

# Accurate Modeling of Antenna Structures by Means of Domain Confinement and Pyramidal Deep Neural Networks

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**Abstract**—The importance of surrogate modeling techniques has been gradually increasing in the design of antenna structures over the recent years. Perhaps the most important reason is a high cost of full-wave electromagnetic (EM) analysis of antenna systems. Although imperative in ensuring evaluation reliability, it entails considerable computational expenses. These are especially pronounced when carrying out EM-driven design tasks such as geometry parameter tuning or uncertainty quantification, both requiring repetitive simulations. Conducting some of the design procedures, e.g., global search or yield optimization, directly at the level of simulation models may be prohibitive. The employment of fast replacement models (or surrogates) may alleviate these difficulties; yet, accurate modeling of antenna structures faces its own challenges. The two major obstacles are the curse of dimensionality, manifesting itself in a rapid growth of the number of training data samples necessary to render a reliable model (as a function of the number of antenna parameters), and high nonlinearity of antenna characteristics. Recently, the concept of performance-driven modeling has been introduced, where the modeling process is focused on a small region of the parameters space, which contains high-quality designs with respect of the considered performance figures. The most advanced variation of this class of methods is nested kriging, where both the model domain and the surrogate itself are constructed through kriging interpolation. Domain confinement is realized using a set of pre-optimized reference designs, and allows for significant improvement of the model predictive power while using a limited number of training data samples. In this work, the constrained modeling concept is coupled with a novel pyramidal deep regression network (PDRN) surrogate, which offers improved handling of highly-nonlinear antenna responses. Three examples of microstrip antennas are used to demonstrate the advantages of constrained PDRN metamodels over the nested kriging surrogates with the (average) accuracy improved by a factor of two without increasing the training data set cardinality.

**Index Terms**—Surrogate modeling, antenna design, domain confinement, nested kriging, deep neural networks.

## I. INTRODUCTION

Design of antenna systems is a complex and multifaceted task, which requires meticulous development of the structure geometry [1], [2], but also careful tuning of its parameters [3]. Depending on the application area and performance demands

imposed upon the device, the antenna topology may incorporate various modifications of the base geometries (e.g., stubs of various shapes [4], ground plane [5] and radiator slots [6], defected ground structures [7], shorting pins [8], etc.), require appropriate allocation of its components (e.g., to excite orthogonal modes in circularly polarized antenna [9], improve radiator isolation in MIMO systems [10]), or a construction of compound devices, e.g., frequency selective surfaces allocated over a radiator for directivity improvement [11], etc. The aforementioned and other design techniques lead to increasingly complex designs described by large numbers of parameters, but also phenomena that affect the system operation (mutual coupling [12], the presence of connectors [13], radomes [14]). Accounting for these in an adequate manner can only be done through full-wave electromagnetic (EM) analysis, which has become ubiquitous in the design of modern antenna structures [15]–[19]. Evaluation accuracy and versatility perhaps the most appealing features of EM simulation tools, whereas potentially long simulation time is a disadvantage. The latter becomes problematic whenever repetitive analyzes are necessary. This is a common issue for most EM-driven design task, including parameter tuning [20], multi-objective design [21], statistical analysis [22], or tolerance-aware optimization [23].

The literature offers various tools for alleviating the difficulties incurred by the aforementioned high-cost issue. Some of these are strictly algorithmic approaches, both intrusive (e.g., adjoint sensitivities [24]), and non-intrusive (e.g., gradient-based procedures accelerated by sparse sensitivity updates [25], [26]); others exploit customized EM solvers tailored to particular classes of antenna structures [27], [28]. Notwithstanding, a large part of recent developments rely on surrogate modeling techniques [29]–[35]. By far, the most popular ones are approximation models, which are fast to evaluate and easily accessible [36], [37]. Because of being data-driven, these models are versatile and readily transferrable between various application domains. Widely used techniques include polynomial regression [38], kriging [39], radial-basis functions [40], neural networks [41], [42], support vector regression [43], Gaussian process regression [44], or polynomial chaos expansion [45].

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Although the surrogates can be used as stand-alone models, i.e., overall replacements of EM simulations, this is only possible for simple design scenarios (low-dimensional parameter spaces, limited parameter ranges, slightly nonlinear system outputs) [46], [47]. In more realistic situations, data-driven models are often combined with nature-inspired optimization procedures [48]–[50], or machine learning frameworks [51], [52], where utilization of the model as a predictor is interleaved with its updating process, typically using some sort of sequential design of experiments [53] with appropriate infill criteria [54]. The latter can be oriented towards improving the model accuracy [55] or identification of the global optimum [56]. Physics-based surrogates constitute a second group of metamodels, which are particularly popular in the context of local optimization [57]. The main idea is to correct an underlying low-fidelity representation of the system (e.g., equivalent network [58], or coarse-mesh EM model) using sparsely-sampled high-fidelity data. Owing to the embedded problem-specific knowledge, physics-based surrogates exhibit better generalization capability (as compared to data-driven models) but they are less versatile, and highly dependent on the setup (selection of the low-fidelity model and the correction methods). Representative examples of physics-based techniques include space mapping [59], cognition-driven design [60], and various response correction approaches (e.g., [61], [62]).

Despite their popularity, data-driven models are severely affected by the curse of dimensionality, which hinders their application to modeling of real-world antenna structures. Due to high nonlinearity of antenna characteristics, handling more than a few parameters becomes a serious problem, especially when broad ranges thereof are to be covered to ensure design utility of the model. Depending on the problem and setup, the scope of applicability can be somehow extended through dimensionality reduction (principal component analysis [63], model order reduction approaches [64]), high-dimensional model representation (HDMR) [65], orthogonal matching pursuit [66], or variable-fidelity methods (Bayesian model fusion [67], co-kriging [68]). An alternative approach is the employment of deep learning (DL) algorithms [69], in particular, Deep Neural Networks (DNN) that have demonstrated their capability of improved handling of nonlinear system outputs as compared to more traditional regression models (e.g., [70], [71]). Unfortunately, DNNs face some serious issues on their own, primarily related to the model setup (adjustment of hyper-parameters, the network architecture, preventing overtraining, etc.) [72]–[74]. Another alternative is ensemble learning (EL) [75], which is essentially a technique of strategically combining different sets of individual models, referred to as learners, to solve a specific computer intelligence challenge such as classification or regression. The main principle of EL is to use base learner models, usually exhibiting low performance as stand-alone surrogates, as the building blocks for generating surrogates with more complex architecture and improved performance [76]. However, an appropriate handling of the building blocks, including their selection and integration, is a non-trivial task [77]. Recently introduced performance-driven (or constrained)

modeling paradigm offers a conceptually different solution to the dimensionality and parameter range issues [78]. Therein, the surrogate model is only constructed in a specified region of the parameter space, containing design that are of high-quality with respect to the assumed performance figures. Identification of this region, and, consequently, the modeling domain, is realized using a set of pre-optimized reference designs and an auxiliary inverse model. The surrogate model itself is constructed using kriging interpolation. As demonstrated in [79] and [80], domain confinement allows for a dramatic improvement of the accuracy while using small number of training data samples.

This work proposes a framework for modeling of antenna structures, which combines the domain confinement approach, and a pyramidal deep regression network (PDRN). The latter is a novel approach incorporating deep neural network surrogates with a pyramidal-shape architecture, and procedures for automated determination of the specific model network and the hyper-parameters. The latter allows for mitigating the common issues pertinent to DNN models, in particular, the risk of overtraining, but also enables improved exploitation of the problem-specific knowledge embedded in the training data set. At the same time, constraining the model domain according to the performance-driven modeling methodology [78], permits efficient handling of parameter space dimensionality and setting up high-quality models valid over broad parameter ranges. The presented procedure has been comprehensively validated using three antenna structures, and benchmarked against conventional surrogates as well as nested kriging [79]. The results demonstrate that our approach fully exploits all advantages implied by domain confinement. At the same time, the predictive power of the obtained models is greatly improved as compared to the nested kriging framework (by a factor of around two on the average), let alone the remaining benchmark methods. The latter is a consequence of inherent suitability of DNN in terms of representing nonlinear frequency characteristics of antenna structures. The proposed approach can be considered a viable alternative to existing techniques whenever a construction of accurate replacement models is required in multi-parameter spaces under limited computational resources.

The novelty and the technical contribution of this work can be summarized as follows: (i) development of a novel ANN-based surrogate retaining the flexibility of deep neural network models but with architecture described by a small number of control parameters, which addresses practical issues pertinent to DNN metamodels (overtraining, etc.); (iii) development of procedures for automated hyper-parameter determination through Bayesian Optimization, (iii) incorporating the proposed surrogate into performance-driven modeling paradigm to alleviate major difficulties of antenna response modeling, (iv) demonstrating the relevance of the proposed approach for modeling of multi-parameter antenna characteristics over broad ranges of geometry parameters and operating conditions, (v) demonstrating superiority of the presented technique over several state-of-the-art surrogates, both conventional and domain-confined ones.

