

Wydruk programu „Krata” do wytworzenia rysunków do siatki zagęszczeń gradientu współczynnika załamania

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Exit[]
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KadaptRK3BS[XY_] :=  
Module[{k1, k2, k3, k4, x = First@XY, Y = Drop[XY, 1], ΔY23, Δk, hstare},  
  hstare = h;  
  k1 = h FIO;  
  k2 = h F[x +  $\frac{1}{2} h$ , ###] &@@ (Y +  $\frac{1}{2} k1$ );  
  k3 = h F[x +  $\frac{3}{4} h$ , ###] &@@ (Y +  $\frac{3}{4} k2$ );  
  Y3 = Y + ( $\frac{2}{9} k1 + \frac{1}{3} k2 + \frac{4}{9} k3$ );  
  FIO = F[x + h, ###] &@@ Y3;  
  k4 = h FIO;  
  ΔY23 = Abs[ $\frac{1}{72} (5 k1 - 6 k2 - 8 k3 + 9 k4)$ ];  
  Δk = Max@  $\frac{\Delta Y23}{\text{Abs}[Y3] + \text{Abs}[Y3 - Y]}$ ;  
  h = hstare If[ $\delta > \Delta k$ , Min[ $(\frac{\delta}{\Delta k})^{1/3}$ , 5], Max[ $(\frac{\delta}{\Delta k})^{1/3}$ , 1/5]];  
  ndone++;  
  Flatten[{x + hstare, Y3}]
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makeGraph[iniDat_ : {-6, -1.5,  $\frac{\pi}{180}$  80, 0}, P_ : 0.8,  $\lambda_-$  : 400] :=
Module[{graf, hstart, v, dvx, dvy,  $\lambda_1 = 400$ ,  $\lambda_2 = 720$ ,
  e = 0.2, kolor = ColorData["VisibleSpectrum"] [ $\lambda$ ]},
{w = 9, An = 1,  $\xi = 8/10$ , Ay = 1, Ax = Ay  $\sqrt{1 - \xi^2}$ };

n1 = 1 + P  $\left( \frac{2 An}{2 + \frac{(Ay)^2}{Ax^2} + \frac{y^2}{Ay^2}} + \frac{2 An}{2 + \frac{(Ay)^2}{Ax^2} + \frac{y^2}{Ay^2}} + 4 \sin[x]^{12} + 4 \sin[y]^{12} \right)$ ;

nn[x_, y_] = n1 +  $\frac{(-1 + n1) e (\lambda^2 - \lambda_1^2) \lambda_2^2}{\lambda^2 (\lambda_1^2 - \lambda_2^2)}$ ;

gWsp = Plot[nn[x, 0], {x, -w, w}, PlotRange → {All, {0, 3}}];
tlo = ContourPlot[nn[x, y],
  {x, -w, w}, {y, -w, w}, Contours → 29, PlotPoints → 39];

v[x_, y_] = Log@ (nn[x, y]);
dvx[x_, y_] = D[v[x, y], x];
dvy[x_, y_] = D[v[x, y], y];
F[s_, x_, y_,  $\phi$ _, t_] = {Cos[ $\phi$ ], Sin[ $\phi$ ],
  dvy[x, y] Cos[ $\phi$ ] - dvx[x, y] Sin[ $\phi$ ], Exp@ (v[x, y])} // Simplify;

{s0, s1} = {0,  $\infty$ };
{x0, y0,  $\phi$ 0, t0} = iniDat;

hstart[] := Module[{f, df, fdf, Y0, x, y,  $\phi$ , t, s, tmp},
  Y0 = Abs[{x0, y0,  $\phi$ 0}];
  f = Take[F[s0, x0, y0,  $\phi$ 0, t0], 3];
  df = Transpose[{D[Take[F[s, x, y,  $\phi$ , t], 3], #] & /@ {x, y,  $\phi$ }} /. s → s0 /.
    x → x0 /. y → y0 /.  $\phi$  →  $\phi$ 0];
  fdf = Abs[f.df];
  tmp = Flatten@

    Table[If[fd f[[i]] > 0, Min[ $\sqrt{\frac{2 Y0[[i]]}{fd f[[i]]}}$ ,  $\frac{Abs[f[[i]]]}{fd f[[i]]}$ ],  $\infty$ ], {i, 1, 3}];

