# 计算几何

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# 1.几何公式

#### 1.1 三角形

- 1. 半周长 P=(a+b+c)/2
- 2. 面积 S=aHa/2=absin(C)/2=sqrt(P(P-a)(P-b)(P-c))
- 3. 中线 Ma=sqrt(2(b^2+c^2)-a^2)/2=sqrt(b^2+c^2+2bccos(A))/2
- 4. 角平分线 Ta=sqrt(bc((b+c)^2-a^2))/(b+c)=2bccos(A/2)/(b+c)
- 5. 高线 Ha=bsin(C)=csin(B)=sqrt(b^2-((a^2+b^2-c^2)/(2a))^2)
- 6. 内切圆半径 r=S/P=asin(B/2)sin(C/2)/sin((B+C)/2) =4Rsin(A/2)sin(B/2)sin(C/2)=sqrt((P-a)(P-b)(P-c)/P) =Ptan(A/2)tan(B/2)tan(C/2)
- 7. 外接圆半径 R=abc/(4S)=a/(2sin(A))=b/(2sin(B))=c/(2sin(C))

#### 1.2 四边形

D1,D2 为对角线,M对角线中点连线,A 为对角线夹角

- 1. a^2+b^2+c^2+d^2=D1^2+D2^2+4M^2
- 2. S=D1D2sin(A)/2

(以下对圆的内接四边形)

- ac+bd=D1D2
- 4. S=sqrt((P-a)(P-b)(P-c)(P-d)),P 为半周长

# 1.3 正 n 边形

R 为外接圆半径, r 为内切圆半径

- 1. 中心角 A=2PI/n
- 2. 内角 C=(n-2)PI/n
- 3. 边长 a=2sqrt(R^2-r^2)=2Rsin(A/2)=2rtan(A/2)
- 4. 面积 S=nar/2=nr^2tan(A/2)=nR^2sin(A)/2=na^2/(4tan(A/2))

#### 1.4 圆

- 1. 弧长 1=rA
- 2. 弦长 a=2sqrt(2hr-h^2)=2rsin(A/2)
- 3. 弓形高 h=r-sqrt(r^2-a^2/4)=r(1-cos(A/2))=atan(A/4)/2
- 4. 扇形面积 S1=r1/2=r^2A/2
- 5. 弓形面积 S2=(rl-a(r-h))/2=r^2(A-sin(A))/2

## 1.5 棱柱

- 1. 体积 V=Ah,A 为底面积,h 为高
- 2. 侧面积 S=1p,1 为棱长,p 为直截面周长
- 3. 全面积 T=S+2A

## 1.6 棱锥

- 1. 体积 V=Ah/3,A 为底面积,h 为高 (以下对正棱锥)
- 2. 侧面积 S=1p/2,1 为斜高,p 为底面周长
- 3. 全面积 T=S+A

## 1.7 棱台

- 1. 体积 V=(A1+A2+sqrt(A1A2))h/3,A1.A2 为上下底面积,h 为高(以下为正棱台)
- 2. 侧面积 S=(p1+p2)1/2,p1.p2 为上下底面周长,1 为斜高
- 3. 全面积 T=S+A1+A2

#### 1.8 圆柱

- 1. 侧面积 S=2PIrh
- 2. 全面积 T=2PIr(h+r)
- 3. 体积 V=PIr^2h

#### 1.9 圆锥

- 1. 母线 l=sqrt(h^2+r^2)
- 2. 侧面积 S=PIrl
- 3. 全面积 T=PIr(l+r)
- 4. 体积 V=PIr^2h/3

#### 1.10 圆台

- 1. 母线 l=sqrt(h^2+(r1-r2)^2)
- 2. 侧面积 S=PI(r1+r2)1
- 3. 全面积 T=PIr1(l+r1)+PIr2(l+r2)
- 4. 体积 V=PI(r1^2+r2^2+r1r2)h/3

# 1.11 球

- 1. 全面积 T=4PIr^2
- 2. 体积 V=4PIr^3/3

# 1.12 球台

- 1. 侧面积 S=2PIrh
- 2. 全面积 T=PI(2rh+r1^2+r2^2)
- 3. 体积 V=PIh(3(r1^2+r2^2)+h^2)/6

# 1.13 球扇形

1. 全面积 T=PIr(2h+r0),h 为球冠高,r0 为球冠底面半径

# 2.直线与线段

# 2.0 预备函数

```
//结构定义与宏定义
#include<stdio.h>
#include<string.h>
#include<stdlib.h>
#include <math.h>
#define eps 1e-8
#define zero(x) (((x)>0?(x):-(x))<eps)
struct point
{
   double x,y;
};
struct line
   point a,b;
};
//计算 cross product (P1-P0)x(P2-P0)
double xmult(point p1,point p2,point p0)
{
   return (p1.x-p0.x)*(p2.y-p0.y)-(p2.x-p0.x)*(p1.y-p0.y);
double xmult(double x1,double y1,double x2,double y2,double x0,double y0)
   return (x1-x0)*(y2-y0)-(x2-x0)*(y1-y0);
}
//计算 dot product (P1-P0).(P2-P0)
double dmult(point p1,point p2,point p0)
{
   return (p1.x-p0.x)*(p2.x-p0.x)+(p1.y-p0.y)*(p2.y-p0.y);
double dmult(double x1,double y1,double x2,double y2,double x0,double y0)
   return (x1-x0)*(x2-x0)+(y1-y0)*(y2-y0);
//两点距离
double distance(point p1,point p2)
{
   return sqrt((p1.x-p2.x)*(p1.x-p2.x)+(p1.y-p2.y)*(p1.y-p2.y));
double distance(double x1,double y1,double x2,double y2)
{
```

```
return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
}
```

## 2.1 判三点是否共线

```
int dots_inline(point p1,point p2,point p3)
{
    return zero(xmult(p1,p2,p3));
}
```

#### 2.2 判点是否在线段上

# 2.3 判断两点在线段的同一侧

```
//判两点在线段同侧,点在线段上返回 0
int same_side(point p1,point p2,line l)
{
    return xmult(l.a,p1,l.b)*xmult(l.a,p2,l.b)>eps;
}
int same_side(point p1,point p2,point l1,point l2)
{
    return xmult(l1,p1,l2)*xmult(l1,p2,l2)>eps;
}
```

#### 2.4 判断两点是否在线段的异侧

```
//判两点在线段异侧,点在线段上返回 0
int opposite_side(point p1,point p2,line 1)
{
    return xmult(l.a,p1,l.b)*xmult(l.a,p2,l.b)<-eps;</pre>
```

```
}
int opposite_side(point p1,point p2,point l1,point l2)
{
    return xmult(l1,p1,l2)*xmult(l1,p2,l2)<-eps;
}</pre>
```

#### 2.5 求点关于直线的对称点

```
// 点关于直线的对称点 // by lyt
// 缺点: 用了斜率
// 也可以利用"点到直线上的最近点"来做,避免使用斜率。
point symmetric_point(point p1, point l1, point l2)
{
   point ret;
   if (11.x > 12.x - eps && 11.x < 12.x + eps)
      ret.x = (2 * 11.x - p1.x);
      ret.y = p1.y;
   }
   else
   {
      double k = (11.y - 12.y) / (11.x - 12.x);
      ret.x = (2*k*k*11.x + 2*k*p1.y - 2*k*11.y - k*k*p1.x + p1.x) / (1 + k*k);
      ret.y = p1.y - (ret.x - p1.x) / k;
   return ret;
}
```

# 2.7 判断两线段是否相交

# 2.7.1 常用版

```
//定义点
struct Point
{
    double x;
    double y;
};
typedef struct Point point;

//叉积
double multi(point p0, point p1, point p2)
{
    return ( p1.x - p0.x )*( p2.y - p0.y )-( p2.x - p0.x )*( p1.y - p0.y );
}
```

#### 2.7.2 不常用版

```
//判两线段相交,包括端点和部分重合
int intersect in(line u,line v)
{
   if (!dots_inline(u.a,u.b,v.a)||!dots_inline(u.a,u.b,v.b))
       return !same side(u.a,u.b,v)&&!same side(v.a,v.b,u);
   return
dot_online_in(u.a,v)||dot_online_in(u.b,v)||dot_online_in(v.a,u)||dot_online_in(v.b,
u);
}
int intersect_in(point u1,point u2,point v1,point v2)
   if (!dots inline(u1,u2,v1)||!dots inline(u1,u2,v2))
       return !same_side(u1,u2,v1,v2)&&!same_side(v1,v2,u1,u2);
   return
dot online in(u1,v1,v2)||dot online in(u2,v1,v2)||dot online in(v1,u1,u2)||dot onlin
e_in(v2,u1,u2);
}
//判两线段相交,不包括端点和部分重合
int intersect_ex(line u,line v)
   return opposite_side(u.a,u.b,v)&&opposite_side(v.a,v.b,u);
int intersect_ex(point u1,point u2,point v1,point v2)
   return opposite_side(u1,u2,v1,v2)&&opposite_side(v1,v2,u1,u2);
}
```

# 2.8 求两条直线的交点

```
//计算两直线交点,注意事先判断直线是否平行!
//线段交点请另外判线段相交(同时还是要判断是否平行!)
point intersection(point u1,point u2,point v1,point v2)
{
```

## 2.9 点到直线的最近距离

```
point ptoline(point p,point l1,point l2)
{
    point t=p;
    t.x+=l1.y-l2.y,t.y+=l2.x-l1.x;
    return intersection(p,t,l1,l2);
}
```

## 2.10 点到线段的最近距离

```
point ptoseg(point p,point l1,point l2)
{
    point t=p;
    t.x+=l1.y-l2.y,t.y+=l2.x-l1.x;
    if (xmult(l1,t,p)*xmult(l2,t,p)>eps)
        return distance(p,l1)<distance(p,l2)?l1:l2;
    return intersection(p,t,l1,l2);
}</pre>
```

# 3.多边形

#### 3.0 预备浮点函数

```
#include <stdlib.h>
#include<stdio.h>
#include<string.h>
#include <math.h>
#define MAXN 1000

//offset 为多变形坐标的最大绝对值
#define offset 10000
#define eps 1e-8

//浮点数判 0
#define zero(x) (((x)>0?(x):-(x))<eps)

//浮点数判断符
#define _sign(x) ((x)>eps?1:((x)<-eps?2:0))
```

```
//定义点
struct point
{
    double x,y;
}pt[MAXN ];

//定义线段
struct line
{
    point a,b;
};

//叉积
double xmult(point p1,point p2,point p0)
{
    return (p1.x-p0.x)*(p2.y-p0.y)-(p2.x-p0.x)*(p1.y-p0.y);
}
```

#### 3.1 判定是否是凸多边形

```
//判定凸多边形,顶点按顺时针或逆时针给出,允许相邻边共线,是凸多边形返回 1, 否则返回 0
int is_convex(int n,point* p)
{
   int i,s[3]=\{1,1,1\};
   for (i=0;i<n\&s[1]|s[2];i++)
      s[_sign(xmult(p[(i+1)%n],p[(i+2)%n],p[i]))]=0;
   return s[1]|s[2];
}
//判凸行, 顶点按顺时针或逆时针给出,不允许相邻边共线,是凸多边形返回 1, 否则返回 0
int is_convex_v2(int n,point* p)
{
   int i,s[3]=\{1,1,1\};
   for (i=0;i<n\&s[0]\&\&s[1]|s[2];i++)
      s[_sign(xmult(p[(i+1)%n],p[(i+2)%n],p[i]))]=0;
   return s[0]&&s[1]|s[2];
}
```

# 3.2 判定点是否在多边形内

```
//判点在凸多边形内或多边形边上时返回 1, 严格在凸多边形外返回 0
int inside_convex(point q,int n,point* p)
{
    int i,s[3]={1,1,1};
    for (i=0;i<n&&s[1]|s[2];i++)
        s[_sign(xmult(p[(i+1)%n],q,p[i]))]=0;
    return s[1]|s[2];
}</pre>
```

```
//判点严格在凸多边形内返回 1,在边上或者严格在外返回 0
int inside convex v2(point q,int n,point* p)
{
   int i,s[3]=\{1,1,1\};
   for (i=0;i<n\&\&s[0]\&\&s[1]|s[2];i++)
       s[_sign(xmult(p[(i+1)%n],q,p[i]))]=0;
   return s[0]\&\&s[1]|s[2];
}
//判点在任意多边形内,顶点按顺时针或逆时针给出
//on_edge 表示点在多边形边上时的返回值, offset 为多边形坐标上限,严格在内返回 1, 严格在外返回
int inside_polygon(point q,int n,point* p,int on_edge=2)
   point q2;
   int i=0,count;
   while (i<n)
      for (count=i=0,q2.x=rand()+offset,q2.y=rand()+offset;i<n;i++)</pre>
       {
          if (zero(xmult(q,p[i],p[(i+1)%n]))&&(p[i].x-q.x)*(p[(i+1)%n].x-q.x)<eps
             &&(p[i].y-q.y)*(p[(i+1)%n].y-q.y)<eps)
              return on_edge;
          else if (zero(xmult(q,q2,p[i])))
             break;
          else if (xmult(q,p[i],q2)*xmult(q,p[(i+1)%n],q2)<-eps&&
              xmult(p[i],q,p[(i+1)%n])*xmult(p[i],q2,p[(i+1)%n])<-eps)
              count++;
       }
   return count&1;
}
```