## II. ANTENNA MODELING USING DOMAIN-CONFINED PYRAMIDAL DEEP REGRESSION NETWORK

This section introduces the modelling methodology proposed in this work. We start by formulating the antenna modelling task in Section II.A. This is followed by an outline of the pyramidal deep regression network (PDRN) surrogate, developed to represent antenna characteristics within the presented framework (Section II.B). The concept and implementation of domain confinement [78] is briefly recalled in Section II.C, whereas Section II.D summarizes the operational flow of the overall modelling procedure. Comprehensive verification of the methodology along with its benchmarking will be discussed in Section III.

### A. Surrogate Modeling: Problem Formulation

For an antenna structure of interest, we will denote by  $\mathbf{x} = [x_1 \dots x_n]^T$  the vector of its independent parameters. Typically, these are antenna dimensions or material parameters (e.g., permittivity of the substrate, the structure is implemented on). It is assumed that the primary computational model of the antenna is based on full-wave electromagnetic (EM) analysis. The relevant antenna responses (reflection, gain, axial ratio characteristics, etc.) at the design  $\mathbf{x}$  are collectively denoted as  $\mathbf{R}(\mathbf{x})$ . The objective is to construct a fast replacement model (surrogate)  $\mathbf{R}_s$ , which is valid within a certain domain  $X$ , typically defined using lower and upper bounds  $\mathbf{l} = [l_1 \dots l_n]^T$  and  $\mathbf{u} = [u_1 \dots u_n]^T$ , on the parameters, so that  $l_k \leq x_k \leq u_k$ , for  $k = 1, \dots, n$ . The surrogate should represent the EM model as well as possible over  $X$ , i.e.,  $\mathbf{R}(\mathbf{x}) - \mathbf{R}_s(\mathbf{x})$  is to be small (e.g., in the RMS sense [81]) for all  $\mathbf{x} \in X$ . At the same time, the surrogate should be computationally cheap so that multiple evaluations of  $\mathbf{R}_s$  do not entail considerable CPU expenses.

In this work, we focus on data-driven models, i.e., the surrogates that are constructed using the data pairs  $\{\mathbf{x}^{(i)}, \mathbf{R}(\mathbf{x}^{(i)})\}_{i=1, \dots, N_T}$ , acquired across the domain  $X$ . This data is approximated, and the model yields predictions concerning the antenna characteristics for arbitrary parameter vectors within  $X$ .

### B. Pyramidal Deep Regression Network (PDRN) Surrogate

This section introduces the proposed pyramidal deep regression network (PDRN) model. By using a pyramid-like structure of the neuron layers, PDRN attempts to find the optimum model by transforming the input parameters into a very high dimensional space to increase the number of degrees of freedom and facilitate handling of nonlinear input-output relationships pertinent to the antenna structure at hand. Subsequently, after a mapping step, the problem is reduced to a low-dimensional space. For preventing model over-fitting, the model leaky ReLU activation function [82], [83], [84] is employed. The detailed description of the PDRN surrogate is provided below, following a brief characterization of the artificial neural network (ANN) and deep neural network (DNN) models.

Universal approximation is a well-known property of ANN, which indicates a possibility of modelling a continuous function over a compact set [85], [86]. Let  $f: \mathbb{R}^{D_i} \rightarrow \mathbb{R}^{D_o}$  be a general transformer function over  $\mathcal{S} \subset \mathbb{R}^{D_i}$ .  $D_i$  and  $D_o$  stand for the

input and output space dimensions. A general feedforward neural network can be defined as

$$f(\mathbf{x}) = \sigma(\mathbf{W}^K \dots \sigma(\mathbf{W}^2 \times \sigma(\mathbf{W}^1 \times \mathbf{x} + \mathbf{b}_1)) \dots + \mathbf{b}_K) \quad (1)$$

where  $\mathbf{x} \in \mathbb{R}^{D_i \times 1}$ ,  $f(\mathbf{x}) \in \mathbb{R}^{D_o \times 1}$  are the input and output vectors,  $\mathbf{W}^l, \mathbf{b}_l$  are the weight matrices and bias vector, respectively, whereas  $\sigma(\cdot)$  is a non-linear activation function. Using this definition, it can be seen that  $f(\mathbf{x})$  is non-linear affine transformation over  $\mathcal{S}$ . Its non-linearity has a vital role in modelling of  $f(\mathbf{x})$ . In the training phase of neural network, an optimizer attempts to identify the optimal set of weights to minimize a given loss function, defined as a metric of the network approximation capability. ANN models are capable of modelling complex data. ANN enact a significant role in the field of regression studies [41], [42]. It is especially in multi-output problems, where ANN ability to simultaneously produce all outputs at the same time makes it superior to algorithms that can only yield a single output, such as Support Vector Regression Machine (SVRM) [43], or Gaussian Process Regression (GPR) [44]. Otherwise, in these algorithms, separate models must be trained for each output. This situation is troublesome for large data sets data, such as frequency characteristics of antenna structures. While nonlinearity leverages NN structures, it also reveals their weakness. In particular, the asymptotic regions of the activation function determine the characteristics of the neural networks. Sigmoid and tanh, which are the most widely used activation functions in ANN models, can be given as an example. The ANN models learning mechanism is based on portioning the error generated in the loss function onto the weights. The process is referred to as back propagation, and enabled using the derivative operator's chain rule. Let  $\mathcal{L}(\mathbf{t}, f(\mathbf{x}))$  be a loss function for the ANN over  $\mathbf{t} \in \mathbb{R}^{D_o \times 1}$  target vector. A derivative of this function with respect to  $\mathbf{W}^l$  can be expressed as

$$\frac{\partial \mathcal{L}(\mathbf{t}, f(\mathbf{x}))}{\partial \mathbf{W}^l} = \frac{\partial \mathcal{L}(\mathbf{t}, f(\mathbf{x}))}{\partial \sigma^K} \times \frac{\partial \sigma^K}{\partial \mathbf{x}^{K-1}} \times \dots \times \frac{\partial \sigma^l}{\partial \mathbf{W}^l} \quad (2)$$

where  $\sigma^l$  are the outputs of the  $l$ th layer activations. Sigmoid and tanh activations have asymptotic regions. Hence, during the back propagation of the error, the derivatives tend to be zero in these regions. This problem is referred to as *vanishing gradient*, where it affects the generalization capabilities of the models using the activation functions featuring a saturation regime [87]. In particular, it makes effective learning of ANN a complicated matter. This issue is especially pronounced for Deep Neural Network (DNN) due to the internal covariate shift problem [88]. Similar problems have been experienced in Convolutional Neural Network (CNN) models, which have been popular in the recent years and have a very deep structure. However, with the increasing interest in Convolutional Neural Network (CNN) structures, many alternative activation functions have been proposed to alleviate this difficulty [82]-[84].

Deep Neural Networks (DNN) is a recent generation of ANN models (Shallow Neural Networks) that generate outputs by passing input information through more than two layers [89]. One of the best known DNN models in this field are CNNs. CNN models have been developed especially for image processing applications. By reducing the raw  $N \times M$  sized image to lower dimensions with the convolution mechanism, it

obtains a feature vector and classifies images at the same time. The principal approach here is that the raw image data in very high dimension is gradually mapped to lower dimensions. This way, raw  $N \times M$  size data is reduced to  $D$  dimension. Inspired by this, we set up a regression model with the strategy of transition from higher dimensional space to lower dimensional space in order to process data featuring complex input/output relationships.

The Pyramidal Deep Regression Network (PDRN) model proposed in this work capitalizes on several improvements and mechanisms introduced into the DNN surrogates. In particular, PDRN is designed to alleviate the issues common to neural networks. The overall architecture of PDRN, shown in Fig. 1, is the pyramid-shaped network. The idea behind this structure is to transform the input parameters into very high dimensional space to increase the number of degrees of freedom and facilitate handling of nonlinear input-output relationships pertinent to the antenna structure at hand. Subsequently, information distillation progresses to low-dimensional space. This process can actually be thought of as a dimensional evolution between the input and output parameters. As mentioned before, PDRN relies on rendering a DNN by reducing the number of neurons for subsequent layers. From the point of view of the network output, the number of neurons is gradually increasing towards the input layer. The scale ratio  $s_c$  is fixed for all layers, which allows for simplifying the network architecture by limiting it to a specific (here, trapezoidal) shape, which can be controlled using a few parameters to be automatically determined during the training process.

