

$$Y = \beta_0 + \beta_1 x$$

$y$  = dependent variable

$\beta_0$  =  $y$  intercept

$\beta_1$  = slope (change in  $y$  for unit change in  $x$ )

$x$  = independent variable

### Assumptions

- 1)  $y$  given  $x$  is normally distributed
- 2) observations need to be independent
- 3)  $E(\epsilon) = 0$
- 4)  $\epsilon$  and  $x$  are not correlated

### Goodness of fit

$R^2$  = Coefficient of Determination

$R^2 = SSR / SST$  = total variation explained by the model

$0 \leq R^2 \leq 1 \rightarrow$  can be a %

$$\text{Wage} = \beta_0 + \beta_1(\text{educ}) + \epsilon$$

Wage = annual salary

educ = # of years of education

$\beta_1$  = effect of educ on wage while all other factors are constant

$\epsilon$  = all other factors that affect wage

$$\text{Wage} = \beta_0 + \beta_1(\text{educ}) + \beta_2(\text{experience}) + \beta_3(\text{skills}) + \epsilon$$

MLR = multiple linear regression

In MLR, all  $x$  variables should not be correlated

Consumption and income

$$\text{Consumption} = \beta_0 + \beta_1(\text{income}) + \beta_2(\text{income})^2 + \epsilon$$

$$x_1 = \text{income} \quad x_2 = \text{income}^2$$

$$\Delta \text{cons} / \Delta \text{inc} = \beta_1 + 2\beta_2(\text{income})$$

### Generalized Form of MLR

#### Assumptions

- 1)  $y$  given  $x_i$  is normally distributed
- 2) observations are independent
- 3) No perfect collinearity between  $x$  values
  - a) none of the independent variables are constant
  - b) no linear relationship among the independent variables
- 4)  $E(\epsilon | x_1, x_2, \dots, x_i) = 0$
- 5) Homoskedasticity  $\rightarrow \text{Var}(\epsilon | x_1, x_2, \dots, x_i) = \sigma^2$