



13. (3)  $\{4, 5\}$

(4)  $\{0, 1, 2, 3, 4, 5, 6, 8, 16, 32\}$

14. (1)  $\{3, 4, \{3, 4\}\}$

(2)  $\{3\}$

15. (1)  $\{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}, \{\emptyset, \{\emptyset\}\}\}$

(2)  $\{\emptyset\}$

16. (1)  $P(A) = \{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}, \{\{\emptyset\}, \{\{\emptyset\}\}\}\}$

$\sqcup P(A) = \{\{\emptyset\}, \{\{\emptyset\}\}\}$

(2)  $\sqcup A = \{\emptyset, \{\emptyset\}\}$

$P(\sqcup A) = \{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}, \{\{\emptyset\}, \{\{\emptyset\}\}\}\}$

17. (1)  $A - (B \cup C) = A \cap ((B \cup C)^c)$   
 $= A \cap (B^c \cap C^c)$   
 $= (A \cap B^c) \cap C^c = (A - B) - C$

(2)  $(A - B) - C = A \cap B^c \cap C^c$   
 $= (A \cap B^c \cap C^c) \sqcup \emptyset = (A \cap (B \cup C)^c) \sqcup (A \cap (B \cup C))$   
 $= (A \cap C^c) \cap (B \cup C)$   
 $= (A - C) \cap (B \cup C) = (A - C) - (B - C)$

18. (1)  $\forall x, x \in A \wedge x \notin B \Leftrightarrow x \in B$   
 $\Rightarrow \forall x, x \in B \Rightarrow x \notin B$   
 $\Rightarrow B = \emptyset \Rightarrow A = \emptyset \Rightarrow A = B = \emptyset$

(2)  $A - B = B - A$

$\therefore A \cap B = B \cap A$

$\therefore A \cap (B \cap B^c) = B \cap (A \cap A^c)$

$\therefore \emptyset = B - A$

$\therefore \forall x, x \in B \Rightarrow x \in A \wedge x \in A \Rightarrow x \in B$

$\therefore A = B$

19. (1)  $(A - B) \sqcup (A - C)$

$= (A \cap B^c) \sqcup (A \cap C^c)$

$= ((A \cap B) \sqcup A) \cap (A \cap (B \cup C)^c)$

$= A \cap A \cap B^c \cap C^c = A - (B \cap C) = A$

$\therefore A \cap (B \cap C) = \emptyset$

(2) 同(1)之理  $A - (B \cap C) = \emptyset$

$\therefore A \subseteq B \cap C$

26. (1)  $A \times B = (A - B) \sqcup (B - A) = \emptyset$

$\Leftrightarrow A - B = \emptyset \text{ 且 } B - A = \emptyset$

$\Rightarrow (\forall x, x \in A \Rightarrow x \in B) \wedge (\forall x, x \in B \Rightarrow x \in A)$

$\Rightarrow A = B$

(2)  $A = \emptyset \sqcup \emptyset = \emptyset$  即可

28. 记  $A_1 = \{x \mid x/2 \in \mathbb{Z}\}$   $A_2 = \{x \mid x/3 \in \mathbb{Z}\}$   
 $\wedge (x \in \mathbb{Z})$   $A_3 = \{x \mid x/5 \in \mathbb{Z}\}$   
 $\wedge (x \in \mathbb{Z})$

(1)  $|A_1| = \lfloor \frac{250}{2} \rfloor = 125$   $|A_2| = \lfloor \frac{250}{3} \rfloor = 83$

$|A_3| = \lfloor \frac{250}{5} \rfloor = 50$

$|A_1 \cap A_2| = 41$   $|A_2 \cap A_3| = 16$   $|A_1 \cap A_3| = 25$

$|A_1 \cap A_2 \cap A_3| = 8$   $\therefore |A_1 \sqcup A_2 \sqcup A_3| = 184$

