

Consider a guessing game with ten players, numbered 1 through 10. Simultaneously and independently, the players select integers between 0 and 10. Thus player i 's strategy space is $S_i = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$, for $i = 1, 2, \dots, 10$. The payoffs are determined as follows: First, the average of the players' selections is calculated and denoted a . That is,

$$a = \frac{s_1 + s_2 + \dots + s_{10}}{10},$$

where s_i denotes player i 's selection, for $i = 1, 2, \dots, 10$. Then, player i 's payoff is given by $u_i = (a - i - 1)s_i$. What is the set of rationalizable strategies for each player in this game?

$$\begin{aligned} \max a &= 100/10 = 10 \\ \min a &= 0/10 = 0 \end{aligned}$$

$$\begin{aligned} \max u &= a - 10 - 1 = a - 11 \rightarrow \text{negative} \\ \min u &= a - 1 - 1 = a - 2 \rightarrow \text{maybe negative} \end{aligned}$$

If everyone chooses 0, Final Payoff is non-negative