

Towards unconditionally E2E verifiable elections: the making of Demos remote e-voting system

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4th Crypto.Sec Day
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What makes a voting system reliable?



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- 2 **Privacy:** No one can learn how the voters have voted or control their free will.

Traditional elections



- 1 **Privacy** is achieved by voting in a booth and using anonymous ballots and envelopes.

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- 2 **Integrity** is **indirect** and relies on faith assumptions (conflict of interests, trust in state representatives, etc.).

Motivation for adopting Electronic voting (e-voting)

- Increasing political participation and representation among traditionally underrepresented groups.
- Cost-efficient and better administered elections.

Types of Electronic voting systems



On-site e-voting

Types of Electronic voting systems



On-site e-voting



Remote e-voting (i-voting)

Privacy in Electronic voting

- **Anonymity** of the votes is ensured via cryptographic primitives (mixnets, homomorphic encryption).
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- At on-site e-voting systems, voters are protected from **coercion** as in traditional elections. At remote e-voting systems, **coercion resistance** is a major challenge. Several solutions have been proposed (voting multiple times, misleading the coercer by using fake credentials or fake ballots).

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 - (ii). Recorded as cast.
 - (iii). Tallied as recorded.
- Any public auditor may verify the correct execution of the elections.

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An e-voting system that satisfies these properties is called

End-to-end (E2E) Verifiable

E2E Verifiable e-voting systems

On-site E2E Verifiable e-voting systems:

- Prêt à Voter [Chaum, Ryan & Schenider - 2005].
- Scantegrity II [Chaum et al. - 2009].

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Remote E2E Verifiable e-voting systems:

- Helios [Adida - 2008].
- Remotegrity [Zagorski et al. - 2013].
- *Demos* [Kiayias, Zacharias & Zhang - 2014].

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- Helios [Adida - 2008].
- Remotegrity [Zagorski et al. - 2013].
- *Demos* [Kiayias, Zacharias & Zhang - 2014].

Demos is the only remote e-voting proven E2E verifiable in the [standard model](#) (does not assume the existence of an external truly random source).

The making of Demos remote e-voting system

The security framework

- We consider a single Election Authority (EA) that controls the whole system (all authorities and the voter clients are potentially corrupted and colluding).
- Our aim is **E2E Verifiability** in the standard model in the case that EA **and** a constant fraction of the voters is malicious.
- We require **Voter Privacy** against anyone but the Election Authority.

Code-voting 101

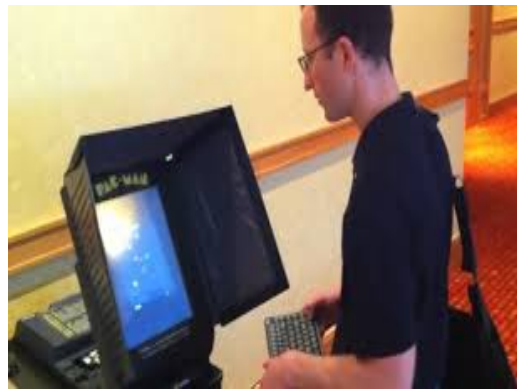
**Election
Authority**



Candidate	Vote-code
Alice	AAAA-1111
Bob	BBBB-2222
Charlie	CCCC-3333
David	DDDD-4444

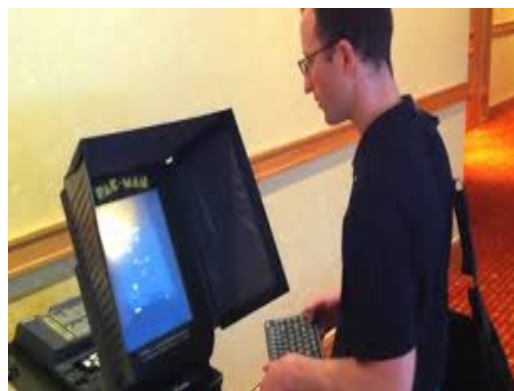
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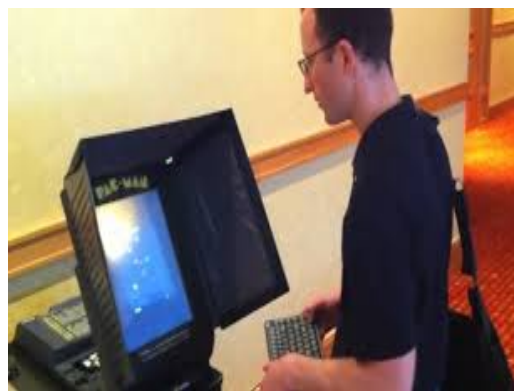
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The described e-voting system is simple and easy. Is it reliable?

