

## Statistics for Medicine

Massimo Borelli

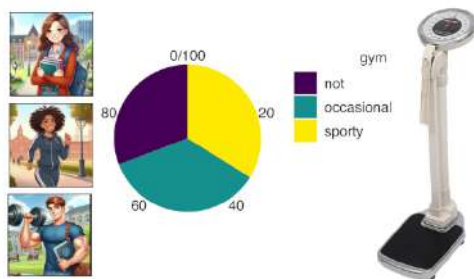
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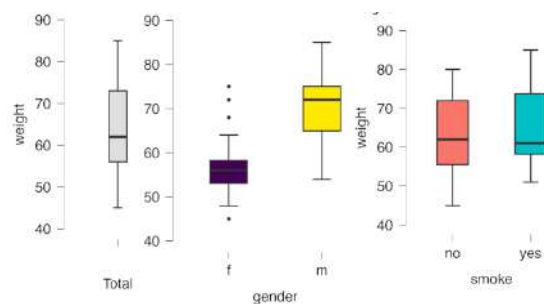
## Does gym activity predict weight? /1



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## key idea



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## Recap

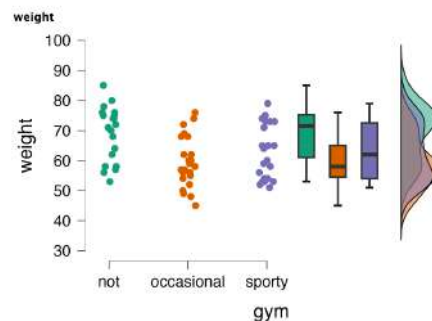
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## Does gym activity predict weight? /2

## Raincloud plots



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	weight	
Mean	63.523	
Variance	92.128	

	weight	
Mean	63.523	
Variance	92.128	

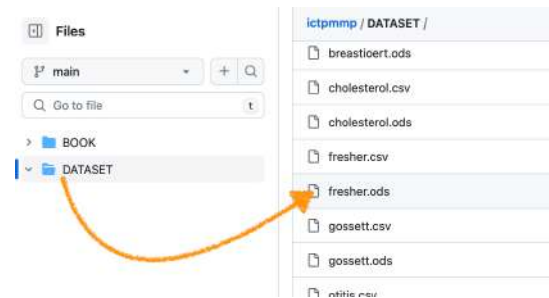
	weight	
gender	f	m
Mean	56.625	70.212
Variance	41.081	50.735

	weight	
smoke	no	yes
Mean	63.098	65.071
Variance	89.410	106.379

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## the fresher dataset



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## oh no!

## Independent Samples T-Test

The following problem(s) occurred while running the analysis:

- Number of factor levels is ≠ 2 in gym

Note: Student's t-test.

$$t = \frac{m_1 - m_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

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## the one-way Anova

- consider as a Fixed Factor the gym physical activity
  - ordered: not < occasional < sporty
- as Dependent Variable the weight

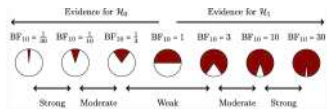
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# the one-way Anova

Cases	Sum of Squares	df	Mean Square	F	p
gym	1020.400	2	510.200	6.488	0.003
Residuals	4875.816	62	78.642		

Models	P(M)	P(M data)	BF <sub>M</sub>	BF <sub>10</sub>	error %
gym	0.500	0.933	<b>14.018</b>	1.000	
Null model	0.500	0.067	0.071	0.071	0.015



# the multiple comparison issue /1

Consider the following simulations:

a = rnorm(n = 30, mean = 0, sd = 1)  
b = rnorm(n = 30, mean = 0, sd = 1)  
c = rnorm(n = 30, mean = 6, sd = 1)

# the one-way Anova

Table: Post Hoc Comparisons - gym

		Mean Difference	SE	t	p <sub>Tukey</sub>
not	occasional	9.665	2.711	3.565	0.002
	sporty	6.373	2.740	2.326	0.060
occasional	sporty	-3.292	2.645	-1.245	0.432

Table: Post Hoc Comparisons - gym

		Prior Odds	Postrr Odds	BF <sub>10,U</sub>	error %
not	occsnl	0.587	21.169	36.039	4.422 × 10 <sup>-7</sup>
	sporty	0.587	1.313	2.236	0.008
occsnl	sporty	0.587	0.328	0.558	0.006