#### 3.3 判定一条线段是否在一个任意多边形内

```
//预备函数
inline int opposite_side(point p1,point p2,point l1,point l2)
{
    return xmult(l1,p1,l2)*xmult(l1,p2,l2)<-eps;
}
inline int dot_online_in(point p,point l1,point l2)
{
    return
zero(xmult(p,l1,l2))&&(l1.x-p.x)*(l2.x-p.x)<eps&&(l1.y-p.y)*(l2.y-p.y)<eps;
}
//判线段在任意多边形内,顶点按顺时针或逆时针给出,与边界相交返回 1
int inside polygon(point l1,point l2,int n,point* p)
```

```
{
   point t[MAXN],tt;
   int i,j,k=0;
   if (!inside_polygon(l1,n,p)||!inside_polygon(l2,n,p))
       return 0;
   for (i=0;i<n;i++)
   {
(opposite\_side(11,12,p[i],p[(i+1)%n])\&&opposite\_side(p[i],p[(i+1)%n],11,12))
           return 0;
       else if (dot_online_in(l1,p[i],p[(i+1)%n]))
           t[k++]=11;
       else if (dot_online_in(l2,p[i],p[(i+1)%n]))
           t[k++]=12;
       else if (dot_online_in(p[i],l1,l2))
           t[k++]=p[i];
   }
   for (i=0;i<k;i++)</pre>
       for (j=i+1;j< k;j++)
       {
           tt.x=(t[i].x+t[j].x)/2;
           tt.y=(t[i].y+t[j].y)/2;
           if (!inside_polygon(tt,n,p))
               return 0;
       }
   return 1;
}
```

# 4.三角形

# 4.0 预备函数

```
#include <math.h>
#include <string.h>
#include <stdlib.h>
#include<stdio.h>
//定义点
struct point
{
    double x,y;
};
typedef struct point point;

//定义直线
struct line
{
    point a,b;
};
```

```
typedef struct line line;
//两点距离
double distance(point p1,point p2)
   return sqrt((p1.x-p2.x)*(p1.x-p2.x)+(p1.y-p2.y)*(p1.y-p2.y));
}
//两直线求交点
point intersection(line u,line v)
   point ret=u.a;
   double t=((u.a.x-v.a.x)*(v.a.y-v.b.y)-(u.a.y-v.a.y)*(v.a.x-v.b.x))
          /((u.a.x-u.b.x)*(v.a.y-v.b.y)-(u.a.y-u.b.y)*(v.a.x-v.b.x));
   ret.x+=(u.b.x-u.a.x)*t;
   ret.y+=(u.b.y-u.a.y)*t;
   return ret;
}
4.1 求三角形的外心
point circumcenter(point a,point b,point c)
{
   line u,v;
   u.a.x=(a.x+b.x)/2;
   u.a.y=(a.y+b.y)/2;
   u.b.x=u.a.x-a.y+b.y;
   u.b.y=u.a.y+a.x-b.x;
   v.a.x=(a.x+c.x)/2;
   v.a.y=(a.y+c.y)/2;
```

## 4.2 求三角形内心

}

v.b.x=v.a.x-a.y+c.y; v.b.y=v.a.y+a.x-c.x;

return intersection(u,v);

```
point incenter(point a,point b,point c)
{
    line u,v;
    double m,n;
    u.a=a;
    m=atan2(b.y-a.y,b.x-a.x);
    n=atan2(c.y-a.y,c.x-a.x);
    u.b.x=u.a.x+cos((m+n)/2);
    u.b.y=u.a.y+sin((m+n)/2);
    v.a=b;
    m=atan2(a.y-b.y,a.x-b.x);
    n=atan2(c.y-b.y,c.x-b.x);
    v.b.x=v.a.x+cos((m+n)/2);
    v.b.y=v.a.y+sin((m+n)/2);
```

```
return intersection(u,v);
}
```

# 4.3 求三角形垂心

```
point perpencenter(point a,point b,point c)
{
    line u,v;
    u.a=c;
    u.b.x=u.a.x-a.y+b.y;
    u.b.y=u.a.y+a.x-b.x;
    v.a=b;
    v.b.x=v.a.x-a.y+c.y;
    v.b.y=v.a.y+a.x-c.x;
    return intersection(u,v);
}
```

5. 圆

#### 5.0 预备函数

```
#include <math.h>
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#define eps 1e-8
struct point
   double x,y;
};
typedef struct point point;
double xmult(point p1,point p2,point p0)
   return (p1.x-p0.x)*(p2.y-p0.y)-(p2.x-p0.x)*(p1.y-p0.y);
}
double distance(point p1,point p2)
   return sqrt((p1.x-p2.x)*(p1.x-p2.x)+(p1.y-p2.y)*(p1.y-p2.y));
}
//点到直线的距离
double disptoline(point p,point 11,point 12)
{
   return fabs(xmult(p,11,12))/distance(11,12);
//求两直线交点
point intersection(point u1,point u2,point v1,point v2)
   point ret=u1;
```

## 5.1 判定直线是否与圆相交

```
//判直线和圆相交,包括相切
int intersect_line_circle(point c,double r,point l1,point l2)
{
    return disptoline(c,l1,l2)<r+eps;
}
```

## 5.2 判定线段与圆相交

```
int intersect_seg_circle(point c,double r, point l1,point l2)
{
    double t1=distance(c,l1)-r,t2=distance(c,l2)-r;
    point t=c;
    if (t1<eps||t2<eps)
        return t1>-eps||t2>-eps;
        t.x+=l1.y-l2.y;
        t.y+=l2.x-l1.x;
    return xmult(l1,c,t)*xmult(l2,c,t)<eps&&disptoline(c,l1,l2)-r<eps;
}</pre>
```

## 5.3 判圆和圆相交

```
int intersect_circle(point c1,double r1,point c2,double r2)
{
    return distance(c1,c2)<r1+r2+eps&&distance(c1,c2)>fabs(r1-r2)-eps;
}
```

# 5.4 计算圆上到点 p 最近点

```
//当p为圆心时,返回圆心本身
point dot_to_circle(point c,double r,point p)
{
    point u,v;
    if (distance(p,c)<eps)
        return p;
    u.x=c.x+r*fabs(c.x-p.x)/distance(c,p);
    u.y=c.y+r*fabs(c.y-p.y)/distance(c,p)*((c.x-p.x)*(c.y-p.y)<0?-1:1);
    v.x=c.x-r*fabs(c.x-p.x)/distance(c,p);
    v.y=c.y-r*fabs(c.y-p.y)/distance(c,p)*((c.x-p.x)*(c.y-p.y)<0?-1:1);</pre>
```

```
return distance(u,p)<distance(v,p)?u:v;
}</pre>
```

#### 5.5 计算直线与圆的交点

```
//计算直线与圆的交点,保证直线与圆有交点
//计算线段与圆的交点可用这个函数后判点是否在线段上
void intersection_line_circle(point c,double r,point l1,point l2,point& p1,point& p2)
{
    point p=c;
    double t;
    p.x+=l1.y-l2.y;
    p.y+=l2.x-l1.x;
    p=intersection(p,c,l1,l2);
    t=sqrt(r*r-distance(p,c)*distance(p,c))/distance(l1,l2);
    p1.x=p.x+(l2.x-l1.x)*t;
    p1.y=p.y+(l2.y-l1.y)*t;
    p2.x=p.x-(l2.x-l1.x)*t;
    p2.y=p.y-(l2.y-l1.y)*t;
}
```

# 5.6 计算两个圆的交点

```
//计算圆与圆的交点,保证圆与圆有交点,圆心不重合
void intersection_circle_circle(point c1,double r1,point c2,double r2,point& p1,point& p2)
{
    point u,v;
    double t;
    t=(1+(r1*r1-r2*r2)/distance(c1,c2)/distance(c1,c2))/2;
    u.x=c1.x+(c2.x-c1.x)*t;
    u.y=c1.y+(c2.y-c1.y)*t;
    v.x=u.x+c1.y-c2.y;
    v.y=u.y-c1.x+c2.x;
    intersection_line_circle(c1,r1,u,v,p1,p2);
}
```

# 6.球面

# 6.0 给出地球经度纬度, 计算圆心角

```
#include <math.h>
const double pi=acos(-1);

//计算圆心角 lat 表示纬度,-90<=w<=90,lng 表示经度

//返回两点所在大圆劣弧对应圆心角,0<=angle<=pi
double angle(double lng1,double lat1,double lng2,double lat2)
```

```
{
   double dlng=fabs(lng1-lng2)*pi/180;
   while (dlng>=pi+pi)
        dlng-=pi+pi;
   if (dlng>pi)
        dlng=pi+pi-dlng;
   lat1*=pi/180,lat2*=pi/180;
   return acos(cos(lat1)*cos(lat2)*cos(dlng)+sin(lat1)*sin(lat2));
}
```

## 6.1 已知经纬度,计算地球上两点直线距离

```
//计算距离,r 为球半径
double line_dist(double r,double lng1,double lat1,double lng2,double lat2)
{
    double dlng=fabs(lng1-lng2)*pi/180;
    while (dlng>=pi+pi)
        dlng-=pi+pi;
    if (dlng>pi)
        dlng=pi+pi-dlng;
    lat1*=pi/180,lat2*=pi/180;
    return r*sqrt(2-2*(cos(lat1)*cos(lat2)*cos(dlng)+sin(lat1)*sin(lat2)));
}
```

# 6.2 已知经纬度, 计算地球上两点球面距离

```
//计算球面距离,r 为球半径
inline double sphere_dist(double r,double lng1,double lat1,double lng2,double lat2)
{
    return r*angle(lng1,lat1,lng2,lat2);
}
```

# 7.三维几何的若干模板

## 7.0 预备函数

```
//三维几何函数库
#include <math.h>
#define eps 1e-8
#define zero(x) (((x)>0?(x):-(x))<eps)
struct point3{double x,y,z;};
struct line3{point3 a,b;};
struct plane3{point3 a,b,c;};
//计算 cross product U x V
point3 xmult(point3 u,point3 v){
    point3 ret;</pre>
```

```
ret.x=u.y*v.z-v.y*u.z;
   ret.y=u.z*v.x-u.x*v.z;
   ret.z=u.x*v.y-u.y*v.x;
   return ret;
}
//计算 dot product U . V
double dmult(point3 u,point3 v){
   return u.x*v.x+u.y*v.y+u.z*v.z;
}
//矢量差 U - V
point3 subt(point3 u,point3 v){
   point3 ret;
   ret.x=u.x-v.x;
   ret.y=u.y-v.y;
   ret.z=u.z-v.z;
   return ret;
}
//取平面法向量
point3 pvec(plane3 s){
   return xmult(subt(s.a,s.b),subt(s.b,s.c));
}
point3 pvec(point3 s1,point3 s2,point3 s3){
   return xmult(subt(s1,s2),subt(s2,s3));
}
//两点距离,单参数取向量大小
double distance(point3 p1,point3 p2){
   return
sqrt((p1.x-p2.x)*(p1.x-p2.x)+(p1.y-p2.y)*(p1.y-p2.y)+(p1.z-p2.z)*(p1.z-p2.z));
//向量大小
double vlen(point3 p){
   return sqrt(p.x*p.x+p.y*p.y+p.z*p.z);
}
7.1 判定三点是否共线
//判三点共线
int dots_inline(point3 p1,point3 p2,point3 p3){
   return vlen(xmult(subt(p1,p2),subt(p2,p3)))<eps;</pre>
```

}

# 7.2 判定四点是否共面

```
//判四点共面
int dots_onplane(point3 a,point3 b,point3 c,point3 d){
    return zero(dmult(pvec(a,b,c),subt(d,a)));
}
```

#### 7.1 判定点是否在线段上

```
//判点是否在线段上,包括端点和共线
int dot_online_in(point3 p,line3 1){
   return zero(vlen(xmult(subt(p,1.a),subt(p,1.b))))&&(1.a.x-p.x)*(1.b.x-p.x)<eps&&</pre>
       (1.a.y-p.y)*(1.b.y-p.y) < eps&&(1.a.z-p.z)*(1.b.z-p.z) < eps;
}
int dot_online_in(point3 p,point3 l1,point3 l2){
   return zero(vlen(xmult(subt(p,11),subt(p,12))))&(11.x-p.x)*(12.x-p.x)<eps&&
       (11.y-p.y)*(12.y-p.y) < eps&&(11.z-p.z)*(12.z-p.z) < eps;
}
//判点是否在线段上,不包括端点
int dot_online_ex(point3 p,line3 1){
   return
dot_online_in(p,1)&&(!zero(p.x-1.a.x)||!zero(p.y-1.a.y)||!zero(p.z-1.a.z))&&
       (!zero(p.x-1.b.x)||!zero(p.y-1.b.y)||!zero(p.z-1.b.z));
int dot_online_ex(point3 p,point3 l1,point3 l2){
   return
dot_online_in(p,11,12)&(!zero(p.x-11.x)||!zero(p.y-11.y)||!zero(p.z-11.z))&
       (!zero(p.x-12.x)||!zero(p.y-12.y)||!zero(p.z-12.z));
}
```

