

Graph Theory

↳ Tree

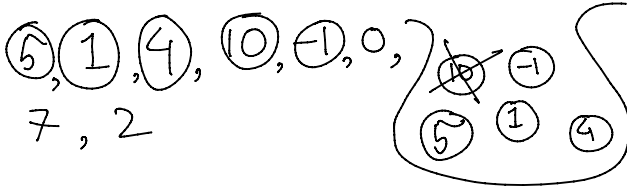
↳ node
↳ edge

maximum 2 direct

children

Node: N

Edge: $N-1$



Binary Heap

getMax $\rightarrow O(1)$

popMax $\rightarrow O(\log N)$

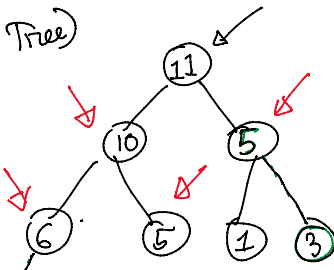
insertion $\rightarrow O(\log N)$

getMax() $\rightarrow O(1)$

popMax() $\rightarrow O(1)$

insert(v) $\rightarrow O(N)$

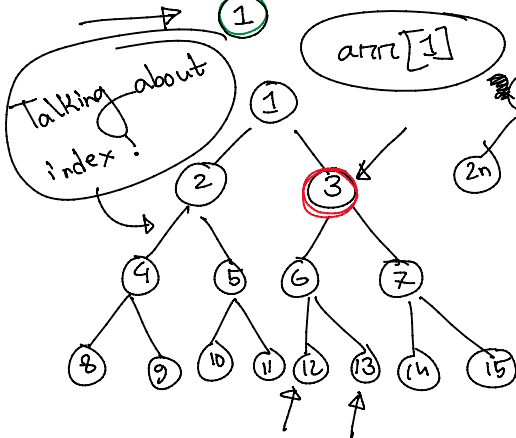
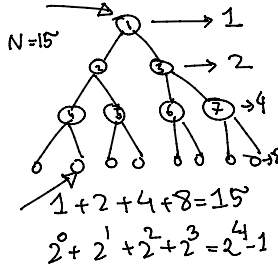
Binary (Binary Tree) Heap



$$2^4 - 1 = 16 - 1 = 15$$

insert(5)

insert(11)



