

Marvin Abisrror Zarate

**On Selecting of
heuristics functions for Domain–Independent
planning.**

Brasil

2015, v-1.9.5

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Paper presented to the Federal University of Viçosa, as part of the requirements of Graduate Computer Science program, for obtaining the title of Magister Scientiae.

Universidade de Viçosa – UFV

Centro de Ciencias Exactas e Tecnologicas (CCE)

Programa de Pós-Graduação

Supervisor: Levi Henrique Santana de Lelis

Co-supervisor: Santiago Franco

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This thesis is dedicated to my Mother.

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*“Não vos amoldeis às estruturas deste mundo,
mas transformai-vos pela renovação da mente,
a fim de distinguir qual é a vontade de Deus:
o que é bom, o que Lhe é agradável, o que é perfeito.
(Bíblia Sagrada, Romanos 12, 2)*

Abstract

In this dissertation we present a greedy method based on the theory of supermodular optimization for selecting a subset of heuristics functions from a large set of heuristics with the objective of reducing the running time of the search algorithms.

([HOLTE et al., 2006](#)) showed that search can be faster if several smaller pattern databases are used instead of one large pattern database. We introduce a greedy method for selecting a subset of the most promising heuristics from a large set of heuristics functions to guide the A* search algorithm. If the heuristics are consistent, our method selects a subset which is guaranteed to be near optimal with respect to the resulting A* search tree size. In addition to being consistent, if all heuristics have the same evaluation time, our subset is guaranteed to be near optimal with respect to the resulting A* running time. We implemented our method in Fast Downward and showed empirically that it produces heuristics which outperform the state of the art heuristics in the International Planning Competition benchmarks.

Key-words: Heuristics. selection.

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Introduction

This thesis is concerned with cost-optimal state-space planning using the A^* algorithm (HART P. E.; NILSSON; RAPHAEL, 1968). We assume that a pool, ζ , of hundreds or even thousands of heuristics is available, and that the final heuristic used to guide A^* , h_{max} , will be defined as the maximum over a subset ζ' of those heuristics ($h_{max}(s, \zeta') = \max_{h \in \zeta'} h(s)$). The choice of the subset ζ' can hugely affect the efficiency of A^* . For a given size N and planning task ∇ , a subset containing N heuristics from ζ is optimal if no other subset containing N heuristics from ζ results in A^* expanding fewer nodes when solving ∇ .

Exists many problems of Artificial Intelligent (AI), such as: Finding the shortest path from one point to another in a game map, 8-tile-puzzle, Rubick's cube, etc. The level of difficulty to solve the problems mentioned are linked with the size of the search space generated.

State-space search algorithms have been used to solve the problems mentioned above. And in this dissertation we study the approach to solve problems in order to reduce the size of the search tree generated and the running time of the search algorithm using the best subset of heuristics selected from a large set of heuristics.

Part I

Preparation of the research

1 About the Problem

The purpose of this section is to motivate the problem.

1.1 Problem Statement and Motivation

Every problem of Artificial Intelligence can be cast as a state space problem. The state space is a set of states where each state represents a possible solution to the problem and each state is linked with other states if there exists a function that goes from one state to another. In the search space there are many solutions that represent the same state, each of these solutions are called nodes. So, many nodes can be represented as one state. To find the solution of the problem is required the use of search algorithms such as: Depth First Search (DFS), which looks for the solution of the problem traversing the search space exploring the nodes in each branch before backtracking up to find the solution. Another search algorithm is Breadth First Search (BFS), which looks for the solution exploring the neighbors nodes first, before moving to the next level of neighbors. The mentioned algorithms have the characteristic that when they do the search, they generate a larger search space. The search space that these algorithms generate are called Brute force search tree (BFST).

There are other types of algorithms called heuristics informed search, which are algorithms that require the use of heuristics. The heuristic is the estimation of the distance for one node in the search tree to get to the near solution. The heuristic informed search generates smaller search tree in comparison to the BFST, because the heuristic guides the search exploring the nodes that are in the solution path and prunes the nodes which are not. Also, the use of heuristics reduces the running time of the search algorithm.

There are different approaches to create heuristics, such as: Pattern Databases (PDBs), Neural Network, and Genetic Algorithm. These systems that create heuristics receive the name of Heuristics Generators. And one of the approaches that have showed most successful results in heuristic generation is the PDBs, which is memory-based heuristic functions obtained by abstracting away certain problem variables, so that the remaining problem ("pattern") is small enough to be solved optimally for every state by blind exhaustive search. The results stored in a table, represent a PDB for the original problem. The abstraction of the search space gives an admissible heuristic function, mapping states to lower bounds.

Exists many ways to take advantage of all the heuristics that can be created, for

example: (HOLTE et al., 2006) showed that search can be faster if several smaller pattern databases are used instead of one large pattern database. In addition (DOMSHLAK; KARPAS; MARKOVITCH, 2010) and (TOLPIN et al., 2013) results showed that evaluating the heuristic lazily, only when they are essential to a decision to be made in the search process is worthy in comparison to take the maximum of the set of heuristics. Then, using all the heuristics do not guarantee to solve the major number of problems in a limit time.

1.2 Aim and Objectives

1.2.1 Aim

The objective of this dissertation is to develop meta-reasoning approaches for selecting heuristics functions from a large set of heuristics with the goal of reducing the running time of the search algorithm employing these functions.

1.2.2 Objectives

- Demonstrate that the problem of finding the optimal subset of ζ of size N for a given problem task is supermodular respect the size of the search tree.
- Develop an approaches to obtain the cardinality of the subsets of heuristics found.
- Develop an approach to find a subset of heuristics from a large pool of heuristics that optimize the number of nodes expanded in the process of search.
- Develop an approach for selecting a subset of heuristic functions based on the minimum evaluation cost of each heuristic.
- Develop an strategy to drop heuristics during the sampling that do not improve the objective function.
- Use Stratified Sampling (SS) algorithm for predicting the search tree size of Iterative-Deepening A* (IDA*). And use SS as our utility function.