# 7.2 判断点是否在空间三角形上

```
//判点是否在空间三角形上,包括边界,三点共线无意义
int dot_inplane_in(point3 p,plane3 s){
    return
zero(vlen(xmult(subt(s.a,s.b),subt(s.a,s.c)))-vlen(xmult(subt(p,s.a),subt(p,s.b)))-
        vlen(xmult(subt(p,s.b),subt(p,s.c)))-vlen(xmult(subt(p,s.c),subt(p,s.a))));
}
int dot_inplane_in(point3 p,point3 s1,point3 s2,point3 s3){
    return
zero(vlen(xmult(subt(s1,s2),subt(s1,s3)))-vlen(xmult(subt(p,s1),subt(p,s2)))-
        vlen(xmult(subt(p,s2),subt(p,s3)))-vlen(xmult(subt(p,s3),subt(p,s1))));
}
//判点是否在空间三角形上,不包括边界,三点共线无意义
int dot_inplane_ex(point3 p,plane3 s){
    return dot_inplane_in(p,s)&&vlen(xmult(subt(p,s.a),subt(p,s.b)))>eps&&
```

```
vlen(xmult(subt(p,s.b),subt(p,s.c)))>eps&&vlen(xmult(subt(p,s.c),subt(p,s.a)))>e
ps;
}
int dot_inplane_ex(point3 p,point3 s1,point3 s2,point3 s3){
    return dot_inplane_in(p,s1,s2,s3)&&vlen(xmult(subt(p,s1),subt(p,s2)))>eps&&
    vlen(xmult(subt(p,s2),subt(p,s3)))>eps&&vlen(xmult(subt(p,s3),subt(p,s1)))>eps;
}
```

## 7.3 判断两点是否在线段同侧

```
//判两点在线段同侧,点在线段上返回 0,不共面无意义
int same_side(point3 p1,point3 p2,line3 l){
    return
dmult(xmult(subt(l.a,l.b),subt(p1,l.b)),xmult(subt(l.a,l.b),subt(p2,l.b)))>eps;
}
int same_side(point3 p1,point3 p2,point3 l1,point3 l2){
    return dmult(xmult(subt(l1,l2),subt(p1,l2)),xmult(subt(l1,l2),subt(p2,l2)))>eps;
}
```

## 7.4 判断两点是否在线段异侧

```
//判两点在线段异侧,点在线段上返回 0,不共面无意义
int opposite_side(point3 p1,point3 p2,line3 l){
    return
dmult(xmult(subt(l.a,l.b),subt(p1,l.b)),xmult(subt(l.a,l.b),subt(p2,l.b)))<-eps;
}
int opposite_side(point3 p1,point3 p2,point3 l1,point3 l2){
    return dmult(xmult(subt(l1,l2),subt(p1,l2)),xmult(subt(l1,l2),subt(p2,l2)))<-eps;
}</pre>
```

#### 7.5 判断两点是否在平面同侧

```
//判两点在平面同侧,点在平面上返回 0
int same_side(point3 p1,point3 p2,plane3 s){
    return dmult(pvec(s),subt(p1,s.a))*dmult(pvec(s),subt(p2,s.a))>eps;
}
int same_side(point3 p1,point3 p2,point3 s1,point3 s2,point3 s3){
    return dmult(pvec(s1,s2,s3),subt(p1,s1))*dmult(pvec(s1,s2,s3),subt(p2,s1))>eps;
}
```

# 7.6 判断两点是否在平面异侧

```
//判两点在平面异侧,点在平面上返回 0
int opposite_side(point3 p1,point3 p2,plane3 s){
```

```
return dmult(pvec(s),subt(p1,s.a))*dmult(pvec(s),subt(p2,s.a))<-eps;
}
int opposite_side(point3 p1,point3 p2,point3 s1,point3 s2,point3 s3){
    return dmult(pvec(s1,s2,s3),subt(p1,s1))*dmult(pvec(s1,s2,s3),subt(p2,s1))<-eps;
}</pre>
```

#### 7.7 判断两空间直线是否平行

```
//判两直线平行
int parallel(line3 u,line3 v){
    return vlen(xmult(subt(u.a,u.b),subt(v.a,v.b)))<eps;
}
int parallel(point3 u1,point3 u2,point3 v1,point3 v2){
    return vlen(xmult(subt(u1,u2),subt(v1,v2)))<eps;
}</pre>
```

#### 7.8 判断两平面是否平行

```
//判两平面平行
int parallel(plane3 u,plane3 v){
    return vlen(xmult(pvec(u),pvec(v)))<eps;
}
int parallel(point3 u1,point3 u2,point3 u3,point3 v1,point3 v2,point3 v3){
    return vlen(xmult(pvec(u1,u2,u3),pvec(v1,v2,v3)))<eps;
}</pre>
```

#### 7.9 判断直线是否与平面平行

```
//判直线与平面平行
int parallel(line3 1,plane3 s){
    return zero(dmult(subt(l.a,l.b),pvec(s)));
}
int parallel(point3 11,point3 12,point3 s1,point3 s2,point3 s3){
    return zero(dmult(subt(l1,l2),pvec(s1,s2,s3)));
}
```

#### 7.10 判断两直线是否垂直

```
//判两直线垂直
int perpendicular(line3 u,line3 v){
    return zero(dmult(subt(u.a,u.b),subt(v.a,v.b)));
}
int perpendicular(point3 u1,point3 u2,point3 v1,point3 v2){
    return zero(dmult(subt(u1,u2),subt(v1,v2)));
}
```

#### 7.11 判断两平面是否垂直

```
//判两平面垂直
int perpendicular(plane3 u,plane3 v){
    return zero(dmult(pvec(u),pvec(v)));
}
int perpendicular(point3 u1,point3 u2,point3 u3,point3 v1,point3 v2,point3 v3){
    return zero(dmult(pvec(u1,u2,u3),pvec(v1,v2,v3)));
}
```

# 7.12 判断两条空间线段是否相交

```
//判两线段相交,包括端点和部分重合
int intersect_in(line3 u,line3 v){
   if (!dots onplane(u.a,u.b,v.a,v.b))
       return 0;
   if (!dots_inline(u.a,u.b,v.a)||!dots_inline(u.a,u.b,v.b))
       return !same_side(u.a,u.b,v)&&!same_side(v.a,v.b,u);
   return
dot_online_in(u.a,v)||dot_online_in(u.b,v)||dot_online_in(v.a,u)||dot_online_in(v.b,
u);
}
int intersect_in(point3 u1,point3 u2,point3 v1,point3 v2){
   if (!dots_onplane(u1,u2,v1,v2))
       return 0;
   if (!dots_inline(u1,u2,v1)||!dots_inline(u1,u2,v2))
       return !same_side(u1,u2,v1,v2)&&!same_side(v1,v2,u1,u2);
dot online in(u1,v1,v2)||dot online in(u2,v1,v2)||dot online in(v1,u1,u2)||dot onlin
e_in(v2,u1,u2);
//判两线段相交,不包括端点和部分重合
int intersect ex(line3 u,line3 v){
   return
dots_onplane(u.a,u.b,v.a,v.b)&&opposite_side(u.a,u.b,v)&&opposite_side(v.a,v.b,u);
int intersect_ex(point3 u1,point3 u2,point3 v1,point3 v2){
dots onplane(u1,u2,v1,v2)&&opposite side(u1,u2,v1,v2)&&opposite side(v1,v2,u1,u2);
```

# 7.13 判断线段是否与空间三角形相交

#### 7.14 计算两条直线的交点

```
//计算两直线交点,注意事先判断直线是否共面和平行!
//线段交点请另外判线段相交(同时还是要判断是否平行!)
point3 intersection(line3 u,line3 v){
   point3 ret=u.a;
   double t=((u.a.x-v.a.x)*(v.a.y-v.b.y)-(u.a.y-v.a.y)*(v.a.x-v.b.x))
          /((u.a.x-u.b.x)*(v.a.y-v.b.y)-(u.a.y-u.b.y)*(v.a.x-v.b.x));
   ret.x+=(u.b.x-u.a.x)*t;
   ret.y+=(u.b.y-u.a.y)*t;
   ret.z+=(u.b.z-u.a.z)*t;
   return ret;
}
point3 intersection(point3 u1,point3 u2,point3 v1,point3 v2){
   point3 ret=u1:
   double t=((u1.x-v1.x)*(v1.y-v2.y)-(u1.y-v1.y)*(v1.x-v2.x))
          /((u1.x-u2.x)*(v1.y-v2.y)-(u1.y-u2.y)*(v1.x-v2.x));
   ret.x+=(u2.x-u1.x)*t;
   ret.y+=(u2.y-u1.y)*t;
   ret.z+=(u2.z-u1.z)*t;
   return ret;
}
```

#### 7.15 计算直线与平面的交点

```
//计算直线与平面交点,注意事先判断是否平行,并保证三点不共线!
//线段和空间三角形交点请另外判断
point3 intersection(line3 1,plane3 s){
    point3 ret=pvec(s);
    double t=(ret.x*(s.a.x-l.a.x)+ret.y*(s.a.y-l.a.y)+ret.z*(s.a.z-l.a.z))/
        (ret.x*(1.b.x-l.a.x)+ret.y*(1.b.y-l.a.y)+ret.z*(1.b.z-l.a.z));
    ret.x=l.a.x+(1.b.x-l.a.x)*t;
    ret.y=l.a.y+(1.b.y-l.a.y)*t;
    ret.z=l.a.z+(1.b.z-l.a.z)*t;
```

```
return ret;
}
point3 intersection(point3 l1,point3 l2,point3 s1,point3 s2,point3 s3){
   point3 ret=pvec(s1,s2,s3);
   double t=(ret.x*(s1.x-l1.x)+ret.y*(s1.y-l1.y)+ret.z*(s1.z-l1.z))/
        (ret.x*(l2.x-l1.x)+ret.y*(l2.y-l1.y)+ret.z*(l2.z-l1.z));
   ret.x=l1.x+(l2.x-l1.x)*t;
   ret.y=l1.y+(l2.y-l1.y)*t;
   ret.z=l1.z+(l2.z-l1.z)*t;
   return ret;
}
```

#### 7.16 计算两平面的交线

```
//计算两平面交线,注意事先判断是否平行,并保证三点不共线!
line3 intersection(plane3 u,plane3 v){
    line3 ret;
    ret.a=parallel(v.a,v.b,u.a,u.b,u.c)?intersection(v.b,v.c,u.a,u.b,u.c):intersection(v.a,v.b,u.a,u.b,u.c);
    ret.b=parallel(v.c,v.a,u.a,u.b,u.c)?intersection(v.b,v.c,u.a,u.b,u.c):intersection(v.c,v.a,u.a,u.b,u.c);
    return ret;
}
line3 intersection(point3 u1,point3 u2,point3 u3,point3 v1,point3 v2,point3 v3){
    line3 ret;
    ret.a=parallel(v1,v2,u1,u2,u3)?intersection(v2,v3,u1,u2,u3):intersection(v1,v2,u1,u2,u3);
    ret.b=parallel(v3,v1,u1,u2,u3)?intersection(v2,v3,u1,u2,u3):intersection(v3,v1,u1,u2,u3);
    return ret;
}
```

#### 7.17 点到直线的距离

```
//点到直线距离
double ptoline(point3 p,line3 l){
    return vlen(xmult(subt(p,l.a),subt(l.b,l.a)))/distance(l.a,l.b);
}
double ptoline(point3 p,point3 l1,point3 l2){
    return vlen(xmult(subt(p,l1),subt(l2,l1)))/distance(l1,l2);
}
```

# 7.18 计算点到平面的距离

```
//点到平面距离
double ptoplane(point3 p,plane3 s){
    return fabs(dmult(pvec(s),subt(p,s.a)))/vlen(pvec(s));
}
double ptoplane(point3 p,point3 s1,point3 s2,point3 s3){
```

```
return fabs(dmult(pvec(s1,s2,s3),subt(p,s1)))/vlen(pvec(s1,s2,s3));
}
```

#### 7.19 计算直线到直线的距离

```
//直线到直线距离
double linetoline(line3 u,line3 v){
    point3 n=xmult(subt(u.a,u.b),subt(v.a,v.b));
    return fabs(dmult(subt(u.a,v.a),n))/vlen(n);
}
double linetoline(point3 u1,point3 u2,point3 v1,point3 v2){
    point3 n=xmult(subt(u1,u2),subt(v1,v2));
    return fabs(dmult(subt(u1,v1),n))/vlen(n);
}
```

## 7.20 空间两直线夹角的 cos 值

```
//两直线夹角 cos 值
double angle_cos(line3 u,line3 v){
    return
dmult(subt(u.a,u.b),subt(v.a,v.b))/vlen(subt(u.a,u.b))/vlen(subt(v.a,v.b));
}
double angle_cos(point3 u1,point3 u2,point3 v1,point3 v2){
    return dmult(subt(u1,u2),subt(v1,v2))/vlen(subt(u1,u2))/vlen(subt(v1,v2));
}
```

