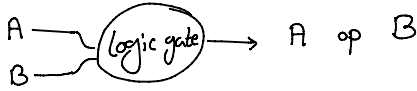


Boolean Algebra → discussion on boolean variables and logic

True/1      False/0

— • —

## Logic Gates



Primary logic gate → AND, OR, NOT

AND

A	B	A · B
0	0	0
0	1	0
1	0	0
1	1	1



OR

A	B	A + B
0	0	0
0	1	1
1	0	1
1	1	1

NOT

A	$\bar{A}$
0	1
1	0

XOR

A	B	A ⊕ B
0	0	0
0	1	1
1	0	1
1	1	0

$$A \oplus B = \bar{A}B + A\bar{B}$$

Half Adder

Truth Table

A	B	$\sum_1$	$\text{CARRY}_2$
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$\text{SUM} = A \oplus B$$

$$\text{CARRY} = A \cdot B$$

0	→	0
1	→	1
2	→	10
3	→	11
4	→	100
⋮		⋮
⋮		⋮

$$\begin{array}{r} 9 \\ 4 \\ \hline 13 \end{array}$$

13 / 10 = 1  
13 % 10 = 3

$$\begin{array}{l} 2/2 = 1 \\ 2 \% 2 = 0 \end{array}$$

C =

c

$$\begin{array}{r} 01011 \\ 01100 \\ \hline 10111 \end{array}$$

→ 11  
→ 12  
→ 23



# Full Adder

$$\begin{array}{r} 01100 \\ 10111 \\ \hline 16+7 \end{array} \rightarrow \begin{array}{r} 10 \\ 23 \end{array}$$

A	B	C <sub>in</sub>	SUM	CARRY
0	0	0	0	0
0	1	0	1	0
1	0	0	1	0
1	1	0	0	1
0	0	1	1	0
0	1	1	0	1
1	0	1	0	1
1	1	1	1	1

H.W.

$$SUM = \overline{A}\overline{B}C_{in} + A\overline{B}C_{in} + \overline{A}B\overline{C}_{in} + AB\overline{C}_{in} + \overline{A}B\overline{C}_{in} + A\overline{B}C_{in} + \overline{A}BC_{in} + ABC_{in}$$

$$= \overline{A}\overline{B}C + A\overline{B}C + \overline{A}B\overline{C} + AB\overline{C}$$

$$= \overline{C}(\overline{A}\overline{B} + A\overline{B}) + C(\overline{A}B + AB)$$

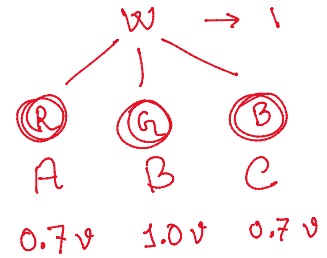
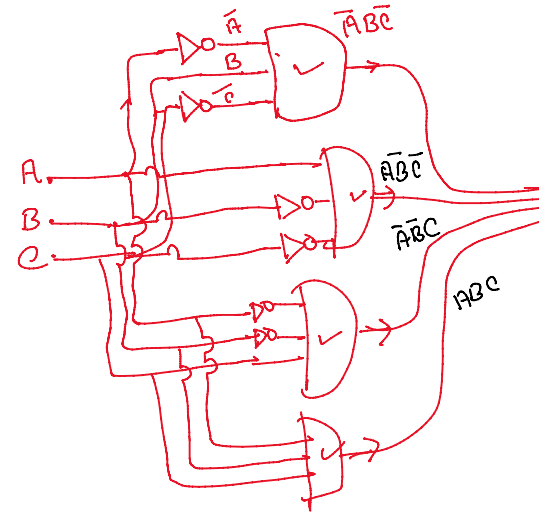
$$= \overline{C}(A \oplus B) + C(A \oplus B)$$

$$= \overline{C}X + CX$$

$$= C \oplus X$$

$$= C \oplus A \oplus B$$

$$= A \oplus B \oplus C$$



$$0.5V \quad 1.0V \quad 50.0V$$

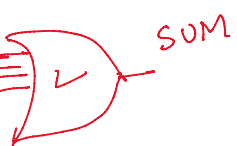
$$\overline{0} \cdot \underline{1} \cdot \overline{0} = 1$$

$$\begin{array}{ccc} \uparrow & \uparrow & \uparrow \\ 1/0 & 1/0 & 1/0 \end{array}$$



A	B	A ⊕ B
0	0	1
0	1	0
1	0	0
1	1	1

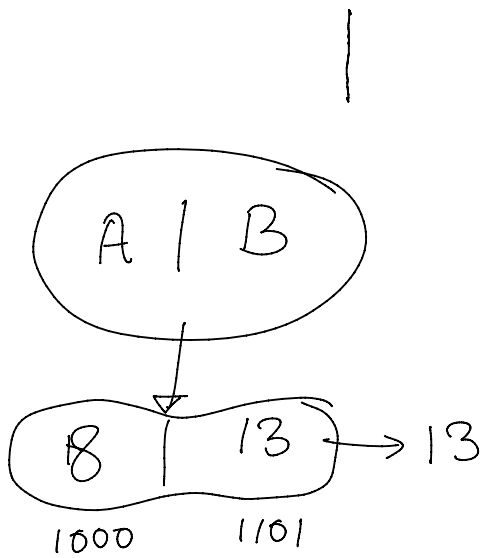
$$\begin{array}{l} A + A = A \\ A \cdot 1 = A \\ A + 1 = 1 \\ A \cdot A = A \\ A + 0 = A \\ A \cdot 0 = 0 \end{array}$$



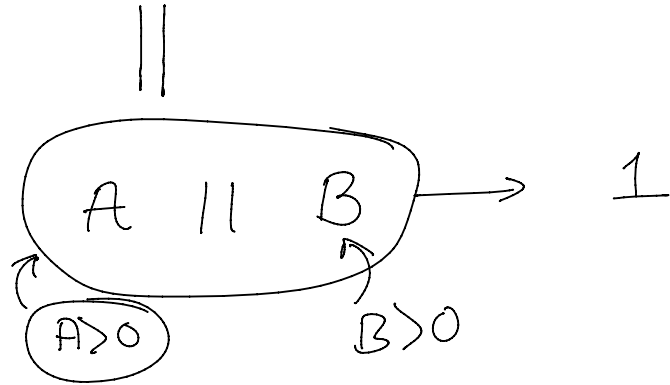
$$\left. \begin{aligned} A \cdot 0 &= A \\ \overline{A+B} &= \overline{A} \cdot \overline{B} \\ \overline{A \cdot B} &= \overline{A} + \overline{B} \end{aligned} \right\}$$

— 0 —

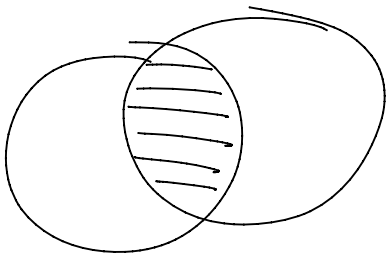
Number



$$\begin{array}{r} 1000 \\ 1101 \\ \hline 1101 \end{array}$$



dfs



IEP

$$P(A \cup B) = \overline{P(A)} + \overline{P(B)} - \underbrace{P(A \cap B)}$$

