Exit[]

```
KadaptRK3BS[XY_] :=

Module[{k1, k2, k3, k4, x = First@XY, Y = Drop[XY, 1], \DeltaY23, \Deltak, hstare}, hstare = h;

k1 = h FIO;

k2 = h F[x + \frac{1}{2} h, ##] &@@ (Y + \frac{1}{2} k1);

k3 = h F[x + \frac{3}{4} h, ##] &@@ (Y + \frac{3}{4} k2);

Y3 = Y + (\frac{2}{9} k1 + \frac{1}{3} k2 + \frac{4}{9} k3);

FIO = F[x + h, ##] &@@Y3;

k4 = h FIO;

\DeltaY23 = Abs[\frac{1}{72} (5 k1 - 6 k2 - 8 k3 + 9 k4)];

\Deltak = Max@ \frac{\DeltaY23}{Abs[Y3] + Abs[Y3 - Y]};

h = hstare If[\delta > \Deltak, Min[(\frac{\delta}{\Delta k})<sup>1/3</sup>, 5], Max[(\frac{\delta}{\Delta k})<sup>1/3</sup>, 1/5]];

ndone++;

Flatten@{x + hstare, Y3}]
```

```
makeGraph[iniDat_: \{-6, -1.5, \frac{\pi}{180}, 0\}, P_: 0.8, \lambda_: 400] :=
 \epsilon = 0.2, kolor = ColorData["VisibleSpectrum"][\lambda]},
    \{w = 6, v = 0.5, a = 1, b = 0.9, ro = 1, u = \sqrt{\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2}\};
   n1 = 1 + P\left(\frac{1 + Exp[-ro/v]}{1 + Exp[u - ro/v]}\right);
   nn\left[\mathbf{x}_{-},\;\mathbf{y}_{-}\right]=n1+\frac{\left(-1+n1\right)\,\varepsilon\,\left(\lambda^{2}-\lambda\mathbf{1}^{2}\right)\,\lambda\mathbf{2}^{2}}{\lambda^{2}\,\left(\lambda\mathbf{1}^{2}-\lambda\mathbf{2}^{2}\right)}\,;
    gWsp = Plot[nn[x, 0], \{x, -w, w\}, PlotRange \rightarrow \{All, \{0, 3\}\}];
    tlo = ContourPlot[nn[x, y],
        \{x, -w, w\}, \{y, -w, w\}, Contours \rightarrow 29, PlotPoints \rightarrow 39\};
    v[x_{, y_{]}} = Log@(nn[x, y]);
    dvx[x_{,} y_{]} = D[v[x, y], x];
    dvy[x_{,} y_{]} = D[v[x, y], y];
    F[s_{x}, x_{y}, \phi_{t}, t_{s}] = \{Cos[\phi], Sin[\phi],
         \texttt{dvy}[\texttt{x},\texttt{y}] \; \texttt{Cos}[\phi] \; \texttt{-} \; \texttt{dvx}[\texttt{x},\texttt{y}] \; \texttt{Sin}[\phi] \; \texttt{,} \; \texttt{Exp@}\left(\texttt{v}[\texttt{x},\texttt{y}]\right) \} \; // \; \texttt{Simplify};
    \{s0, s1\} = \{0, \infty\};
    \{x0, y0, \phi0, t0\} = iniDat;
    \texttt{hstart[]} := \texttt{Module} \big[ \{\texttt{f},\, \texttt{df},\, \texttt{fdf},\, \texttt{Y0},\, \texttt{x},\, \texttt{y},\, \phi,\, \texttt{t},\, \texttt{s},\, \texttt{tmp} \} \,,
       Y0 = Abs[{x0, y0, \phi0}];
        f = Take[F[s0, x0, y0, \phi0, t0], 3];
       df = Transpose \left[ \left( D[Take[F[s, x, y, \phi, t], 3], \#] \& /@ \{x, y, \phi\} \right) /. s \rightarrow s0 /. \right]
                 x \rightarrow x0 /. y \rightarrow y0 /. \phi \rightarrow \phi0;
        fdf = Abs[f.df];
        tmp = Flatten@
           Table \Big[ If \Big[ fdf[[i]] > 0, Min \Big[ \sqrt{\frac{2 \, Y0[[i]]}{fdf[[i]]}}, \frac{Abs[f[[i]]]}{fdf[[i]]} \Big], \infty \Big], \{i, 1, 3\} \Big];