   $\sqrt{\delta}$  Min@tmp];
Clear[sol, tor];
{ $\delta = 10^{-8}$ , h = hstart[], hmax =  $\infty$ , nmax = 10 000, ndone = 0,};
FIO = F[s0, x0, y0,  $\phi$ 0, 0];
sol = NestWhileList[KadaptrK3BS, {s0, x0, y0,  $\phi$ 0, t0},
  (w ≥ Abs[#[[2]]] && w ≥ Abs[#[[3]]] && #[[1]] < s1 && ndone < nmax) &;
Print["ndone= ", ndone];
tor[tkolor_] :=
  ListPlot[{#[[2]], #[[3]]} & /@ sol, Joined → True, PlotStyle → tkolor];
graf = Show[tor[kolor], PlotRange → All, AspectRatio → 1];
Print[Show[{tlo, graf}]];
graf]

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Rysunek 7.23

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gr355 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  355, 0}, 0.1, 650];
go355 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  355, 0}, 0.1, 615];
gy355 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  355, 0}, 0.1, 590];
gg355 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  355, 0}, 0.1, 510];
gb355 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  355, 0}, 0.1, 470];
gp355 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  355, 0}, 0.1, 410];
gr340 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  340, 0}, 0.1, 650];
go340 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  340, 0}, 0.1, 615];
gy340 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  340, 0}, 0.1, 590];
gg340 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  340, 0}, 0.1, 510];
gb340 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  340, 0}, 0.1, 470];
gp340 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  340, 0}, 0.1, 410];
gr325 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  325, 0}, 0.1, 650];
go325 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  325, 0}, 0.1, 615];
gy325 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  325, 0}, 0.1, 590];
gg325 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  325, 0}, 0.1, 510];
gb325 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  325, 0}, 0.1, 470];
gp325 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  325, 0}, 0.1, 410];
gr310 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  310, 0}, 0.1, 650];
go310 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  310, 0}, 0.1, 615];
gy310 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  310, 0}, 0.1, 590];
gg310 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  310, 0}, 0.1, 510];
gb310 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  310, 0}, 0.1, 470];
gp310 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  310, 0}, 0.1, 410];
gr300 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  300, 0}, 0.1, 650];
go300 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  300, 0}, 0.1, 615];
gy300 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  300, 0}, 0.1, 590];

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gg300 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  300, 0}, 0.1, 510];
gb300 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  300, 0}, 0.1, 470];
gp300 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  300, 0}, 0.1, 410];
gr285 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  285, 0}, 0.1, 650];
go285 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  285, 0}, 0.1, 615];
gy285 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  285, 0}, 0.1, 590];
gg285 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  285, 0}, 0.1, 510];
gb285 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  285, 0}, 0.1, 470];
gp285 = makeGraph[{-7.8, 7.8,  $\frac{\pi}{180}$  285, 0}, 0.1, 410];

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Show[{tlo, gr355, go355, gy355, gg355, gb355, gp355, gr340, go340,
      gy340, gg340, gb340, gp340, gr325, go325, gy325, gg325, gb325,
      gp325, gr310, go310, gy310, gg310, gb310, gp310, gr300, go300, gy300,
      gg300, gb300, gp300, gr285, go285, gy285, gg285, gb285, gp285}]

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Rysunek 7.24

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gr0 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  10, 0}, 0.1, 650];
go0 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  10, 0}, 0.1, 615];
gy0 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  10, 0}, 0.1, 590];
gg0 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  10, 0}, 0.1, 510];
gb0 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  10, 0}, 0.1, 470];
gp0 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  10, 0}, 0.1, 410];
gr70 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  70, 0}, 0.1, 650];
go70 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  70, 0}, 0.1, 615];
gy70 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  70, 0}, 0.1, 590];
gg70 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  70, 0}, 0.1, 510];
gb70 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  70, 0}, 0.1, 470];
gp70 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  70, 0}, 0.1, 410];
gr130 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  130, 0}, 0.1, 650];
go130 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  130, 0}, 0.1, 615];