As seen in the Fig. 1, the neural architecture of PDRN depends of  $\phi_K$  that is the number of neurons for the last layer. The number of neurons for other layers are determined by factoring of  $\phi_K$ . The depth size  $d_s$  is another parameter of PDRN, which controls the number of hidden layers between the input and the output layers. For example, according to this definition,  $\phi_K = 64$ ,  $s_c = 1.2$  and  $d_s = 3$  yields the architecture of PDRN as

$$\mathcal{M} : r(64 \times (s_c)^2) \rightarrow r(64 \times (s_c)^1) \rightarrow r(64 \times (s_c)^0) \quad (3)$$

where  $\mathcal{M}$  represents the model structure and  $r(\cdot)$  is rounding operator to ensure an integer number of neurons in each layer. Thus, the PDRN structure can be fully controlled using the three parameters,  $\phi_K$ ,  $s_c$ , and  $d_s$ . As mentioned before, the classical activation function lead to the vanishing gradient issues in DNN. To prevent this phenomena, a leaky ReLU (LReLU) activation employed in CNNs is selected [90] to work with PDRN. LReLU activation and its derivative are defined as

$$\sigma_\alpha(x) = \begin{cases} x & x \geq 0 \\ \alpha x & \text{otherwise} \end{cases} \quad \frac{d\sigma_\alpha(x)}{dx} = \begin{cases} 1 & x \geq 0 \\ \alpha & \text{otherwise} \end{cases} \quad (4)$$

where the parameter  $\alpha \in (0,1)$  is referred to as the leakage ratio. Leaky ReLU has a negative slope, and this makes it operable at every gradient flow. As can be observed that the derivative of the activation function is non-zero in every training iteration. This makes it suitable for modelling complex data relations. In PDRN, LReLU activation and  $\alpha$  are fixed for all layers, therefore, it is sufficient to only select one parameter ( $\alpha$ ) in the construction phase of the surrogate. In summary, the

PDRN hyper-parameters determining the architecture of the model are: (i) the number of neurons in the last layer  $\phi_K$ , (ii) the depth of the model  $d_s$ , (iii) the scale parameter for determination of neurons in other layers  $s_c$ , and (iv) the leakage parameter  $\alpha$  of the LReLU.

Let  $\mathbf{v} \in \mathbb{R}^{D_i \times 1}$  be the input vector containing the parameters of the regression problem. PDRN maps it to a desired output parameter domain. The output values are compared with the target values using the Mean Absolute Error (MAE) loss function, and the error is propagated to the neural weights. The MAE loss is defined as,

$$\mathcal{L}_{MAE}(\mathbf{o}) = \mathbb{E}\{\|\mathbf{o} - \mathbf{t}\|\} \quad (5)$$

where  $\mathbf{o}, \mathbf{t} \in \mathbb{R}^{D_o \times 1}$  stand for the prediction values of network and the target vector in  $D_o$  dimension output space, respectively.  $\mathbb{E}\{\cdot\}$  is expectation operator. This loss indicates that the training process is equivalent to the  $\ell_1$ -norm minimization task.

In DNN models, including the proposed PDRN surrogate, it is vital to use a pre-processing step for heterogeneous-valued data which may feature considerably different parameter ranges. For data standardization, a z-score methodology is preferred [91], [92]. Let  $\mathbf{V} \in \mathbb{R}^{N_{tr} \times D_i}$  stores the training samples as row vector. Z-score is defined as,

$$\mathbf{v}_i^z = \frac{1}{N_{tr}} \times \sum_i \frac{\mathbf{v}_i - \boldsymbol{\mu}_z}{\boldsymbol{\eta}_z} \quad (6)$$

where  $\boldsymbol{\mu}_z, \boldsymbol{\eta}_z$  and  $\mathbf{v}_i^z$  are sample mean, standard deviation of dimensions of  $\mathbf{V}$ , and normalized training sample. Division in (6) is understood in the Hadamard sense (component-wise).

Having established the generic architecture with hyper-parameters along with the pre-processed training data, the next step is the model training process itself. The key element thereof is to compute the derivatives of the loss function with respect to the network weights. By using gradient-based descent algorithms, the model is trained to attain a local optimum in the solution space.

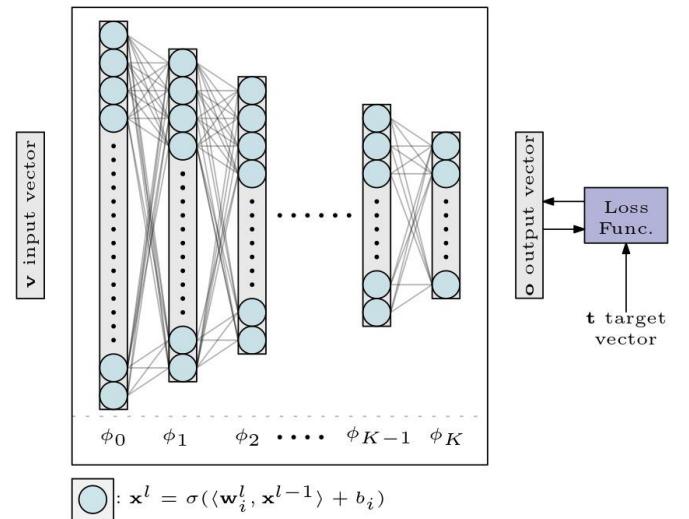


Fig. 1. Generic PDRN model architecture:  $\mathbf{x}^l$  and  $\mathbf{w}^l$  are output and weight values of  $l$ th layer.  $\sigma(\cdot)$  is the activation function.

If the DNN models are trained with a small amount of data, the training error can be readily reduced with no improvement of the model predictive power. This situation is referred to as overfitting [87]. Utilization of large-scale training data prevents the model from entering the overfitting regime. Although handling large-scale data is problematic for algorithms such as SVRM or GPR, it can be tackled with *stochastic gradient descent*-based optimizers such as Adagrad [93], RMSProp [94], and Adam [95]. Stochastic gradient-based descent procedures are the preferred training strategies for neural networks, which differ from a classical approach in utilization of the error function gradients. The former uses the gradients to train the model after passing the entire data through the network. Stochastic gradient descent uses a partition of data called mini batch to generate gradients, then train neurons by using this particular subset. Sweeping the entire data determines one training epoch. In this study, Adam optimizer is preferred to update the model weights. One of the fundamental issues in DNN, including the proposed model, is the adjustment of the network architecture, which is often realized by trial and error. In this work, Bayesian Optimization (BO) is employed to determine the architecture-defining hyper-parameters of PDRN in a fully automated manner. This will be elaborated on in Section II.C.

### C. PDRN Architecture Search via Bayesian Optimization

Optimal hyper-parameters determination is critical for the models designed for any classification or regression tasks where these parameters can be continuous variables (such as weights) or discrete variables such as the number of layers and the number of neurons. Herein, the optimal hyper-parameter determination of the proposed PDRN model is executed by means of Bayesian Optimization (BO). BO utilizes probabilistic modelling techniques to enable global optimisation of complex and expensive functions [96].

Probabilistic Surrogate Model (PSM) of the objective function iteratively improved at each observation, and the acquisition function (used to explore the state space based on the surrogate model optimally) are the two essential parts of Bayesian Optimization (BO) [97], [98], [99]. While PSM is being used to evaluate the uncertainty of the model, the acquisition function allows for balancing the exploration and exploitation during the optimization run. The model uncertainty plays a key role in this process. One of the most commonly used acquisition function is Expected Improvement (EI) [100]. The initial models are generated based on the random sampling or design of experiment (DoE) [101]. At each iteration, the PSMs are updated using the sampled data. Subsequent (in-fill) sample points are then generated by maximizing the acquisition function. Table I provides a pseudocode of the BO.

Although various models can be used for the prior distribution of probabilistic model [101], Gaussian Process (GP) is applied more frequently for BO as compared to others [102], [103]. For  $f: X \rightarrow R$ , GP assumes that for any finite set of samples  $\{\mathbf{x}_1, \dots, \mathbf{x}_n\} \in X^n$ , the vector  $(f(\mathbf{x}_1), \dots, f(\mathbf{x}_n))^T$  follows joint multivariate Gaussian distribution

$$[f(\mathbf{x}_1) \dots f(\mathbf{x}_n)]^T \sim N(\boldsymbol{\mu}, K) \quad (7)$$

where  $\boldsymbol{\mu}$  is a  $n \times 1$  mean vector,  $K$  is  $n \times n$  a covariance matrix.

TABLE I  
PSEUDOCODE OF BAYESIAN OPTIMIZATION

Bayesian Optimization <sup>#</sup> [96]
<b>1: Initial Sampling</b>
2: Generate probabilistic surrogate model
<b>3: for</b> $t = 1, 2, 3, \dots$ <b>do</b>
4: Find $\mathbf{x}_t$ optimizing the acquisition function
5: Sample $y_t = f(\mathbf{x}_t) + N(0, \sigma_{noise}^2)$ ,
6: update the probabilistic model
<b>7: End for</b>
<b>8: return optimal <math>f(\mathbf{x})</math></b>

<sup>#</sup> Here,  $\mathbf{x}_t$  is the  $t$ th sample,  $y_t$  is the noisy observation of the objective function at  $\mathbf{x}_t$ .

