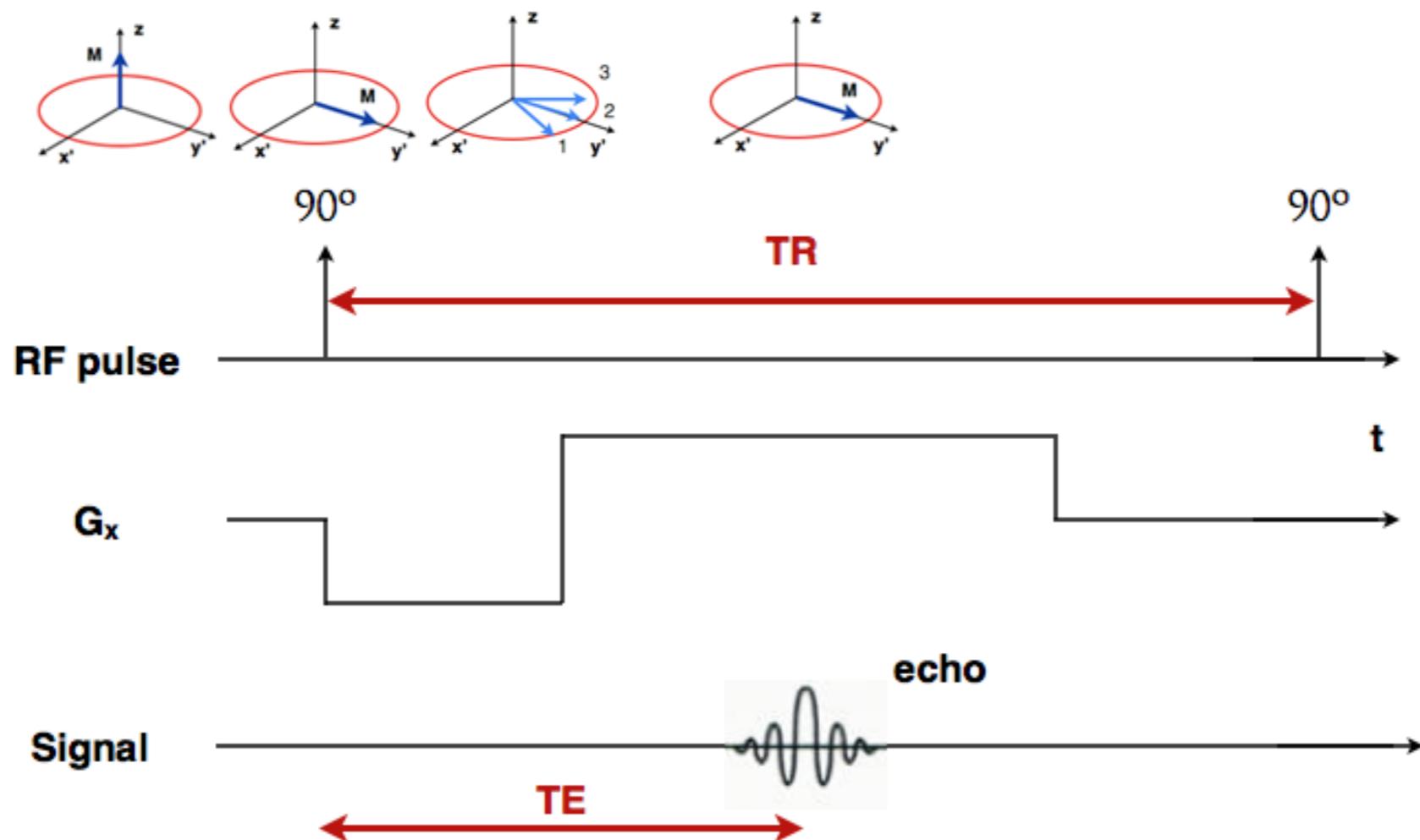
1. **Repetition Time (TR)** is the time from the application of an excitation RF pulse to the next.
2. **Echo Time (TE)** presents the time between the application of the excitation RF pulse and the peak of the echo signal or signal readout.
3. **Flip angle (FA)** is the angle that the net magnetization is tipped relative to the main field direction by the RF pulse.

