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 Dis 2A

SECTION 2.6

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$$\frac{\partial(\ln(xy) + x^2y^3)}{\partial x}$$

$$\Rightarrow \left(\frac{1}{x} + 2xy^3\right)dx$$

$$\frac{\partial(\ln(xy) + x^2y^3)}{\partial y}$$

$$\Rightarrow \left(\frac{1}{y} + 3x^2y^2\right)dy$$

$$dF = \left(\frac{1}{x} + 2xy^3\right)dx + \left(\frac{1}{y} + 3x^2y^2\right)dy$$

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$$\frac{\partial(\tan^{-1}(\frac{x}{y}) + y^4)}{\partial x}$$

$$\Rightarrow \left(\frac{y}{x^2 + y^2}\right)dx$$

$$\frac{\partial(\tan^{-1}(\frac{x}{y}) + y^4)}{\partial y}$$

$$\Rightarrow \left(-\frac{x}{x^2 + y^2} + 4y^3\right)dy$$

$$dF = \left(\frac{y}{x^2 + y^2}\right)dx + \left(-\frac{x}{x^2 + y^2} + 4y^3\right)dy$$

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$$\phi(u, v) = \int \frac{2u}{u^2 + v^2} du + g(v)$$

$$= \ln|v^2 + u^2| + g(v)$$

$$\frac{\partial \phi}{\partial v} = \frac{2v}{v^2 + u^2} + g'(v)$$

$$\Rightarrow g'(v) = 0 \Rightarrow g(v) = C$$

$$\phi(u, v) = \ln|v^2 + u^2| + C$$