#### 7.21 两平面夹角的 cos 值

```
//两平面夹角 cos 值
double angle_cos(plane3 u,plane3 v){
    return dmult(pvec(u),pvec(v))/vlen(pvec(u))/vlen(pvec(v));
}
double angle_cos(point3 u1,point3 u2,point3 u3,point3 v1,point3 v2,point3 v3){
    return
dmult(pvec(u1,u2,u3),pvec(v1,v2,v3))/vlen(pvec(u1,u2,u3))/vlen(pvec(v1,v2,v3));
}
```

#### 7.22 直线与平面夹角 sin 值

```
//直线平面夹角 sin 值
double angle_sin(line3 l,plane3 s){
    return dmult(subt(l.a,l.b),pvec(s))/vlen(subt(l.a,l.b))/vlen(pvec(s));
}
double angle_sin(point3 l1,point3 l2,point3 s1,point3 s2,point3 s3){
    return dmult(subt(l1,l2),pvec(s1,s2,s3))/vlen(subt(l1,l2))/vlen(pvec(s1,s2,s3));
}
```

# 1. 最远曼哈顿距离

```
#include <stdio.h>
#define INF 999999999999.0
struct Point
    double x[5];
}pt[100005];
double dis[32][100005], coe[5], minx[32], maxx[32];
//去掉绝对值后有 2^D 种可能
void GetD(int N, int D)
    int s, i, j, tot=(1<<D);
   for (s=0;s<tot;s++)</pre>
    {
       for (i=0;i<D;i++)</pre>
           if (s&(1<<i))
               coe[i]=-1.0;
           else coe[i]=1.0;
       for (i=0;i<N;i++)</pre>
       {
           dis[s][i]=0.0;
           for (j=0;j<D;j++)</pre>
               dis[s][i]=dis[s][i]+coe[j]*pt[i].x[j];
       }
    }
}
//取每种可能中的最大差距
void Solve(int N, int D)
{
    int s, i, tot=(1<<D);</pre>
    double tmp, ans;
   for (s=0;s<tot;s++)</pre>
   {
       minx[s]=INF;
       maxx[s]=-INF;
       for (i=0; i<N; i++)
           if (minx[s]>dis[s][i]) minx[s]=dis[s][i];
           if (maxx[s]<dis[s][i]) maxx[s]=dis[s][i];</pre>
       }
    }
   ans=0.0;
   for (s=0; s<tot; s++)
    {
       tmp=maxx[s]-minx[s];
       if (tmp>ans) ans=tmp;
    printf("%.21f\n", ans);
```

```
}
int main (void)
{
    int n, i;
    while (scanf("%d",&n)==1)
    {
        for (i=0;i<n;i++)

scanf("%lf%lf%lf%lf%lf",&pt[i].x[0],&pt[i].x[1],&pt[i].x[2],&pt[i].x[3],&pt[i].x[4])
;
        GetD(n, 5);
        Solve(n, 5);
    }
    return 0;
}</pre>
```

# 2.最近点对

```
#include <stdio.h>
#include <math.h>
#include <stdlib.h>
#define Max(x,y) (x)>(y)?(x):(y)
struct Q
{
   double x, y;
}q[100001], sl[10], sr[10];
int cntl, cntr, lm, rm;
double ans;
int cmp(const void*p1, const void*p2)
{
   struct Q*a1=(struct Q*)p1;
   struct Q*a2=(struct Q*)p2;
   if (a1->x<a2->x)return -1;
   else if (a1->x==a2->x) return 0;
   else return 1;
}
double CalDis(double x1, double y1, double x2, double y2)
{
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
}
void MinDis(int 1, int r)
{
   if (l==r) return;
   double dis;
   if (l+1==r)
```

```
{
       dis=CalDis(q[1].x,q[1].y,q[r].x,q[r].y);
       if (ans>dis) ans=dis;
       return;
    int mid=(l+r)>>1, i, j;
   MinDis(1,mid);
   MinDis(mid+1,r);
   lm=mid+1-5;
   if (lm<1) lm=1;
   rm=mid+5;
   if (rm>r) rm=r;
   cntl=cntr=0;
   for (i=mid;i>=lm;i--)
       if (q[mid+1].x-q[i].x>=ans)break;
       sl[++cntl]=q[i];
   for (i=mid+1;i<=rm;i++)</pre>
       if (q[i].x-q[mid].x>=ans)break;
       sr[++cntr]=q[i];
    }
   for (i=1;i<=cntl;i++)</pre>
       for (j=1;j<=cntr;j++)</pre>
       {
           dis=CalDis(sl[i].x,sl[i].y,sr[j].x,sr[j].y);
           if (dis<ans) ans=dis;</pre>
       }
}
int main (void)
    int n, i;
   while (scanf("%d",&n)==1&&n)
   {
       for (i=1;i<=n;i++)
           scanf("%lf %lf", &q[i].x,&q[i].y);
       qsort(q+1,n,sizeof(struct Q),cmp);
       ans=CalDis(q[1].x,q[1].y,q[2].x,q[2].y);
       MinDis(1,n);
       printf("%.21f\n",ans/2.0);
   return 0;
}
```

# 3.最近点对

```
#include <stdio.h>
#include <math.h>
#include <stdlib.h>
#define Max(x,y) (x)>(y)?(x):(y)
struct Q
   double x, y;
}q[100001], sl[10], sr[10];
int cntl, cntr, lm, rm;
double ans;
int cmp(const void*p1, const void*p2)
{
   struct Q*a1=(struct Q*)p1;
   struct Q*a2=(struct Q*)p2;
   if (a1->x<a2->x)return -1;
   else if (a1->x==a2->x) return 0;
   else return 1;
}
double CalDis(double x1, double y1, double x2, double y2)
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
}
void MinDis(int 1, int r)
{
   if (l==r) return;
   double dis;
   if (l+1==r)
   {
       dis=CalDis(q[1].x,q[1].y,q[r].x,q[r].y);
       if (ans>dis) ans=dis;
       return;
   int mid=(l+r)>>1, i, j;
   MinDis(1,mid);
   MinDis(mid+1,r);
   lm=mid+1-5;
   if (lm<1) lm=1;
   rm=mid+5;
   if (rm>r) rm=r;
   cntl=cntr=0;
   for (i=mid;i>=lm;i--)
```

```
{
       if (q[mid+1].x-q[i].x>=ans)break;
        sl[++cntl]=q[i];
   for (i=mid+1;i<=rm;i++)</pre>
       if (q[i].x-q[mid].x>=ans)break;
       sr[++cntr]=q[i];
    }
   for (i=1;i<=cntl;i++)</pre>
       for (j=1;j<=cntr;j++)</pre>
       {
           dis=CalDis(sl[i].x,sl[i].y,sr[j].x,sr[j].y);
           if (dis<ans) ans=dis;</pre>
       }
}
int main (void)
   int n, i;
   while (scanf("%d",&n)==1&&n)
   {
       for (i=1;i<=n;i++)
           scanf("%lf %lf", &q[i].x,&q[i].y);
       qsort(q+1,n,sizeof(struct Q),cmp);
       ans=CalDis(q[1].x,q[1].y,q[2].x,q[2].y);
       MinDis(1,n);
       printf("%.21f\n",ans/2.0);
   return 0;
}
```

# 4.最小包围圆

```
#include<stdio.h>
#include<string.h>
#include<math.h>
struct Point
{
    double x;
    double y;
}pt[1005];
struct Traingle
{
    struct Point p[3];
};
struct Circle
{
```

```
struct Point center;
                 double r;
}ans;
//计算两点距离
double Dis(struct Point p, struct Point q)
                 double dx=p.x-q.x;
                double dy=p.y-q.y;
                 return sqrt(dx*dx+dy*dy);
//计算三角形面积
double Area(struct Traingle ct)
{
                return
fabs((ct.p[1].x-ct.p[0].x)*(ct.p[2].y-ct.p[0].y)-(ct.p[2].x-ct.p[0].x)*(ct.p[1].y-ct.p[0].x)
 .p[0].y))/2.0;
}
//求三角形的外接圆,返回圆心和半径(存在结构体"圆"中)
struct Circle CircumCircle(struct Traingle t)
{
                struct Circle tmp;
                 double a, b, c, c1, c2;
                double xA, yA, xB, yB, xC, yC;
                a = Dis(t.p[0], t.p[1]);
                b = Dis(t.p[1], t.p[2]);
                c = Dis(t.p[2], t.p[0]);
                //根据 S = a * b * c / R / 4;求半径 R
                tmp.r = (a*b*c)/(Area(t)*4.0);
                xA = t.p[0].x;
                yA = t.p[0].y;
                xB = t.p[1].x;
                yB = t.p[1].y;
                xC = t.p[2].x;
                yC = t.p[2].y;
                c1 = (xA*xA+yA*yA - xB*xB-yB*yB) / 2;
                c2 = (xA*xA+yA*yA - xC*xC-yC*yC) / 2;
                tmp.center.x = (c1*(yA - yC)-c2*(yA - yB)) / ((xA - xB)*(yA - yC)-(xA - xC)*(yA - yB)) / ((xA - xB)*(yA - yB)) / ((xA - xB)*
yB));
                 tmp.center.y = (c1*(xA - xC)-c2*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - 
xB));
                return tmp;
}
//确定最小包围圆
struct Circle MinCircle(int num, struct Traingle ct)
{
                 struct Circle ret;
                 if (num==0) ret.r = 0.0;
                else if (num==1)
                 {
```

```
ret.center = ct.p[0];
       ret.r = 0.0;
   }
   else if (num==2)
   {
       ret.center.x = (ct.p[0].x+ct.p[1].x)/2.0;
       ret.center.y = (ct.p[0].y+ct.p[1].y)/2.0;
       ret.r = Dis(ct.p[0], ct.p[1])/2.0;
   else if(num==3) ret = CircumCircle(ct);
   return ret;
}
//递归实现增量算法
void Dfs(int x, int num, struct Traingle ct)
{
   int i, j;
   struct Point tmp;
   ans = MinCircle(num, ct);
   if (num==3) return;
   for (i=1; i<=x; i++)
       if (Dis(pt[i], ans.center)>ans.r)
           ct.p[num]=pt[i];
           Dfs(i-1, num+1, ct);
           tmp=pt[i];
           for (j=i;j>=2;j--)
              pt[j]=pt[j-1];
           pt[1]=tmp;
       }
void Solve(int n)
{
   struct Traingle ct;
   Dfs(n, 0, ct);
int main (void)
   int n, i;
   while (scanf("%d", &n)!=EOF && n)
   {
       for (i=1;i<=n;i++)
           scanf("%lf %lf", &pt[i].x, &pt[i].y);
       printf("%.21f %.21f %.21f\n", ans.center.x, ans.center.y, ans.r);
   return 0;
}
```

# 5.求两个圆的交点

```
#include<stdio.h>
#include<string.h>
#include<math.h>
#include<stdlib.h>
const double eps = 1e-8;
const double PI = acos(-1.0);
struct Point
    double x;
    double y;
typedef struct Point point;
struct Line
{
    double s, t;
};
typedef struct Line Line;
struct Circle
    Point center;
    double r;
    Line line[505];
    int cnt;
    bool covered;
}circle[105];
double distance(point p1, point p2)
{
    double dx = p1.x-p2.x;
    double dy = p1.y-p2.y;
    return sqrt(dx*dx + dy*dy);
}
point intersection(point u1,point u2, point v1,point v2)
    point ret = u1;
    double t=((u1.x-v1.x)*(v1.y-v2.y)-(u1.y-v1.y)*(v1.x-v2.x)) / (u1.y-v1.y)*(v1.x-v2.x)) / (u1.y-v1.y)*(v1.x-v2.x)
             ((u1.x-u2.x)*(v1.y-v2.y)-(u1.y-u2.y)*(v1.x-v2.x));
    ret.x += (u2.x-u1.x)*t;
    ret.y += (u2.y-u1.y)*t;
   return ret;
}
```

```
void intersection_line_circle(point c,double r,point l1,point l2,point& p1,point& p2)
{
   point p=c;
   double t;
   p.x+=l1.y-l2.y;
   p.y+=12.x-11.x;
   p=intersection(p,c,l1,l2);
   t=sqrt(r*r-distance(p,c)*distance(p,c))/distance(11,12);
   p1.x=p.x+(12.x-11.x)*t;
   p1.y=p.y+(l2.y-l1.y)*t;
   p2.x=p.x-(12.x-11.x)*t;
   p2.y=p.y-(12.y-11.y)*t;
}
//计算圆与圆的交点,保证圆与圆有交点,圆心不重合
void intersection_circle_circle(point c1,double r1,point c2,double r2,point& p1,point&
p2)
{
   point u,v;
   double t;
   t=(1+(r1*r1-r2*r2)/distance(c1,c2)/distance(c1,c2))/2;
   u.x=c1.x+(c2.x-c1.x)*t;
   u.y=c1.y+(c2.y-c1.y)*t;
   v.x=u.x+c1.y-c2.y;
   v.y=u.y-c1.x+c2.x;
   intersection_line_circle(c1,r1,u,v,p1,p2);
}
```