        \sqrt{\delta} Min@tmp];
Clear[sol, tor];
    \{\delta = 10^{-8}, h = hstart[], hmax = \infty, nmax = 10000, ndone = 0, \};
    FIO = F[s0, x0, y0, \phi0, 0];
    sol = NestWhileList[KadaptRK3BS, \{s0, x0, y0, \phi0, t0\},
        (w \ge Abs[#[[2]]] \&\& w \ge Abs[#[[3]]] \&\& #[[1]] < s1 \&\& ndone < nmax) \&];
    Print["ndone= ", ndone];
    tor[tkolor_] :=
     ListPlot[\{\#[[2]], \#[[3]]\} \& /@ sol, Joined <math>\rightarrow True, PlotStyle \rightarrow tkolor];
    graf = Show[tor[kolor], PlotRange → All, AspectRatio → 1];
    Print[Show[{tlo, graf}]];
    graf
```

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```
gr1 = makeGraph[\{-5, -5, \frac{\pi}{180}, 0.1, 0\}, 0.9, 650];
go1 = makeGraph[\{-5, -5, \frac{\pi}{180}, 0.1, 0\}, 0.9, 615];
gy1 = makeGraph[\{-5, -5, \frac{\pi}{180} 0.1, 0\}, 0.9, 590];
gg1 = makeGraph[\{-5, -5, \frac{\pi}{180}, 0.1, 0\}, 0.9, 510];
gb1 = makeGraph[\{-5, -5, \frac{\pi}{180}, 0.1, 0\}, 0.9, 470];
gp1 = makeGraph[\{-5, -5, \frac{\pi}{180} 0.1, 0\}, 0.9, 410];
gr15 = makeGraph[\{-5, -5, \frac{\pi}{180} 15, 0\}, 0.9, 650];
go15 = makeGraph[\{-5, -5, \frac{\pi}{180} 15, 0\}, 0.9, 615];
gy15 = makeGraph[\{-5, -5, \frac{\pi}{180}, 15, 0\}, 0.9, 590];
gg15 = makeGraph[\{-5, -5, \frac{\pi}{100}, 15, 0\}, 0.9, 510];
gb15 = makeGraph[\{-5, -5, \frac{\pi}{180} 15, 0\}, 0.9, 470];
gp15 = makeGraph[\{-5, -5, \frac{\pi}{180} 15, 0\}, 0.9, 410];
gr30 = makeGraph[\{-5, -5, \frac{\pi}{180} 30, 0\}, 0.9, 650];
go30 = makeGraph[\{-5, -5, \frac{\pi}{180} 30, 0\}, 0.9, 615];
gy30 = makeGraph[\{-5, -5, \frac{\pi}{180}, 30, 0\}, 0.9, 590];
gg30 = makeGraph[\{-5, -5, \frac{\pi}{180} 30, 0\}, 0.9, 510];
gb30 = makeGraph[\{-5, -5, \frac{\pi}{180} 30, 0\}, 0.9, 470];
gp30 = makeGraph[\{-5, -5, \frac{\pi}{180} 30, 0\}, 0.9, 410];
gr45 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180}, 44.9, 0 \right\}, 0.9, 650 \right];
go45 = makeGraph[\{-5, -5, \frac{\pi}{180}, 44.9, 0\}, 0.9, 615];
gy45 = makeGraph[\{-5, -5, \frac{\pi}{180} 44.9, 0\}, 0.9, 590];
gg45 = makeGraph[\{-5, -5, \frac{\pi}{180}, 44.9, 0\}, 0.9, 510];
gb45 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180}, 44.9, 0 \right\}, 0.9, 470 \right];
gp45 = makeGraph[\{-5, -5, \frac{\pi}{180}, 44.9, 0\}, 0.9, 410];
gr60 = makeGraph[\{-5, -5, \frac{\pi}{180}, 60, 0\}, 0.9, 650];
go60 = makeGraph[\{-5, -5, \frac{\pi}{180} 60, 0\}, 0.9, 615];
gy60 = makeGraph[\{-5, -5, \frac{\pi}{180}, 60, 0\}, 0.9, 590];
```

```
 gg60 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 60, 0 \right\}, 0.9, 510 \right]; 