1.3 Scope, Limitations, and Delimitations

We implemented our method in Fast Downward (HELMERT, 2006) and the problems we want to solve are the optimal domains benchmarks. Our meta-reasoning described in this thesis are going to try to solve the major number of problems using the most promising heuristics from a large set of heuristics. The exact way to create the large set of heuristics is beyond the scope of this thesis.

1.4 Justification

In the last few decades, Artificial Intelligence has made significant strides in domain-independent planning. The use of heuristics search approach have contributed to problem solving, where the use of an appropriate heuristic often means substantial reduction in the time needed to solve hard problems.

That is why we propose a meta-reasoning that will try to solve the major number of problems without relying on domain knowledge, to guide the A* search algorithm.

1.5 Hypothesis

This thesis will intend to prove the hypotheses listed below:

- **H1:** Probe that our objective function of selection is related with two mathematical properties: Monotonicity and Submodularity.
- **H2:** Reducing the size of the search tree generated helps to solve more problems.

1.6 Contribution of the Thesis

The main contributions of this Thesis are:

- Provide a prediction method to estimate the size of the search tree generated.
- Provide a meta-reasoning approach based on the size of the search tree generated.
- Provide a meta-reasoning approach based on the evaluation cost of each heuristic.

1.7 Organization of the Thesis

The Thesis is organized as follows:

1. In Part 1, the background of the thesis is provided which also includes our motivation and define the scope.
2. In Part 2, we review the State of the Art.
3. In Part 3, we introduce our meta-reasoning approach.
4. In Part 4, we introduce.
5. In Part 5, we .

6. We conclude in Part 6 by discussing further improvements and future work.

In the next chapter, the domain 8–tile–puzzle is used to understand the concepts that will be helpful for the other Parts.

Part II

Literature Review

2 Background

The purpose of this section is to understand the problem.

2.1 Similar Selection Systems

An optimization procedure which is similar to ours is presented by (RAYNER; STURTEVANT; BOWLING, 2013), but their procedure maximizes the average heuristic value. By contrast, the meta-reasoning we are proposing minimizes the search tree size.

Our meta-reasoning requires a prediction of the number of nodes expanded by A^* using any given subset. Although there are methods for accurately predicting the number of nodes expanded by Iterative Deepening- A^* (KORF, 1985) (IDA^*). (SS system (LELIS; ZILLES; HOLTE, 2013)), these methods can't be easily adapted to A^* because A^* 's duplicate pruning makes it very difficult to predict how many nodes will occur at depth d of A^* 's search tree (the tree of nodes expanded by A^*). As a part of our proposal, we present SS for predicting the size of the search tree.

The system most similar to ours is **RIDA*** (BARLEY; FRANCO; RIDDLE, 2014). **RIDA*** also selects a subset from a pool of heuristics to guide the A^* search. In **RIDA*** this is done by starting with an empty subset and trying all combination of size one before trying the combination of size two and so on. **RIDA*** stops after evaluating a fixed number of subsets. While **RIDA*** is able to evaluate a set of heuristics with tens of elements, our meta-reasoning is able to evaluate a set of heuristics with thousands of elements.

2.2 Problem definition

A SAS^+ planning task (BÄCKSTRÖM; NEBEL, 1995) is a 4 tuple $\nabla = \{V, O, I, G\}$. V is a set of *state variables*. Each variable $v \in V$ is associated with a finite domain of possible D_v . A state is an assignment of a value to every $v \in V$. The set of possible states, denoted V , is therefore $D_{v_1} \times \dots \times D_{v_2}$. O is a set of operators, where each operator $o \in O$ is triple $\{pre_o, post_o, cost_o\}$ specifying the preconditions, postconditions (effects), and non-negative cost of o . pre_o and $post_o$ are assignments of values to subsets of variables, V_{pre_o} and V_{post_o} , respectively. Operator o is applicable to state s if s and pre_o agree on the assignment of values to variables in V_{pre_o} . The effect of o , when applied to s , is to set the variables in V_{post_o} to the values specified in $post_o$ and to set all other variables to the value they have in s . G is the goal condition, an assignment of values to a subset of variables, V_G . A state is a goal state if it and G agree on the assignment of values to the variable in V_G . I is the initial state, and the planning task, ∇ , is to find an optimal (least-cost)

sequence of operators leading from I to a goal state. We denote the optimal solution cost of ∇ as C^*

The state space problem illustrated in the figure 1 is a game that consists of a frame of numbered square tiles in random order with one tile missing. The puzzle also exists in other sizes, particularly the smaller 8-puzzle. If the size is 3×3 tiles, the puzzle is called the 8-puzzle or 9-puzzle, and if 4×4 tiles, the puzzle is called the 15-puzzle or 16-puzzle named, respectively, for the number of tiles and the number of spaces. The object of the puzzle is to place the tiles in order by making sliding moves that use the empty space.

The legal operators are to slide any tile that is horizontally or vertically adjacent to the blank into the blank position. The problem is to rearrange the tiles from some random initial configuration into a particular desired goal configuration. The 8-puzzle contains 181,440 reachable states, the 15-puzzle contains about 10^{13} reachable states, and the 24-puzzle contains almost 10^{25} states.

Initial			Goal		
4	1	2	1	2	3
8		3	4	5	6
5	7	6	7	8	

Figure 1: The left tile-puzzle is the initial distribution of tiles and the right tile-puzzle is the goal distribution of tiles. Each one represent a State.

Instead of using an algorithm of Brute force search that will analyze all the possible solutions. We can obtain heuristics from the problem of the slide tile puzzle that will help us to solve the problem.

