

初期条件より

$$x_1(0) = \frac{A_1}{\sqrt{2}} \sin \phi_1 + \frac{A_2}{\sqrt{2}} \sin \phi_2 = 0 \quad \dots (1)$$

$$x_2(0) = \frac{A_1}{\sqrt{2}} \sin \phi_1 - \frac{A_2}{\sqrt{2}} \sin \phi_2 = 0 \quad \dots (2)$$

$$\dot{x}_1(0) = \frac{A_1 \omega_1}{\sqrt{2}} \cos \phi_1 + \frac{A_2 \omega_2}{\sqrt{2}} \cos \phi_2 + \frac{rP}{2} \left( \frac{1}{\omega_1^2 - p^2} + \frac{1}{\omega_2^2 - p^2} \right) = 0 \quad \dots (3)$$

$$\dot{x}_2(0) = \frac{A_1 \omega_1}{\sqrt{2}} \cos \phi_1 - \frac{A_2 \omega_2}{\sqrt{2}} \cos \phi_2 + \frac{rP}{2} \left( \frac{1}{\omega_1^2 - p^2} - \frac{1}{\omega_2^2 - p^2} \right) = 0 \quad \dots (4)$$

$$(1) + (2) \text{ より } \frac{2}{\sqrt{2}} A_1 \sin \phi_1 = 0 \quad \phi_1 = 0$$

$$(1) - (2) \text{ より } \frac{2}{\sqrt{2}} A_2 \sin \phi_2 = 0 \quad \phi_2 = 0$$

$$(3) + (4) \text{ より } \frac{2 A_1 \omega_1}{\sqrt{2}} \cos \phi_1 + rP \left( \frac{1}{\omega_1^2 - p^2} \right) = 0$$

$$\phi_1 = 0 \text{ より } \sqrt{2} A_1 \omega_1 + rP \left( \frac{1}{\omega_1^2 - p^2} \right) = 0$$

$$A_1 = \frac{rP}{\sqrt{2} \omega_1 (p^2 - \omega_1^2)}$$

$$(3) - (4) \text{ より } \frac{2 A_2 \omega_2}{\sqrt{2}} \cos \phi_2 + rP \left( \frac{1}{\omega_2^2 - p^2} \right) = 0$$

$$\phi_2 = 0 \text{ より } \sqrt{2} A_2 \omega_2 + rP \left( \frac{1}{\omega_2^2 - p^2} \right) = 0$$

$$A_2 = \frac{rP}{\sqrt{2} \omega_2 (p^2 - \omega_2^2)}$$

$x_1(t), x_2(t)$  に代入して

角周波

$$\begin{cases} x_1(t) = \frac{rP}{2 \omega_1 (p^2 - \omega_1^2)} \sin \omega_1 t + \frac{rP}{2 \omega_2 (p^2 - \omega_2^2)} \sin \omega_2 t + \frac{r}{2} \left( \frac{1}{\omega_1^2 - p^2} + \frac{1}{\omega_2^2 - p^2} \right) \sin p t \\ x_2(t) = \frac{rP}{2 \omega_1 (p^2 - \omega_1^2)} \sin \omega_1 t - \frac{rP}{2 \omega_2 (p^2 - \omega_2^2)} \sin \omega_2 t + \frac{r}{2} \left( \frac{1}{\omega_1^2 - p^2} - \frac{1}{\omega_2^2 - p^2} \right) \sin p t \end{cases}$$

$$t = 2\pi, m=5, k=10, f_0=5, p=1 \text{ より } \omega_1^2 = \frac{k}{m} = 2, \omega_2^2 = \frac{3k}{m} = 6, r = \frac{f_0}{k} = 1$$

$$\begin{cases} x_1(t) = -\frac{\sqrt{2}}{4} \sin \sqrt{2} t - \frac{\sqrt{6}}{60} \sin \sqrt{6} t + \frac{3}{5} \sin t \\ x_2(t) = -\frac{\sqrt{2}}{4} \sin \sqrt{2} t + \frac{\sqrt{6}}{60} \sin \sqrt{6} t + \frac{1}{5} \sin t \end{cases}$$

—H

cf 8.3.