# 6. 求三角形外接圆圆心

```
struct Point
   double x;
   double y;
}pt[1005];
struct Traingle
{
   struct Point p[3];
};
struct Circle
{
   struct Point center;
   double r;
}ans;
//计算两点距离
double Dis(struct Point p, struct Point q)
   double dx=p.x-q.x;
   double dy=p.y-q.y;
```

```
return sqrt(dx*dx+dy*dy);
}
//计算三角形面积
double Area(struct Traingle ct)
{
                    return
fabs((ct.p[1].x-ct.p[0].x)*(ct.p[2].y-ct.p[0].y)-(ct.p[2].x-ct.p[0].x)*(ct.p[1].y-ct.p[0].x)
 .p[0].y))/2.0;
}
//求三角形的外接圆,返回圆心和半径(存在结构体"圆"中)
struct Circle CircumCircle(struct Traingle t)
{
                     struct Circle tmp;
                     double a, b, c, c1, c2;
                    double xA, yA, xB, yB, xC, yC;
                    a = Dis(t.p[0], t.p[1]);
                    b = Dis(t.p[1], t.p[2]);
                    c = Dis(t.p[2], t.p[0]);
                    //根据 S = a * b * c / R / 4;求半径 R
                    tmp.r = (a*b*c)/(Area(t)*4.0);
                    xA = t.p[0].x;
                    yA = t.p[0].y;
                    xB = t.p[1].x;
                    yB = t.p[1].y;
                    xC = t.p[2].x;
                    yC = t.p[2].y;
                    c1 = (xA*xA+yA*yA - xB*xB-yB*yB) / 2;
                    c2 = (xA*xA+yA*yA - xC*xC-yC*yC) / 2;
                    tmp.center.x = (c1*(yA - yC)-c2*(yA - yB)) / ((xA - xB)*(yA - yC)-(xA - xC)*(yA - yB)) / ((xA - xB)*(yA - yB)) / ((xA - xB)*
yB));
                     tmp.center.y = (c1*(xA - xC)-c2*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - yC)*(xA - xB)) / ((yA - yB)*(xA - xC)-(yA - 
xB));
                    return tmp;
}
```

# 7. 求凸包

```
#include <stdio.h>
#include <string.h>
#include <stdlib.h>
#include <math.h>
#define INF 99999999999
#define PI acos(-1.0)
struct Point
{
    double x, y, dis;
}pt[1005], stack[1005], p0;
```

```
int top, tot;
//计算几何距离
double Dis(double x1, double y1, double x2, double y2)
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
}
//极角比较, 返回-1: p0p1 在 p0p2 的右侧, 返回 0:p0,p1,p2 共线
int Cmp_PolarAngel(struct Point p1, struct Point p2, struct Point pb)
   double delta=(p1.x-pb.x)*(p2.y-pb.y)-(p2.x-pb.x)*(p1.y-pb.y);
   if (delta<0.0) return 1;
   else if (delta==0.0) return 0;
   else return -1;
// 判断向量 p2p3 是否对 p1p2 构成左旋
bool Is LeftTurn(struct Point p3, struct Point p2, struct Point p1)
   int type=Cmp_PolarAngel(p3, p1, p2);
   if (type<0) return true;
   return false;
}
//先按极角排,再按距离由小到大排
int Cmp(const void*p1, const void*p2)
{
   struct Point*a1=(struct Point*)p1;
   struct Point*a2=(struct Point*)p2;
   int type=Cmp_PolarAngel(*a1, *a2, p0);
   if (type<0) return -1;
   else if (type==0)
   {
       if (a1->dis<a2->dis) return -1;
       else if (a1->dis==a2->dis) return 0;
       else return 1;
   }
   else return 1;
}
//求凸包
void Solve(int n)
{
   int i, k;
   p0.x=p0.y=INF;
   for (i=0;i<n;i++)
   {
       scanf("%lf %lf",&pt[i].x, &pt[i].y);
       if (pt[i].y < p0.y)
          p0.y=pt[i].y;
          p0.x=pt[i].x;
          k=i;
```

```
}
       else if (pt[i].y==p0.y)
           if (pt[i].x<p0.x)</pre>
           {
               p0.x=pt[i].x;
               k=i;
           }
       }
    }
   pt[k]=pt[0];
   pt[0]=p0;
   for (i=1;i<n;i++)</pre>
       pt[i].dis=Dis(pt[i].x,pt[i].y, p0.x,p0.y);
    qsort(pt+1, n-1, sizeof(struct Point), Cmp);
    //去掉极角相同的点
   tot=1;
   for (i=2;i<n;i++)</pre>
       if (Cmp_PolarAngel(pt[i], pt[i-1], p0))
           pt[tot++]=pt[i-1];
   pt[tot++]=pt[n-1];
   //求凸包
   top=1;
   stack[0]=pt[0];
    stack[1]=pt[1];
   for (i=2;i<tot;i++)</pre>
   {
       while (top>=1 && Is_LeftTurn(pt[i], stack[top], stack[top-1])==false)
           top--;
       stack[++top]=pt[i];
    }
}
int main (void)
{
   int n;
   while (scanf("%d",&n)==2)
       Solve(n);
   return 0;
}
```

### 8.包卡壳旋转求出所有对踵点、最远点对

```
#include <stdio.h>
#include <string.h>
#include <stdlib.h>
#include <math.h>
#define INF 999999999.9
```

```
#define PI acos(-1.0)
struct Point
{
   double x, y, dis;
}pt[6005], stack[6005], p0;
int top, tot;
//计算几何距离
double Dis(double x1, double y1, double x2, double y2)
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
}
//极角比较, 返回-1: p0p1 在 p0p2 的右侧,返回 0:p0,p1,p2 共线
int Cmp_PolarAngel(struct Point p1, struct Point p2, struct Point pb)
   double delta=(p1.x-pb.x)*(p2.y-pb.y)-(p2.x-pb.x)*(p1.y-pb.y);
   if (delta<0.0) return 1;
   else if (delta==0.0) return 0;
   else return -1;
// 判断向量 p2p3 是否对 p1p2 构成左旋
bool Is_LeftTurn(struct Point p3, struct Point p2, struct Point p1)
   int type=Cmp_PolarAngel(p3, p1, p2);
   if (type<0) return true;
   return false;
//先按极角排,再按距离由小到大排
int Cmp(const void*p1, const void*p2)
{
   struct Point*a1=(struct Point*)p1;
   struct Point*a2=(struct Point*)p2;
   int type=Cmp_PolarAngel(*a1, *a2, p0);
   if (type<0) return -1;
   else if (type==0)
   {
       if (a1->dis<a2->dis) return -1;
       else if (a1->dis==a2->dis) return 0;
       else return 1;
   else return 1;
}
//求凸包
void Hull(int n)
   int i, k;
   p0.x=p0.y=INF;
   for (i=0;i<n;i++)
   {
       scanf("%lf %lf",&pt[i].x, &pt[i].y);
```

```
if (pt[i].y < p0.y)
       {
           p0.y=pt[i].y;
           p0.x=pt[i].x;
           k=i;
       }
       else if (pt[i].y==p0.y)
           if (pt[i].x<p0.x)
           {
              p0.x=pt[i].x;
              k=i;
           }
       }
   }
   pt[k]=pt[0];
   pt[0]=p0;
   for (i=1;i<n;i++)
       pt[i].dis=Dis(pt[i].x,pt[i].y, p0.x,p0.y);
   qsort(pt+1, n-1, sizeof(struct Point), Cmp);
   //去掉极角相同的点
   tot=1;
   for (i=2;i<n;i++)</pre>
       if (Cmp_PolarAngel(pt[i], pt[i-1], p0))
           pt[tot++]=pt[i-1];
   pt[tot++]=pt[n-1];
   //求凸包
   top=1;
   stack[0]=pt[0];
   stack[1]=pt[1];
   for (i=2;i<tot;i++)</pre>
   {
       while (top>=1 && Is_LeftTurn(pt[i], stack[top], stack[top-1])==false)
           top--;
       stack[++top]=pt[i];
   }
}
//计算叉积
double CrossProduct(struct Point p1, struct Point p2, struct Point p3)
{
   return (p1.x-p3.x)*(p2.y-p3.y)-(p2.x-p3.x)*(p1.y-p3.y);
//卡壳旋转,求出凸多边形所有对踵点
void Rotate(struct Point*ch, int n)
{
   int i, p=1;
   double t1, t2, ans=0.0, dif;
   ch[n]=ch[0];
   for (i=0;i<n;i++)
```

```
{
      //如果下一个点与当前边构成的三角形的面积更大,则说明此时不构成对踵点
                         (fabs(CrossProduct(ch[i],ch[i+1],ch[p+1]))
                                                                             >
fabs(CrossProduct(ch[i],ch[i+1],ch[p])))
          p=(p+1)%n;
      dif=fabs(CrossProduct(ch[i],ch[i+1],ch[p+1]))
fabs(CrossProduct(ch[i],ch[i+1],ch[p]));
      //如果当前点和下一个点分别构成的三角形面积相等,则说明两条边即为平行线,对角线两端都
可能是对踵点
      if (dif==0.0)
      {
          t1=Dis(ch[p].x, ch[p].y, ch[i].x, ch[i].y);
          t2=Dis(ch[p+1].x, ch[p+1].y, ch[i+1].x, ch[i+1].y);
          if (t1>ans)ans=t1;
          if (t2>ans)ans=t2;
      }
      //说明 p, i 是对踵点
      else if (dif<0.0)
          t1=Dis(ch[p].x, ch[p].y, ch[i].x, ch[i].y);
          if (t1>ans)ans=t1;
   }
   printf("%.21f\n",ans);
}
int main (void)
{
   int n;
   while (scanf("%d",&n)==1)
      Hull(n);
      Rotate(stack, top+1);
   return 0;
}
```

# 9. 凸包+旋转卡壳求平面面积最大三角

```
int top, tot;
double Dis(double x1, double y1, double x2, double y2)
{
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
}
int Cmp_PolarAngel(struct Point p1, struct Point p2, struct Point pb)
{
   double delta=(p1.x-pb.x)*(p2.y-pb.y)-(p2.x-pb.x)*(p1.y-pb.y);
   if (delta<0.0) return 1;
   else if (delta==0.0) return 0;
   else return -1;
}
bool Is LeftTurn(struct Point p3, struct Point p2, struct Point p1)
   int type=Cmp_PolarAngel(p3, p1, p2);
   if (type<0) return true;
   return false;
int Cmp(const void*p1, const void*p2)
   struct Point*a1=(struct Point*)p1;
   struct Point*a2=(struct Point*)p2;
   int type=Cmp_PolarAngel(*a1, *a2, p0);
   if (type<0) return -1;
   else if (type==0)
   {
       if (a1->dis<a2->dis) return -1;
       else if (a1->dis==a2->dis) return 0;
       else return 1;
   else return 1;
}
void Hull(int n)
   int i, k;
   p0.x=p0.y=INF;
   for (i=0;i<n;i++)</pre>
       scanf("%lf %lf",&pt[i].x, &pt[i].y);
       if (pt[i].y < p0.y)
           p0.y=pt[i].y;
           p0.x=pt[i].x;
           k=i;
       }
       else if (pt[i].y==p0.y)
           if (pt[i].x<p0.x)</pre>
           {
```

```
p0.x=pt[i].x;
               k=i;
           }
       }
   }
   pt[k]=pt[0];
   pt[0]=p0;
   for (i=1;i<n;i++)
       pt[i].dis=Dis(pt[i].x,pt[i].y, p0.x,p0.y);
   qsort(pt+1, n-1, sizeof(struct Point), Cmp);
   tot=1;
   for (i=2;i<n;i++)
       if (Cmp_PolarAngel(pt[i], pt[i-1], p0))
           pt[tot++]=pt[i-1];
   pt[tot++]=pt[n-1];
   top=1;
   stack[0]=pt[0];
   stack[1]=pt[1];
   for (i=2;i<tot;i++)</pre>
   {
       while (top>=1 && Is_LeftTurn(pt[i], stack[top], stack[top-1])==false)
           top--;
       stack[++top]=pt[i];
   }
}
double TArea(struct Point p1, struct Point p2, struct Point p3)
{
   return fabs((p1.x-p3.x)*(p2.y-p3.y)-(p2.x-p3.x)*(p1.y-p3.y));
}
void Rotate(struct Point*ch, int n)
   if (n<3)
   {
       printf("0.00\n");
       return;
   int i, j, k;
   double ans=0.0, tmp;
   ch[n]=ch[0];
   for (i=0;i<n;i++)
   {
       j=(i+1)%n;
       k=(j+1)%n;
       while ((j!=k) \&\& (k!=i))
           while (TArea(ch[i],ch[j],ch[k+1])>TArea(ch[i],ch[j],ch[k]))
               k=(k+1)%n;
           tmp=TArea(ch[i],ch[j], ch[k]);
           if (tmp>ans) ans=tmp;
```

```
j=(j+1)%n;
}
printf("%.2lf\n",ans/2.0);
}
int main (void)
{
   int n;
   while (scanf("%d",&n)==1)
   {
      if (n==-1)break;
      Hull(n);
      Rotate(stack, top+1);
   }
   return 0;
}
```

