

Passed Solution Review

5. This exercise explores how, in a mixed-strategy equilibrium, players must put positive probability only on best responses. Consider the game in the following figure.

$$\begin{aligned} x > 1 &\rightarrow x = 2 \\ x < 1 &\rightarrow x = 1 \end{aligned}$$

		2		
1		L	M	R
	U	x, x	$x, 0$	$x, 0$
	C	$0, x$	$2, 0$	$0, 2$
	D	$0, x$	$0, 2$	$2, 0$

Compute the pure-strategy and mixed-strategy Nash equilibria for this game, and note how they depend on x . In particular, what is the difference between $x > 1$ and $x < 1$?

For both $x > 1$ and $x < 1$, $NE = (U, L)$. When $x < 1$ there is also $\{(0, 1, 1), (0, 1, 1)\}$ unless $x > 2$

This whole question is very confusing if $x \geq 2$ or $x \leq 0$

If all three played... $\pi_1 = \pi_2 = (1-x, 1/2, 1/2)$
 \uparrow
 symmetric game

If $x < 0$, U, L is dominated which forces $\pi_1 = \pi_2 = (0, 1/2, 1/2)$

If $0 \leq x \leq 1$, U, L is pure eq and $(1-x, x/2, x/2)$ is mixed

I initially had the basis, but did not consider all cases