

$$x_n = x_{n+m-1} \iff (a^{n-1} - 1)x_n + a^{n-2}b + \dots + ab + b = 0$$