GP can be defined by the mean function  $m(\mathbf{x})$  and the covariance function  $k(\mathbf{x}_1, \mathbf{x}_2)$ . The mean vector  $\boldsymbol{\mu}$  is determined as

$$\mu_i = m(\mathbf{x}_i), \forall i \in 1, \dots, n \quad (8)$$

whereas the covariance matrix is determined by

$$K_{ij} = k(\mathbf{x}_i, \mathbf{x}_j) \quad (9)$$

Herein, Squared Exponential Covariance (Kernel) is used as the covariance function

$$k(\mathbf{x}_i, \mathbf{x}_j) = \sigma_f^2 \exp \left[ -\frac{1}{2} \frac{(\mathbf{x}_i - \mathbf{x}_j)^T (\mathbf{x}_i - \mathbf{x}_j)}{\sigma_l^2} \right] \quad (10)$$

where  $\sigma_l$  is the characteristic length scale, and  $\sigma_f$  is the standard deviation of the signal. Let  $D = \{X, \mathbf{y}\}$  be the training set, where  $X = \{\mathbf{x}_1, \dots, \mathbf{x}_n\}$  and  $\mathbf{y} = \{f(\mathbf{x}_1), \dots, f(\mathbf{x}_n)\}$ . For a new observation point  $\mathbf{x}_*$ , the corresponding function value  $\mathbf{y}_* = f(\mathbf{x}_*)$  follows joint Gaussian distribution

$$\begin{bmatrix} \mathbf{y}_* \\ \mathbf{y} \end{bmatrix} \sim N \left[ \begin{bmatrix} m(\mathbf{x}_*) \\ \mathbf{m} \end{bmatrix}, \begin{bmatrix} k(\mathbf{x}_*, \mathbf{x}_*) & k(\mathbf{x}_*, X) \\ k(X, \mathbf{x}_*) & K_n \end{bmatrix} \right] \quad (11)$$

where  $\mathbf{m} = (m(\mathbf{x}_1), \dots, m(\mathbf{x}_n))^T$  is the  $n \times 1$  mean vector,  $l$  is the length scale, and

$$k(\mathbf{x}_*, X) = (k(\mathbf{x}_*, \mathbf{x}_1), \dots, k(\mathbf{x}_*, \mathbf{x}_n)) \quad (12)$$

$$k(X, \mathbf{x}_*) = k(\mathbf{x}_*, X)^T \quad (13)$$

$$K_n = \begin{bmatrix} k(\mathbf{x}_1, \mathbf{x}_1) & \dots & k(\mathbf{x}_1, \mathbf{x}_n) \\ k(\mathbf{x}_2, \mathbf{x}_1) & \dots & k(\mathbf{x}_2, \mathbf{x}_n) \\ \vdots & \ddots & \vdots \\ k(\mathbf{x}_n, \mathbf{x}_1) & \dots & k(\mathbf{x}_n, \mathbf{x}_n) \end{bmatrix} \quad (14)$$

Here, it should be noted that  $\mathbf{y}_*$  is bounded by  $\mathbf{y}$  and also follows the normal distribution [104] defined as

$$\mathbf{y}_* \sim N(\boldsymbol{\mu}_{\mathbf{y}_*|\mathbf{y}}, \sigma_{\mathbf{y}_*|\mathbf{y}}^2) \quad (15)$$

$$\boldsymbol{\mu}_{\mathbf{y}_*|\mathbf{y}} = m(\mathbf{x}_*) + k(\mathbf{x}_*, X) K_n^{-1} (\mathbf{y} - \mathbf{m}) \quad (16)$$

$$\sigma_{\mathbf{y}_*|\mathbf{y}}^2 = k(\mathbf{x}_*, \mathbf{x}_*) - k(\mathbf{x}_*, X) K_n^{-1} k(X, \mathbf{x}_*) \quad (17)$$

The mean  $\boldsymbol{\mu}_{\mathbf{y}_*|\mathbf{y}}$  can be taken as the prediction while  $\sigma_{\mathbf{y}_*|\mathbf{y}}^2$  is the confidence of the prediction for probabilistic prediction of  $\mathbf{y}_*$ . A Gaussian noise  $\epsilon \sim N(0, \sigma_n^2)$ ,  $\sigma_n^2$ : variance of Gaussian noise, can be added to  $f(\mathbf{x})$  for observation of the noise effects. The covariance function and prediction of GP model after applying noise would be defined as:

$$k_n(\mathbf{x}_i, \mathbf{x}_j) = k(\mathbf{x}_i, \mathbf{x}_j) + \sigma_n^2 \delta_{ij} \quad \delta_{ij} = \begin{cases} 0 & i \neq j \\ 1 & i = j \end{cases} \quad (18)$$

$$\boldsymbol{\mu}_{\mathbf{y}_*|\mathbf{y}} = m(\mathbf{x}_*) + k(\mathbf{x}_*, X) (K_n + \sigma_n^2 \delta_{ij})^{-1} (\mathbf{y} - \mathbf{m}) \quad (19)$$



$$\sigma_{y_*|y}^2 = k(\mathbf{x}_*, \mathbf{x}_*) - k(\mathbf{x}_*, X)(K_n + \sigma_n^2 \delta_{ij})^{-1} k(X, \mathbf{x}_*) \quad (20)$$

The acquisition function is a key component of BO, which is used to determine the new (infill) points by balancing the trade-off between exploration and exploitation [98]. By using GP, the acquisition function attempts to minimize the objective function  $y = f(\mathbf{x})$ . As mentioned before, one of the commonly used acquisition functions is Expected Improvement (EI) [105], [106]. Let take  $\tau$  as the currently known minimal value of  $f(\mathbf{x})$ . The improvement  $I$  for  $y$  can be defined as

$$I(y, \tau) = \begin{cases} \tau - y & y < \tau \\ 0 & \text{otherwise} \end{cases} \quad (21)$$

and indicates that the improvement only occur when  $y$  is less than  $\tau$ . Based on the GP, the prediction of  $y$  at observation point  $x$  use the distribution of

$$p(y|D, S) = N(\mu(\mathbf{x}), \sigma^2(\mathbf{x})) \quad (22)$$

where  $\mu(x)$  and  $\sigma$  are the mean and variance of the distribution,  $S$  is the vector of hyper-parameters. Based on these, EI can be defined as

$$EI(\mathbf{x}) = E[I(y, \tau)] = \int_{-\infty}^{\infty} I(y, \tau) p(y|D, S) dy \quad (23)$$

$$= (\tau - \mu(\mathbf{x})) \Omega\left(\frac{\tau - \mu(\mathbf{x})}{\sigma(\mathbf{x})}\right) + \sigma(\mathbf{x}) \omega\left(\frac{\tau - \mu(\mathbf{x})}{\sigma(\mathbf{x})}\right)$$

where  $\Omega(\cdot)$  is the cumulative distribution function of standard normal distribution, and  $\omega(\cdot)$  is the probability density function.

In the following, the application of BO for PDRN neural architecture search is presented. BO estimates the number of neurons in the last layer  $\phi_K$ , the depth  $d_s$  of the model, the scale parameter  $s_p$ , and the leakage parameter  $\alpha$  of LReLU. The PDRN architecture parameters can be jointly described as  $S = \{\phi_K, d_s, s_c, \alpha\}$ . The operation of the BO search algorithm in the context of PDRN has been summarized in Table II.

Figure 2 shows the flow chart of the PDRN neural architecture search by BO. The output of the algorithm is the set of optimal hyper-parameters, which corresponds to the minimum average  $k$ -fold loss value  $\mathcal{L}_{(avg)}$  [107-110]. BO randomly generated a sample from the given hyper-parameter space that would be used to evaluate the  $k$ -fold error for a model created using these parameters. Subsequently, the parameter set  $S$ , and the average loss value  $\mathcal{L}_{(avg)}$  are stored, and  $S$  is updated. Towards the end of the optimization process, the parameter set  $S$  that gives the minimum average loss value  $\mathcal{L}_{(avg)}$  will be taken as the optimal model for the given training dataset.

In this study, the parameter ranges for the neural architecture search using BO are taken as follows:  $\phi_K \in \{16, 32, 48, \dots, 128\}$ ,  $d_s \in \{3, 4, 5, 6, 7\}$ ,  $s_c \in \{1, 1.25, 1.5, \dots, 3\}$ ,  $\alpha \in [0, 0.5]$ . Here, in order to reduce the computational overhead of the optimization process,  $\phi_K$  and  $s_c$  are taken as discrete values. Although these value can also be considered as continues variables, the effect of small variations in their values can generally be neglected. The maximum number of iteration is taken as 30 in this study. As mentioned before, over-fitting is one of the most challenging problems of DNN. Apart from using the appropriate activation function, the employment of regularization layers such as Dropout and Batch normalizations

are efficient solutions to prevent the over-fitting of the models [111], [112].

Construction of the proposed PDRN model is a three-stage process as explained in Fig. 3. In Stage 1, BO is used to determine the optimum network architecture for a given training data set. In this work,  $k = 2$ -fold is selected to evaluate the neural architecture quality. In Stage 2, the best hyper-parameter set  $S^{best}$  is used to generate the PDRN model, which is then trained using the entire input data set. In Stage 3, the final model performance is evaluated using the test data.

