

FA	NFA	TG
no relaxation	2 relaxation [1 and 2 only]	4 relaxations 1) $\Delta$ -transitions 2) non-determinism 3) multiple start states 4) multiple letters on edge

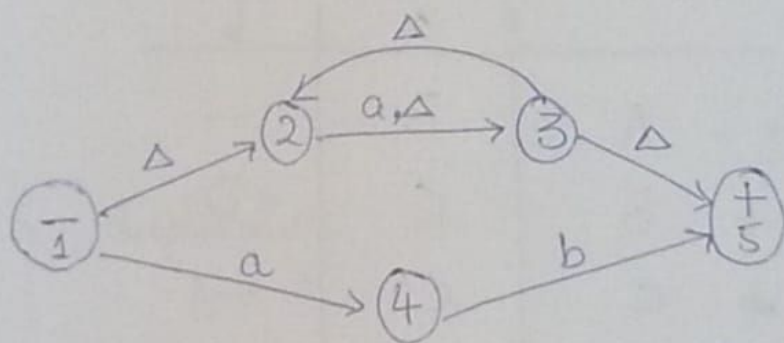
[RE to FA conversion]

- RE  $\rightarrow$  NFA
- NFA  $\rightarrow$  FA
- FA  $\rightarrow$  minimized FA

FA = DFA

Ex: 1  $a^* + ab$

a) RE  $\rightarrow$  NFA



b) NFA to FA :

$$\lambda\text{-closure}\{1\} = \{1, 2, 3, 5\} \quad \text{--- } \textcircled{A}$$

$$\text{gotoset}_a(A) = \{3, 4\} (B)$$

$$\text{gotoset}_b(A) = \{ \}$$

$$\lambda\text{-closure}\{3, 4\} = \{3, 4, 5, 2\} - (B_+)$$

$$\text{goto}_{\text{set}_a}(B) = \{3\}_{(C)}$$

$$\text{goto}_{\text{set}_b}(B) = \{5\}_{(D)}$$

$$\lambda\text{-closure}\{3\} = \{3, 2, 5\} - (C_+)$$

$$\text{goto}_{\text{set}_a}(C) = \{3\}_{(C)}$$

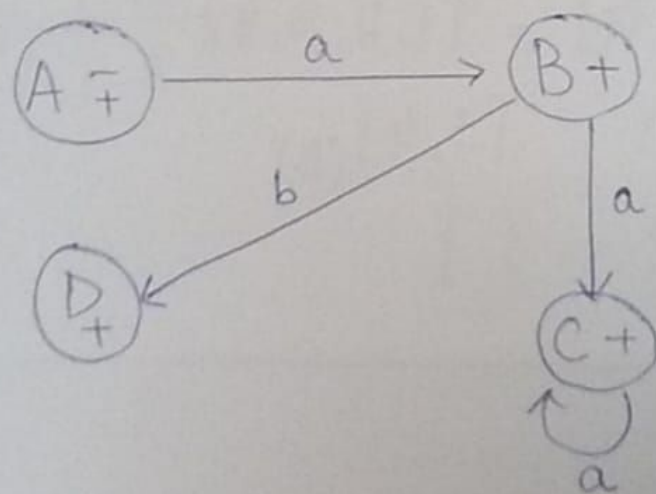
$$\text{goto}_{\text{set}_b}(C) = \{\}$$

$$\lambda\text{-closure}\{5\} = \{5\} - (D_+)$$

$$\text{goto}_{\text{set}_a}(D) = \{\}$$

$$\text{goto}_{\text{set}_b}(D) = \{\}$$

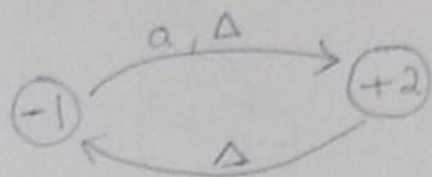
		a	b
+-	A	B	-
+	B	C	D
+	C	C	-
+	D	-	-



Ex 2:

$a^*$

a) RE  $\rightarrow$  NFA



b) NFA  $\rightarrow$  FA

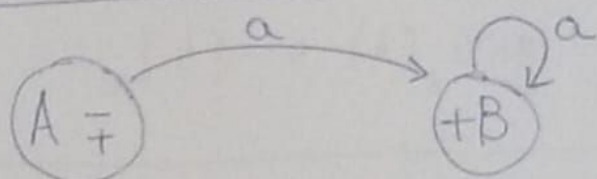
$$\lambda\text{-closure}\{1\} = \{1, 2\} \text{ --- (A)}$$

$$\text{goto}_a(A) = \{2\} \text{ (B)}$$

$$\lambda\text{-closure}\{2\} = \{2, 1\} \text{ --- (B)}$$

$$\text{goto}_a(B) = \{2\} \text{ (B)}$$

	a
$\bar{+}$ A	B
$+$ B	B



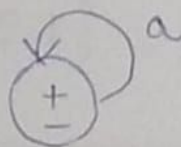
c) NFA  $\rightarrow$  minimized FA

	a
$\bar{+}$ A	<del>B</del> A
$+$ B	B

} duplication  
 $A = B$

$\Rightarrow$

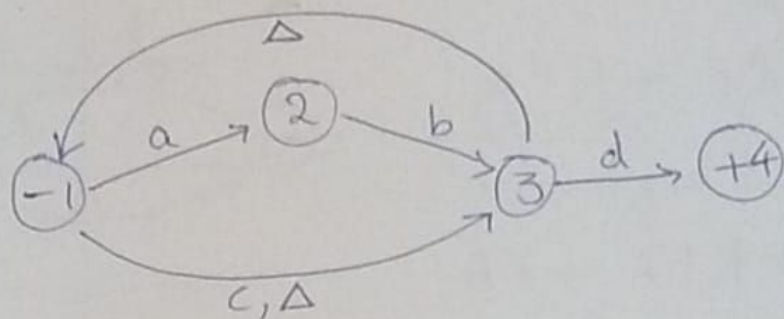
	a
$\bar{+}$ A	A





Ex 3:  $(ab+c)^*d$

a)  $RE \rightarrow NFA$



b)  $NFA \rightarrow FA$

$$\lambda\text{-closure}\{1\} = \{1, 3\} - \textcircled{A}$$

$$\text{goto}_a(A) = \{2\}_B$$

$$\text{goto}_b(A) = \{\}$$

$$\text{goto}_c(A) = \{3\}_A$$

$$\text{goto}_d(A) = \{4\}_C$$

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$$\lambda\text{-closure}\{2\} = \{2\} - \textcircled{B}$$

$$\text{goto}_a(B) = \{\}$$

$$\text{goto}_b(B) = \{3\}_A$$

$$\text{goto}_c(B) = \{\}$$

$$\text{goto}_d(B) = \{\}$$

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$$\lambda\text{-closure}\{3\} = \{1, 3\} - \textcircled{A}$$

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$$\lambda\text{-closure}\{4\} = \{4\} - \textcircled{C+}$$

$$\text{goto}_a(C) = \{\}$$

$$\text{goto}_c(C) = \{\}$$

$$\text{goto}_b(C) = \{\}$$

$$\text{goto}_d(C) = \{\}$$

	a	b	c	d
- A	B	-	A	C
B	-	A	-	-
+ C	-	-	-	-

[Already minimized]

