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硕士学位论文

高维因子模型的极大似然分析的理论与方法

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High-dimension Factor Model

by

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in

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of

Hunan University

Supervisor

Professor LI, Si

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湖南大学

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摘 要

在过去的20年里，经济学见证了经济统计工作的飞跃发展。

关键词：高维分位数因子模型

Abstract

In order to investigate the dynamic connectedness among the four variables...

Key Words: High-dimension factor model

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附录A 抽样算法

A.1 算法细节

引理 A.1 令 $N_{t+1} = \text{Var}(y_{t+1}|y^{0,t}, x_t, \mathbb{K}^{1,t+1})$ 。于是,

$$N_{t+1} = h'_{t+1} \tilde{\Gamma}_{t+1} \tilde{\Gamma}'_{t+1} h_{t+1} + G_{t+1} G'_{t+1} \quad (\text{A.1})$$

$$\mathbb{E}(y_{t+1}|y^{0,t}, x_t, \mathbb{K}^{1,t+1}) = g_{t+1} + h'_{t+1} (f_{t+1} + F_{t+1} x_t) \quad (\text{A.2})$$

$(x_{t+1}|y^{0,t+1}, x_t, \mathbb{K})$ 的均值和方差为:

$$\mathbb{E}(x_{t+1}|y^{0,t+1}, x_t, \mathbb{K}) = a_{t+1} + A_{t+1} x_t + B_{t+1} y_{t+1} \quad (\text{A.3})$$

$$\text{Var}(x_{t+1}|y^{0,t+1}, x_t, \mathbb{K}) = C_{t+1} C'_{t+1} \quad (\text{A.4})$$

其中,

$$a_{t+1} = (I - B_{t+1} h'_{t+1}) f_{t+1} - B_{t+1} g_{t+1} \quad (\text{A.5})$$

$$A_{t+1} = (I - B_{t+1} h'_{t+1}) F_{t+1} \quad (\text{A.6})$$

$$B_{t+1} = \tilde{\Gamma}_{t+1} \tilde{\Gamma}'_{t+1} h_{t+1} N_{t+1}^{-1} \quad (\text{A.7})$$

$$C_{t+1} C'_{t+1} = \tilde{\Gamma}_{t+1} \tilde{\Gamma}'_{t+1} - B_{t+1} N_{t+1} B'_{t+1} \quad (\text{A.8})$$

假设,

$$x_{t+1} = a_{t+1} + A_{t+1} x_t + B_{t+1} y_{t+1} + C_{t+1} z_{t+1} \quad (\text{A.9})$$

其中, $z_{t+1}|\mathbb{K} \sim \mathcal{N}(0, I)$ 独立于 x_t 和 y_{t+1} 。 \square

证明:

$$\begin{aligned} \text{Cov}(x_{t+1}, y_{t+1}) &= \mathbb{E}[(x_{t+1} - \mathbb{E}(x_{t+1}|\mathbb{K}))(y_{t+1} - \mathbb{E}(y_{t+1}|\mathbb{K}))'] \\ &= \mathbb{E}\{[B_{t+1}(y_{t+1} - \mu_{y_{t+1}}) + C_{t+1} z_{t+1}](y_{t+1} - \mu_{y_{t+1}})'\} \\ &= B_{t+1} N_{t+1} \end{aligned}$$

$$\begin{aligned} \text{Cov}(x_{t+1}, y_{t+1}) &= \text{Cov}(x_{t+1}, g_{t+1} + h'_{t+1} x_{t+1} + G_{t+1} u_{t+1}) \\ &= \mathbb{E}[(x_{t+1} - \mu_{x_{t+1}})((x_{t+1} - \mu_{x_{t+1}})' h_{t+1} + u'_{t+1} G'_{t+1})] \\ &= \tilde{\Gamma}_{t+1} \tilde{\Gamma}'_{t+1} h_{t+1} \end{aligned}$$

$$B_{t+1} = \tilde{\Gamma}_{t+1} \tilde{\Gamma}'_{t+1} h_{t+1} N_{t+1}^{-1} \quad (\text{A.10})$$

显然,

$$\begin{aligned} C_{t+1}C'_{t+1} &= \text{Var}_{t+1}(x|y) = \tilde{\Gamma}_{t+1}\tilde{\Gamma}'_{t+1} - B_{t+1}N_{t+1}N_{t+1}^{-1}N_{t+1}B'_{t+1} \\ &= \tilde{\Gamma}_{t+1}\tilde{\Gamma}'_{t+1} - B_{t+1}N_{t+1}B'_{t+1} \end{aligned} \quad (\text{A.11})$$

$$\begin{aligned} x_{t+1} &= a_{t+1} + A_{t+1}x_t + B_{t+1}(g_{t+1} + h'_{t+1}x_{t+1} + G_{t+1}\mu_{t+1}) \\ &= a_{t+1} + A_{t+1}x_t + B_{t+1}g_{t+1} + B_{t+1}h'_{t+1}f_{t+1} + B_{t+1}h'_{t+1}x_t + B_{t+1}h'_{t+1}\tilde{\Gamma}_{t+1}v_{t+1} + B_{t+1}G_{t+1}\mu_{t+1} \\ &= f_{t+1} + F_{t+1}x_t + \tilde{\Gamma}_{t+1}v_{t+1} \end{aligned}$$

因此,

$$\begin{aligned} A_{t+1} + B_{t+1}h'_{t+1}F_{t+1} &= F_{t+1} \\ a_{t+1} + B_{t+1}g_{t+1} + B_{t+1}h'_{t+1}f_{t+1} &= f_{t+1} \end{aligned}$$

□

表 A.1 混合分布中对应的七个正态分布的参数

ω	$q_j = \Pr\{\omega = j\}$	m_j	v_j^2
1	0.00730	-10.12999	5.79596
2	0.10556	-3.97281	2.61369
3	0.00002	-8.56686	5.17950
4	0.04395	2.77786	0.16735
5	0.34001	0.61942	0.64009
6	0.24566	1.79518	0.34023
7	0.25750	-1.08819	1.26261

* 来源: Kim 等 (1998)

附录A.2 后验分布

本节将介绍部分参数的后验分布。

附录B 发表论文和参加科研情况说明

（一）发表的学术论文

[1]

（二）申请及已获得的专利（无专利时此项不必列出）

[1] XXX, XXX. XXXXXXXXXX: 中国, 1234567.8[P]. 2012-04-25.

（三）参与的科研项目

[1] XXX, XXX. XX 信息管理与信息系统, 国家自然科学基金项目.课题编号: XXXX.

致 谢