## SPIN-ECHO (SE) SEQUENCE



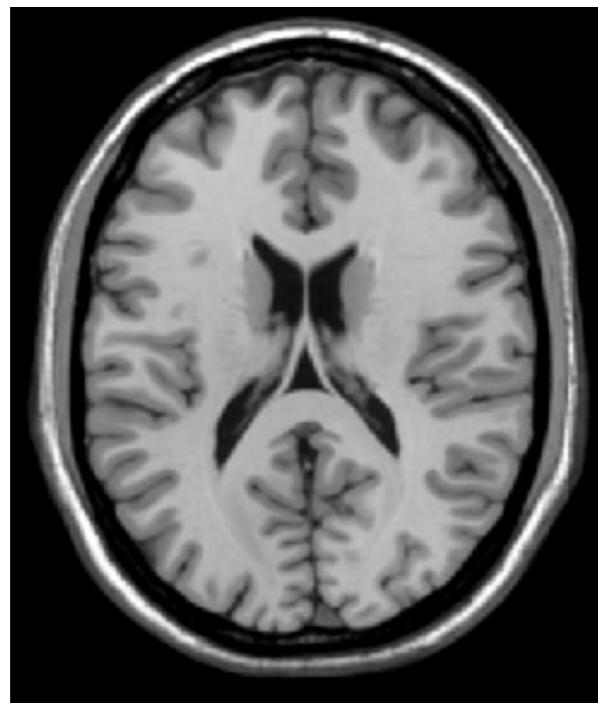
This ensures T2 relaxation

## GRADIENT-ECHO (GRE) SEQUENCE

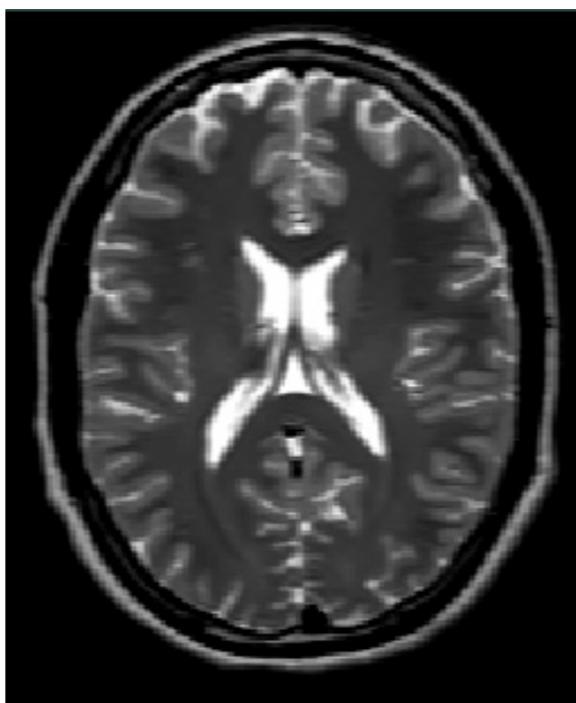


This can be used to take advantage of  $T2^*$  relaxation

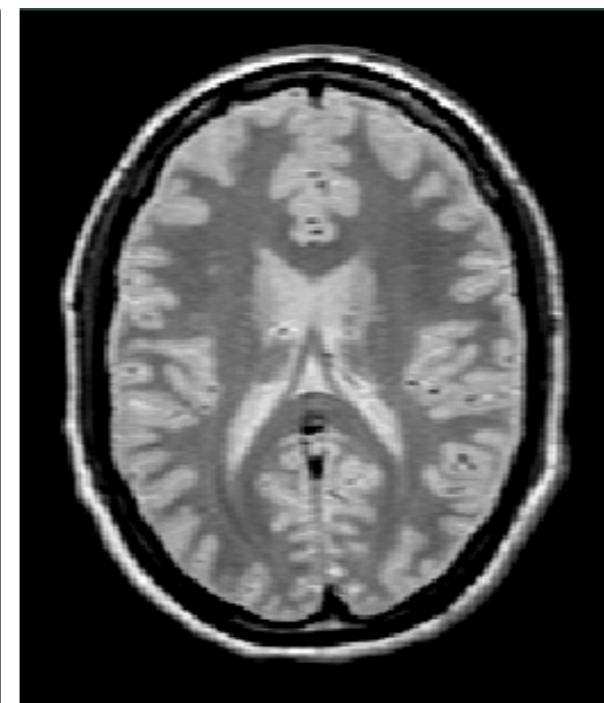
## IMAGE CONTRASTS



(a) T1w MRI



(b) T2w MR



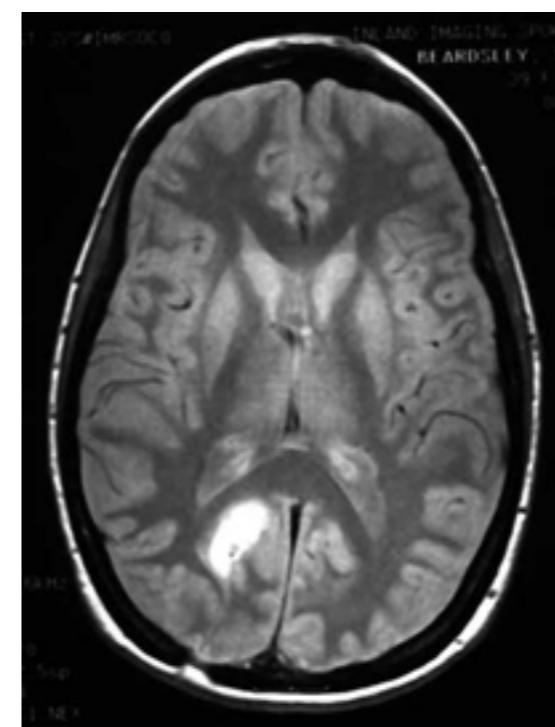
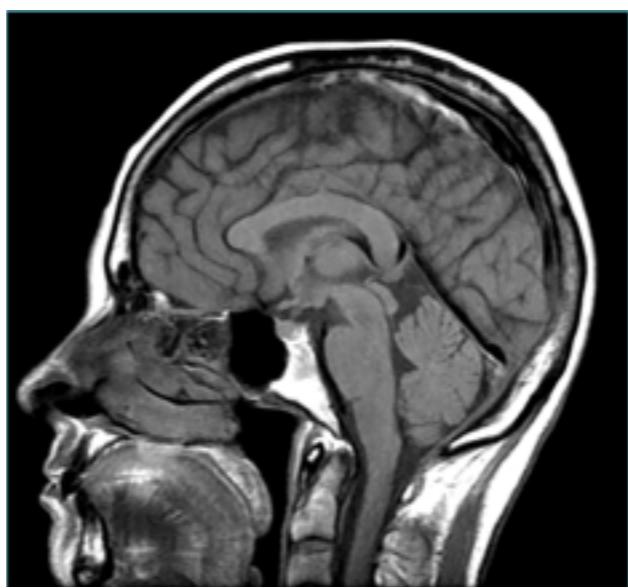
