

# HW1-Deep learning with Graphs

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## P1

Since the constant  $\beta$  shows the magnitude to have an easier case, consider  $\beta = 1$ . To skip divergency,  $I - \alpha A$  should not goes to zero because  $I - \alpha A \Rightarrow 0$  and  $(I - \alpha A)^{-1} \Rightarrow \infty$ . It happens when  $1 - \alpha a_1 = 0$  where  $a_1$  is the largest value of  $A$  because the matrix's treatment depends on the largest eigenvalue. So,  $1 - \alpha a_1 > 0$  and it means that  $\alpha < 1/a_1$ .

## P2

At the adjacency matrix  $A$ , we have  $d_i = \sum_j A_{ij}$  and  $d_j = \sum_i A_{ij}$  then in the row of  $i$  and  $j$  we can see how many connection exist between two noods it can be by  $A_i.A_j$  or  $ij$ -th entry of the  $A^2$  it means that  $[A^2]_{ij}$ .