

Problème 1 :

$$V_u = 230 \text{ 000 V}$$

$$f = 60 \text{ Hz}$$

$$D = 250 \text{ Km}$$

$$S_{\text{direct}} = Z = 0,2 \Omega / \text{Km}$$

$$Y_{\text{shunt}} = 6,5 \cdot 10^{-6} \text{ S/Km}$$

$$\text{a) } 0,2j = j\omega L$$

$$6,5 \cdot 10^{-6} = j\omega C$$

$$\frac{0,2 \cdot 250}{360 \cdot 60} L = 0,002314 \text{ H} \quad C = 0,000000075$$

$$Z_c = 178,38$$

$$SIL = \frac{\frac{230000^2}{30}}{178,38} = 301629491,4 \text{ W}$$

$$\text{b) } I = \frac{S}{\sqrt{3} V_{\text{nominal}}} \quad I = \frac{530000000}{\sqrt{3} 0,83 \cdot 230000} = 1583,82$$

$$A = 1 + \frac{0,00065j (50j)}{2} = 0,959375$$

$$B = 50j$$

$$V_3 = 0,459375 \cdot 0,83 \frac{230000}{\sqrt{3}} + 50j \cdot 1583,82$$

$$V_3 = 105738,63 + 79191j =$$

$$\text{c) } \frac{0,84 \frac{230000}{\sqrt{3}} - 105738,63 + 79191j}{0,84 \frac{230000}{\sqrt{3}}} = \frac{5805,43 + 79191j}{111544 \angle 0} = \frac{-111544}{111544} = 0,09745 \angle 57,72^\circ$$

$$\text{d) } \frac{111544 - 105738,63 + 79191j}{105738,63 + 79191j} = \frac{10830,94 \angle 57,72}{106137,32 \angle 4,96} = 0,1024 \angle 52,76$$

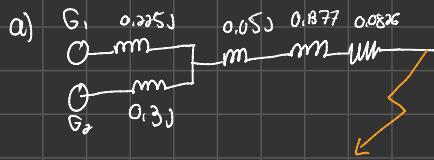
Probleme 2:

$$z_{\text{nom}} = \frac{33000^2}{30000000} = 36.3$$

$$\text{Ligne} = (0.0826 + 0.1877j) \text{pu}$$

$$G_1 = 0.5 \cdot \frac{30}{20} = 0.225$$

$$G_2 = 0.10 \cdot \frac{30}{40} = 0.3$$



$$\text{b)} (0.0255 // 0.3j) + (0.1877j + 0.0826)$$

$$\frac{0.0255j \cdot 0.3j}{0.3255j} = \frac{0.00765}{0.3255} \text{ J} = 0.1286 \cdot \text{J}$$

$$0.31627 \text{ J} + 0.0826 = z$$

$$\frac{1}{\sqrt{0.31627^2 + 0.0826^2}} = 3.059 \text{ pu} \angle -75^\circ$$

$$I_{\text{base}} = \frac{30000000}{\sqrt{3} \cdot 33000} = 524.86$$

$$I = 3.059 \cdot 524.86 = 1605.55 \text{ A}$$

### Probleme 3

$$V_{\text{L}} = 230 \text{ kV}$$

$$f = 60 \text{ Hz}$$

$$\text{distance} = 200 \text{ km}$$

$$GMR = 0,0122834 \text{ m}$$

$$L_a = 2 \cdot 10^{-7} \ln \frac{GMD}{GMR}$$

$$GMR' = 0,009566343$$

$$d = 0,5 \text{ m}$$

$$(\sqrt[4]{0,009566343^3}) \cdot 1,09$$

$$GMR' = 0,202879769$$

$$GMD = \sqrt[3]{34 \cdot 470 \cdot 470} = 15,6594$$

$$L_a = 2 \cdot 10^{-7} \ln \frac{15,6594}{0,202879769}$$

$$L_a = 0,000000869 \text{ H/m}$$

$$\text{b) } \frac{0,000000869 \text{ H}}{1 \text{ m}} \cdot \frac{1000 \text{ m}}{1 \text{ km}} \cdot 200 \text{ km} = 0,173848 \text{ H}$$

$$X = JW_L = J \cdot 2\pi \cdot 60 \cdot 0,173848$$

$$X = 65,54 \text{ J } \Omega$$

$$\text{c) } C_{\text{an}} = \frac{2\pi \cdot 8,854 \cdot 10^{-9}}{\ln \left( \frac{15,6594}{0,202879769} \right)} = 1,24 \cdot 10^{-11} \text{ F/m}$$