(c) PDw MRI

$$\rho_m = \rho_0 e^{-TE/T2*} \frac{\sin\alpha(1 - e^{-TR/T1})}{1 - \cos\alpha \cdot e^{-TR/T1}}$$

# WHAT CAN WE USE MRI FOR?

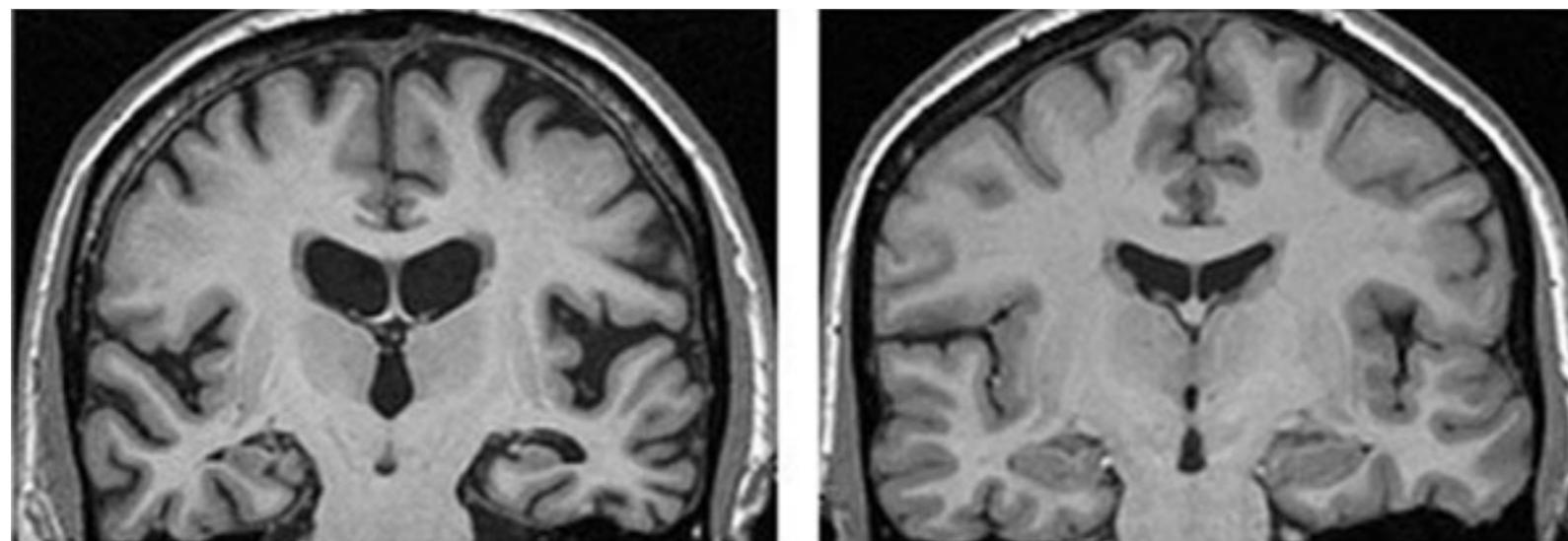
## REVEALING THE ANATOMY

- Qualitatively and quantitatively imaging the structures
- Tendons, muscles, fat, tumours, lesion & blood vessels
- Surgical planning and structural analysis