 gb60 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 60, 0 \right\}, 0.9, 470 \right]; 
 gp60 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 60, 0 \right\}, 0.9, 410 \right]; 
 gr75 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 75, 0 \right\}, 0.9, 650 \right]; 
 go75 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 75, 0 \right\}, 0.9, 615 \right]; 
 gy75 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 75, 0 \right\}, 0.9, 590 \right]; 
 gg75 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 75, 0 \right\}, 0.9, 590 \right]; 
 gb75 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 75, 0 \right\}, 0.9, 470 \right]; 
 gp75 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 75, 0 \right\}, 0.9, 410 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 650 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 590 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 590 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 590 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 590 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 470 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 470 \right]; 
 gp90 = makeGraph \left[ \left\{ -5, -5, \frac{\pi}{180} 89.9, 0 \right\}, 0.9, 410 \right];
```

```
Show[{tlo, gr1, go1, gy1, gg1, gb1, gp1, gr15, go15, gy15,
gg15, gb15, gp15, gr30, go30, gy30, gg30, gb30, gp30, gr45, go45,
gy45, gg45, gb45, gp45, gr60, go60, gy60, gg60, gb60, gp60, gr75,
go75, gy75, gg75, gb75, gp75, gr90, go90, gy90, gg90, gb90, gp90}]
```

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```
gr90 = makeGraph[\{-1.5, -6, \frac{\pi}{180} 89.9, 0\}, 0.9, 650];
go90 = makeGraph[\{-1.5, -6, \frac{\pi}{180} 89.9, 0\}, 0.9, 615];
gy90 = makeGraph[\{-1.5, -6, \frac{\pi}{180} 89.9, 0\}, 0.9, 590];
gg90 = makeGraph[\{-1.5, -6, \frac{\pi}{180} 89.9, 0\}, 0.9, 510];
gb90 = makeGraph[\{-1.5, -6, \frac{\pi}{180} 89.9, 0\}, 0.9, 470];
gp90 = makeGraph[\{-1.5, -6, \frac{\pi}{180} 89.9, 0\}, 0.9, 410];
```

```
Show[{tlo, gr90, go90, gy90, gb90, gp90}]
```

```
gr10 = makeGraph \left[ \left\{ -5, 1, \frac{\pi}{180} 10, 0 \right\}, 0.9, 650 \right];
go10 = makeGraph \left[ \left\{ -5, 1, \frac{\pi}{180} 10, 0 \right\}, 0.9, 615 \right];
gy10 = makeGraph[\{-5, 1, \frac{\pi}{180} 10, 0\}, 0.9, 590];
gg10 = makeGraph[{-5, 1, \frac{\pi}{180} 10, 0}, 0.9, 510];
gb10 = makeGraph[{-5, 1, \frac{\pi}{180} 10, 0}, 0.9, 470];
gp10 = makeGraph[\{-5, 1, \frac{\pi}{180} 10, 0\}, 0.9, 410];
```

```
Show[{tlo, gr60, go60, gy60, gg60, gb60, gp60}]
```