

Primality Testing

Prime?

$$N > 1$$

divisors

$$N \rightarrow 1, N \rightarrow$$

$18 = \begin{matrix} \overline{a} & \overline{b} \\ 1 \times 18 \\ 2 \times 9 \\ 3 \times 6 \end{matrix}$
 $\Delta = 17$
 $\Delta = 7$
 $\Delta = 3$
 $a \leq \sqrt{n}$

$a \leq \sqrt{N}$
 $N=16$

| a | b |
|---|---|
| 1 | ✓ |
| 2 | ✓ |
| 3 | ✗ |
| 4 | ✓ |

$$\therefore a = \sqrt{N}$$

$$i! = \frac{n}{i}$$

$$\Rightarrow i \times i \neq n$$

```
bool isPrime(int N) {
    if (N ≤ 1) return false;
    for (int i = 2; i < N; i++) {
        if (N % i == 0)
            return false;
    }
    return true;
}
```

| lower half | upper half |
|----------------------------|-------------------|
| \textcircled{a} $d=0$ | \textcircled{b} |
| $N=ab$ | |

$$\log_2(N)$$

$$y = \sqrt{x}$$

$$f(x) = N - x^2$$

Newton-Raphson

$\gcd(a, b) = \gcd(b, a) \quad \boxed{f(x) = 0}$ Hence, $x = \sqrt{N}$

GCD

$$\gcd(a, b) = \gcd(b, a) \quad [F(x) = 0] \quad \text{Hence, } x = \dots$$

$$\gcd(a, 0) = a$$

$$\gcd(a, b) = \gcd(b, a \% b)$$

$$\gcd(a, b) = \gcd(b, a-b)$$

$$O(\log_2(\max(a, b)))$$

$$(15, 25) = (10, 15)$$

$$(10, 15) = (5, 10)$$

$$(5, 10) = (0, 5)$$

$$\begin{array}{c|c|c} 15 & 25 & 1 \\ \hline & 10 & \end{array}$$

$$\begin{array}{c|c|c} 10 & 15 & 1 \\ \hline & 5 & \end{array}$$

$$\begin{array}{c|c|c} 5 & 10 & 2 \\ \hline & 0 & \end{array}$$

```
int getgcd(a, b) {  
    if (b == 0) return a;  
    return getgcd(b, a % b);  
}
```