2.3 Heuristics

State-space algorithms, such as A^* (HART P. E.; NILSSON; RAPHAEL, 1968), are important in many AI applications. A^* uses the $f(s) = g(s) + h(s)$ cost function to guide its search. Here, $g(s)$ is the cost of the path from the start state s , and $h(s)$ is the estimated cost-to-go from s to a goal; $h(\cdot)$ is known as the heuristic function. The heuristic is the mathematical concept that represent to the estimate distance from the node s to the nearest goal state.

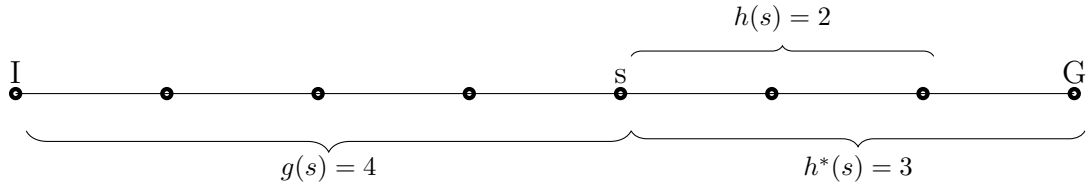


Figure 2: Heuristic Search: I : Initial State, s : Some Sate, G : Goal State

In the figure 2 the optimal distance from the Initial State I to the state s is 4 and represented by $g(s)$. The $h^*(s)$ represent the optimal distance from s to the Goal State G . And the $h(s)$ is the estimation distance from s to G .

A heuristic function $h(s)$ estimates the cost of a solution path from s to a goal state. A heuristic is admissible if $h(s) \leq h^*(s)$ for all $s \in V$, where $h^*(s)$ is the optimal cost of s . A heuristic is consisten iff $h(s) \leq c(s, t) + h(t)$ for all states s and t , where $c(s, t)$ is the cost of the cheapest path from s to t . For example, the heuristic function provided by a pattern database (PDB) heuristic (CULBERSON; SCHAEFFER, 1998) is admissible and consistent.

Given a set of admissible and consistent heuristics $\zeta = \{h_1, h_2, \dots, h_M\}$, the heuristic $h_{max}(s, \zeta) = \max_{h \in \zeta} h(s)$ is also admissible and consistent. When describing our method we assume all heuristics to be consistent. We define $f_{max}(s, \zeta) = g(s) + h_{max}(s, \zeta)$, where $g(s)$ is the cost of the path expanded from I to s . $g(s)$ is minimal when A* using a consistent heuristic expands s . We call an A* search tree the tree defined by the states expanded by A* using a consistent heuristic while solving a problem ∇ .

The heuristics can be obtained from each state of the problem. For example, for the problem of the 8–tile–puzzle figure 1 we can get two heuristics.

2.3.1 Out of place (O.P)

Counts the number of objects out of place.



Figure 3: Out of place heuristic

The tiles numbered with 4, 1, 2, 3, 6, 7, 5, 8, and 4 are out of place then each object count as 1 and the sum would be 8.

2.3.2 Manhatham Distance (M.D)

Counts the minimum number of operations to get to the goal state.

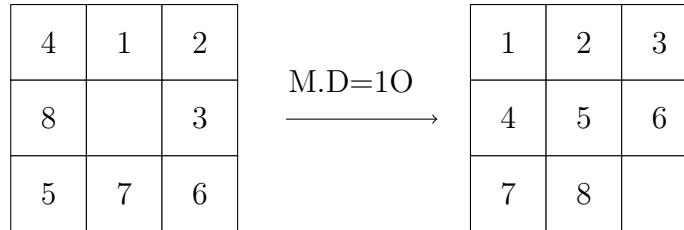


Figure 4: Manhatham distance heuristic

The tile 4 count 1 to get to the goal position. The tile 1 count 1 to get to the goal position. The tile 2 count 1 to get to the goal position. The tile 3 count 1 to get to the goal position. The tile 6 count 1 to get to the goal position. The tile 7 count 1 to get to the goal position. The tile 5 count 1 to get to the goal position. The tile 8 count 1 to get to the goal position. Then the sum would be 10.

In order to solve the problem, we get the heuristics, which are information from the problem to solve the problem. Exists systems that can create heuristics for each problem. Those systems are called Heuristic Generators.

2.4 Heuristic Generators

Heuristic Generators works by creating abstractions of the original problem space. The approach that has showed more successful results lately is PDB.

2.4.1 Pattern Database (PDB)

It's obtained by abstracting away certain problem variables, so that the remaining problem ("pattern") is small enough to be solved optimally for every state by blind exhaustive search. The results stored in a table, represent a PDB for the original problem. The abstraction of the search space gives an admissible heuristic function, mapping states to lower bounds.

2.5 Take advantage of Heuristics

The heuristics generators can create hundreds or even thousand of heuristics. In fact, exists different ways to take advantage of those heuristics. For example: If we want to use all the heuristics created by the heuristic generator. It would not be a good idea to use all of them because the main problem involved would be the time to evaluate each

heuristic in the search tree, it could take too much time.

One way to take advantage of heuristics would be to take the maximum of the set of heuristics. For example, using three different heuristics $h1, h2$ and $\max(h1, h2)$. Heuristic $h1$ and $h2$ are based on domain abstractions and the $\max(h1, h2)$ is the maximum heuristic value of $h1$ and $h2$.

Exists different approaches to take advantage from a large set of heuristics. In this dissertation we use the meta-reasoning based on the minimum size of the search tree generated and the minimum evaluation time.

2.6 Number of heuristics created

Let's suppose we have to run our meta-reasoning using M amount of memory available. The question would be: How many heuristics our system should handle in order to avoid out of memory errors? So, one of the objectives of this tesis is to find the number of heuristics that our subset ζ' should have.

([HOLTE et al., 2006](#)) observed that maximizing over N pattern databases of size M/N , for a suitable choice N , produces a significant reduction in the number of nodes generated compared to using a single pattern database of size M .

In the Figures 6 and 7 we are taking advantage of the heuristics doing the maximization of all the heuristics created. In this thesis we are interested in heuristics that generate smaller search tree.