$$\text{d) } = 0,00000258 \text{ F} \quad \frac{1}{J 2\pi 60 \cdot 0,000}$$

$$X_C = -1028,13 \text{ J } \Omega$$

$$Y_C = 0,000472637 \text{ J } S$$

e) on peut diminuer la distance entre les fils pour diminuer

### Problem 4

$$S = 100 \text{ MVA}$$

$$V_u = 13800 \text{ V}$$

$$x_0 = 0.05 \text{ pu}$$

$$x_1 = 0.15 \text{ pu}$$

$$x_2 = 0.17 \text{ pu}$$



$$V_a = 0$$

$$V_b = V_c$$

$$I_b = -I_c = I_{cc}$$

$$V_0 = \frac{1}{3}(V_a + V_b + V_c)$$

$$V_1 = \frac{1}{3}(V_a + \alpha V_b + \alpha^2 V_c) = \frac{1}{3}(V_a + (\alpha + \alpha^2)V_c) = \frac{1}{3}(V_a - V_c)$$

$$V_2 = \frac{1}{3}(V_a + \alpha^2 V_b + \alpha V_c) = \frac{1}{3}(V_a + (\alpha^2 + \alpha)V_c) = \frac{1}{3}(V_a - V_c)$$

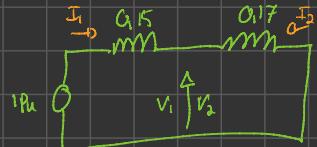
$$V_1 = V_2$$

$$I_0 = \frac{1}{3}(I_a + I_b + I_c)$$

$$I_1 = \frac{1}{3}(I_a + \alpha I_b + \alpha^2 I_c) = \frac{1}{3}(I_a + (\alpha + \alpha^2)I_c)$$

$$I_2 = \frac{1}{3}(I_a + \alpha^2 I_b + \alpha I_c) = \frac{1}{3}(I_a + (\alpha^2 + \alpha)I_c)$$

$$I_1 = -I_2$$



$$I_1 = \frac{1}{0.15 + 0.17} = -3.125 \text{ J pu}$$

$$I_2 = -I_1 = 3.125 \text{ J pu}$$

$$I_b = I_0 + \alpha^2 I_1 + \alpha I_2$$

$$I_{cc} = (\alpha^2 - \alpha) I_1$$

$$I_{cc} = -1.732 \text{ J} \cdot 3.125 \text{ J}$$

$$I_{cc} = -5.4125 \text{ pu}$$

$$\text{b)} \quad V_1 = \frac{0.17 \text{ J}}{(0.17 + 0.15) \text{ J}} = 0.53125 \text{ pu}$$

$$V_a = 2V_1$$

$$V_a = 2 \cdot 0.53125 = 1.0625 \text{ pu}$$

$$V_1 = \frac{1}{3}(V_a - V_b) \approx V_b = V_a - 3V_1 = 2V_1 - 3V_1 = -V_1$$

$$V_b = -0.53125 \text{ pu}$$

$$V_c = -V_b = 0.53125 \text{ pu}$$

Problem 1:

$$a) \quad 0.2 \text{F} \cdot \text{jw} = 65 \cdot 10^{-6} \text{J} = \text{jwL}$$

$$\frac{0.2 \text{J}}{\text{j} 2\pi 60} = L \quad \frac{65 \cdot 10^{-6} \text{J}}{\text{j} 2\pi 60} = C$$

$$L = 0.3269 \quad C = 0.00000491$$

$$Z_L = \sqrt{\frac{0.132624}{0.00000491}} = 175.41 \Omega$$

$$b) \quad V_s = A V_R + B I_R$$

$$I_R = \frac{P}{3 \cdot V_R} = \frac{530000 \text{ mW}}{3 \cdot 0.84 \cdot \frac{230000}{\sqrt{3}}} = 1583.82 \text{ A}$$

$$V_s = 0.959375 \left( 0.84 \cdot \frac{230000}{\sqrt{3}} \right) + 50 \text{ J} (1583.82)$$

$$V_s = 105736.63 + 74191 \text{ J} = 132105 \angle 36.83^\circ$$

$$c) \quad V_s = \frac{132105 - 111544}{132105} = 0.155\% \quad = \quad \frac{74403 \angle -85^\circ}{111544 \angle 0^\circ}$$