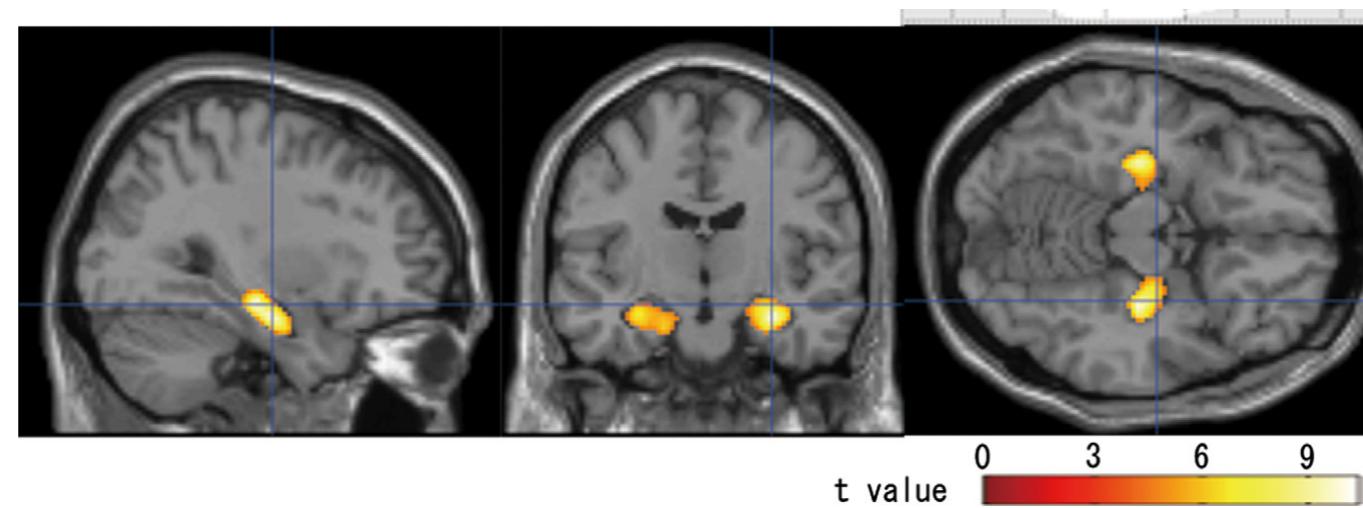
## REVEALING THE ANATOMY

- Morphometric Analysis



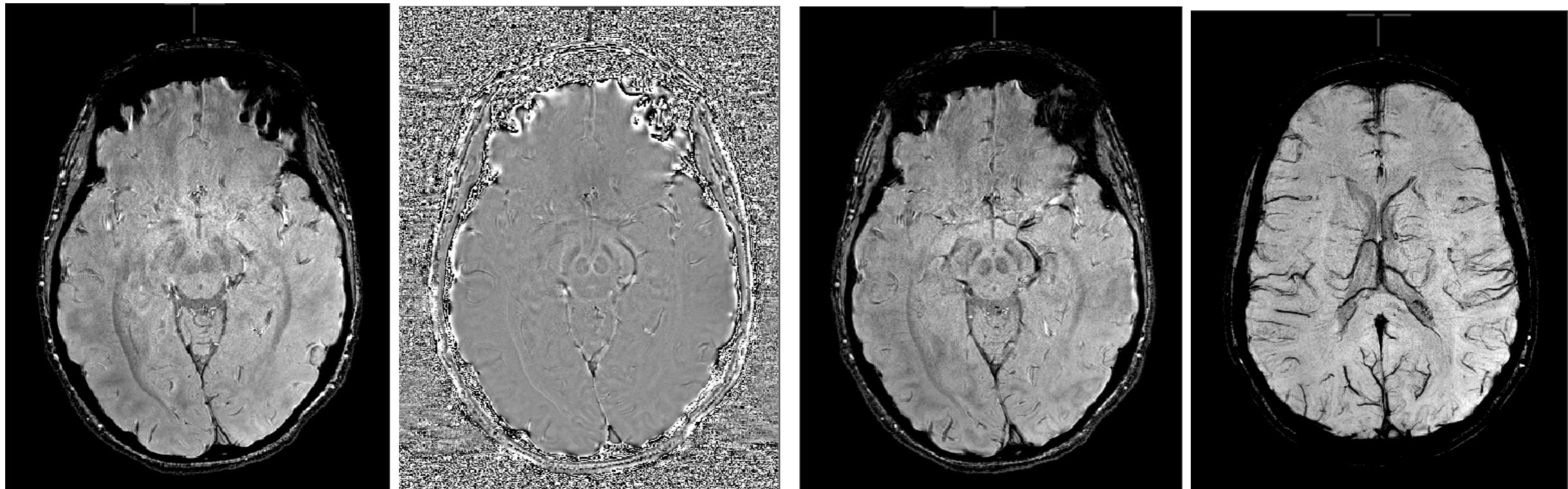
Alzheimer's Disease

Healthy



Imabayashi et al., 2013