TABLE II  
BAYESIAN OPTIMIZATION OF PDRN HYPER-PARAMETERS

**Algorithm 2:** Bayesian Optimization Search Algorithm

**Input of**  $S(\cdot): V, iter$

**Output**  $\{\phi_K, d_s, s_c, \alpha\} = S(V, iter)$

**Procedure**

1. Set  $t = 0$ ; Initialize  $S^t = \{\phi_K, d_s, s_c, \alpha\}$
2. Generate PDRN model by using  $S^t$
3. Evaluate  $k$ -fold average score  $L_{avg}$  for the model
4. Update  $S$  using BO, store  $\{S^t, L_{avg}\}$ , and set  $t = t + 1$
5. **If**  $t = iter$ , **then** terminate the process, **else** go to 3
6. **Return**  $S^{best}$  corresponding to minimum  $L_{avg}$

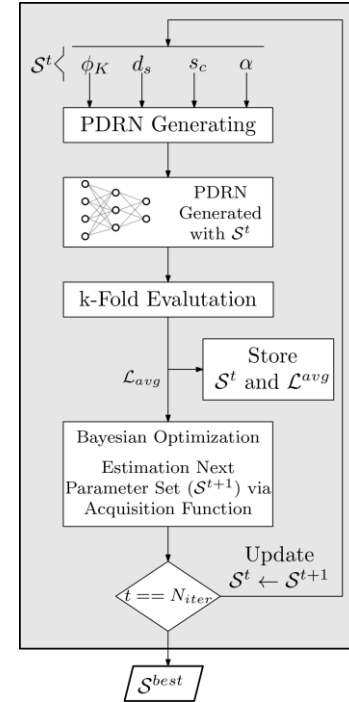


Fig. 2. Flow diagram of the neural architecture search of PDRN using Bayesian optimization.

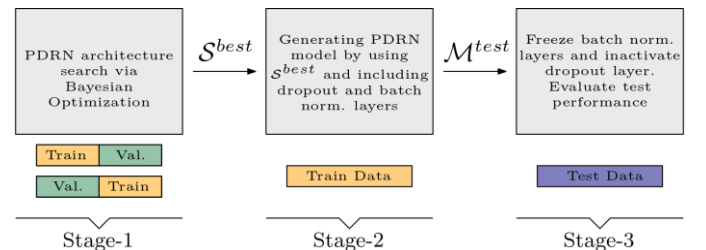


Fig. 3. Flow diagram of the PDRN surrogate training and architecture optimization.

#### D. Domain Confinement

As it will be demonstrated in Section 3, PDRN does ensure improved handling of highly-nonlinear antenna characteristics as compared to standard regression surrogates, e.g., kriging or support vector regression. In this work, for further enhancement of the accuracy, it is coupled with the performance-driven modeling paradigm of [79]. For the convenience of the reader, this section briefly outlines the concept and analytical formulation of domain confinement.

The key concept is the objective space  $F$  that consists of objective vectors  $\mathbf{f} = [f_1 \dots f_N]^T$ , where  $f_k$  is the  $k$ th figure of interest (e.g., center frequency, bandwidth, power split ratio, substrate permittivity, etc.) or material parameter (e.g., permittivity of the substrate the antenna is to be implemented on). The space  $F$  is delimited by the lower and upper bounds  $f_{k,\min}$  and  $f_{k,\max}$ ,  $k = 1, \dots, N$ , that determine the intended region of validity of the surrogate model.

The second fundamental concept of performance-driven modeling is design optimality. Given the objective function  $U(\mathbf{x}, \mathbf{f})$  that quantifies the quality of the design  $\mathbf{x}$  for a selected objective vector  $\mathbf{f}$ , the optimum design  $\mathbf{x}^*$  is understood as

$$\mathbf{x}^* = U_F(\mathbf{f}) = \arg \min_{\mathbf{x}} U(\mathbf{x}, \mathbf{f}) \quad (24)$$

As an elementary example, consider a patch antenna to be matched at the center frequency  $f_0$ , and implemented on the dielectric substrate of relative permittivity  $\epsilon_r$ . The surrogate model of the antenna input characteristic is to be constructed within the range of center frequencies  $f_{0,\min} \leq f_0 \leq f_{0,\max}$ , and the range of permittivity  $\epsilon_{r,\min} \leq \epsilon_r \leq \epsilon_{r,\max}$ . Then, the objective space  $F$  is the interval  $[f_{0,\min} f_{0,\max}] \times [\epsilon_{r,\min} \epsilon_{r,\max}]$ , and the objective function may be defined as  $U(\mathbf{x}, \mathbf{f}) = \max\{|S_{11,\epsilon_r}(\mathbf{x}, f_0)|\}$ , where  $S_{11,\epsilon_r}(\mathbf{x}, f)$  is the antenna reflection coefficient at the design  $\mathbf{x}$  and frequency  $f$ , simulated for the structure implemented on the substrate with permittivity  $\epsilon_r$ .

The set of all designs optimal in the sense of (24) for all objective vectors  $\mathbf{f} \in F$  will be denoted as

$$U_F(F) = \{U_F(\mathbf{f}) : \mathbf{f} \in F\} \quad (25)$$

It can be observed that restricting the surrogate model domain to  $U_F(F)$  and its vicinity is sufficient to capture all designs that are of interest in a particular design context (i.e., from the point of view of the objective  $f_k$ ) [79]. Thus, the immediate task is to approximate  $U_F(F)$  as a subset of the parameter space  $X$ . In the nested kriging framework [79] this is realized using a set of reference designs  $\mathbf{x}^{(j)} = [x_1^{(j)} \dots x_n^{(j)}]^T$ ,  $j = 1, \dots, p$ , pre-optimized w.r.t. the vectors  $\mathbf{f}^{(j)} = [f_1^{(j)} \dots f_N^{(j)}]^T$ , which are distributed (in a possibly uniform manner) in  $F$ . In practice, the reference designs have to be acquired beforehand, but in some cases, they may be available from the previous design work with the same antenna structure.

The definition of the constrained domain of the surrogate model is a two-step process. In the first step, the first-level kriging interpolation model  $s_I(\mathbf{f}) : F \rightarrow X$  is obtained using the training data set  $\{\mathbf{f}^{(j)}, \mathbf{x}^{(j)}\}$ ,  $j = 1, \dots, p$ . Note that  $s_I$  is an inverse model with  $s_I(F)$  approximating  $U_F(F)$ . Furthermore, we have  $s_I(\mathbf{f}^{(j)}) = \mathbf{x}^{(j)}$  for  $j = 1, \dots, p$ , but the two sets do not coincide outside the reference set. This makes it necessary to fatten  $s_I(F)$  so that the entire  $U_F(F)$  can be accommodated therein. In [76],

this is realized by extending  $s_I(F)$  using the orthonormal basis  $\{\mathbf{v}_n^{(k)}(\mathbf{f})\}$ ,  $k = 1, \dots, n-N$ , of vectors normal to  $s_I(F)$  at  $\mathbf{f}$ . To this end, the extension coefficients are defined as

$$\alpha(\mathbf{f}) = [\alpha_1(\mathbf{f}) \dots \alpha_{n-N}(\mathbf{f})]^T = 0.5T \left[ |\mathbf{x}_d \mathbf{v}_n^{(1)}(\mathbf{f})| \dots |\mathbf{x}_d \mathbf{v}_n^{(n-N)}(\mathbf{f})| \right]^T \quad (26)$$

where  $\mathbf{x}_d = \mathbf{x}_{\max} - \mathbf{x}_{\min}$ , with  $\mathbf{x}_{\max} = \max\{\mathbf{x}^{(k)}, k = 1, \dots, p\}$ ,  $\mathbf{x}_{\min} = \min\{\mathbf{x}^{(k)}, k = 1, \dots, p\}$ . Here,  $T$  is a thickness parameter. The vertical bounds of the surrogate model domain  $X_S$  are the manifolds  $M_+$  and  $M_-$

$$M_{\pm} = \left\{ \mathbf{x} \in X : \mathbf{x} = s_I(\mathbf{f}) \pm \sum_{k=1}^{n-N} \alpha_k(\mathbf{f}) \mathbf{v}_n^{(k)}(\mathbf{f}) \right\} \quad (27)$$

The domain itself is then defined as [76]

$$X_S = \left\{ \mathbf{x} = s_I(\mathbf{f}) + \sum_{k=1}^{n-N} \lambda_k \alpha_k(\mathbf{f}) \mathbf{v}_n^{(k)}(\mathbf{f}) : \mathbf{f} \in F, -1 \leq \lambda_k \leq 1, k = 1, \dots, n-N \right\} \quad (28)$$

Figure 4 provides a graphical illustration of the concepts involved in the domain definition. The second-level (ultimate) surrogate is rendered in  $X_S$  using the training data  $\{\mathbf{x}_B^{(k)}, \mathbf{R}(\mathbf{x}_B^{(k)})\}$ ,  $k = 1, \dots, N_B$ . The data samples  $\mathbf{x}_B^{(k)}$  are uniformly allocated in  $X_S$  [79].