## 10.Pick 定理

```
// Pick 定理求整点多边形内部整点数目
//(1) 给定顶点座标均是整点(或正方形格点)的简单多边形,皮克定理说明了其面积 A 和内部格点数目
i、边上格点数目 b 的关系: A = i + b/2 - 1;
// (2) 在两点(x1, y1),(x2, y2)连线之间的整点个数(包含一个端点)为: gcd(|x1-x2|, |y1
-y2|);
// (3) 求三角形面积用叉乘
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
#include<string.h>
long long x[3], y[3], area, b;
long long My_Abs(long long t)
{
   if (t<0) return -t;
   return t;
}
long long Gcd(long long x, long long y)
   if (y==0) return x;
   long long mod=x%y;
   while (mod)
   {
      x=y;
      y=mod;
      mod=x%y;
   return y;
}
```

```
int main (void)
   int i;
   while (1)
   {
       for (i = 0; i < 3; i ++)
           scanf("%1ld %1ld", &x[i], &y[i]);
       if(x[0]==0\&&y[0]==0\&&x[1]==0\&&y[1]==0\&&x[2]==0\&&y[2]==0) break;
       area = (x[1]-x[0])*(y[2]-y[0])-(x[2]-x[0])*(y[1]-y[0]);
       area = My_Abs(area);
       b=0;
       b=Gcd(My\_Abs(x[1]-x[0]),
                                  My_Abs(y[1]-y[0])) + Gcd(My_Abs(x[2]-x[0]),
My_Abs(y[2]-y[0])) + Gcd(My_Abs(x[1]-x[2]), My_Abs(y[1]-y[2]));
       printf("%lld\n", (area-b+2)/2);
   }
   return 0;
}
```

#### 11.求多边形面积和重心

```
#include <stdio.h>
#include <math.h>
int x[1000003], y[1000003];
double A, tx, ty, tmp;
int main (void)
{
   int cases, n, i;
   scanf ("%d", &cases);
   while (cases --)
   {
       scanf ("%d", &n);
       A = 0.0;
       x[0] = y[0] = 0;
       for (i = 1; i \le n; i ++)
           scanf ("%d %d", &x[i], &y[i]);
           A += (x[i-1]*y[i] - x[i]*y[i-1]);
       }
       A += x[n]*y[1] - x[1]*y[n];
       A = A / 2.0;
       tx = ty = 0.0;
       for (i = 1; i < n; i ++)
       {
           tmp = x[i]*y[i+1] - x[i+1]*y[i];
           tx += (x[i]+x[i+1]) * tmp;
           ty += (y[i]+y[i+1]) * tmp;
       }
       tmp = x[n]*y[1] - x[1]*y[n];
       tx += (x[n]+x[1])*tmp;
```

```
ty += (y[n]+y[1])*tmp;
    printf ("%.2lf %.2lf\n", tx/(6.0*A), ty/(6.0*A));
}
return 0;
}
```

## 12.判断一个简单多边形是否有核

```
#include <stdio.h>
#include <string.h>
const int INF = (1 << 30);
struct Point
{
   int x, y;
}pt[150];
typedef struct Point Point;
bool turn_right[150];
int det(Point s1, Point t1, Point s2, Point t2)
{
   int d1x = t1.x-s1.x;
   int d1y = t1.y-s1.y;
   int d2x = t2.x-s2.x;
   int d2y = t2.y-s2.y;
   return d1x*d2y - d2x*d1y;
}
void Swap(int &a, int &b)
{
   if (a>b)
   {
       int t=a;
       a=b;
       b=t;
   }
int main (void)
   int n, i, cross, maxx, minx, maxy, miny, maxn, minn, countn=0;
   while (scanf("%d", &n)==1&&n)
   {
       maxx=maxy=-INF;
       minx=miny=INF;
       //点按顺时针给出
       for (i=1; i<=n; i++)
           scanf("%d %d", &pt[i].x, &pt[i].y);
           if (maxx<pt[i].x) maxx=pt[i].x;</pre>
           if (maxy<pt[i].y) maxy=pt[i].y;</pre>
```

```
if (minx>pt[i].x) minx=pt[i].x;
           if (miny>pt[i].y) miny=pt[i].y;
       }
       pt[n+1]=pt[1];
       pt[n+2]=pt[2];
       pt[n+3]=pt[3];
       pt[n+4]=pt[4];
       //求每条线段的转向
       for (i=1; i<=n+1; i ++)
           cross = det(pt[i],pt[i+1], pt[i+1], pt[i+2]);
           if (cross<0)
              turn right[i+1]=true;
           else turn_right[i+1]=false;
       }
       //两条边连续右转的为凸处,只有此时才可影响"核"肯恩存在的范围
       for (i=2; i<= n+1; i++)
           if (turn_right[i] && turn_right[i+1])
              if (pt[i].x==pt[i+1].x)
              {
                  minn=pt[i].y;
                  maxn=pt[i+1].y;
                  Swap(minn, maxn);
                  if (minn>miny) miny=minn;
                  if (maxn<maxy) maxy=maxn;</pre>
              }
              else
              {
                  minn=pt[i].x;
                  maxn=pt[i+1].x;
                  Swap(minn, maxn);
                  if (minn>minx) minx=minn;
                  if (maxn<maxx) maxx=maxn;</pre>
              }
           }
       if (minx<=maxx && miny<=maxy)</pre>
           printf("Floor #%d\nSurveillance is possible.\n\n", ++countn);
       else printf("Floor #%d\nSurveillance is impossible.\n\n", ++countn);
   }
   return 0;
}
```

# 13.模拟退火

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
```

```
#define Lim 0.999999
#define EPS 1e-2
#define PI acos(-1.0)
double Temp, maxx, minx, maxy, miny, lx, ly, dif;
int nt, ns, nc;
struct Target
{
   double x, y;
}T[105];
struct Solution
{
   double x, y;
   double f;
}S[25], P, A;
double Dis(double x1, double y1, double x2, double y2)
{
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
void Seed(void)
   int i, j;
   for (i=0;i<ns;i++)
   {
       S[i].x=minx+((double)(rand()%1000+1)/1000.0)*lx;
       S[i].y=miny+((double)(rand()%1000+1)/1000.0)*ly;
       S[i].f=0.0;
       for (j=0;j<nt;j++)
           S[i].f=S[i].f+Dis(S[i].x,S[i].y, T[j].x, T[j].y);
   }
}
void Trans(void)
{
   int i, j, k;
   double theta;
   for (i=0;i<ns;i++)
   {
       P=S[i];
       for (j=0;j<nc;j++)
       {
           theta=(((double)(rand()%1000+1))/1000.0)*2.0*PI;
           A.x=P.x+Temp*cos(theta);
           A.y=P.y+Temp*sin(theta);
           if (A.x<minx||A.x>maxx||A.y<miny||A.y>maxy)
               continue;
           A.f=0.0;
           for (k=0;k<nt;k++)
               A.f=A.f+Dis(A.x,A.y,T[k].x,T[k].y);
           dif=A.f-S[i].f;
           if (dif<0.0)S[i]=A;
```

```
else
           {
               dif=exp(-dif/Temp);
               if (dif>Lim) S[i]=A;
           }
       }
    }
}
int main (void)
   int i, k;
   while (scanf("%d",&nt)==1&&nt)
    {
       maxx=maxy=0;
       minx=miny=(1<<20);
       for (i=0;i<nt;i++)</pre>
           scanf("%lf %lf",&T[i].x,&T[i].y);
           if (maxx<T[i].x)maxx=T[i].x;</pre>
           if (minx>T[i].x)minx=T[i].x;
           if (maxy<T[i].y)maxy=T[i].y;</pre>
           if (miny>T[i].y)miny=T[i].y;
       }
       1x=maxx-minx;
       ly=maxy-miny;
       Temp=sqrt(lx*lx+ly*ly)/3.0;
       ns=5, nc=10;
       Seed();
       while (Temp>EPS)
           Trans();
           Temp=Temp*0.40;
        }
       k=0;
       for (i=1;i<ns;i++)</pre>
           if (S[k].f>S[i].f)
               k=i;
       printf ("%.01f\n", S[k].f);
    }
   return 0;
}
```

### 14.六边形坐标系

```
//第一种六边形坐标系
#include<stdio.h>
#include<math.h>
#include<string.h>
#include<stdlib.h>
```

```
double Dis(double x1, double y1, double x2, double y2)
{
   double dx=x1-x2;
   double dy=y1-y2;
   return sqrt(dx*dx+dy*dy);
void Get_KL(double L, double x, double y, int &k, int &l, double &cd)
   k=floor((2.0*x)/(3.0*L));
   l=floor((2.0*y)/(sqrt(3.0)*L));
   double d1, d2, x1, y1, x2, y2;
   if ((k+1)&1)
   {
       x1=k*L*1.5;
       y1=(1+1.0)*L*sqrt(3.0)*0.5;
       x2=(k+1.0)*L*1.5;
       y2=1*L*sqrt(3.0)*0.5;
       d1=Dis(x1,y1, x,y);
       d2=Dis(x2,y2, x,y);
       if (d1>d2)
       {
           k++;
           cd=d2;
       }
       else
       {
           1++;
           cd=d1;
       }
   }
   else
   {
       x1=k*L*1.5;
       y1=l*L*sqrt(3.0)*0.5;
       x2=(k+1.0)*L*1.5;
       y2=(1+1.0)*L*sqrt(3.0)*0.5;
       d1=Dis(x1,y1, x,y);
       d2=Dis(x2,y2, x,y);
       if (d1>d2)
       {
           k++,1++;
           cd=d2;
       else cd=d1;
   }
int My_Abs(int x)
{
   if (x<0) return -x;
```

```
return x;
}
int main (void)
   double L, x1, y1, x2, y2, ans, cd1, cd2;
   int k1, l1, k2, l2;
   while (scanf("%lf %lf %lf %lf",&L,&x1,&y1,&x2,&y2)==5)
   {
       if (L==0.0\&x1==0.0\&x1==0.0\&x2==0.0\&x2==0.0) break;
       Get_KL(L, x1, y1, k1, l1, cd1);
       Get_KL(L, x2, y2, k2, 12, cd2);
       if (k1==k2\&l1==l2) printf("%.3lf\n", Dis(x1,y1, x2,y2));
       else
       {
           ans=cd1+cd2;
           if (My\_Abs(k1-k2) > My\_Abs(l1-l2))
               ans=ans+sqrt(3.0)*L*My_Abs(k1-k2);
           else
ans=ans+sqrt(3.0)*L*My_Abs(k1-k2)+sqrt(3.0)*L*(double)(My_Abs(l1-l2)-My_Abs(k1-k2))/
2.0;
           printf("%.31f\n", ans);
       }
   }
   return 0;
}
//第二种六边形坐标系
#include <stdio.h>
#include <string.h>
#include <stdlib.h>
#include <math.h>
struct A
   int x, y, num;
}a[10001];
const int dec[6][2] = \{\{-1,1\},\{-1,0\},\{0,-1\},\{1,-1\},\{1,0\},\{0,1\}\};
bool adj(int x1, int y1, int x2, int y2)
   if (x1 == x2 \&\& abs(y1-y2) == 1) return true;
   if (y1 == y2 \&\& abs(x1-x2) == 1) return true;
   if (x1 == x2 + 1 \&\& y1 == y2 - 1) return true;
   if (x1 == x2 - 1 \&\& y1 == y2 + 1) return true;
   return false;
}
bool flag[10001];
int main (void)
{
   int i, j, k, x, u, v, cut, minn, cnt[6];
   memset(cnt, 0, sizeof(cnt));
```

```
a[1].num = 1, cnt[1] = 1;
a[1].x = a[1].y = 0;
for (i = 2; i < 10001; i ++)
{
   k = (int)((3.0+sqrt(12.0*i - 3.0))/6.0+0.0000001);
   if (i == 3*(k-1)*(k-1)+3*(k-1)+1) k --;
   j = i - (3*(k-1)*(k-1)+3*(k-1)+1);
   // 当前的六边形是第 k 层的第 j 个六边形
   if (j == 1) a[i].x = a[i-1].x, a[i].y = a[i-1].y + 1;
   else
   {
       x = (j-1) / k;
       a[i].x = a[i-1].x + dec[x][0], a[i].y = a[i-1].y + dec[x][1];
   memset(flag, false, sizeof(flag));
   x = 12*k-6, cut = 0;
   for (u = i-1, v = 0; u)=1&v< x; u --, v ++)
       if (adj(a[u].x, a[u].y, a[i].x, a[i].y))
       {
           cut ++;
           flag[a[u].num] = true;
           if (cut == 3) break;
       }
   minn = 10001;
   for (u = 1; u < 6; u ++)
       if ((!flag[u])&&minn > cnt[u])
           minn = cnt[u];
           x = u;
   a[i].num = x;
   cnt[x] ++;
scanf ("%d", &x);
while (x --)
{
   scanf ("%d", &i);
   printf ("%d\n", a[i].num);
return 0;
```

#### 15.用一个给定半径的圆覆盖最多的点

