Regression Comparison Table

| Feature | Simple Linear Regression | Simple Non-linear Regression | Polynomial Regression | Multiple Non-linear Regression | Multiple Linear Regression |
|---------------------------|--|---|--|--|---|
| Definition | Models the relationship between a dependent variable and a single predictor using a linear equation. | Models the relationship between a dependent variable and a single predictor using a non- linear function. | Models the relationship between a dependent variable and one or more predictors using polynomial terms (e.g., X^2, X^3, etc.). | Models the relationship between a dependent variable and multiple predictors with nonlinear relationships. | Models the relationship between a dependent variable and multiple predictors using a linear equation. |
| Predictors | Single predictor variable X. | Single predictor variable X with a non-linear transformation. | Predictors are polynomial terms of the original variables (e.g., X, X^2, X^3). | Predictors can be any non-linear functions of the original variables (e.g., sin(X), e^X, log(X)). | Multiple predictor variables X1, X2,, Xn. |
| Equation Example | $y = \beta 0 + \beta 1 X + \varepsilon$ | $y = \beta 0 + \beta 1 e^{\Lambda} X + \varepsilon$ | y = β0 + β1 X + β2 $X^2 + β3 X^3 + ε$ | $y = \beta 0 + \beta 1 \sin(X1) + \beta 2 e^X 2 + \epsilon$ | y = β0 + β1 X1 + β2 X2 + + βn Xn + ε |
| Nature of Relationship | Linear relationship with the predictor. | Non-linear relationship with the predictor. | Polynomial relationship with the predictors. | General non-linear relationship with the predictors. | Linear relationship with the predictors. |
| Linear with Respect to | Linear with respect to the coefficients (parameters). | Non-linear with respect to the predictor but can be linear with respect to coefficients. | Linear with respect to the coefficients (parameters). | Non-linear with respect to both the predictors and the coefficients. | Linear with respect to the coefficients (parameters). |
| Complexity | Simplest form of regression, easy to implement and solve. | More complex than simple linear regression, often requiring transformation. | Simpler to implement and solve as it reduces to a linear problem. | More complex, often requiring iterative optimization techniques. | More complex than simple linear regression due to multiple predictors, but still linear in nature. |

| Estimation Method | Uses ordinary least squares (OLS) for estimation. | Can use non-linear least squares or other non-linear optimization techniques. | Can use ordinary least squares (OLS) for estimation. | Often requires non- linear optimization methods for estimation. | Uses ordinary least squares (OLS) for estimation. |
|-------------------|---|---|--|---|--|
| Common Uses | Useful for modeling linear relationships in data. | Useful for modeling specific non-linear relationships in data. | Useful for modeling curved relationships in data. | Useful for modeling complex relationships where polynomial terms may not suffice. | Useful for modeling linear relationships involving multiple predictors. |
| Interpretability | Easiest to interpret with clear linear relationships. | Interpretation depends on the specific non- linear function used. | Easier to interpret as extensions of linear regression. | Can be more difficult to interpret due to complex functional forms. | Interpretable with clear linear relationships among multiple predictors. |
| Example Models | Simple linear regression with one predictor. | Exponential growth/decay, logarithmic models. | Quadratic, cubic, quartic polynomial regression. | Exponential, logarithmic, trigonometric regression. | Multiple linear regression models in various fields. |
| Flexibility | Least flexible, limited to linear relationships. | Flexible within the specific non-linear function used. | Less flexible, limited to polynomial terms. | More flexible, allowing various types of non-linear functions. | More flexible than simple linear regression due to multiple predictors, but limited to linear relationships. |