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gy130 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  130, 0}, 0.1, 590];
gg130 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  130, 0}, 0.1, 510];
gb130 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  130, 0}, 0.1, 470];
gp130 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  130, 0}, 0.1, 410];
gr190 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  190, 0}, 0.1, 650];
go190 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  190, 0}, 0.1, 615];
gy190 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  190, 0}, 0.1, 590];
gg190 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  190, 0}, 0.1, 510];
gb190 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  190, 0}, 0.1, 470];
gp190 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  190, 0}, 0.1, 410];
gr250 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  250, 0}, 0.1, 650];
go250 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  250, 0}, 0.1, 615];
gy250 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  250, 0}, 0.1, 590];
gg250 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  250, 0}, 0.1, 510];
gb250 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  250, 0}, 0.1, 470];
gp250 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  250, 0}, 0.1, 410];
gr310 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  310, 0}, 0.1, 650];
go310 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  310, 0}, 0.1, 615];
gy310 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  310, 0}, 0.1, 590];
gg310 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  310, 0}, 0.1, 510];
gb310 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  310, 0}, 0.1, 470];
gp310 = makeGraph[{-0.001, 0.001,  $\frac{\pi}{180}$  310, 0}, 0.1, 410];

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Show[{tlo, gr0, go0, gy0, gg0, gb0, gp0, gr70, go70, gy70,
      gg70, gb70, gp70, gr130, go130, gy130, gg130, gb130, gp130,
      gr190, go190, gy190, gg190, gb190, gp190, gr250, go250, gy250,
      gg250, gb250, gp250, gr310, go310, gy310, gg310, gb310, gp310}]

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Rysunek 7.25

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gr1 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  0.1, 0}, 0.1, 650];

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go1 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  0.1, 0}, 0.1, 615];
gy1 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  0.1, 0}, 0.1, 590];
gg1 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  0.1, 0}, 0.1, 510];
gb1 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  0.1, 0}, 0.1, 470];
gp1 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  0.1, 0}, 0.1, 410];
gr15 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  15, 0}, 0.1, 650];
go15 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  15, 0}, 0.1, 615];
gy15 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  15, 0}, 0.1, 590];
gg15 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  15, 0}, 0.1, 510];
gb15 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  15, 0}, 0.1, 470];
gp15 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  15, 0}, 0.1, 410];
gr30 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  30, 0}, 0.1, 650];
go30 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  30, 0}, 0.1, 615];
gy30 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  30, 0}, 0.1, 590];
gg30 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  30, 0}, 0.1, 510];
gb30 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  30, 0}, 0.1, 470];
gp30 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  30, 0}, 0.1, 410];
gr45 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  44.9, 0}, 0.1, 650];
go45 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  44.9, 0}, 0.1, 615];
gy45 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  44.9, 0}, 0.1, 590];
gg45 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  44.9, 0}, 0.1, 510];
gb45 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  44.9, 0}, 0.1, 470];
gp45 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  44.9, 0}, 0.1, 410];
gr60 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  60, 0}, 0.1, 650];
go60 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  60, 0}, 0.1, 615];
gy60 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  60, 0}, 0.1, 590];
gg60 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  60, 0}, 0.1, 510];
gb60 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  60, 0}, 0.1, 470];

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gp60 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  60, 0}, 0.1, 410];
gr75 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  75, 0}, 0.1, 650];
go75 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  75, 0}, 0.1, 615];
gy75 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  75, 0}, 0.1, 590];
gg75 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  75, 0}, 0.1, 510];
gb75 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  75, 0}, 0.1, 470];
gp75 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  75, 0}, 0.1, 410];
gr90 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  89.9, 0}, 0.1, 650];
go90 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  89.9, 0}, 0.1, 615];
gy90 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  89.9, 0}, 0.1, 590];
gg90 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  89.9, 0}, 0.1, 510];
gb90 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  89.9, 0}, 0.1, 470];
gp90 = makeGraph[{-9, -9,  $\frac{\pi}{180}$  89.9, 0}, 0.1, 410];

```

```

Show[{tlo, gr1, go1, gy1, gg1, gb1, gp1, gr15, go15, gy15,
  gg15, gb15, gp15, gr30, go30, gy30, gg30, gb30, gp30, gr45, go45,
  gy45, gg45, gb45, gp45, gr60, go60, gy60, gg60, gb60, gp60, gr75,
  go75, gy75, gg75, gb75, gp75, gr90, go90, gy90, gg90, gb90, gp90}]

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