```
//同半径圆的圆弧表示
#include <stdio.h>
#include <string.h>
#include <stdlib.h>
#include <math.h>
```

}

```
#define PI acos(-1.0)
struct Point
{
   double x, y;
}pt[2005];
double dis[2005][2005];
struct List
   double a;
   bool flag;
   int id;
}list[8005];
int cnt;
double Dis(int i, int j)
{
   double dx=pt[i].x-pt[j].x;
   double dy=pt[i].y-pt[j].y;
   return sqrt(dx*dx+dy*dy);
int Cmp(const void*p1, const void*p2)
{
   struct List*a1=(struct List*)p1;
   struct List*a2=(struct List*)p2;
   if (a1->a<a2->a)return -1;
   else if (a1->a==a2->a) return a1->id-a2->id;
   else return 1;
}
int main (void)
{
   int n, i, j, ans, num;
   double r, theta, delta, a1, a2;
   while (scanf("%d %lf",&n,&r)==2)
       if (n==0&&r==0.0) break;
       r=r+0.001;
       r=r*2.0;
       for (i=1;i<=n;i++)
           scanf("%lf %lf", &pt[i].x, &pt[i].y);
       for (i=1;i<n;i++)
           for (j=i+1;j<=n;j++)
               dis[i][j]=Dis(i, j);
               dis[j][i]=dis[i][j];
           }
       ans=0;
       for (i=1;i<=n;i++)
       {
           cnt=0;
           for (j=1;j<=n;j++)
```

```
if ((j!=i)&&(dis[i][j]<=r))</pre>
               {
                   theta=atan2(pt[j].y-pt[i].y, pt[j].x-pt[i].x);
                   if (theta<0.0) theta=theta+2.0*PI;</pre>
                   delta=acos(dis[i][j]/r);
                   a1=theta-delta;
                   a2=theta+delta;
                   list[++cnt].a=a1;
                   list[cnt].flag=true;
                   list[cnt].id=cnt;
                   list[++cnt].a=a2;
                   list[cnt].flag=false;
                   list[cnt].id=cnt;
           qsort(list+1,cnt,sizeof(struct List),Cmp);
           num=0;
           for (j=1;j<=cnt;j++)</pre>
               if (list[j].flag)
               {
                   num++;
                   if (num>ans) ans=num;
               else num--;
       }
       printf("It is possible to cover %d points.\n", ans+1);
    }
   return 0;
}
```

## 16.不等大的圆的圆弧表示

```
intersection_circle_circle(circle[i].center,
                                                  circle[i].r, circle[j].center,
circle[j].r, p1, p2);
                  a1= atan2(p1.y-circle[j].center.y, p1.x-circle[j].center.x);
                  if (a1<0.0) a1=a1+2.0*PI;
                  a2= atan2(p2.y-circle[j].center.y, p2.x-circle[j].center.x);
                  if (a2<0.0) a2=a2+2.0*PI;
                  if (a1>a2)
                  {
                      tmp=a1;
                      a1=a2;
                      a2=tmp;
                  }
                  mid=(a1+a2)/2.0;
                  xtest = circle[j].center.x +circle[j].r*cos(mid);
                  ytest = circle[j].center.y +circle[j].r*sin(mid);
                  if (!point_in_circle(xtest, ytest, i))
```

```
{
    circle[j].cnt++;
    circle[j].line[circle[j].cnt].s=0;
    circle[j].line[circle[j].cnt].t=a1;
    circle[j].line[circle[j].cnt].s=a2;
    circle[j].line[circle[j].cnt].t=2.0*PI;
}
else
{
    circle[j].cnt++;
    circle[j].cnt++;
    circle[j].line[circle[j].cnt].s=a1;
    circle[j].line[circle[j].cnt].t=a2;
}
```

# 17.矩形面积并

```
#include<stdio.h>
#include<string.h>
#include<stdlib.h>
#include<math.h>
struct Node
   int 1, r, cnt;
   double cover;
}node[80005];
struct Point
   double x;
   double y1, y2;
   int id_y1, id_y2, id_x;
   bool flag;
}pt[20005];
double y[20005];
int total, cnty;
int cmp1(const void*p1, const void*p2)
{
   double*a1=(double*)p1;
   double*a2=(double*)p2;
   if (*a1<*a2) return -1;
   else if (*a1==*a2) return 0;
   else return 1;
}
int cmp2(const void*p1, const void*p2)
{
   struct Point*a1=(struct Point*)p1;
   struct Point*a2=(struct Point*)p2;
   if (a1->x<a2->x) return -1;
   else if (a1->x==a2->x)
```

```
{
       if (a1->id_x<a2->id_x) return -1;
       else if (a1->id_x==a2->id_x) return 0;
       else return 1;
   else return 1;
}
int find(double target)
    int head=1, tail=cnty, mid;
   while (head<=tail)</pre>
    {
       mid=(head+tail)>>1;
       if (y[mid]==target) return mid;
       else if (y[mid]<target) head=mid+1;</pre>
       else tail=mid-1;
    }
   return 0;
}
void Build(int 1, int r, int s)
{
   node[s].l=1;
   node[s].r=r;
   node[s].cnt=0;
   node[s].cover=0.0;
   if (l+1<r)
   {
       int mid=(l+r)>>1;
       Build(1,mid,s<<1);</pre>
       Build(mid,r,(s<<1)+1);</pre>
    }
}
void Update(int s)
    if (node[s].cnt>0)
       node[s].cover=y[node[s].r]-y[node[s].1];
    else if(node[s].l+1==node[s].r)
       node[s].cover=0.0;
   else node[s].cover=node[s<<1].cover+node[(s<<1)+1].cover;</pre>
}
void Insert(int 1, int r, int s)
{
    if (l<=node[s].1&&node[s].r<=r)</pre>
    {
       node[s].cnt++;
       Update(s);
       return;
   if (node[s].l+1<node[s].r)</pre>
```

```
{
       int mid=(node[s].l+node[s].r)>>1;
       if (l<mid) Insert(l,r,s<<1);</pre>
       if (r>mid) Insert(l,r,(s<<1)+1);</pre>
       Update(s);
    }
}
void Delete(int 1, int r, int s)
   if (l<=node[s].1&&node[s].r<=r)</pre>
   {
       if (node[s].cnt>0)
           node[s].cnt--;
       Update(s);
       return;
   if (node[s].l+1<node[s].r)</pre>
    {
       int mid=(node[s].l+node[s].r)>>1;
       if (l<mid) Delete(l,r,s<<1);</pre>
       if (r>mid) Delete(l,r,(s<<1)+1);</pre>
       Update(s);
    }
}
int main (void)
   int n, i, j, countn=0;
   double ans;
   while (scanf("%d", &n)==1 && n)
       cnty=total=0;
       for (i=1;i<=n;i++)
           total++;
           scanf("%lf %lf", &pt[total].x, &pt[total].y1);
           pt[total].flag=true;
           pt[total].id_x=total;
           y[++cnty]=pt[total].y1;
           total++;
           scanf("%lf %lf", &pt[total].x, &pt[total].y2);
           pt[total].flag=false;
           pt[total].id_x=total;
           y[++cnty]=pt[total].y2;
           pt[total].y1=pt[total-1].y1;
           pt[total-1].y2=pt[total].y2;
       }
       qsort(y+1, cnty, sizeof(double), cmp1);
```

```
j=cnty;
       cnty=1;
       for (i=2;i<=j;i++)
           if (y[i]!=y[i-1])
               y[++cnty]=y[i];
       for (i=1;i<=total;i++)</pre>
           pt[i].id_y1=find(pt[i].y1);
           pt[i].id_y2=find(pt[i].y2);
       qsort(pt+1, total, sizeof(struct Point), cmp2);
       ans=0.0;
       Build(1,cnty,1);
       Insert(pt[1].id_y1, pt[1].id_y2, 1);
       for (i=2;i<=total;i++)</pre>
       {
           ans=ans+(pt[i].x-pt[i-1].x)*node[1].cover;
           if (pt[i].flag) Insert(pt[i].id_y1, pt[i].id_y2, 1);
           else Delete(pt[i].id_y1, pt[i].id_y2, 1);
       printf("%.0lf\n", ans+1e-10);
   return 0;
}
```

# 18.矩形的周长并

```
#include <stdio.h>
#include <string.h>
#include <stdlib.h>
struct Point
   int x, y;
}plist[10001];
struct Line
   int x, b, e, flag;
}llist[10001];
struct Item
   int y, id, idx;
}ilist[10001];
struct Node
{
   int l, r, c, m, line;
   bool lf, rf;
}node[40005];
```

```
int ys[10001];
int cmp1(const void*p1, const void*p2)
{
   struct Item *a1 = (struct Item*)p1;
   struct Item *a2 = (struct Item*)p2;
   return a1->y - a2->y;
}
int cmp2(const void*p1, const void*p2)
   struct Item *a1 = (struct Item*)p1;
   struct Item *a2 = (struct Item*)p2;
   return a1->id - a2->id;
}
int cmp3(const void*p1, const void*p2)
{
   struct Line *a1 = (struct Line*)p1;
   struct Line *a2 = (struct Line*)p2;
   return a1->x - a2->x;
void getm(int s)
{
   if (node[s].c > 0)
   {
       node[s].m = ys[node[s].r-1] - ys[node[s].l-1];
       node[s].line = 1;
       node[s].rf = node[s].lf = true;
   else if (node[s].r - node[s].l <= 1)
   {
       node[s].m = node[s].line = 0;
       node[s].rf = node[s].lf = false;
   }
   else
   {
       node[s].m = node[s << 1].m + node[(s << 1)+1].m;
       node[s].line = node[s<<1].line + node[(s<<1)+1].line;
       if (node[s<<1].rf && node[(s<<1)+1].lf) node[s].line --;</pre>
       node[s].lf = node[s << 1].lf;
       node[s].rf = node[(s<<1)+1].rf;
   }
}
void build(int 1, int r, int s)
{
   node[s].l = 1;
   node[s].r = r;
   node[s].c = node[s].line;
   if (node[s].r - node[s].l > 1)
   {
       int mid = (node[s].l + node[s].r)>>1;
```

```
build(1,mid,s<<1);</pre>
       build(mid,r,(s<<1)+1);
    }
}
void insert(int 1, int r, int s)
   if (1 <= node[s].1 && node[s].r <= r)</pre>
    {
       node[s].c ++;
       getm(s);
   if (node[s].r - node[s].l > 1)
   {
       int mid = (node[s].l + node[s].r)>>1;
       if (1 < mid) insert(1, r, s<<1);</pre>
       if (mid < r) insert(l, r, (s<<1)+1);</pre>
       getm(s);
    }
}
void delet(int 1, int r, int s)
{
   if (1 <= node[s].1 && node[s].r <= r)</pre>
   {
       node[s].c --;
       getm(s);
   if (node[s].r - node[s].l > 1)
   {
       int mid = (node[s].l + node[s].r)>>1;
       if (1 < mid) delet(1, r, s<<1);</pre>
       if (mid < r) delet(l, r, (s<<1)+1);</pre>
       getm(s);
    }
}
int main (void)
   int n, i, j, l, r, x1, y1, x2, y2, tot, p, ans;
   while (scanf ("%d", &n) == 1 \&\& n)
   {
       for (i = 0; i < n; i ++)
           scanf ("%d %d %d %d", &x1, &y1, &x2, &y2);
           1 = 2*i;
           r = 1 + 1;
           plist[1].x = x1;
            plist[1].y = y1;
           plist[r].x = x2;
            plist[r].y = y2;
```

```
ilist[1].y = y1;
   ilist[1].id = 1;
   ilist[r].y = y2;
   ilist[r].id = r;
}
tot = 2*n;
qsort(ilist, tot, sizeof(struct Item), cmp1);
ys[0] = ilist[0].y;
ilist[0].idx = 0;
j = 0;
for (i = 1; i < tot; i ++)
   if (ilist[i].y != ilist[i-1].y)
   {
       j ++;
       ys[j] = ilist[i].y;
   ilist[i].idx = j;
}
p = j + 1;
qsort(ilist, tot, sizeof(struct Item), cmp2);
for (i = 0; i < n; i ++)
{
   1 = 2*i;
   r = 1 + 1;
   llist[1].x = plist[1].x;
   llist[1].b = ilist[1].idx;
   llist[l].e = ilist[r].idx;
   llist[1].flag = 1;
   llist[r].x = plist[r].x;
   llist[r].b = ilist[l].idx;
   llist[r].e = ilist[r].idx;
   llist[r].flag = 0;
}
qsort(llist, tot, sizeof(struct Line), cmp3);
build(1,p,1);
insert(llist[0].b+1, llist[0].e+1,1);
int now_m = node[1].m, now_line = node[1].line;
ans = now_m;
for (i = 1; i < tot; i ++)
{
   if (llist[i].flag) insert(llist[i].b+1, llist[i].e+1, 1);
   else delet(llist[i].b+1, llist[i].e+1, 1);
   ans += (abs(node[1].m - now_m) + 2*(llist[i].x - llist[i-1].x)*now_line);
   now m = node[1].m;
   now_line = node[1].line;
}
```