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- **Integrity** of the system can be verified only at the minimum level.
 - The voters know that their vote was *cast-as-intended* by submitting the vote-code that corresponds to the candidates of their choice.
 - The voters cannot verify that their was *recorded-as-cast* (the vote-code could be not be accepted or altered due to system failure without any notice).
 - No audit information is published by the Election Authority, so the voters can verify that their vote was *tallied-as-recorded* or some party can verify the correct execution of the election.

Taking a step further: proving correct record of the votes

Election
Authority



Candidate	Vote-code	Receipt
Alice	AAAA-1111	REC1
Bob	BBBB-2222	REC2
Charlie	CCCC-3333	REC3
David	DDDD-4444	REC4

Ballot No. 100

Taking a step further: proving correct record of the votes

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Each vote-code is paired with a (pseudo) randomly generated receipt.

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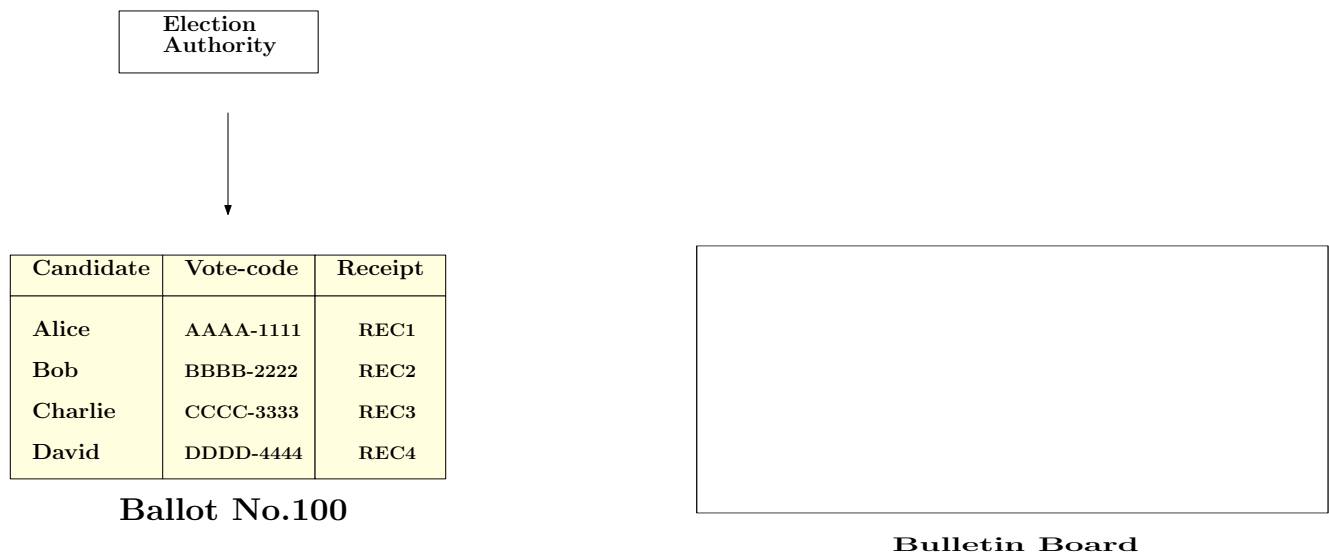
REC1

