

we consider the integral

$$\int_C \mathbf{F}(\mathbf{r}) \cdot d\mathbf{r} = \int_C (F_1 dx + F_2 dy + F_3 dz) \quad (d\mathbf{r} = [dx, \quad dy, \quad dz])$$

$$\int_A^B (F_1 dx + F_2 dy + F_3 dz) = f(B) - f(A) \quad [\mathbf{F} = \text{grad } f]$$

$$\mathbf{F} \cdot d\mathbf{r} = F_1 dx + F_2 dy + F_3 dz$$

in components (see Sect. 9.9)

$$(6') \quad \frac{\partial F_3}{\partial y} = \frac{\partial F_2}{\partial z}, \quad \frac{\partial F_1}{\partial z} = \frac{\partial F_3}{\partial x}, \quad \frac{\partial F_2}{\partial x} = \frac{\partial F_1}{\partial y}.$$

$$\begin{aligned} \iint_S \mathbf{F} \cdot \mathbf{n} \, dA &= \iint_S (F_1 \cos \alpha + F_2 \cos \beta + F_3 \cos \gamma) \, dA \\ &= \iint_R (F_1 N_1 + F_2 N_2 + F_3 N_3) \, du \, dv. \end{aligned}$$

$$\iint_S \mathbf{F} \cdot \mathbf{n} \, dA = \iint_S (F_1 \, dy \, dz + F_2 \, dz \, dx + F_3 \, dx \, dy).$$

$$\cos \alpha \, dA = dy \, dz, \cos \beta \, dA = dz \, dx, \cos \gamma \, dA = dx \, dy.$$

where  $\mathbf{n}$  is the outward normal

$$\iint_S G(\mathbf{r}) \, dA = \iint_R G(\mathbf{r}(u, v)) |\mathbf{N}(u, v)| \, du \, dv.$$

$$dA = |\mathbf{N}| \, du \, dv = |\mathbf{r}_u \times \mathbf{r}_v| \, du \, dv$$

where  $\mathbf{r}_u$  and  $\mathbf{r}_v$  are the orientation

$$A(S) = \iint_S dA = \iint_R |\mathbf{r}_u \times \mathbf{r}_v| \, du \, dv.$$

$$\iint_S G(\mathbf{r}) \, dA = \iint_R G(x, y, f(x, y)) \sqrt{1 + \left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2} \, dx \, dy.$$

$$\Delta m = \rho \Delta V = \rho v a \Delta t. \quad \frac{\Delta m}{\Delta t} = \rho v a. \quad \left. \frac{dm}{dt} \right|_{ax}$$