## SUSCEPTIBILITY-WEIGHTED IMAGING (SWI)



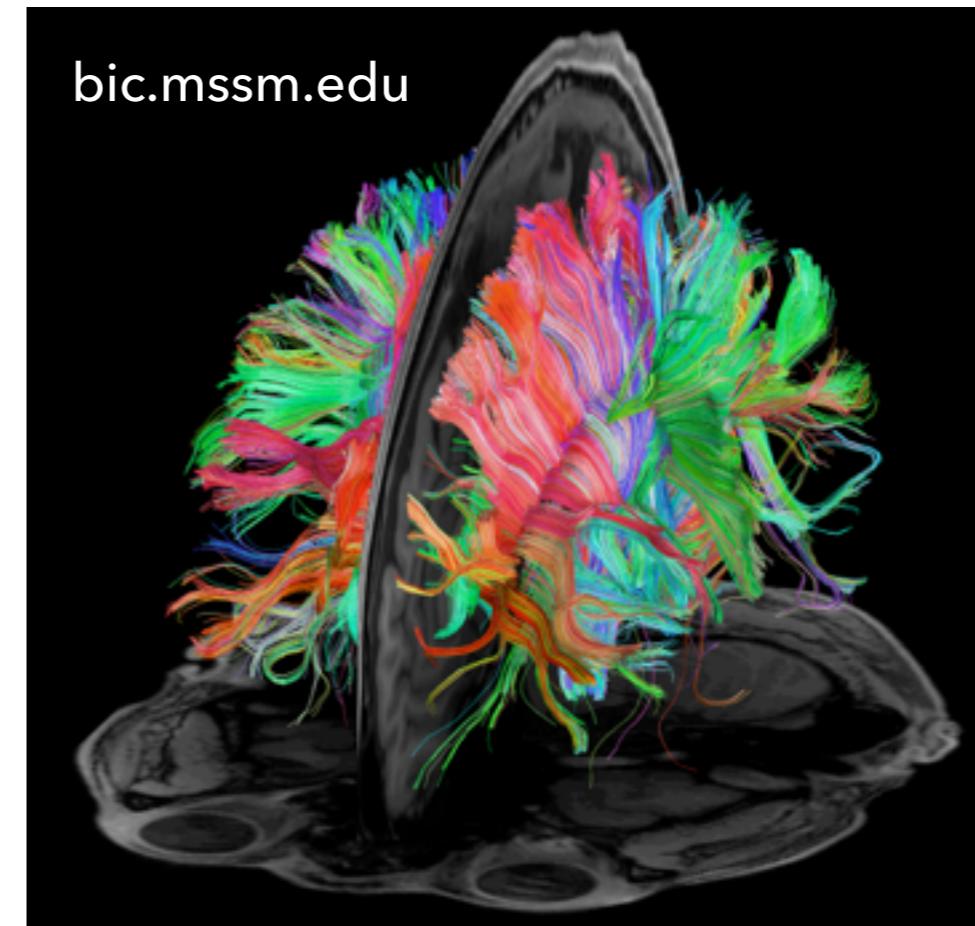
- Use iron in the tissue as natural contrast enhancement
- Reveals veins in the brain
- Lesions, micro-bleeding, and measure iron cumulation