```
printf ("%d\n", ans);
}
return 0;
}
```

#### 19.最近圆对

```
#include<iostream>
#include<stdlib.h>
#include<string.h>
#include<set>
#include <math.h>
using namespace std;
set <int>tree;
set <int>::iterator iter;
struct Point
{
   double x;
   int id, flag;
}p1[100001], p2[100001];
int tot1, tot2;
struct Q
   double x,y, r;
}q[50001];
int cmp(const void*p1, const void*p2)
{
   struct Point*a1=(struct Point*)p1;
   struct Point*a2=(struct Point*)p2;
   if (a1->x<a2->x) return -1;
   else if (a1->x==a2->x) return a2->flag-a1->flag;
   else return 1;
int cmp1(const void*p1, const void*p2)
{
   struct Q*a1=(struct Q*)p1;
   struct Q*a2=(struct Q*)p2;
   if (a1->y<a2->y)return -1;
   else if (a1->y==a2->y)return 0;
   else return 1;
double dis(double x1, double y1, double x2, double y2)
{
   return sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2));
bool judge(int i, int j, double d)
   if (dis(q[i].x, q[i].y, q[j].x, q[j].y)<=q[i].r+q[j].r+2.0*d)
       return true;
```

```
return false;
}
bool insert(int v,double d)
   iter = tree.insert(v).first;
   if (iter != tree.begin())
   {
       if (judge(v, *--iter,d))
           return true;
       ++iter;
   if (++iter != tree.end())
   {
       if (judge(v, *iter,d))
           return true;
   }
   return false;
bool remove(int v,double d)
{
   iter = tree.find(v);
   if (iter != tree.begin() && iter != --tree.end())
   {
       int a = *--iter;
       ++iter;
       int b = *++iter;
       if (judge(a, b,d))
           return true;
       }
   tree.erase(v);
   return false;
bool check(double d)
   int i=1, j=1;
   while (i<=tot1&&j<=tot2)</pre>
   {
       if (p1[i].x-d<=p2[j].x+d)</pre>
       {
           if (insert(p1[i++].id, d))
               return true;
       }
```

```
else
           if (remove(p2[j++].id, d))
              return true;
       }
   }
   while (i<=tot1)
   {
       if (insert(p1[i++].id, d))
           return true;
   }
   while (j<=tot2)
       if (remove(p2[j++].id, d))
           return true;
   return false;
}
int main (void)
{
   int cases, n, i;
   scanf("%d",&cases);
   while (cases--)
   {
       scanf("%d",&n);
       tot1=tot2=0;
       for (i=1;i<=n;i++)
           scanf("%lf %lf %lf",&q[i].x,&q[i].y, &q[i].r);
       qsort(q+1,n,sizeof(struct Q),cmp1);
       for (i=1;i<=n;i++)
       {
           tot1++;
           p1[tot1].x=q[i].x-q[i].r;
           p1[tot1].id=i;
           p1[tot1].flag=1;
           tot2++;
           p2[tot2].x=q[i].x+q[i].r;
           p2[tot2].id=i;
           p2[tot2].flag=-1;
       }
       qsort(p1+1,tot1,sizeof(struct Point),cmp);
       qsort(p2+1,tot2,sizeof(struct Point),cmp);
       double head=0.0, tail=dis(q[1].x,q[1].y,q[2].x,q[2].y)+1.0, mid;
       while (tail-head>1e-8)
       {
           tree.clear();
```

```
mid=(head+tail)/2.0;
    if (check(mid))
    {
        tail=mid;
    }
    else head=mid;
    }
    printf ("%.6lf\n",2.0*head);
}
    return 0;
}
```

## 20. 求两个圆的面积交

```
double area_of_overlap(point c1, double r1, point c2, double r2)
{
   double a = distance(c1, c2), b = r1, c = r2;
double cta1 = acos((a * a + b * b - c * c) / 2 / (a * b)),
     cta2 = acos((a * a + c * c - b * b) / 2 / (a * c));
   double s1 = r1*r1*cta1 - r1*r1*sin(cta1)*(a * a + b * b - c * c) / 2 / (a * b);
   double s2 = r2*r2*cta2 - r2*r2*sin(cta2)*(a * a + c * c - b * b) / 2 / (a * c);
   return s1 + s2;
}
                  21 半平面交(线段形式)
//poj 3525 Most Distant Point from the Sea
#include<cstdio>
#include<cmath>
#include<iostream>
#include<cstdlib>
#include<ctime>
#include<algorithm>
using namespace std;
const double eps = 1e-8;
const double pi = acos((double) (-1));
const double oo=1000000000000.0;
inline int dcmp(double a) //判断一个 double 型的符号
   if (fabs(a) < eps)
       return 0;
   if (a > 0)
       return 1;
   else
       return -1;
}
struct point
{
   double x, y;
```

```
int made;
   inline point(double _x = 0.0, double _y = 0.0)
   {
       x = _x;
       y = y;
   inline point operator -(const point &b) const
       return point(x - b.x, y - b.y);
   inline point operator +(const point &b) const
       return point(x + b.x, y + b.y);
   inline point operator | (const double &b) const
       return point(x * b, y * b);
   inline double operator ^(const point &b) const
       return x * b.y - y * b.x;
   inline double operator *(const point &b) const
   {
       return x * b.x + y * b.y;
   inline void input()
   {
       scanf("%lf%lf", &x, &y);
   }
};
struct Line
   point s,e;
   double k;
   Line(){}
   Line(point _s,point _e)
       s = _s; e = _e;
       k = atan2(e.y - s.y,e.x - s.x);
   point operator &(const Line &b)const//两直线交点
   {
       point res = s;
       double t = ((s - b.s)^(b.s - b.e))/((s - e)^(b.s - b.e));
       res.x += (e.x - s.x)*t;
       res.y += (e.y - s.y)*t;
       return res;
   }
```

```
};
//逆时针的有向直线!!
//半平面交,直线的左边代表有效区域
//****************
bool HPIcmp(Line a, Line b)
   if(fabs(a.k - b.k) > eps)return a.k < b.k;</pre>
   return ((a.s - b.s)^(b.e - b.s)) < 0;
}
Line Q[110];
void HPI(Line line[], int n, point res[], int &resn)//resn 为半平面交形成的凸包上的顶点
数 , res[]存放点
{
   int tot = n;
   sort(line,line+n,HPIcmp);
   tot = 1;
   for(int i = 1; i < n; i++)
       if(fabs(line[i].k - line[i-1].k) > eps)
           line[tot++] = line[i];
   int head = 0, tail = 1;
   Q[0] = line[0];
   Q[1] = line[1];
   resn = 0;
   for(int i = 2; i < tot; i++)</pre>
       if(fabs((Q[tail].e-Q[tail].s)^(Q[tail-1].e-Q[tail-1].s))
                                                                                   | |
                                                                           eps
fabs((Q[head].e-Q[head].s)^(Q[head+1].e-Q[head+1].s)) < eps)</pre>
           return;
       while(head < tail && (((Q[tail]&Q[tail-1]) - line[i].s)^(line[i].e-line[i].s)) >
eps)
           tail--;
        while(head < tail \&\& (((Q[head]\&Q[head+1]) - line[i].s)^{(line[i].e-line[i].s)) > 
eps)
           head++;
       Q[++tail] = line[i];
   while(head < tail && (((Q[tail] & Q[tail-1]) - Q[head].s)^(Q[head].e-Q[head].s)) > eps)
   while(head < tail && (((Q[head]&Q[head-1]) - Q[tail].s)^(Q[tail].e-Q[tail].e)) > eps)
       head++;
   if(tail <= head + 1)return;</pre>
   for(int i = head; i < tail; i++)</pre>
       res[resn++] = Q[i]&Q[i+1];
   if(head < tail - 1)</pre>
       res[resn++] = Q[head]&Q[tail];
point p[110];
Line line[110];
//*两点间距离
```

```
double dist(point a,point b)
{
   return sqrt((a-b)*(a-b));
}
void change(point a, point b, point &c, point &d, double p)//将线段 ab 往左移动距离 p
   double len = dist(a,b);
   double dx = (a.y - b.y)*p/len;
   double dy = (b.x - a.x)*p/len;
   c.x = a.x + dx; c.y = a.y + dy;
   d.x = b.x + dx; d.y = b.y + dy;
}
point pp[110];//答案, 逆时针, 编号 0--n-1!!
             **************
void solve(int n){
   double 1=0,r=100000;
   double ans=0;
   while(r-l>=eps)
   {//printf("**%.3f %.3f\n",1,r);
       double mid=(1+r)/2;
       for(int i=0;i<n;i++)</pre>
       {
          point t1,t2;
          change(p[i],p[(i+1)%n],t1,t2,mid);
          line[i]=Line(t1,t2);
       }
       int resn;
       HPI(line,n,pp,resn);
       //printf("%d***",resn);
       if(resn==0)//空集
          r=mid-eps;
       else
       {
          ans=mid;
           l=mid+eps;
       }
   printf("%.6f\n",ans);
}
int main(){
   int n;
   while(scanf("%d",&n),n){
       for(int i=0;i<n;i++)</pre>
          p[i].input();
       solve(n);
   }
   return 0;
}
```

#### 22 半平面交(方程形式)

```
#include<cstdio>
#include<cmath>
#include<iostream>
#include<cstdlib>
#include<ctime>
#include<algorithm>
using namespace std;
const double eps = 1e-16;
const double pi = acos((double) (-1));
const double oo=100000000000.0;
inline int dcmp(double a) //判断一个 double 型的符号
   if (fabs(a) < eps)</pre>
       return 0;
   if (a > 0)
       return 1;
   else
       return -1;
}
struct point
{
   double x, y;
   int made;
   inline point(double _x = 0.0, double _y = 0.0)
   {
       x = _x;
       y = _y;
   inline point operator -(const point &b) const
   {
       return point(x - b.x, y - b.y);
   inline point operator +(const point &b) const
   {
       return point(x + b.x, y + b.y);
   inline point operator | (const double &b) const
   {
       return point(x * b, y * b);
   inline double operator ^(const point &b) const
   {
       return x * b.y - y * b.x;
   inline double operator *(const point &b) const
   {
       return x * b.x + y * b.y;
```

```
}
   inline void input()
   {
       scanf("%lf%lf", &x, &y);
}p[115],tp[115],q[115];
struct Node{
   double u,v,w;
}z[105];
inline bool operator ==(const point &a, const point &b)
{
   return dcmp(a.x - b.x) == 0 && dcmp(a.y - b.y) == 0;
inline double len(point a) //向量的摸
{
   return sqrt(a * a);
}
//求交点
point Intersection(point p1,point p2,double a,double b,double c)
   double u = fabs(a*p1.x + b*p1.y + c);
   double v = fabs(a*p2.x + b*p2.y + c);
   point t;
   t.x = (p1.x*v + p2.x*u)/(u+v);
   t.y = (p1.y*v + p2.y*u)/(u+v);
   return t;
double Get_area(point p[],int n){
   double area=0;
   for(int i=2;i<n;i++)</pre>
       area+=(p[i]-p[1])^(p[(i+1)%n]-p[1]);
   return fabs(area)/2.0;
}
void Cut(double a,double b,double c,point p[],int &cnt){ //半平面切,逆时针切
// a*x+b*y+c<=0
 int tmp=0;
   for(int i=1;i<=cnt;i++){</pre>
       if(dcmp(a*p[i].x+b*p[i].y+c)<=0) tp[++tmp]=p[i];
       else{
           if(dcmp(a*p[i-1].x+b*p[i-1].y+c)<0)
               tp[++tmp]=Intersection(p[i-1],p[i],a,b,c);
           if(dcmp(a*p[i+1].x+b*p[i+1].y+c)<0)
               tp[++tmp]=Intersection(p[i+1],p[i],a,b,c);
       }
   for(int i=1;i<=tmp;i++)</pre>
       p[i]=tp[i];
   p[0]=p[tmp];p[tmp+1]=p[1];
   cnt=tmp;
```

```
}
int slove(int n,int idx){
   p[1].x=0;p[1].y=0;
   p[2].x=oo;p[2].y=0;
   p[3].x=oo;p[3].y=oo;
   p[4].x=0;p[4].y=oo;
p[0]=p[4];p[5]=p[1];
   int cnt=4;
   for(int i=0;i<n;i++){</pre>
       if(i==idx) continue;
       double a,b,c;
       a=(z[i].u-z[idx].u)/(z[idx].u*z[i].u);
       b=(z[i].v-z[idx].v)/(z[idx].v*z[i].v);
       c=(z[i].w-z[idx].w)/(z[idx].w*z[i].w);
       if(dcmp(a)>=0\&dcmp(b)>=0\&dcmp(c)>=0) return 0;
       Cut(a,b,c,p,cnt);
   }
   return dcmp(Get_area(p,cnt))!=0;
}
int main(){
   int n;
   while( scanf("%d",&n)!=EOF){
       for(int i=0;i<n;i++)</pre>
           scanf("%lf%lf",&z[i].u,&z[i].v,&z[i].w);
       for(int i=0;i<n;i++)</pre>
           puts(slove(n,i)?"Yes":"No");
   return 0;
```