$$N = 15 = 2^h - 1$$

$h = 4$

#node $N = 2^h$

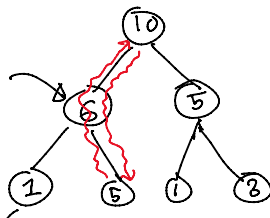
$$\Rightarrow \log_2 N = \log_2 2^h$$

$$\Rightarrow \log_2 N = h \cdot \log_2 2$$

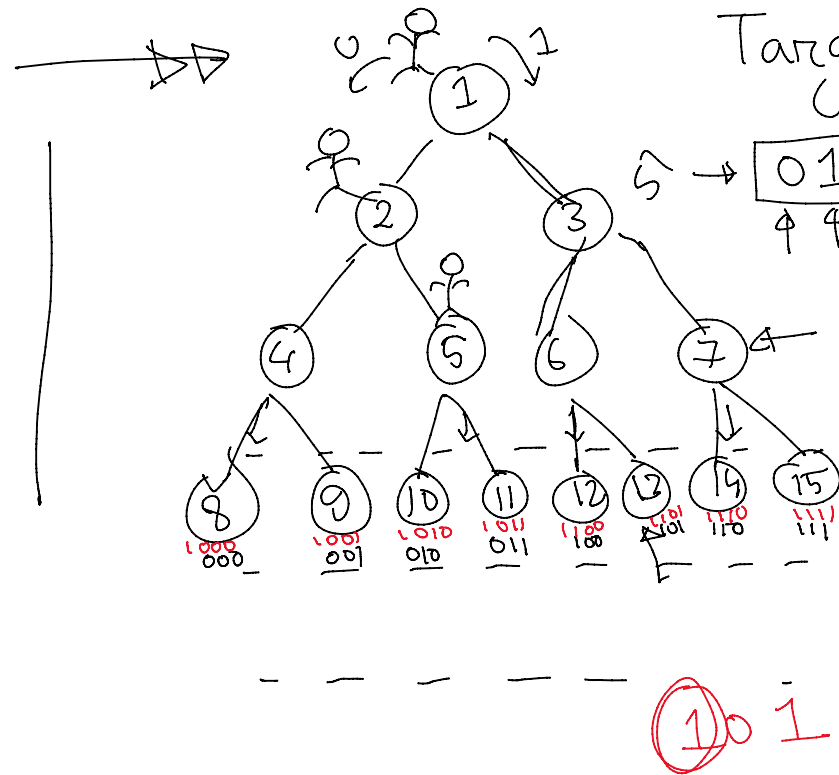
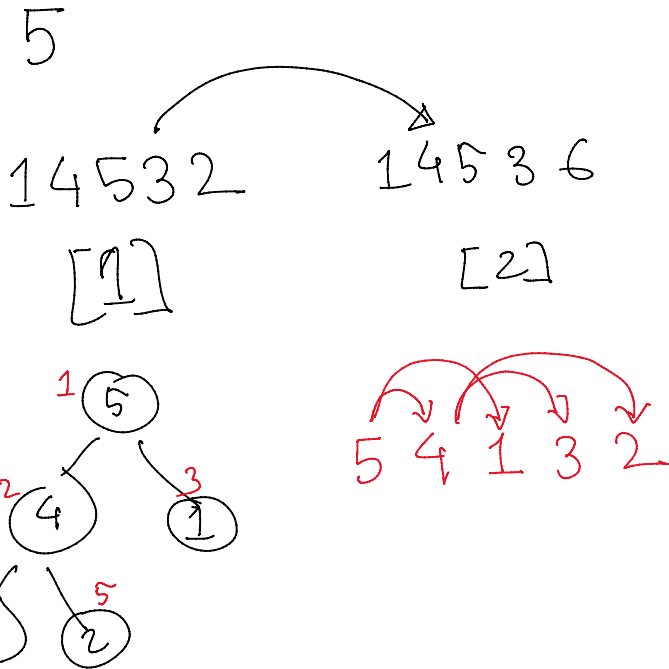
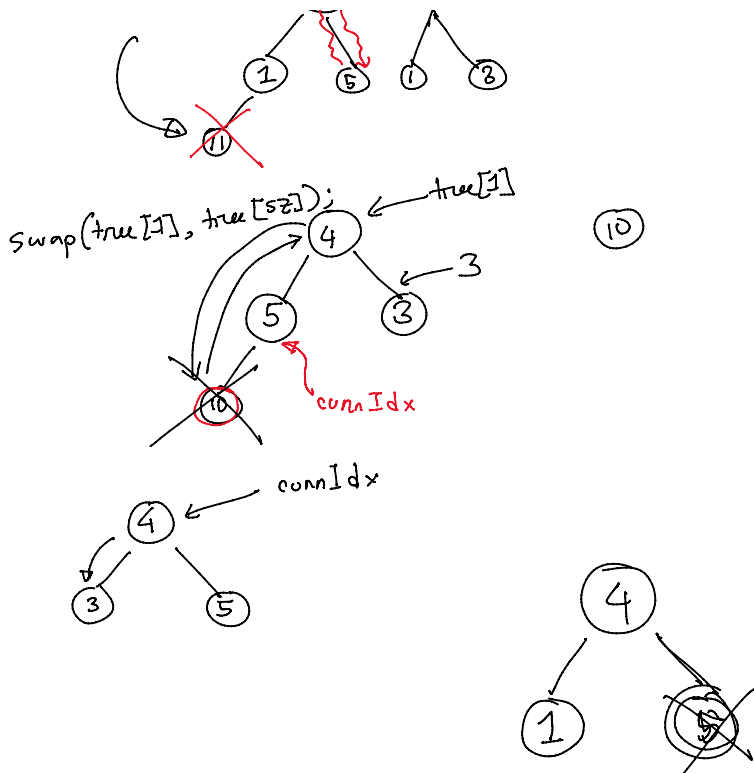
$$\therefore h = \log_2 N$$

size = 7

POP



h h



$$get = 5$$



$$7 \rightarrow 11$$