$$d) \quad V_{rVde} = I_p = 0$$

$$V_s = A V_R$$

$$\frac{V_s}{B} = V_R = \frac{132105}{0.959375} = 137644$$

$$RT = \frac{137644 - 111544}{111544} = 0.2344$$

$$e) \quad 0.05 = \frac{132105 - V_R}{132105}$$

$$V_R = 125499.75 \quad \checkmark$$

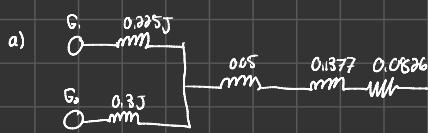
$$Q_R = 3 \frac{V_{R2} V_{A3}}{x'} \cos(\varphi_0 - \delta) - 3 \frac{A V_{R3}}{x'} \cos(\varphi)$$

$$530000 \text{ mW} = \frac{125499.75 \cdot 137644}{50} \sin(\delta)$$

$$\delta = 30.74^\circ$$

$$Q_R = \frac{125499.75 \cdot 137644 \cdot e^{j30.74^\circ}}{50} - \frac{A \cdot 125499^2}{50} \cos(\varphi_0)$$

Problem 2:



b)  $(0.12857 + 0.05 + 0.1377)J + 0.0826$   
 $0.31627 J + 0.0826$

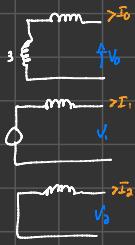
$$I_{ac} = \frac{1}{\sqrt{0.31627^2 \cdot 0.0826^2}} = 305 \text{ pu}$$

$$I_{base} = \frac{30 \text{ } 000 \text{ } 000}{\sqrt{3} \cdot 33000}$$

$$I_{base} = 524.86 \cdot 3.08$$

$$I = 1600 \text{ A}$$

Probleme 4:



Cant circuit entre b et c donc

$$V_a = 0$$

$$I_a = 0$$

$$V_b = V_c$$

$$I_b = -I_c$$

$$V_o = \frac{1}{3} (V_a + V_b - V_c)$$

$$V_1 = \frac{1}{3} (V_a + \alpha V_b + \alpha^2 V_c)$$

$$V_1 = \frac{1}{3} (V_a + \alpha V_b + \alpha^2 V_b)$$

$$V_1 = \frac{1}{3} (V_a + (\alpha + \alpha^2) V_b)$$

$$V_1 = \frac{1}{3} (V_a - V_b)$$

$$V_1 = V_2$$

$$V_2 = \frac{1}{3} (V_a + \alpha^2 V_b + \alpha V_c)$$

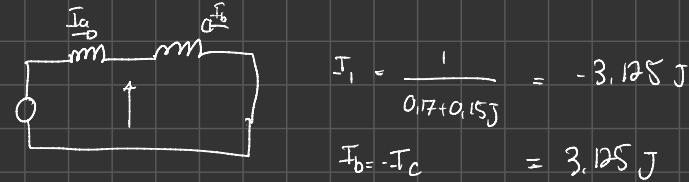
$$V_2 = \frac{1}{3} (V_a - V_b)$$

$$I_o = 0$$

$$I_1 = \frac{1}{3} (I_a + \alpha I_b + \alpha^2 I_c)$$

$$I_1 = \frac{1}{3} (I_a + (\alpha - \alpha^2) I_b) =$$

$$I_2 = \frac{1}{3} (I_a + (\alpha^2 - \alpha) I_b) = \frac{1}{3} (I_a - (\alpha - \alpha^2) I_b)$$



$$I_1 = \frac{1}{0.17 + 0.15} = -3.125 \text{ A}$$

$$I_b = -I_c = 3.125 \text{ A}$$

$$I_{cc} = I_b = I_a + \alpha^2 I_1 + \alpha I_2$$

$$I_{cc} = (\alpha^2 - \alpha) I_1$$

$$I_{cc} = (-1.73 \text{ A}) (-3.125 \text{ A})$$

$$I_{cc} = 5.412 \text{ Pa}$$

b)  $V_1 = V_b + V_c$

$$V_1 = 2V_b$$

$$\frac{0.17}{0.17 + 0.15} = 0.53125 \text{ Pa}$$

$$V_b = \frac{0.53125}{2}$$

$$V_b = V_c$$

$$V_a = 0$$