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assignment 2

1) For heavily doped p-side $\rho = 2 \Omega \text{ cm}$

For heavily doped n-side $\rho = 1 \Omega \text{ cm}$

$$n_i = 2.5 \times 10^{13} / \text{cm}^3$$

$$\mu_p = 1800 \text{ cm}^2/\text{V}\cdot\text{s} \quad \mu_n = 3800$$

$$\text{p-side } q = q_p \mu_p \quad n = \frac{n_i^2}{p} \quad \mu_A = p = \checkmark$$

$$\frac{1}{2} = (1.6 \times 10^{-19} / \text{cm}^3 \times p \times 1800)$$

$$q = q_n \mu_n \quad 1 = (1.6 \times 10^{-19} / \text{cm}^3 \times n \times 3800)$$

$$N_D = n = \checkmark$$

$$p = \frac{n_i^2}{n} = \checkmark$$

$$V_0 = 2.5 \times 10^{13} \times p_n \left(\frac{\mu_A \mu_D}{D^2} \right) = 0.219 \text{ V}$$

$$\text{For p-side } p = 1.736 \times 10^{15} \text{ cm}^{-3}$$

$$\frac{n_i^2}{p} = \frac{(2.5 \times 10^{13})^2}{1.736 \times 10^{15}} = 3.60 \times 10^{11} \text{ cm}^{-3}$$

For n-Side:

$$n = 1.665 \times 10^{15} \text{ cm}^{-3}$$

$$p = \frac{n_i^2}{n} = \frac{(2.5 \times 10^{13})^2}{1.665 \times 10^{15}} = 3.799 \times 10^{11} \text{ cm}^{-3}$$

$$2b) V_0 = \frac{kT}{q} \ln \left| \frac{N_A N_D}{n_i^2} \right|$$

heavily doped

$$N_A = p = 1.736 \times 10^{15} \text{ cm}^{-3}, N_D = n = 1.665 \times 10^{15} \text{ cm}^{-3}$$

$$V_0 = \frac{(1.38 \times 10^{-23}) (300)}{1.6 \times 10^{-19}} \ln \left| \frac{1.736 \times 10^{15}}{(2.5 \times 10^{13})^2} \right|$$

$$V_0 = 0.218 \text{ V}$$

2) a) Forward direction

$$V_r = \frac{1125 + 273}{11600} = 0.0343 \text{ V}$$

$$I = I_0 \left(e^{\frac{V}{nV_T}} - 1 \right) = 130 \times 10^{-6} \left(e^{\frac{0.2}{0.0343}} - 1 \right) \\ = 0.01 \text{ A}$$

$$r = \frac{nV_T}{I} = \frac{0.0343}{0.01} = 3.43 \Omega$$

b) Reverse direction

$$V_r = 0.0343 \text{ V}, V_s = -0.2 \text{ V}$$

$$I = I_0 \left(e^{\frac{V}{nV_T}} - 1 \right)$$

$$= (30 \times 10^{-6}) \left(e^{\frac{-0.2}{0.0343}} - 1 \right) = -2.991 \times 10^{-5} \text{ A}$$

$$r = \frac{nV_T}{I + I_0} = \frac{0.0343}{|-2.991 \times 10^{-6}| + |30 \times 10^{-6}|}$$

$$= 38111.11 \Omega$$

3) Two diodes are connected to forward bias,
So they are ON.

For diode D1:

$$I = I_0 \left(e^{\frac{eV}{kT}} - 1 \right)$$

$$= (5 \times 10^{-9}) \left(e^{\frac{11.6 \times 10^{-6} (11)}{211.38 \times 10^{-23} (300)}} - 1 \right)$$

$$= 1.233 \text{ A}$$

$$r = \frac{mV}{I} = \frac{210.025862}{1.233} = 0.0419 \Omega$$

For diode D2:

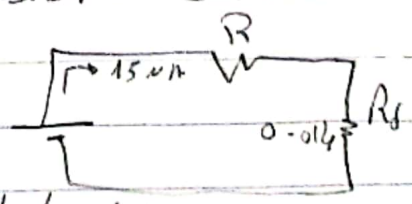
$$I = I_0 \left(e^{\frac{eV}{kT}} - 1 \right)$$

$$= (110 \times 10^{-9}) \left(e^{\frac{1.6 \times 10^{-19} (11)}{211.38 \times 10^{-23} (300)}} - 1 \right)$$

$$= 2.467 \text{ A}$$

$$r = \frac{mV}{I} = \frac{210.025862}{2.467} = 0.021 \Omega$$

The two are parallel their equivalent resistance is:

$$R_d = \frac{0.0419 \parallel 0.021}{0.0419 + 0.021} = 0.014 \Omega$$


$$R + R_d = \frac{V}{I} \quad R + 0.014 = \frac{1}{15 \times 10^{-3}} \quad R = 66.65 \Omega$$

4) Voltage across each diode is

$$\frac{V}{3} = \frac{2}{3} \text{ V}$$

$$I = I_0 (e^{\frac{V}{nV_T}} - 1)$$

$= V_T = 0.025 \text{ V}$ at room temperature

$$I = 10^{14} |e^{\frac{2/3}{0.025}} - 1| = 3.812 \times 10^{-3} \text{ A}$$

$$\text{b) } I = |3.812 \times 10^{-3}| - |1 \times 10^{-3}| \\ = 2.812 \times 10^{-3} \text{ A}$$

$$I = I_0 (e^{\frac{V}{nV_T}} - 1)$$

$$e^{\frac{V}{0.025}} = \frac{2.812 \times 10^{-3}}{10^{14}} + 1$$

$V = 0.659 \text{ V}$ per each diode

$$3V = 3(0.659) = 1.977 \text{ V}$$

Change in out put voltage

$$2 - 1.977 = 0.023 \text{ V}$$

$$\text{c) } R = \frac{V}{I} = \frac{2}{1 \times 10^{-3}} = 2 \text{ K}\Omega$$

5) Built-in Voltage - Barrier potential

$$V_0 = V_T \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

$$= \frac{300}{11600} \ln \left(\frac{10^{12} / 10^{14}}{1.5 \times 10^{10}} \right) = 0.7532 \text{ V}$$

$$w = \sqrt{\frac{2\epsilon_s}{q} \left| \frac{1}{N_A} + \frac{1}{N_D} \right| V_0}$$

$$= \sqrt{\frac{2(11.04 \times 10^{-12})}{1.6 \times 10^{-19}} \left| \frac{1}{10^{12}} + \frac{1}{10^{14}} \right| (0.7532)}$$

$$= 3.28 \times 10^{-5} \text{ m}$$

$$\frac{x_n}{x_p} = \frac{N_D}{N_A} = \frac{10^{14}}{10^{12}} = 10$$

$$x_n = 10 x_p$$

$$w = x_n + x_p = 10 x_p + x_p = 11 x_p$$

$$3.28 \times 10^{-5} = 11 x_p$$

$$x_p = 2.98 \times 10^{-6} \text{ m} \quad x_n = 10 / (2.98 \times 10^{-6}) =$$

$$= 2.98 \times 10^{-6} \text{ m}$$