## IMAGING FIBRES IN AN ORGAN

Diffusion-tensor image (DTI): image water diffusion directions



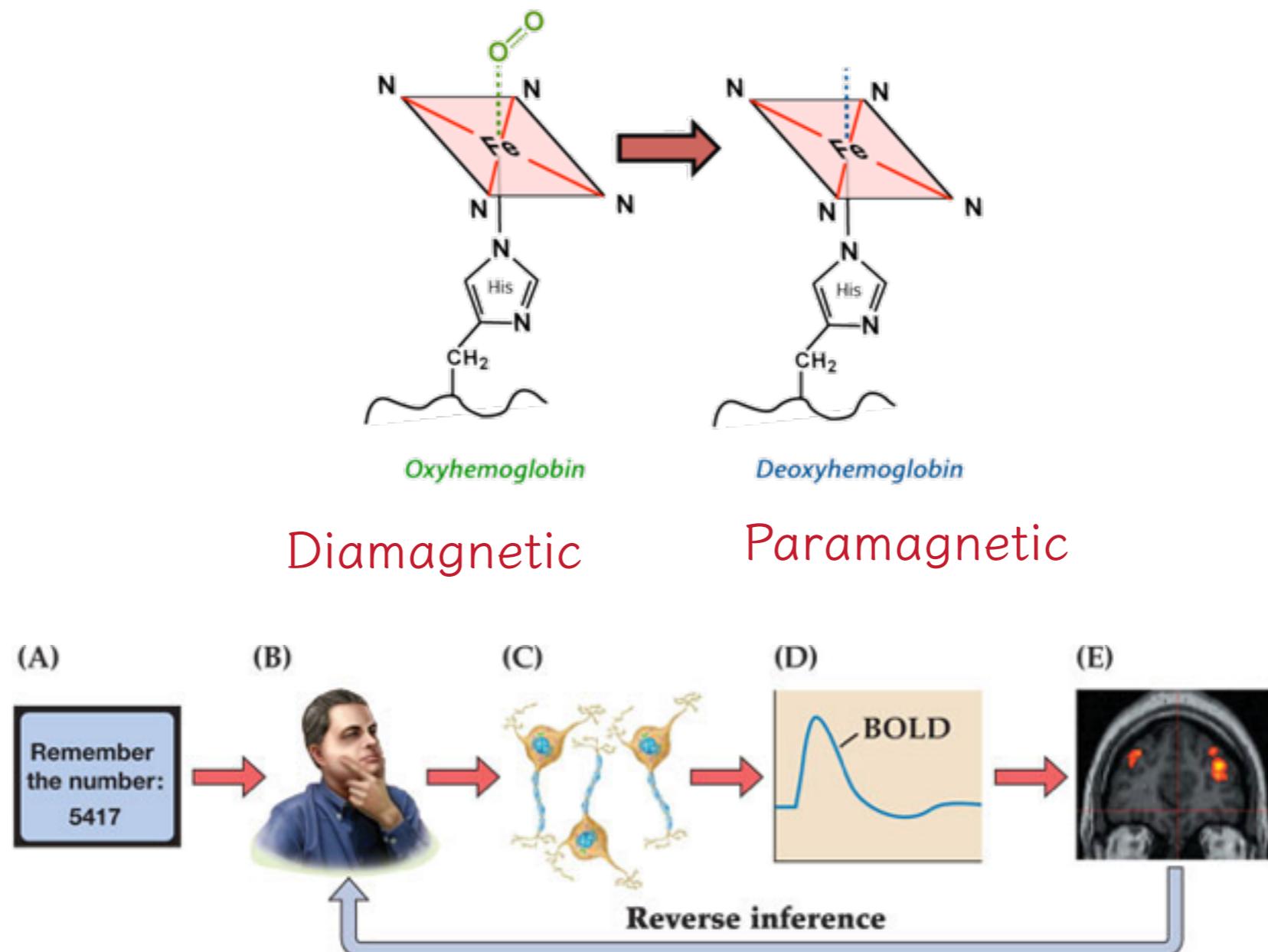
[www.hhmi.org](http://www.hhmi.org)