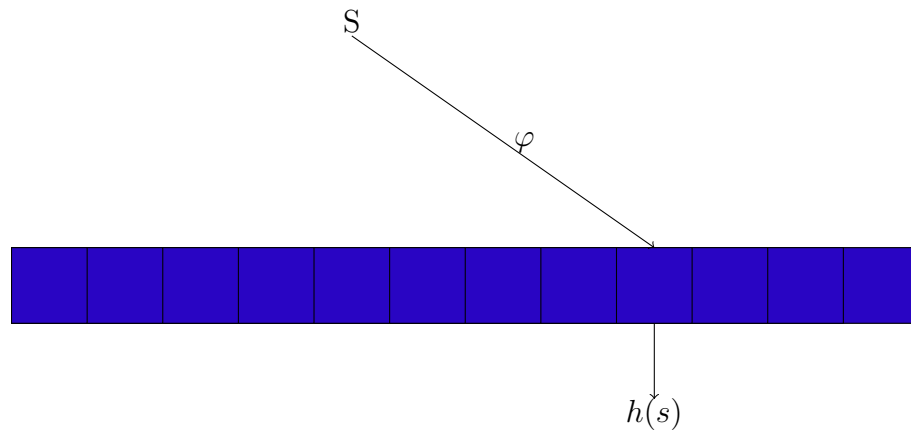


Figure 5: One heuristic of size M

Figure 6: Two heuristics of size $M/2$ Figure 7: N heuristics of size M/N

2.7 Heuristic Subset

The heuristics generator systems can create a large number of heuristics. Let's suppose $|\zeta| = 1000$ heuristics were created considering the time and memory available and we want to select the best $N = 100$ heuristics. This would be:

$$\binom{1000}{100} = 10^{138} \text{possibilities}$$

So, try to select heuristics from a large set of heuristics are going to be treated as an optimization problem. Then, in order to obtain a good selection of subset of heuristics, our objective function should guarantee two properties: Monotonicity and Submodularity, that would be explained in the next Part.

2.8 Problem Domains

Some of the problems we are trying to solve are the optimal domains for International Planning Competition (IPC).

2.8.1 Blocks world

This domain consists of a set of blocks, a table and a robot hand. The blocks can be on top of other blocks or on the table; a block that has nothing on it is clear; and the robot hand can hold one block or be empty. The goal is to find a plan to move from one configuration of blocks to another.

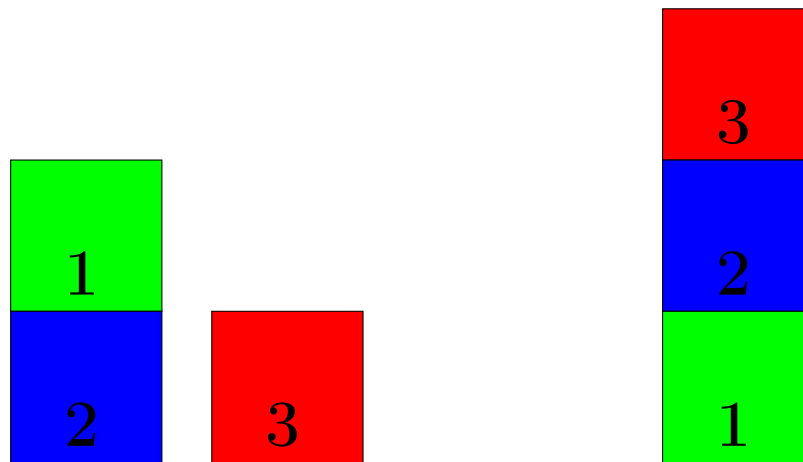


Figure 8: Blocks world with three blocks.

The solution shown in Figure 8 is to unblock number 1 from block number 2; stack block number 2 on block number 1; finally, stack block number 3 on block number 2. We are interested in optimal or near-optimal solutions for this kind of problem.

Depending on the number n of blocks this domain can have very large state spaces. For example, using $n = 20$ this domain has approximately 10^{20} different states.

2.8.2 Barman

In this domain there is a robot barman that manipulates drink dispensers, glasses and a shaker. The goal is to find a plan of the robot's actions that serves a desired set of drinks.

2.8.3 Elevators

The idea for this domain came up from the Miconic domain of IPC2, however the domain has been designed from scratch. The scenario is the following: There is a building

with $N+1$ floors, numbered from 0 to N . The building can be separated in blocks of size $M+1$, where M divides N . Adjacent blocks have a common floor. For example, suppose $N=12$ and $M=4$, then we have 13 floors in total (ranging from 0 to 12), which form 3 blocks of 5 floors each, being 0 to 4, 4 to 8 and 8 to 12.

The building has K fast (accelerating) elevators that stop only in floors that are multiple of $M/2$ (so M has to be an even number). Each fast elevator has a capacity of X persons. Furthermore, within each block, there are L slow elevators, that stop at every floor of the block. Each slow elevator has a capacity of Y persons (usually $Y < X$).

There are costs associated with each elevator starting/stopping and moving. In particular, fast (accelerating) elevators have negligible cost of starting/stopping but have significant cost while moving. On the other hand, slow (constant speed) elevators have significant cost when starting/stopping and negligible cost while moving. Travelling times between floors are given for any type of elevator, taking into account the constant speed of the slow elevators and the constant acceleration of the fast elevators.

There are several passengers, for which their current location (i.e. the floor they are) and their destination are given. The planning problem is to find a plan that moves the passengers to their destinations while it maximizes some criterion.

2.8.4 Floortile

A set of robots use different colors to paint patterns in floor tiles. The robots can move around the floor tiles in four directions (up, down, left and right). Robots paint with one color at a time, but can change their spray guns to any available color. However, robots can only paint the tile that is in front (up) and behind (down) them, and once a tile has been painted no robot can stand on it.

For the IPC set, robots need to paint a grid with black and white, where the cell color is alternated always. This particular configuration makes the domain hard because robots should only paint tiles in front of them, since painting tiles behind make the search to reach a dead-end.