**Election
Authority**

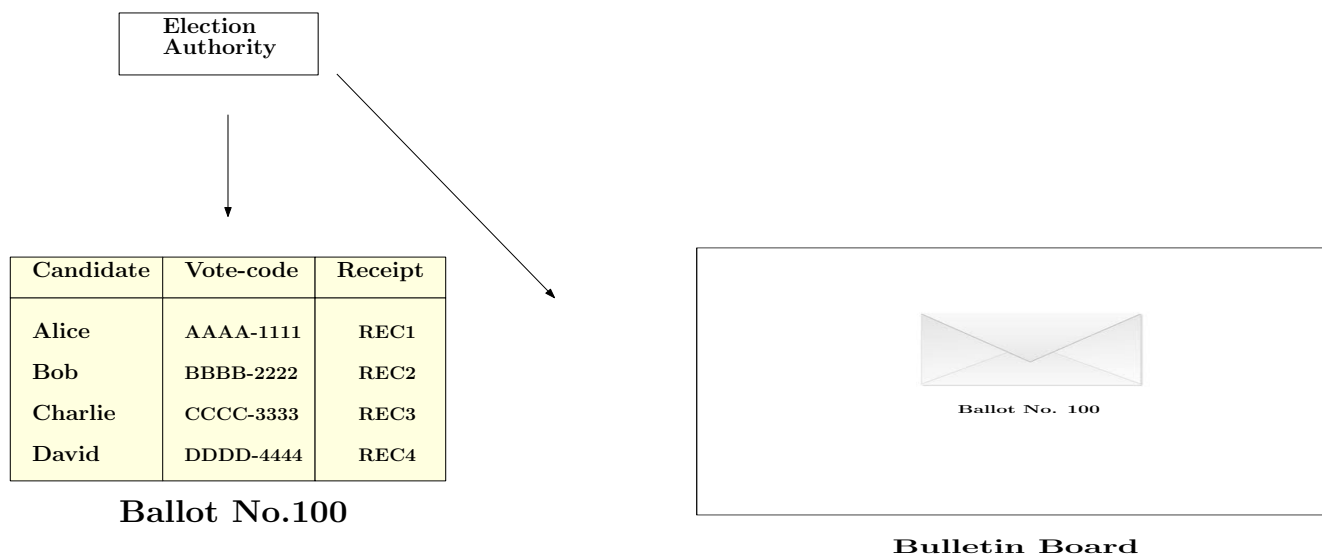
What do we gain using receipts

- Privacy remains at the same levels since including random receipts does not leak any information about the vote-code and candidate correspondence.
- The voters can verify that their vote was cast-as-intended **and** that it was recorded-as-cast (the only way that the system may reply with the correct receipt is that they read the correct vote-code).
- **Still**, lack of further audit information does not make any further verification possible (that the recorded vote was counted-as-intended and the election was executed properly).

Enabling audit: introducing the Bulletin Board



Enabling audit: introducing the Bulletin Board



What we gain by using the Bulletin Board

- After voting ends, EA announces the result and opens the envelopes, so audit can be performed.
- The use of an electronic envelope prevents a malicious EA from posting audit information which is inconsistent.
- The electronic envelope is realised by a perfectly **binding**, computationally **hiding** and **additively homomorphic commitment scheme** $\text{Com}(\cdot)$.

Exploiting the properties of a commitment scheme

The “envelope” effect:

- (i). **Binding**: EA cannot open $\text{Com}(m)$ to a message other than m , so the audit information is perfectly consistent.
- (ii). **Hiding**: Any PPT algorithm that does not have the opening key cannot read m from $\text{Com}(m)$, so sensitive information about the voters' ballots is not leaked.

Exploiting the properties of a commitment scheme

Computing the tally in a verifiable way:

(iii). **Additively homomorphic:**

$$\text{Com}(m_1) \cdot \text{Com}(m_2) = \text{Com}(m_1 + m_2)$$

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Computing the tally in a verifiable way:

(iii). Additively homomorphic:

$$\text{Com}(m_1) \cdot \text{Com}(m_2) = \text{Com}(m_1 + m_2)$$

- The EA encodes the candidates in “message” format and posts the pairs of vote-codes and encoded candidates in committed form.
- The EA opens all vote-code commitments and marks all the cast vote-codes and the commitments that are associated with them.
- The EA multiplies all the marked commitments, opens the result and posts the openings in the Bulletin Board (BB).
- Due to the binding property, anyone can verify that these computations were done correctly.

Example

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$$\begin{aligned} \text{Com}(\langle \text{Alice} \rangle) \cdot \text{Com}(\langle \text{Alice} \rangle) \cdot \text{Com}(\langle \text{Bob} \rangle) &= \\ &= \text{Com}(2 \cdot \langle \text{Alice} \rangle + \langle \text{Bob} \rangle). \end{aligned}$$

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- EA posts the encoded result $2 \cdot \langle \text{Alice} \rangle + \langle \text{Bob} \rangle$, which is decoded as $\langle \text{Alice} : 2, \text{Bob} : 1, \text{Charlie} : 0, \text{David} : 0 \rangle$.

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We have to enhance the system with verification mechanisms that prevent a malicious EA from committing inconsistently.

Fixing the first weakness...

