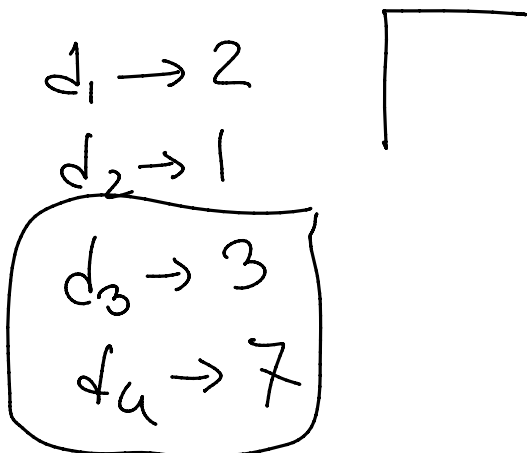


$d_1$     $d_1$     $d_2$     $d_3$     $d_3$     $d_3$



Exponential  
 $n, M$

5, 17

$$n^{n-1} \dots n^2 \dots n^1 \pmod{M}$$

$$5^4 \quad 3^2 \quad 1$$

$$5^{2621441} \pmod{17}$$



$$f(n) = n$$

$$f(n) = \left( n^{\phi(m) + f(n-1) \% \phi(m)} \right) \% m$$

$$5^0 \% 17$$

$$\phi(17) = 16$$

$$\text{mod-expo}(a, b) \rightarrow \text{mod-expo}(n, \phi(m) + f(n-1) \% \phi(m)) \% m$$

Hashing

String hashing

# String hashing

$$(abcd)_{26} \rightarrow 1 \times 26^3 + 2 \times 26^2 + 3 \times 26^1 + 4 \times 26^0$$

$$\rightarrow (19010)_{10}$$

$$(10110)_2 \rightarrow 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

$$16 + 0 + 4 + 2 + 0 \rightarrow (22)_{10}$$

prefix hash values

a	b	c	d	
1	2	3		
→				1
→				12
→				$12 \times 10 + 3 \rightarrow 123$
→				$123 \times 10 + 4 \rightarrow 1234$

$$abc \rightarrow 123$$

$$a \rightarrow \frac{100}{23}$$

$$\text{hash}[1, 2] \rightarrow 23$$

$$R - L + 1$$

how prefix hash[2] - (prefix hash[0] × 10<sup>2</sup>)

$$(23 - (1 \times 10^2)) = 23$$

$$PH[R] - (PH[L-1] \times B^{R-L+1})$$

$$\rightarrow [abc]d$$

$$(a-b) \% M \rightarrow (a \% M - b \% M + M) \% M$$

$$(17 - 14) \% 15 \rightarrow (2 - 14) \% 15$$

$$(-12 + 15) \% 15 \rightarrow 3 \% 15$$

-12, 3, 18, 33, ... equal

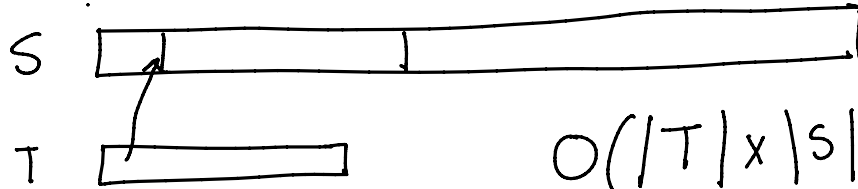
$$3 \% 15 = 18 \% 15 = 33 \% 15$$

...

P1

Pattern matching

S, T



$$O(|T| \times |S|) \approx N^2$$

$$(L-1) - i$$

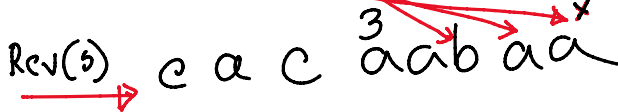
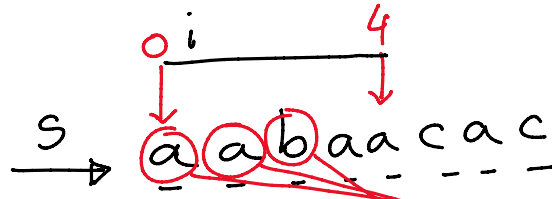
$$\begin{matrix} 0 \rightarrow 7 \\ 4 \rightarrow 3 \end{matrix}$$

$$O(|S|)$$

P2

S → find out the number of palindromic substring

8  
7  
6  
5  
4  
3  
2  
1



$$h_1 = h_2$$

$$n \approx \frac{n(n+1)}{2}$$

$$n = 5000$$

$$O(n) \times n^2 \rightarrow n^3$$

$$\begin{matrix} 0+7=7 \\ 1+6=7 \\ 2+5=7 \end{matrix}$$

$$7-0$$

ababab

S → axaabaabbaabzz

T → aab