2.8.5 Nomystery

In this domain, a truck moves in a weighted graph; a set of packages must be transported between nodes; actions move along edges, and load/unload packages; each

move consumes the edge weight in fuel. In brief, Nomystery is a straightforward problem similar to the ones contained in many IPC benchmarks.

2.8.6 Openstacks

The openstacks domain is based on the "minimum maximum simultaneous open stacks" combinatorial optimization problem, which can be stated as follows: A manufacturer has a number of orders, each for a combination of different products, and can only make one product at a time.

The total required quantity of each product is made at the same time (because changing from making one product to making another requires a production stop). From the time that the first product included in an order is made to the time that all products included in the order have been made, the order is said to be "open" and during this time it requires a "stack" (a temporary storage space). The problem is to order the making of the different products so that the maximum number of stacks that are in use simultaneously, or equivalently the number of orders that are in simultaneous production, is minimized (because each stack takes up space in the production area).

2.8.7 ParcPrinter

This domain models the operation of the multi-engine printer, for which one prototype is developed at the Palo Alto Research Center (PARC). This type of printer can handle multiple print jobs simultaneously. Multiple sheets, belonging to the same job or different jobs, can be printed simultaneously using multiple Image Marking Engines (IME). Each IME can either be color, which can print both color and black and white images, or mono, which can only print black and white image. Each sheet needs to go through multiple printer components such as feeder, transporter, IME, inverter, finisher and need to arrive at the finisher in order.

2.8.8 Parking

This domain involves parking cars on a street with N curb locations, and where cars can be double-parked but not triple-parked. The goal is to find a plan to move from one configuration of parked cars to another configuration, by driving cars from one curb location to another. The problems in the competition contain $2^{*(N-1)}$ cars, which allows one free curb space and guarantees solvability.

2.8.9 Sokoban

This domain is inspired by the popular Sokoban puzzle game where an agent has the goal of pushing a set of boxes into specified goal locations in a grid with walls. The competition problems are generated in a way that guarantees solvability and generally are easy problem instances for humans.

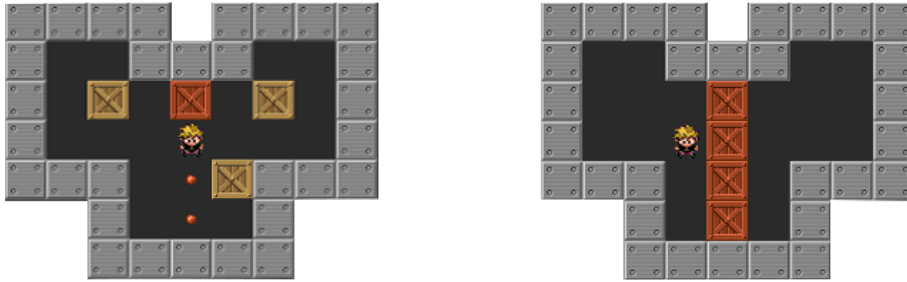


Figure 9: Sokoban with four blocks solved

In the next Part, we will introduce the meta–reasoning proposed for selecting heuristics and will expand on the properties of our objective functions.

Part III

Approach Proposal

3 Greedy Heuristic Selection

The purpose of this section is to introduce the meta-reasoning proposed.

3.1 Problem Formulation

When solving ∇ using the consistent heuristic function $h_{max}(\zeta')$ for $\zeta' \subseteq \zeta$, A^* expands in the worst case $J(\zeta', \nabla)$ nodes, where

$$J(\zeta', \nabla) = |\{s \in V | f_{max}(s, \zeta') \leq C^*\}| \quad (3.1)$$

$$J(\zeta', \nabla) = |\{s \in V | h_{max}(s, \zeta') \leq C^* - g(s)\}| \quad (3.2)$$

We present a greedy algorithm for approximately solving the following optimization problem,

$$\begin{aligned} & \textbf{minimize}_{\zeta' \in 2^{|\zeta|}} J(\zeta', \nabla) \\ & \textbf{subject to} |\zeta'| = N \end{aligned} \quad (3.3)$$

Where N could be determined by a hard constraint such as the maximum number of PDBs one can store in memory.

3.2 GHS Algorithm

Algorithm 1 presents Greedy Heuristic Selection (GHS), an approximation algorithm for selecting a subset $\zeta' \subseteq \zeta$.

The algorithm receives as input a planning problem ∇ , a set of heuristics ζ , a cardinality size N , and it returns a subset $\zeta' \subseteq \zeta$ of size N . In each iteration **GHS** greedily selects from ζ the heuristic h which will result in the largest reduction of the value of J (line 3). **GHS** returns ζ' once it has the desired cardinality size N .

Algoritmo 1: Greedy Heuristic Selection

```

1 Input: Problem  $\nabla$ , set of heuristics  $\zeta$ , cardinality  $N$ 
2 Output: heuristic subset  $\zeta' \subseteq \zeta$  of size  $N$ 
3  $\zeta' \leftarrow \emptyset$ 
4 while  $|\zeta'| < N$  do do
5    $h \leftarrow \operatorname{argmin}_{h \in \zeta} J(\zeta' \cup \{h\}, \nabla)$ 
6    $\zeta' \leftarrow \zeta' \cup \{h\}$ 
7   return  $\zeta'$ 
8 end

```

3.2.1 GHS Approximation Analysis

In the following analysis all heuristic functions are assumed to be consistent. We also assume that A^* expands all nodes n with $f(n) \leq C^*$ while solving ∇ , as shown in Equation (3.1).

Lemma 3.2.1. $J(\zeta' \cup \{h\}) \leq J(\zeta')$ for any ζ' and any h .