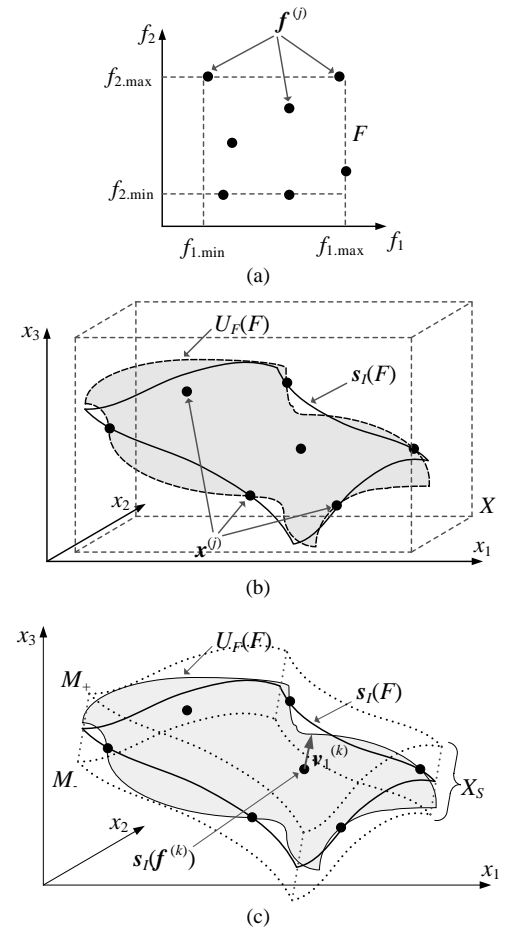


Fig. 4. Performance-driven (constrained) modeling: (a) graphical illustration of the objective space (here shown for two performance figures); (b) parameter space  $X$ , reference designs, and the optimum design set  $U_F(F)$  along with the image  $s_I(F)$  of the first-level surrogate; note that  $U_F(F)$  and  $s_I(F)$  only coincide at the reference designs, therefore, extension is necessary; (c) definition of the domain  $X_S$  through orthogonal extension of  $s_I(F)$ : for illustration the normal vector  $\mathbf{v}_1^{(k)}$  is shown at  $\mathbf{f}^{(k)}$  along with the manifolds  $M_-$  and  $M_+$  and the domain  $X_S$ .

As expected, domain confinement has a profound effect on the model predictive power. In particular, it opens the door to constructing accurate metamodels over broad ranges of antenna geometry parameters and operating conditions using reasonably small numbers of training samples [79]. This feature is explored in the modeling methodology proposed in this work.

### E. Modeling Framework

Figure 5 summarizes the operational flow of the modeling methodology proposed in this work. The objective space is set up by the user according to the intended range of validity of the surrogate. The reference designs are assumed to be acquired beforehand. The first step of the procedure is to define the model domain, which is followed by design of experiments (cf. [79] for details), and the acquisition of the EM simulation data. The PDRN surrogate is then established by first determining its specific architecture, then the model itself (hyper-parameters, etc.).

## III. VERIFICATION CASE STUDIES AND BENCHMARKING

This section provides a comprehensive numerical validation of the modelling methodology proposed in this work. On the one hand, we investigate the advantages of modelling antenna characteristics using PDRN rather than standard regression techniques. On the other hand, we demonstrate the benefits of combining PDRN with the domain confinement paradigm. The surrogates are constructed using the data sets of various sizes, from 50 to 800 samples. Furthermore, constrained PDRN is compared to several benchmark methods, including kriging, support vector regression, and ensemble learning. The experiments are based on modelling of reflection and gain characteristics of three microstrip antennas with the figures of interest including operating frequencies as well as substrate permittivity.

### A. Test Cases

The geometries of the verification antenna structures, referred to as Antenna I, II, and III, are shown in Fig. 6. Antenna I is a uniplanar dual-band dipole [113]. Antenna II is a ring-slot structure [114], whereas Antenna III is a quasi-Yagi structure with a parabolic reflector [115]. Table 3 provides the details concerning the antenna substrates and geometry parameters as well as the computational models. It should be noted that for Antennas II and III, the relative permittivity of the substrate is to be considered as one of the operating conditions (i.e., a component of the objective space), so that the surrogate model to be constructed is valid for a range of permittivity values.

### B. Experimental Setup. Benchmark Methods

Table IV gathers the information concerning the parameter and objective spaces, as well as the reference designs. In all cases, the objective spaces are two-dimensional. For Antenna I, the operating conditions are the operating frequencies of the lower and upper operating band. In the case of Antennas II and III, the first component of the objective space is the operating frequency, whereas the second is the relative permittivity of the dielectric substrate the antenna is to be implemented on. The objective spaces in Table IV determine the intended region of validity of the surrogate to be constructed. The allocation of the reference designs can be found in the second-but-last row of the table; the average number of designs is ten. The parameter spaces are determined as the smallest intervals containing the reference points. It can be observed that the parameter ranges are wide, which, along with broad ranges of the operating conditions, make the modeling tasks extremely challenging. The details concerning design optimality are provided in the last row of Table IV.

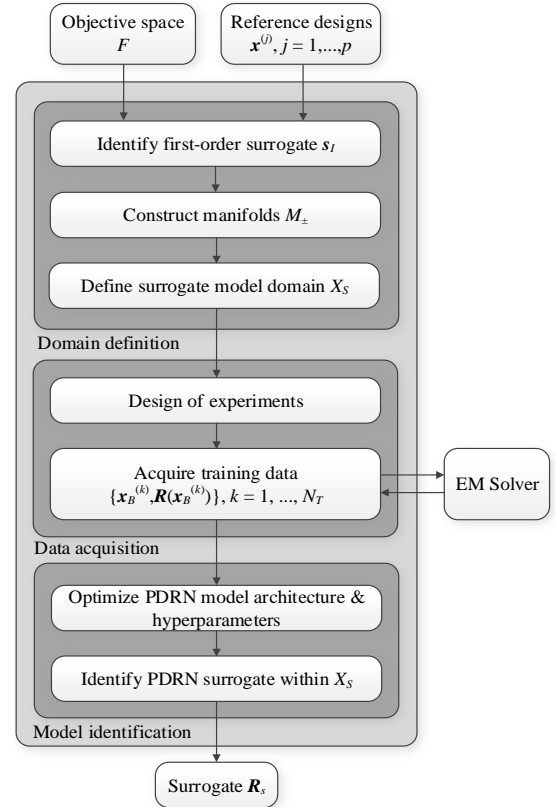


Fig. 5. Flowchart of the proposed modeling framework involving PDRN with automated architecture determination and domain confinement.

TABLE III  
VERIFICATION CASE STUDIES: ANTENNA PARAMETERS AND COMPUTATIONAL MODELS

	Antenna		
	I	II	III
Substrate	RO4350 ( $\epsilon_r = 3.5$ , $h = 0.76$ mm)	$h = 0.76$ mm $\epsilon_r$ – one of objective space components	$h = 1.5$ mm $\epsilon_r$ – one of objective space components
Independent parameters	$\mathbf{x} = [l_1 \ l_2 \ l_3 \ w_1 \ w_2 \ w_3]^T$	$\mathbf{x} = [l_f \ l_d \ w_d \ r \ s \ s_d \ o \ g]^T$	$\mathbf{x} = [W \ L \ L_m \ L_p \ S_d \ S_r \ W_2 \ W_d \ g]^T$
Other parameters	$l_0 = 30$ , $w_0 = 3$ , $s_0 = 0.15$ , and $o = 5$	$w_f$ computed for given $\epsilon_r$ to ensure 50-ohm line impedance	$W_1$ computed for given $\epsilon_r$ to ensure 50-ohm line impedance
Computational model	CST (~100,000 cells, simulation time, ~60 seconds)	CST (~300,000 cells, simulation time, ~90 seconds)	CST (~1,100,000 cells, simulation time, ~3 minutes)



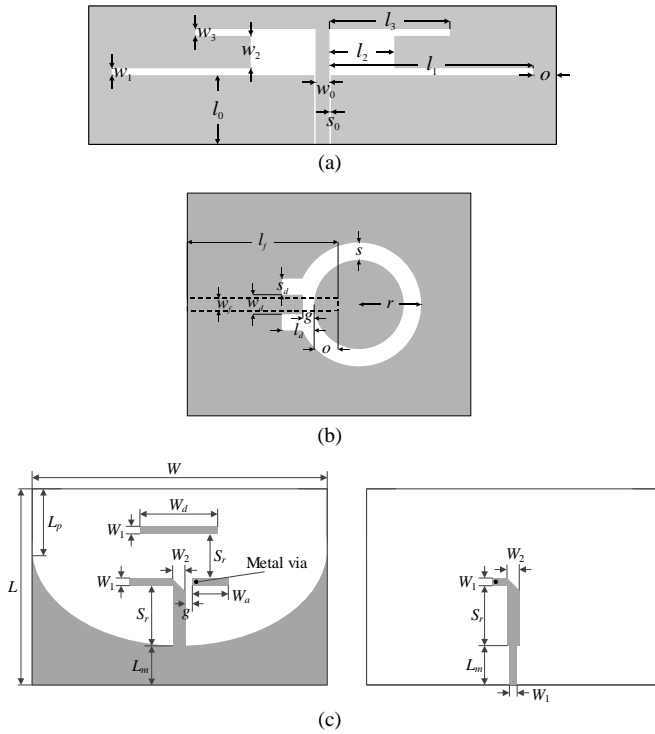


Fig. 6. Geometries of the verification antenna structures: (a) Antenna I [114], (b) Antenna II [114], and (c) Antenna III (front and back on the left- and right-hand side of the picture) [115].