# the one-way Anova

## Normality assumptions

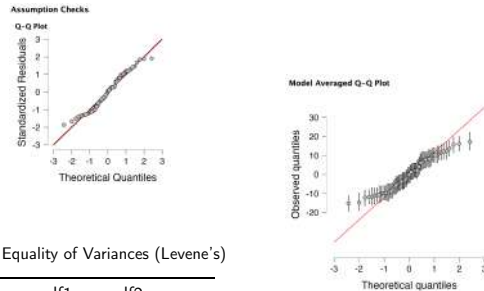
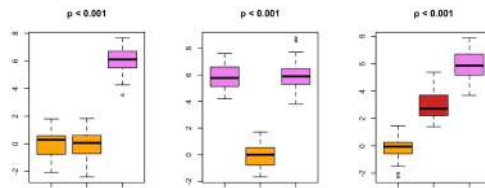


Table: Equality of Variances (Levene's)

F	df1	df2	p
0.470	2.000	62.000	0.627

# the multiple comparison issue /2



# the one-way Anova

## ALERT: very difficult with JASP

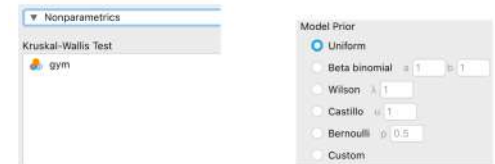
the tooth.ods dataset

? heteroskedasticity ?  
Can you detect wether il1b is a predictor of areainfl ?

explore one-way anova and look to raincloud plot

# the one-way Anova

## Nonparametric one-way Anova



# the multiple comparison issue /3

bad idea: to make multiple t-tests on all possible pairs of means

α = 0.05

$$1 - \left(1 - \frac{5}{100}\right) \cdot \left(1 - \frac{5}{100}\right) \cdot \left(1 - \frac{5}{100}\right) = 1 - \left(1 - \frac{5}{100}\right)^3 = 0.143$$

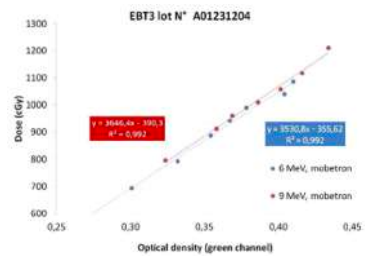
multiple tests increases the probability of a type-I error.

Carlo Bonferroni 'radical' solution (Bernoulli  $1 + nh < (1 + h)^n$ )  
n = 3 groups, n · (n - 1)/2 = 3 comparisons, then  
h = α/3 = 0.05/3 = 0.017.

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a calibration procedure

## classical linear regression

Table: classical linear regression - Fixed effects

Model		Unstndr	Std Err	Stndrd	t	p
H <sub>0</sub>	(Intercept)	63.523	1.191	53.357	< .001	
H <sub>1</sub>	(Intercept)	-83.891	16.677	-5.030	< .001	
	height	0.854	0.096	0.744	8.850	< .001

Table: Random component

Model	R	R <sup>2</sup>	Adjusted R <sup>2</sup>	RMSE
H <sub>0</sub>	0.000	0.000	0.000	9.598
H <sub>1</sub>	0.744	0.554	0.547	6.459

## toward statistical modelling

### ANTHROPOLOGICAL MISCELLANEA.

#### REGRESSION *towards* MEDIOCRITY *in* HEREDITARY STATURE.

By FRANCIS GALTON, F.R.S., &c.

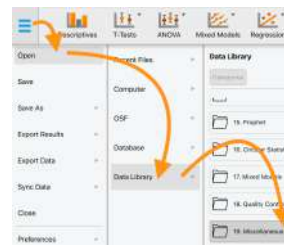
[WITH PLATES IX AND X.]

THIS memoir contains the data upon which the remarks on the Law of Regression were founded, that I made in my Presidential Address to Section H, at Aberdeen. That address, which will appear in due course in the Journal of the British Association, has already been published in "Nature," September 24th. I reproduce here

## diagnostic tools: why we need them

the Anscombe's Quartet

$$y = 0.5x + 3 ; R^2 = \frac{2}{3}$$



## the fresher.ods dataset

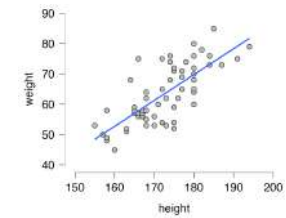


Table: Pearson's Correlations

Variable	height	...
weight	Pearson's r 0.744	...
	p-value < .001	...

## diagnostic tools