Proof. Fix ζ' and h . Then

$$\begin{aligned}
 J(\zeta' \cup \{h\}) &= |\{s \in V \mid h_{\max}(s, \zeta' \cup \{h\}) \leq C^* - g(s)\}| \\
 &\leq |\{s \in V \mid h_{\max}(s, \zeta') \leq C^* - g(s)\}| \\
 &= J(\zeta')
 \end{aligned}$$

Where the inequality follows from the fact that $h_{\max}(s, \zeta' \cup \{h\}) \geq h_{\max}(s, \zeta')$ for all s .

Let S be a set and ϕ a function over 2^S . ϕ is supermodular if for any A, B, x with $A \subset B \subset S$ and $x \in S \setminus B$:

$$\phi(A) - \phi(A \cup \{x\}) \geq \phi(B) - \phi(B \cup \{x\}) \quad (3.4)$$

Intuitively, Equation 3.4 captures the idea of diminishing returns. In the context of search tree size, if we add a heuristic function h to a set of heuristics A strictly contained in a set B , then we would expect, then we would expect $J(A) - J(A \cup \{h\})$ to be larger than $J(B) - J(B \cup \{h\})$ as h would "contribute more" to A than to B .

Lemma 3.2.2. J is supermodular.

Proof. Let $A \subset B \subset \zeta$ and $h \in \zeta \setminus B$. By Lemma 3.2.1, $J(A) - J(A \cup \{h\}) \geq 0$ and $J(B) - J(B \cup \{h\}) \geq 0$. We consider two cases.

Case 1. $J(B) - J(B \cup \{h\}) = 0$. Then $J(A) - J(A \cup \{h\}) \geq 0$ yields $J(A) - J(A \cup \{h\}) \geq$

$J(B) - J(B \cup \{h\})$.

Case 2. $J(B) - J(B \cup \{h\}) = k > 0$. Let s_1, \dots, s_k be all the states in V that satisfy $h_{\max}(s_i, B) \leq C^* - g(s_i)$ and $h_{\max}(s_i, B \cup \{h\}) > C^* - g(s_i)$. This implies $h(s_i) > C^* - g(s_i)$, for all $i \in \{1, \dots, k\}$. Further, since $A \subset B$, we have $h_{\max}(s_i, A) \leq h_{\max}(s_i, B) \leq C^* - g(s_i)$, for all $i \in \{1, \dots, k\}$. Consequently, $J(A) - J(A \cup \{h\}) \geq k = J(B) - J(B \cup \{h\})$.

A stronger version of Lemma 3.2.1 can be proven: if $S(\zeta')$ denotes the set of states $\{s \in V \mid h_{\max}(s, \zeta') \leq C^* - g(s)\}$, so that $J(\zeta')$ is the cardinality of S' , we obtain

$$S(\zeta' \cup \{h\}) \subseteq S(\zeta') \text{ for any } h. \quad (3.5)$$

Similarly, one can strengthen the statement of Lemma 3.2.2: the proof given above contains the core idea for proving $S(A) \setminus S(A \cup \{h\}) \supseteq S(B) \setminus S(B \cup \{h\})$, which, together with Equation 3.5, immediately implies the weaker statement $J(A) - J(A \cup \{h\}) \geq J(B) - J(B \cup \{h\})$. In the form stated above, however, Lemma 3.2.1 and 3.2.2 are already sufficient for using a result by (NEMHAUSER; WOLSEY; FISHER, 1978) to conclude the following.

Theorem 3.2.3. *Let ζ' be a subset selected by GHS. Then $J(\zeta', \nabla)$ is within a factor of $\frac{e+1}{e} \approx 1.36$ of optimal*

3.3 Stratified Sampling (SS)

Stratified Sampling is a prediction algorithm that estimate the number of nodes expanded by some heuristic.

(KNUTH, 1975) created a method to estimate the size of the search tree such as IDA*. It works doing random walk from the root of the tree. Knuth's assumption is that all branches have the same structure. So, performing a random walk down one branch is enough to estimate the size of the search tree. However, the method does not work well for unbalanced search tree. (CHEN, 1992) solved this problem with a stratification of the search tree through a *type system* to reduce the variance of the sampling process (LELIS; ZILLES; HOLTE, 2013)

In the figure 10 each node of the Search Space is mapped to the *Type System*

3.3.1 Type System

The *Type System* is a partition of the states in the state space. It is calculated based of any property of each node in the search tree. (LELIS, 2013)

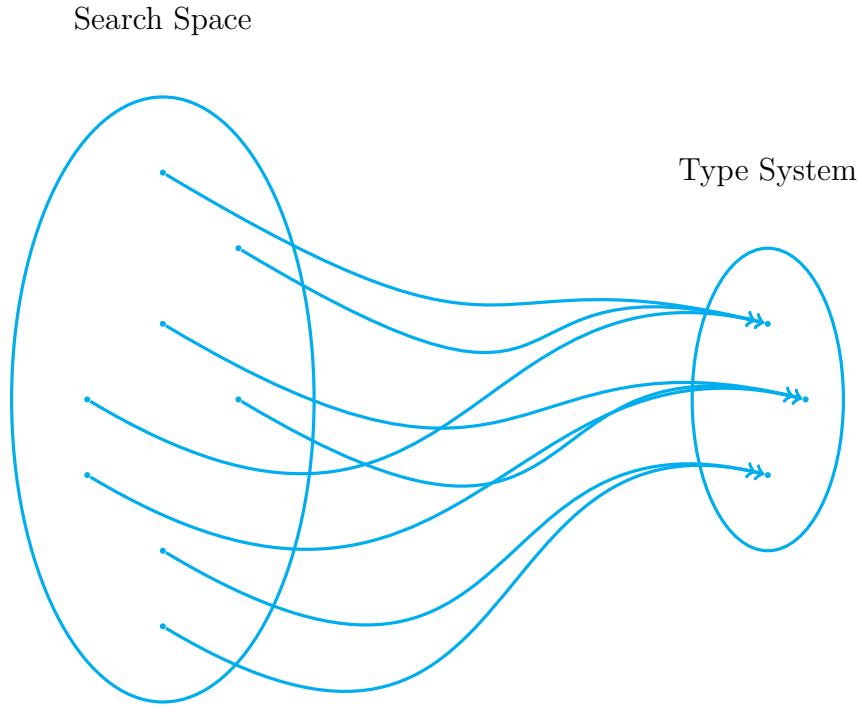


Figure 10: Type system and the Search Space Representation.

