$\Gamma_1$ 

Show that  $\tau(G) \leq 2 \mathrm{opt}(\mathrm{VCLP}(G))$  for all graphs G (including non-bipartite graphs).

*Proof.* From (2) we know that  $\tau(G) \leq 2\nu(G)$ . Since  $\nu(G) \leq \operatorname{opt}(\operatorname{MLP}(G)) \leq \operatorname{opt}(\operatorname{VCLP}(G))$ , it follows that  $\tau(G) \leq 2\nu(G) \leq 2\operatorname{opt}(\operatorname{VCLP}(G))$ .