

বিভাজক/ Divisor

$$N=12 \rightarrow \text{divisor}(12) = 1, 2, 3, 4, 6, 12$$

$$N=13 \rightarrow \text{divisor}(13) = 1, 13$$

 $a, b \rightarrow \text{div}(a) \rightarrow \text{common divisor} \rightarrow \max$

$$\begin{aligned} \text{div}(12) &= 1, 2, 3, 4, 6, 12 \\ \text{div}(18) &= 1, 2, 3, 6, 9, 18 \\ \text{div}(24) &= 1, 2, 3, 4, 6, 8, 12, 24 \end{aligned}$$

18, 24

$$\text{gcd}(18, 24) = \text{gcd}(12, 18) = \text{gcd}(6, 12) = \text{gcd}(0, 6) = 6$$

$$\begin{aligned} \text{gcd}(a, b) &= \text{gcd}\left(\frac{b-a}{a}, \frac{a}{b}\right) = \text{gcd}(2a-b, b-a) \\ a &\leq b \\ b-a &= 2a-b \end{aligned}$$

$$\begin{aligned} \text{gcd}(18, 40) &= \text{gcd}(22, 18) \\ &= \text{gcd}(4, 18) = \text{gcd}(18, 22) \\ &= \text{gcd}(4, 18) \end{aligned}$$

$$\begin{array}{r} 18 \overline{) 40} (2 \\ \underline{36} \\ 4 \end{array}$$

$$40 \% 18$$

$$b \% a = b - a \left\lfloor \frac{b}{a} \right\rfloor$$

$$\begin{aligned} b - ak &\geq 0 \\ \Rightarrow b &\geq ak \\ \therefore k &\leq \frac{b}{a} \end{aligned}$$

$$\text{gcd}(a, b) \rightarrow \text{gcd}(b \% a, a)$$

$$\text{gcd}(0, b) \rightarrow b$$

$$\text{gcd}(18, 15) \rightarrow \text{gcd}(15, 18)$$

$$100 \% 51 = 49$$

$$5 \% 3 = 2$$

$$49 \% 25 = 24$$

$$2 \% 1 = 0$$

$$24 \% 13 = 12$$

$$12 \% 7 = 5$$

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$$\begin{aligned} \text{gcd}(34, 55) &\rightarrow \text{gcd}(34, 21) \rightarrow \text{gcd}(21, 34) \rightarrow \text{gcd}(5, 34) \\ &\rightarrow \text{gcd}(13, 21) \rightarrow \text{gcd}(3, 21) \\ &\rightarrow \text{gcd}(8, 13) \rightarrow \text{gcd}(2, 13) \\ &\rightarrow \text{gcd}(1, 2) \rightarrow \text{gcd}(1, 1) \end{aligned}$$

12	15
24	30
36	45
48	60
60	

$$\text{lcm}(a, b) \times \text{gcd}(a, b)$$

26

$[2 \dots 10]$

$N=12$

$1 \dots \sqrt{N}$

1, 25
5, ~~4~~

$$10^2 = 100$$

d	$\times N/d$	
1	12	↑
2	6	
3	4	
4	3	
$x = \sqrt{N}$	0	x

$$\begin{aligned} & \frac{1}{1} \\ & \frac{12}{2} \neq \\ & x \cdot x = \\ & \Rightarrow x^2 = 1 \\ & \therefore x = \sqrt{N} \end{aligned}$$



