



$$\begin{aligned}
 &P(\text{HIV} | \text{tested +ve}) \\
 &= \frac{P(\text{HIV and testing +ve})}{P(\text{testing +ve})} \\
 &= \frac{0.259 \times 0.997}{0.259 \times 0.997 + 0.741 \times 0.074} = 0.8247
 \end{aligned}$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

If A and B are independent

$$P(A \text{ and } B) = P(A) \times P(B)$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$= \frac{P(A) \times P(B)}{P(B)}$$

$$P(A|B) = P(A)$$

Probability of Success

$$p = 0.1 \quad q = 1 - 0.1$$

$$x = 1 \quad n = 5 \quad = 0.9$$

$$P(X=1) = {}^n C_x p^x (1-p)^{n-x}$$
$$= {}^5 C_1 (0.1)^1 (0.9)^{5-1}$$

$$= \frac{5!}{1! (5-1)!} (0.1) (0.9)^4$$

$$= \frac{5 \times \cancel{4!}}{\cancel{4!}} (0.1) (0.9)^4$$

probability student passes
a course = 0.82

total students = $n = 8$

Probability that all 8 will
pass the class

$$\text{failing probability} = 1 - 0.82 = 0.18$$
$${}^8_8 (0.82)^8 (0.18)^{8-8}$$

\Rightarrow

Probability that none will pass

$${}^8_0 (0.82)^0 (0.18)^{8-0}$$

Probability that atleast 6 students
will pass the course

$$P(X=6) + P(X=7) + P(X=8)$$

$${}^8C_6 (0.82)^6 (0.18)^2 + {}^8C_7 (0.82)^7 (0.18)^1$$

$$+ {}^8C_8 (0.82)^8 (0.18)^0$$

=

Probability that atmost 2 students
will pass the exam

$$P(X=0) + P(X=1) + P(X=2)$$

$${}^8C_0 (0.82)^0 (0.18)^8 + {}^8C_1 (0.82)^1 (0.18)^7$$

$$+ {}^8C_2 (0.82)^2 (0.18)^6$$

=

Probability a fuse is defective
 $= 0.1$

Probability of failure $= 1 - 0.1$
 $= 0.9$

1st defective fuse on first
test $= 0.1$

1st defective fuse on the second
test 0.9×0.1

1st defective fuse on the third
test $0.9 \times 0.9 \times 0.1$