A common misconception is think of *type system* as state–space abstractions. (PRIEDITIS, 1993) defines a state–space abstraction as a simplified version of the problem in which:

- The cost of the least–cost path between two abstracted states must less than or equal to the cost of the least–cost path between the corresponding two states in the original state–space.
- Goal states in the original state–space must be goal states in the abstracted state–space.

In contrast with state–space abstractions, a *type system* does not have these two requeriments. A *type system* is just a partition of the nodes in the search tree.

The *type system* can not be represented as a graph since *type system* does not necessarily define relation between the types.

The relation between *type system* and abstractions is the following: The *type system* can not necessarily be used as abstractions, abstractions can always be used as *type system*.

3.4 Search Space and Search Tree

(LELIS; ZILLES; HOLTE, 2013) defines the search space and search tree in the following way: Let the *underlying search tree* (UST) be the full brute-force tree created from a connected, undirected and implicitly defined *underlying search graph* (USG) describing a state space. Some search algorithms expand a subtree of the UST while searching for a solution (e.g., a portion of the UST might not be expanded due to heuristic guidance); we call this subtree the *expanded search tree* (EST).

Let $G = (N, E)$ be a graph representing an ESG where N is its set of states and for each $n \in N$ $Op(n) = \{op_i | (n, n_i) \in E\}$ is its set of operators.

Definition 3.4.1. Type System Let $S = (N, E)$ be a UST . $T = \{t_1, \dots, t_n\}$ is a *type system* for S if it is a disjoint partitioning of N . If $n \in N$ and $t \in T$ with $n \in t$, we write $T(n) = t$.

In this thesis we use *type system* based only in heuristics. (ZAHAVI et al., 2010) use the simplest heuristic-based *type system* in which two nodes n and n' are of the same type if they have the same heuristic value.

C	E	C
E	M	E
C	E	C

1	2	3
4	5	6
7	8	

Figure 11: The heuristic value is the position of the empty tile in a Specific state.

Let's explain how *type system* works through an example. The problem of 8-tile-puzzle in the Figure 11, the center tile is labeled with the letter M and the corners are labeled with C and the mediums with E. For this problem, for example, we can define the *type system* based on the position of the empty tile regarding the position of the empty tile in the goal State. For this case, two nodes n and n' would be of the same type if n and n' have the blank tile with the same letter and with the same distance to the empty tile of the goal state.

In the Figure 12, each row represent a type. The first board shows the empty tile in the center with distance to the empty tile in the goal state equal to 2, down left and right down. Then, the type would be (2,M). In the next board the empty tile is in the left top corner, and use the letter C. The minimum distance is 4 because to get the goal

empty tile is necessary to do: down, down, right, right or right, right, down, down, etc. So the type would be (4, C). In the next board there are two tiles that have the same type, because both have the same letter M with distance equal to 3. Then, both have the type (3,E). The fourth row have two boards with the same type, because both have the same letter C with distance equal to 2. Then, both have the type (2,C). The fifth row have two boards with the same type, because both have the same letter E with distance equal to 1. Then, both have the type (1,E). In the last row the empty tile is in the goal empty tile. So, the distance is zero and the letter is C . The type would be (0,C).

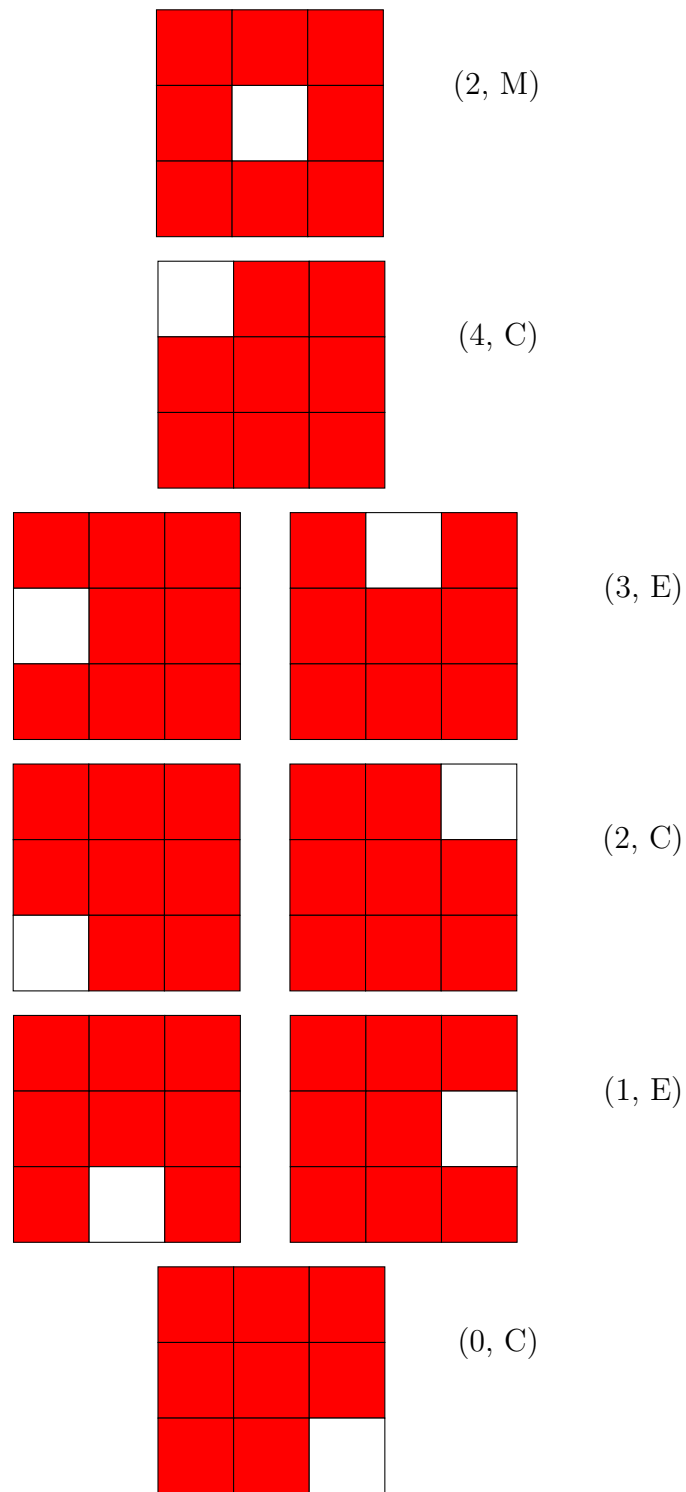
In the Figure 13, we can see how *Type System* works. In the Level 1, we have the root node, we add the property called weight or (W) initialized with one. Let's suppose that three nodes are generated by the root node in the Level 2. The nodes in the Level 2 have the following types: red, blue and red respectively, and each node receive the same W of the father. In the Level 2 we apply the concept of *Type System*, two states in the same level that have the same type (The same color) root subtrees of the same type and only one state per state must be explored. There are two nodes with type red in Level 2. So, we choose randomly one of them. Let's suppose we choose the right red node. Then, we have to update the number of nodes with the type red using the W , both red node types have $W = 1$, then we sum the W and the the new $W = 2$. So, in the Level 2 we will have two nodes of red type and one node with blue type.