For all test antennas, the surrogate models are constructed both in the original parameter space  $X$ , and in the confined domain defined as described in Section II.C, using the thickness parameters  $T = 0.05$  in all cases. The models are rendered using five different data sets containing 50, 100, 200, 400, and 800 samples. This is to investigate the scalability of the models, i.e., the relationship between the dataset cardinality and the model predictive power.

The modeling error is estimated using a split-sample method based on a separate set of 100 testing samples. The error measure is the relative RMS error defined as  $\|\mathbf{R}(\mathbf{x}) - \mathbf{R}_s(\mathbf{x})\|/\|\mathbf{R}(\mathbf{x})\|$ , where  $\mathbf{R}$  and  $\mathbf{R}_s$  stand for the EM simulated and surrogate-evaluated antenna characteristics (complex in the case of reflection response, and dB-valued for realized gain).

The following four techniques are considered:

- The modeling approach proposed in this work, pyramidal deep regression network (PDRN) of Section 2.2;
- Kriging interpolation [55];
- Convolutional neural network (CNN) [43];
- Ensemble learning [75];

The last three methods are the benchmark approaches. The kriging surrogate used second-order polynomial (as a trend function) and Gaussian correlation function [55]. CNN algorithm had been used as a counterpart method [82–84], CNN had been used as a state of the art regression method for prediction of reflection phase characteristics of a reflect-array FSS in [116], same hyper parameters (Depth size of 3 and first filter amount of 64) in [116] are also used here for generating a counterpart model for proposed PDRN. Finally, the ensemble learning method had been used as a final counterpart model. The ensemble aggregation method had been taken as LSBoost, which is one of the regression ensembles that aims at minimizing the mean-squared error [117], Learning rate of the model is obtained via the use of Bayesian Optimization [77] using the data set belong to Antenna I in parameter space  $X$  with 50 samples which is found as 0.24.

### C. Results and Discussion

The numerical results have been gathered in Tables V through VIII. Figures 5, 6, and 7 show the responses of the proposed surrogate model and the EM-simulation data for selected test designs.

TABLE IV  
VERIFICATION CASE STUDIES: PARAMETER AND OBJECTIVE SPACES, REFERENCE DESIGNS

	Antenna		
	I	II	III
Parameter space $X$ (lower and upper bounds $\mathbf{l}$ and $\mathbf{u}$ )	$\mathbf{l} = [29 \ 5.0 \ 17 \ 0.2 \ 1.5 \ 0.5]^T$ $\mathbf{u} = [42 \ 12 \ 25 \ 0.6 \ 5.2 \ 3.5]^T$	$\mathbf{l} = [22.0 \ 3.5 \ 0.3 \ 6.5 \ 3.0 \ 0.5 \ 3.5 \ 0.2]^T$ $\mathbf{u} = [27.0 \ 8.0 \ 2.3 \ 16.0 \ 7.0 \ 5.5 \ 6.0 \ 2.3]^T$	$\mathbf{l} = [100 \ 55 \ 10 \ 14.5 \ 6.0 \ 10 \ 2.0 \ 7.5 \ 16.3 \ 0.5]^T$ $\mathbf{u} = [137 \ 81 \ 29 \ 28 \ 21 \ 18 \ 5.0 \ 20 \ 40 \ 1.0]^T$
Objective space $F$	Lower and upper operating frequencies: $2.0 \text{ GHz} \leq f_1 \leq 3.0 \text{ GHz};$ $4.0 \text{ GHz} \leq f_2 \leq 5.5 \text{ GHz}$ $\Rightarrow \mathbf{f} = [f_1 \ f_2]^T$	Operating frequency: $2.5 \text{ GHz} \leq f_0 \leq 6.5 \text{ GHz};$ Substrate permittivity $2.0 \leq \epsilon_r \leq 5.0$ $\Rightarrow \mathbf{f} = [f_0 \ \epsilon_r]^T$	Operating frequency: $2.5 \text{ GHz} \leq f_0 \leq 5.0 \text{ GHz};$ Substrate permittivity $2.5 \leq \epsilon_r \leq 4.5$ $\Rightarrow \mathbf{f} = [f_0 \ \epsilon_r]^T$
Reference designs <sup>§</sup>	$\{f_1, f_2\} = \{2.0, 4.0\}, \{2.2, 5.0\}, \{2.0, 5.5\}, \{2.3, 4.5\}, \{2.4, 5.5\}, \{2.6, 4.0\}, \{2.7, 3.5\}, \{2.8, 4.7\}, \{3.0, 4.0\}, \text{ and } \{3.0, 3.5\}.$	$\{f, \epsilon_r\} = \{2.5, 2.0\}, \{2.5, 3.5\}, \{2.5, 5.0\}, \{4.0, 3.5\}, \{4.5, 2.0\}, \{4.5, 5.0\}, \{5.0, 3.5\}, \{6.5, 2.0\}, \{6.5, 3.5\}, \{6.5, 5.0\}.$	$\{f_0, \epsilon_r\} = \{2.5, 4.5\}, \{3.5, 4.5\}, \{5.0, 4.5\}, \{2.5, 2.5\}, \{5.0, 2.5\}, \{3.5, 2.5\}, \{4.5, 3.5\}, \text{ and } \{3.0, 3.5\}$
Design optimality <sup>#</sup>	$U(\mathbf{x}, \mathbf{f}) = \max\{ S_{11}(\mathbf{x}, f_1) ,  S_{11}(\mathbf{x}, f_2) \}$	$U(\mathbf{x}, \mathbf{f}) = \max\{ S_{11}(\mathbf{x}, f_0) \}$	$U(\mathbf{x}, \mathbf{f}) = U(\mathbf{x}, [f_0 \ \epsilon_r]^T) =$ $-(f_0 B)^{-1} \int_{f_0(1-B/2)}^{f_0(1+B/2)} G(\mathbf{x}, f) df + \beta c(\mathbf{x})$ Here, $G(\mathbf{x}, f)$ is the realized gain at frequency $f$ ; $\beta c(\mathbf{x})$ is a penalty term

<sup>§</sup>The allocation of the reference designs in terms of the pairs of the objective vector components.

<sup>#</sup>Formulation of the objective function defining the design optimality. Antenna I and II are to be optimized in a minimax sense. Antenna III is to be designed for maximum (average) in-band gain while ensuring  $-10$  dB in-band matching. The bandwidth  $B$  is 0.08 (eight percent);  $\beta$  is a penalty coefficient and  $c$  is a penalty function that quantifies violation of the constraint  $|S_{11}| \leq -10$  dB (e.g.,  $c(\mathbf{x}) = \max\{\max\{f_0(1 - B/2) \leq f \leq f_0(1 + B/2) : |S_{11}(\mathbf{x}, f)| + 10\}, 0\}^2$ ).

TABLE V  
MODELING RESULTS AND BENCHMARKING FOR ANTENNA I

Number of training samples	Relative RMS error							
	Modeling in parameter space $X$				Modeling in confined domain $X_S$			
	Kriging	CNN	Ensemble learning	Proposed PDRN	Kriging	CNN	Ensemble learning	Proposed PDRN
50	21.7 %	29.2 %	31.1 %	10.4 %	6.9 %	8.6 %	14.5 %	3.0 %
100	17.3 %	16.1 %	29.1 %	7.0 %	4.5 %	6.0 %	13.1 %	2.4 %
200	12.6 %	10.2 %	27.5 %	4.1 %	2.8 %	4.5 %	11.6 %	1.9 %
400	9.3 %	7.0 %	25.7 %	3.3 %	2.6 %	3.9 %	11.0 %	1.6 %
800	7.2 %	6.1 %	25.0 %	2.7 %	2.4 %	3.7 %	10.7 %	1.6 %

TABLE VI  
MODELING RESULTS AND BENCHMARKING FOR ANTENNA II

Number of training samples	Relative RMS error							
	Modeling in parameter space $X$				Modeling in confined domain $X_S$			
	Kriging	CNN	Ensemble learning	Proposed PDRN	Kriging	CNN	Ensemble learning	Proposed PDRN
50	56.9 %	67.7 %	73.8 %	36.2 %	12.9 %	13.1 %	28.9 %	4.1 %
100	50.8 %	58.8 %	69.1 %	23.3 %	6.9 %	8.2 %	25.4 %	2.6 %
200	35.8 %	34.0 %	63.9 %	12.8 %	4.9 %	6.4 %	23.1 %	2.3 %
400	31.5 %	22.3 %	58.1 %	7.5 %	3.1 %	4.8 %	19.9 %	1.9 %
800	25.6 %	13.5 %	55.8 %	5.3 %	2.2 %	5.3 %	19.1 %	1.5 %