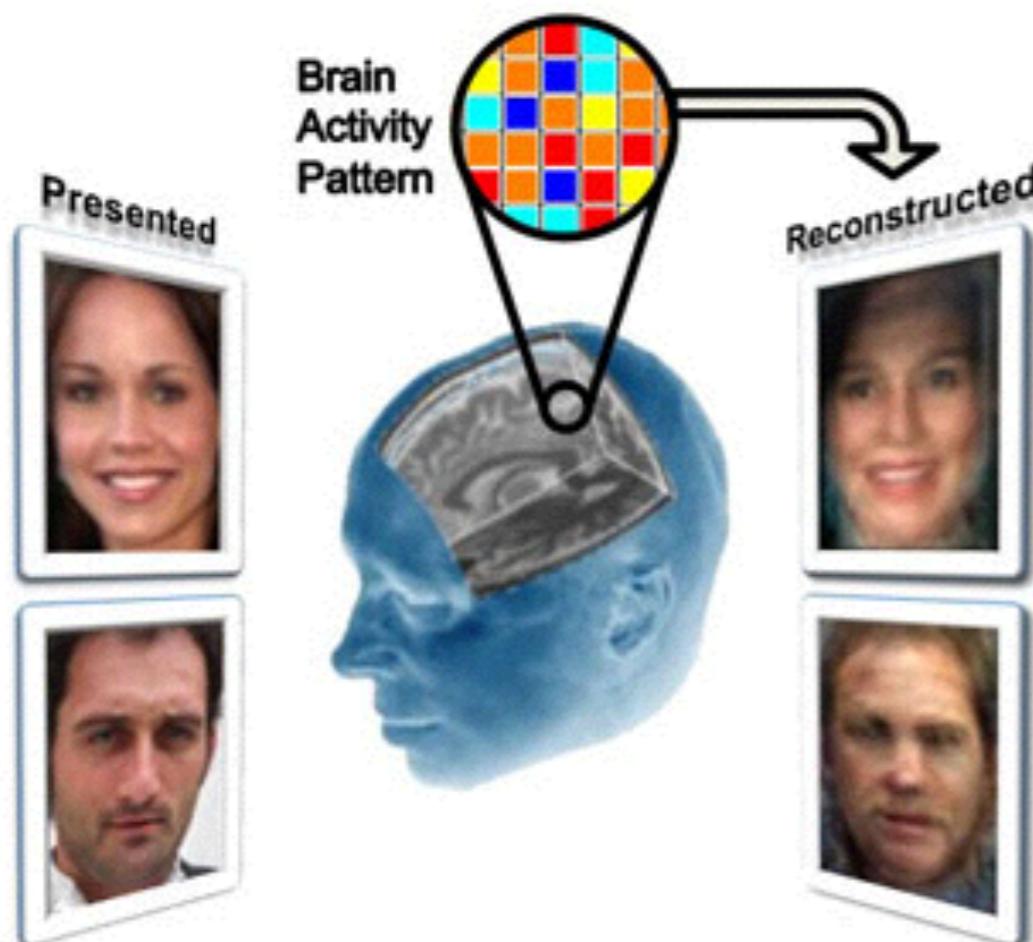
[bic.mssm.edu](http://bic.mssm.edu)

# BRAIN ACTIVITY

- Functional MRI (fMRI) measures the blood-oxygen-dependent (BOLD) signal



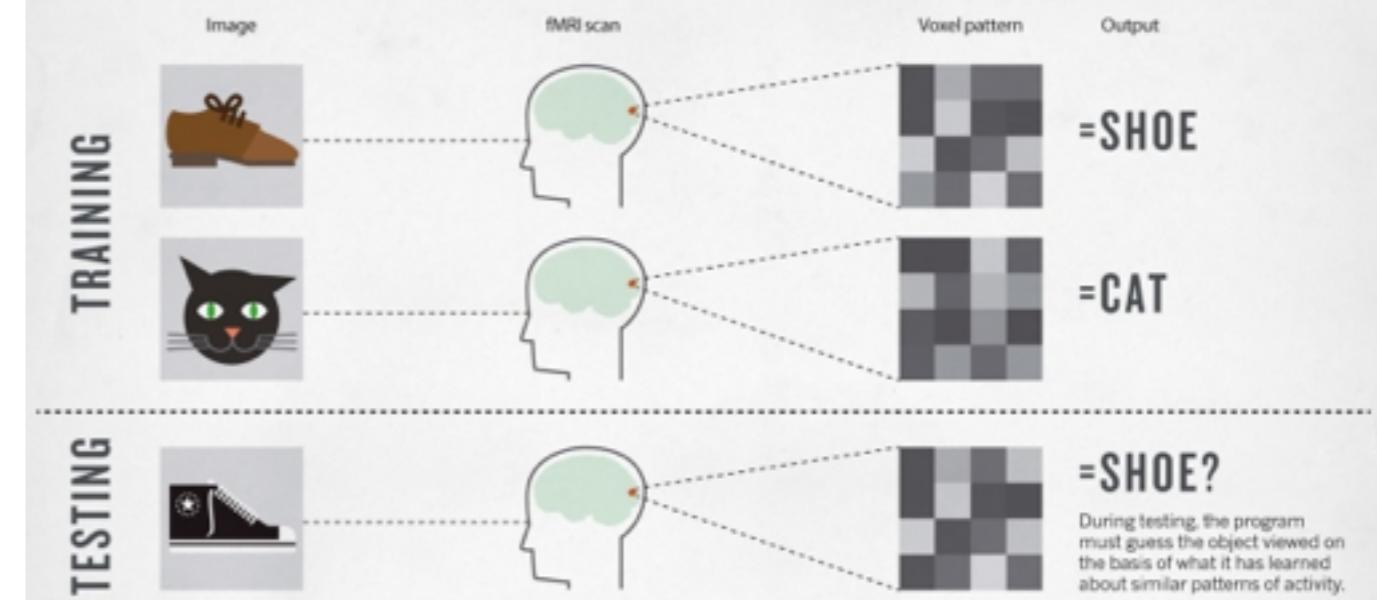
# BRAIN ACTIVITY



[www.nydailynews.com](http://www.nydailynews.com)

## DECODING FOR DUMMIES

Scientists train a computer program by showing it brain-scan data associated with seeing certain images. Once it has built a database of activity patterns, it can be tested with images the participant hasn't necessarily seen before.