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Finalization of the construction of Demos: introducing the use of double ballots

Election
Authority

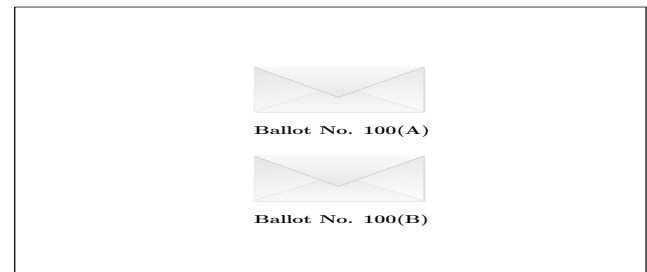


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Ballot No.100(A)

Candidate	Vote-code	Receipt
Alice	EEEE-5555	REC5
Bob	FFFF-6666	REC6
Charlie	GGGG-7777	REC7
David	HHHH-8888	REC8

Ballot No.100(B)



Bulletin Board

Voting with double ballots

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Ballot No.100(A)

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Ballot No.100(B)



No. 100
AAAA-1111
Open (B)

Election
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Ballot No.100(B)



**Election
Authority**

Voting with double ballots

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Ballot No.100(B)



REC1

Election
Authority

What we gain by using double ballots

Privacy preservation:

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Integrity:

- The EA cannot know in advance which side the voter is going to use, so any malicious behaviour will be detected with probability $1/2$ by the voter.
- If the EA attempts to alter t ballots, it will be caught with probability $1 - (1/2)^t$.
- Assuming a large enough number of voters, we verify that almost all votes have been counted correctly with high probability.

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By injecting 1000 votes for Alice, EA could change the result significantly with 50% probability (the invalid encoding is not in the side of the ballot used for audit).

Fixing the last weakness

- 1 The voters can verify that the EA has not committed to a different vote-code and candidate correspondence at setup.
- 2 Anyone can verify that the commitments correspond to well-formed ballots, i.e. one commitment per (encoded) candidate in every side of all ballots.

Fixing the last weakness

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- ZK soundness requires a source of **true randomness** that could come from an external source (assuming a random oracle or a randomness beacon) **but...**
- We promised E2E verifiability in the **standard model for the first time**.

ZK soundness via human interaction

- When an honest voter chooses which side (A or B) she will use to vote, she concurrently inserts **1 bit of randomness** in the system by flipping a coin. This bit is public and cannot be altered by a malicious EA without being detected.

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- Assuming that a small fraction of the voters are not corrupted and vote successfully, we can extract **true randomness** from the voters' choice and apply it to the verification of the ZK proofs.

Overview of the construction of Demos

- 1 We generate code-based ballots for a private and simple voting procedure from the voters' side.
- 2 We associate the vote-codes with receipts, so that the voters are sure that their vote was accepted by the system.
- 3 We introduce a public BB, that contains all necessary audit information, consistently committed by the EA.
- 4 We provide the voters with double ballots, so that they can choose one side of the ballot to vote and the other to audit the election without revealing their votes.
- 5 We use the voters' coin flips to extract true randomness for the ZK proofs, thus maintaining Demos E2E verifiable in the standard model.



Activities of the FINER research team: Implementation of Demos and the European Elections 2014 experiment

The FINER research team members

Professors:

Alex Delis (DI&T), Aggelos Kiayias (DI&T), Charalampos Koutalakis (DPS&PA), Elias Nikolakopoulos (DPS&PA), Mema Roussopoulou (DI&T), Georgios Sotirellis (DPS&PA)

Postdoctoral researchers:

Foteini Baldimtsi (DI&T), Pavlos Vasilopoulos (DPS&PA), Bingsheng Zhang (DI&T)

PhD students:

Konstadina Gavatha (DPS&PA), Lampros Paschos (DPS&PA), Thomas Zacharias (DI&T)

The FINER project is funded by the General Secretariat of Research and Technology of Greece (2013-15).

Implementation of Demos by **Bingsheng Zhang**

- The server is implemented in *Django*.
- We implement Elliptic Curve ElGamal using the fastest elliptic curve crypto library *MIRACL*.
- We support ballot distribution in three ways: via CAS, paper or email.

The European Elections 2014 experiment



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The European Elections 2014 experiment

- Two groups performed parallel pilot runs of Demos into two different polling places (Ilioupoli & Chalandri).
- The goal of the experiment was (i) to get the voters familiar with Demos and (ii) test the current implementation.
- The participants (747 in total) were issued paper ballots (one side of the double ballot was printed in one side of the paper) that contained a QR code in each side.
- The QR codes were scanned by the cameras of the tablets (two for each station) and the participants were prompted in a user-friendly (web page) environment to vote.
- After voting, the participants filled in a questionnaire.

The European Elections 2014 experiment

- A paper with the analysis of the results of the experiment under the title:
“Pressing the Button for European Elections 2014: Public Attitudes towards Verifiable E-Voting In Greece”
is accepted at the upcoming EVOTE2014 conference.
- The above paper and the election result of our experiment can be found in our website:

[http : //www.demos – voting.com](http://www.demos-voting.com)



Thank you!

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