TABLE VII  
MODELING RESULTS AND BENCHMARKING FOR ANTENNA III

Number of training samples	Relative RMS error							
	Modeling in parameter space $X$				Modeling in confined domain $X_S$			
	Kriging	CNN	Ensemble learning	Proposed PDRN	Kriging	CNN	Ensemble learning	Proposed PDRN
50	61.4 %	70.1 %	56.4 %	30.7 %	17.9 %	31.3 %	34.1 %	9.7 %
100	50.7 %	56.4 %	54.5 %	19.6 %	13.3 %	21.5 %	27.1 %	7.7 %
200	39.8 %	46.6 %	46.1 %	13.8 %	7.5 %	15.7 %	24.5 %	5.3 %
400	32.8 %	38.0 %	44.4 %	10.7 %	5.4 %	11.9 %	22.7 %	3.9 %
800	31.8 %	29.8 %	40.4 %	8.8 %	4.5 %	9.3 %	19.9 %	3.2 %

TABLE VIII  
OPTIMALLY SELECTED PDRN MODEL ARCHITECTURES

Case Study		Antenna I				Antenna II				Antenna III ( $ S_{11} $ )				Antenna III (Gain)			
Number of training samples	Domain	$\phi_K$	$d_s$	$s_p$	$\alpha$	$\phi_K$	$d_s$	$s_p$	$\alpha$	$\phi_K$	$d_s$	$s_p$	$\alpha$	$\phi_K$	$d_s$	$s_p$	$\alpha$
50	original $X$	48	5	2.5	0.13	48	6	1.75	0.03	96	6	1.5	0.06	80	5	1.25	0.18
	confined $X_S$	64	6	2	0.06	64	5	2.5	0.03	80	6	1.75	0.01	48	5	2	0.05
100	original $X$	32	6	2.5	0.02	32	6	2.5	0.04	80	6	1.5	0.06	80	5	1.5	0.09
	confined $X_S$	64	6	1.5	0.17	64	6	2	0.02	96	6	1.25	0.18	96	6	2	0.01
200	original $X$	64	5	2.25	0.02	32	6	1.5	0.01	80	6	1.75	0.03	96	6	2	0.03
	confined $X_S$	64	5	2.5	0.01	48	6	1.25	0.01	64	5	2	0.02	80	6	1.5	0.02
400	original $X$	64	5	2.5	0.01	64	6	2	0.02	32	6	2	0.02	96	4	2	0.05
	confined $X_S$	48	6	1.75	0.03	48	5	2	0.01	96	5	1.25	0.06	80	6	2	0.001
800	original $X$	48	6	2.5	0.01	48	5	1.75	0.01	64	4	2	0.08	32	6	1.5	0.05
	confined $X_S$	48	6	1.25	0.01	64	6	1.5	0.01	96	4	2	0.01	48	6	1.75	0.01

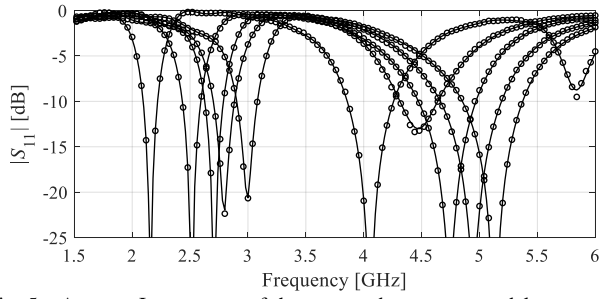


Fig. 5. Antenna I: responses of the proposed surrogate model constructed in the confined domain using 400 training samples (o) versus EM-simulation data (—). The curves represent antenna input characteristics as the selected test designs.

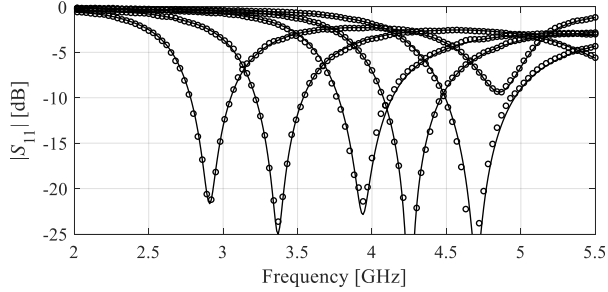


Fig. 6. Antenna II: responses of the proposed surrogate model constructed in the confined domain using 400 training samples (o) versus EM-simulation data (—). The curves represent antenna input characteristics as the selected test designs.

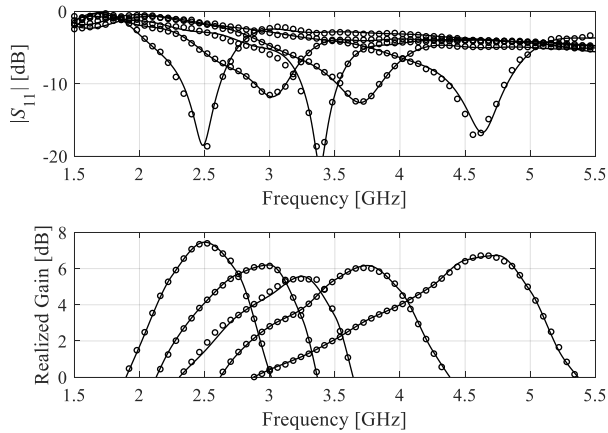


Fig. 7. Antenna III: responses of the proposed surrogate model constructed in the confined domain using 400 training samples (o) versus EM-simulation data (—). The curves represent antenna input characteristics (top) and realized gain (bottom) as the selected test designs.

The hyper-parameters of the proposed PDRN surrogate have been optimized on Intel Core i7-7600K CPU @ 4 GHz with 16 GB RAM and GTX1080TI GPU. The computing times of model training were as follows:

- Antenna I: 3, 7, 18, 39, and 91 minutes for 50, 100, 200, 400, and 800 samples, respectively (space  $X$ ); 3, 7, 19, 43, and 96 minutes for 50, 100, 200, 400, and 800 samples, respectively (confined domain  $X_S$ );
- Antenna II: 5, 11, 25, 55, and 127 minutes for 50, 100, 200, 400, and 800 samples, respectively (space  $X$ ); 6, 13, 26, 59, and 134 minutes for 50, 100, 200, 400, and 800 samples, respectively (confined domain  $X_S$ );
- Antenna III: 5, 13, 31, 69, and 157 minutes for 50, 100,

200, 400, and 800 samples, respectively (space  $X$ ); 9, 14, 34, 74, and 162 minutes for 50, 100, 200, 400, and 800 samples, respectively (confined domain  $X_S$ ).

It can be observed that the computational complexity of the model training process grows slightly faster than linearly with respect to the training data set size.

The data provided in the Tables V through VIII allows for drawing conclusions concerning the performance of the proposed modeling approach in both the original and confined spaces. These are summarized below:

- The proposed PDRN model exhibits a considerably better predictive power than the benchmark techniques, both in the original parameter space  $X$  and in the confined domain  $X_S$ .
- The differences in the modeling error are significant in favor of PDRN, and they are more pronounced for smaller training sets (50 to 200 samples), which indicates that the proposed technique is capable of exploiting the allocation of the available data through the automated architecture and hyper-parameter determination;
- The above observation is confirmed in Table VIII, which indicates that the specific model architecture achieved during the training phase depends on both the considered antenna structure and the training data set size;
- PDRN model capitalizes on domain confinement, which allows for further improvements of the predictive power of the surrogate, especially for smaller data sets;
- In particular, constrained PDRN outperforms the nested kriging framework and the accuracy improvement is by a factor two to three for the data sets of 50 samples, and by about 1.5 for the largest sets. These differences are significant given that all considered test cases are very challenging both in terms of the parameter space dimensionality and—even more importantly—the parameter and operating condition ranges;
- The obtained results are consistent throughout the entire set of antenna structures utilized for verification, which demonstrates that the proposed technique can be successfully used for handling a variety of antenna modeling tasks without any additional tuning of its control parameters.

Overall, to the authors' knowledge, the performance of the proposed constrained PDRN surrogate is perhaps the best ever reported in the antenna modeling literature thus far. It should also be mentioned that experimental validation of the presented antennas is not included in this work as being irrelevant to the paper topic. Notwithstanding, it can be found in other works employing these antenna structures for benchmark purposes (e.g., [79], [81]).

#### IV. CONCLUSION

This paper proposed a novel framework for accurate and reduced-cost modelling of antenna structures. Our methodology combines enhanced pyramidal deep regression network (PDRN) surrogates with automated architecture and hyper-parameter determination, and the concept of performance-driven modelling. The former offers improved flexibility in terms of representing highly-nonlinear antenna characteristics, whereas the latter enables significant

computational savings in terms of training data acquisition. The presented approach has been demonstrated using three microstrip antennas with their replacement models constructed over broad ranges of geometry and material parameters as well as operating frequencies. All considered test cases are challenging also due to the dimensionality of the parameter spaces as well as the parameter ranges. Comprehensive benchmarking indicates superiority of the domain-confined PDRN technique over both conventional regression models (kriging, CNN) but also the ensemble learning model. In particular, the predictive power of the confined surrogates has been improved by a factor of two over the nested kriging method without increasing cardinality of the training data set. The proposed framework can be suitable for rendering reliable surrogates under challenging scenarios, such modelling of multi-band antennas over wide ranges of centre frequencies, or modelling of multiple frequency characteristics of antennas implemented on various substrates of different height and permittivity.

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