$$\iff (a^{m-1} - 1)(x_n + (a - 1)^{-1}b) = 0$$