When nodes in the Level 2 are expanded. The blue node expands one node of type blue and the red node expands two nodes of type red and blue. The question here is how many nodes would be generated in the Level 3? The answer is: $1 \times \text{blue} + 2 \times \text{red} + 2 \times \text{blue}$. So, in the Level 3 we will have 2 nodes of red type and 3 nodes of type blue.

In the Level 3 the W of the node blue would be the same W of the father. The father has the $W = 1$, then the child has the $W = 1$. The W of the red type and blue type would be 2. Once the W has been updated for each node in the Level 3 we apply the concept of *Type System* again. There are two nodes with type blue. So, we choose randomly one of them and update the W . Let's choose the right blue type and the updated W would be 3 because 1 from the left blue type plus the 2 from the right blue type.

When nodes in the Level 3 are expanded. The red node expands two nodes of types red and blue and the blue node expands one of the red. How many nodes would be generated at Level 4? The answer is: $2 \times \text{red} + 3 \times \text{red} + 2 \times \text{blue}$. So, in the Level 4 we will have five nodes of type red and two nodes of type blue.

The number of nodes expanded in the search tree is obtained summing all W

Figure 12: Using *type system*

plus one (The root node). So, the number of nodes expanded in the search tree would be $15 + 1 = 16$.

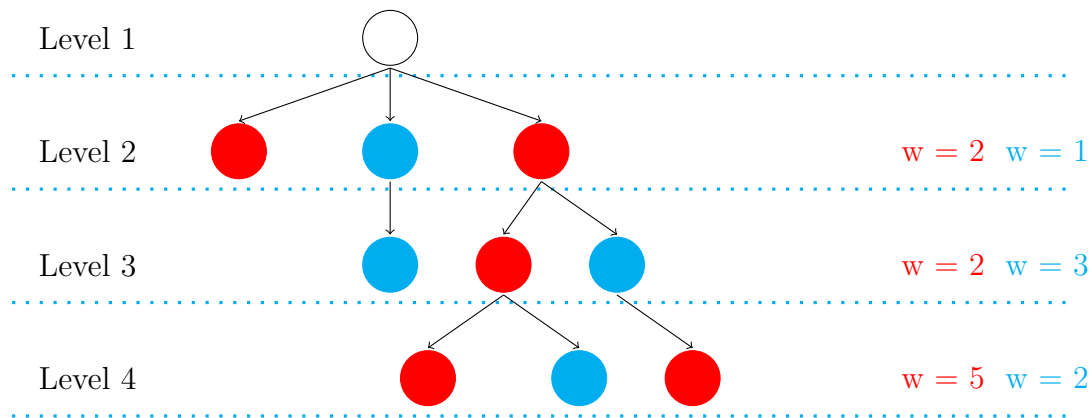


Figure 13: Search tree using Type System

3.5 Modeling

The resources of how to run the experiments.

3.6 Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae

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5 Conclusão

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Appendix

APPENDIX A – Quisque libero justo

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Annex

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ANNEX B – Cras non urna sed feugiat cum sociis natoque penatibus et magnis dis parturient montes nascetur ridiculus mus

Sed consequat tellus et tortor. Ut tempor laoreet quam. Nullam id wisi a libero tristique semper. Nullam nisl massa, rutrum ut, egestas semper, mollis id, leo. Nulla ac massa eu risus blandit mattis. Mauris ut nunc. In hac habitasse platea dictumst. Aliquam eget tortor. Quisque dapibus pede in erat. Nunc enim. In dui nulla, commodo at, consectetur nec, malesuada nec, elit. Aliquam ornare tellus eu urna. Sed nec metus. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas.

ANNEX C – Fusce facilisis lacinia dui

Phasellus id magna. Duis malesuada interdum arcu. Integer metus. Morbi pulvinar pellentesque mi. Suspendisse sed est eu magna molestie egestas. Quisque mi lorem, pulvinar eget, egestas quis, luctus at, ante. Proin auctor vehicula purus. Fusce ac nisl aliquam ante hendrerit pellentesque. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos hymenaeos. Morbi wisi. Etiam arcu mauris, facilisis sed, eleifend non, nonummy ut, pede. Cras ut lacus tempor metus mollis placerat. Vivamus eu tortor vel metus interdum malesuada.

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