[www.nature.com](http://www.nature.com)

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## IN SUMMARY

- MRI is based on the nuclear magnetic resonance (NMR) phenomenon
- Three main magnetic fields interact with spins to generate FID
- Different image contrasts can be generated by playing with the timing and duration that the magnetic fields are applied.
- K-space vs image space
- Many applications, but need the help of image processing and data science

## TAKE HOME MESSAGE

Not all MRIs are equal

Get to know your images before  
processing them!

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## WHAT WE DID NOT TALK ABOUT

- How to control the image resolution
- Signa-to-noise ratio (SNR)
- Imaging artifacts
- Mechanism of fast imaging & more...

# WANT TO KNOW THE COMPLETE STORY?

Xray Physics - Interactive Radiology Physics

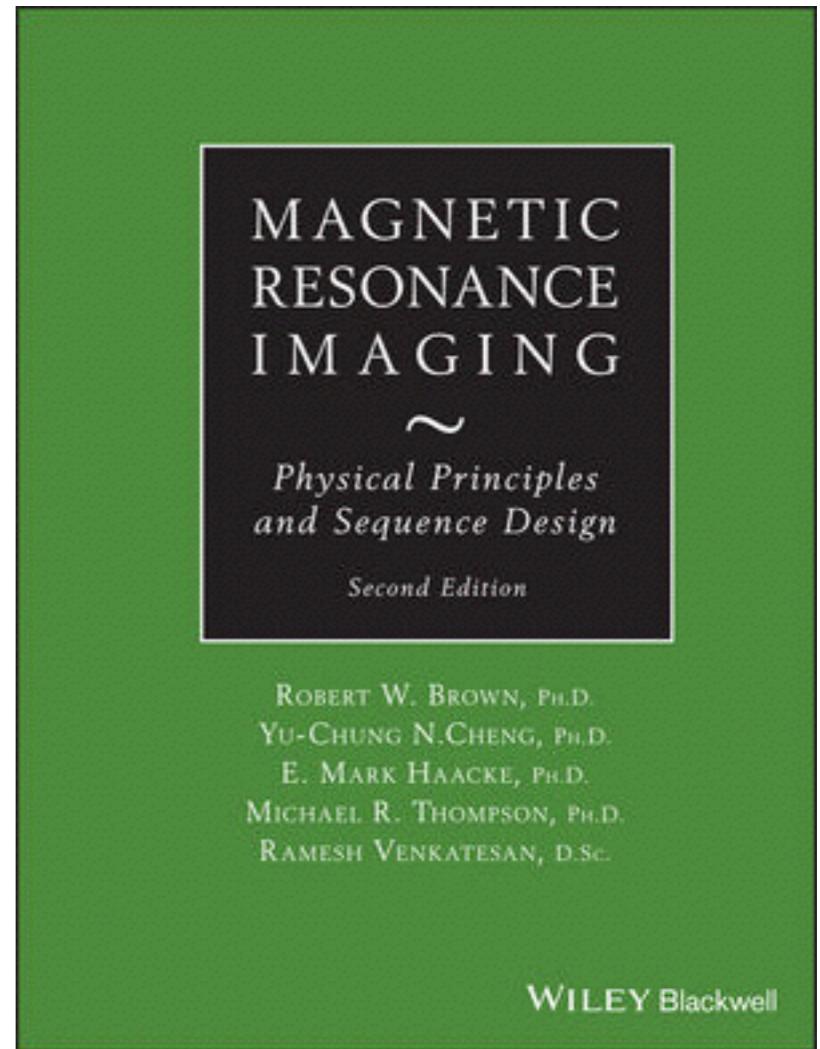
Check out the MRI physics section

<http://www.xrayphysics.com/sequences.html>

Joseph Hornak's Web Tutorial, *The Basics of MRI*

<http://www.cis.rit.edu/htbooks/mri>

E. Mark Haacke, et al 2014 Magnetic Resonance Imaging: Physical Principles and Sequence Design, 2nd Ed.



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# QUESTIONS?

