

The Social Discount Rate

$w_t = \text{weights} \rightarrow NPV = \sum_{t=0}^{\infty} w_t NSB_t$
 \downarrow social discount factors

$w_t = 1/(1+r)^t$
 \downarrow $r = \text{real social discount rate}$

Weights generally decline over time

$w_t = w_{t-1}/(1+r)$ where $t > 0$ and $w_0 = 1$

To determine r :

- 1) social opportunity cost of capital (SOC) \rightarrow descriptive
- 2) social time preference (STP) \rightarrow prescriptive

10.1 Does the choice of Discount Rate matter?

yes!

10.2 When there's no doubt about the value of the social discount rate

time preference

marginal rate of time preference (MTRP)

10.2.1 Individual marginal rate of time preference

money now or later?

10.2.2 Equality of MTRPs and market rates in perfect markets

$C = \text{consumption}$ $i = \text{interest rate}$ $T = \text{PV of } \$$

$$\max U(C_1, C_2) \text{ s.t. } C_1 + C_2/(1+i) = T$$

marginal rate of substitution (MRS)

10.2.3 Equality of social rate of time preference and the return on investment in imperfect markets

social indifference curves

10.2.4 Complications in real economics

consumption rate of interest (CRI)

10.3 The social opportunity of cost of capital (SOC) method

$$SOC = (a \cdot CRI) + (b \cdot ROI)$$

10.3.1 Special cases of the SOC

10.3.2 Estimation of, and numerical values for, the SOC

10.4 The social time preference (STP) method

10.4.1 The Ramsey formula

$W = \text{social welfare}$

$$W = \int_0^{\infty} e^{-\rho t} U(c_t) dt$$

$U(c_t) = \text{utility from per capita consumption during period } t$

$e^{-\rho t} = \text{discount factor}$

$\rho = \text{future utility discount rate}$

$$STP = \rho + g\epsilon$$

$g = \% \Delta \text{ in per-capita consumption}$
 $\epsilon = \text{elasticity of marginal utility}$

10.4.2 Estimation of, and numerical values for, the STP

10.4.3 Special case for STP: shadow price of capital (SPC)

consumption equivalents

$$SPC = ROI / STP$$

10.4.4 Numerical values of the SPC

10.5 Discounting intergenerational projects

hyperbolic discounting

10.6 the social discount rate in practice