

# Sieve

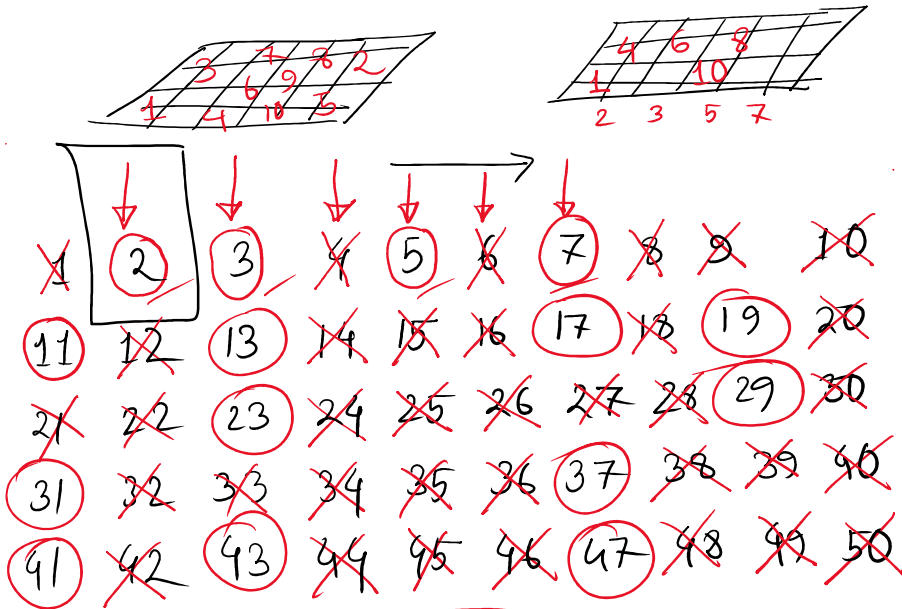
Primality Testing: Decide whether  $N$  is prime or not

Prime Generation: Generates primes within a specific range

1, 3, 5, 7, ...  
1021<sup>th</sup>  $\rightarrow$  Sieve of eratosthenes

$N\sqrt{N}$

3



1~200

$\sqrt{121} = 11$  1~10

$N=50$   
bool marked[100];  
for(int i=2; i<=N; i++)

for(i=1; i<=4; i++)  
22%1==0  
1,22  
2,11  
3,7  
4,5

$$\lim_{N \rightarrow \infty} \sum_{i=1}^N \frac{1}{i} = \infty$$

$$i \leq \sqrt{N}$$

$$\Rightarrow i^2 \leq N$$

$$[2 \sim N] \rightarrow \frac{N}{2}$$

$$[3 \sim N] \rightarrow \frac{N}{3}$$

$$[4 \sim N] \rightarrow \frac{N}{4}$$

$$\vdots$$

$$[N \sim N] \rightarrow \frac{N}{N}$$

$$= N \left( 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{N} \right)$$

$$= N (\log_2 N)$$

$$\log_2(N)$$

$$+ \dots + \frac{N}{N}$$

$$+ \dots + \frac{1}{N})$$

N

$$\underline{\underline{5 \times 10^8}}$$

$$\hookrightarrow [N \sim N] \rightarrow \left( \frac{N}{N} \right) = N \log_2$$

$$\frac{N}{2} + \frac{N}{3} + \frac{N}{5} \rightarrow N \log_2$$

$$+ \frac{N}{7} \\ (\log_2 N)$$