Exit[]

```
KadaptRK3BS[XY_] :=

Module[{k1, k2, k3, k4, x = First@XY, Y = Drop[XY, 1], \DeltaY23, \Deltak, hstare}, hstare = h;

k1 = h FIO;

k2 = h F[x + \frac{1}{2} h, ##] &@@ (Y + \frac{1}{2} k1);

k3 = h F[x + \frac{3}{4} h, ##] &@@ (Y + \frac{3}{4} k2);

Y3 = Y + (\frac{2}{9} k1 + \frac{1}{3} k2 + \frac{4}{9} k3);

FIO = F[x + h, ##] &@@Y3;

k4 = h FIO;

\DeltaY23 = Abs[\frac{1}{72} (5 k1 - 6 k2 - 8 k3 + 9 k4)];

\Deltak = Max@ \frac{\DeltaY23}{Abs[Y3] + Abs[Y3 - Y]};

h = hstare If[\delta > \Deltak, Min[(\frac{\delta}{\Delta k})<sup>1/3</sup>, 5], Max[(\frac{\delta}{\Delta k})<sup>1/3</sup>, 1/5]];

ndone++;

Flatten@{x + hstare, Y3}]
```

```
makeGraph[iniDat_: \{-6, -1.5, \frac{\pi}{180}, 0\}, P_: 0.8, \lambda_: 400] :=
 Module [graf, hstart, v, dvx, dvy, \lambda 1 = 400, \lambda 2 = 720,
     \epsilon = 0.2, kolor = ColorData["VisibleSpectrum"][\lambda]},
   \{w = 6, v = 0.2, a = 1, b = 0.9, ro = 0.9, u = \sqrt{\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2}\};
  n1 = 1 + P \left( \frac{1 + Exp[-ro/v]}{1 + Exp[u - ro/v]} + \frac{(x-1)}{1 + Exp[u - ro/v]} \right);
   nn[x_{-}, y_{-}] = n1 + \frac{\left(-1 + n1\right) \in \left(\lambda^{2} - \lambda 1^{2}\right) \lambda 2^{2}}{\lambda^{2} \left(\lambda 1^{2} - \lambda 2^{2}\right)};
   gWsp = Plot[nn[x, 0], \{x, -w, w\}, PlotRange \rightarrow \{All, \{0, 3\}\}];
   tlo = ContourPlot[nn[x, y],
       \{x, -w, w\}, \{y, -w, w\}, Contours \rightarrow 29, PlotPoints \rightarrow 39\};
   v[x_{-}, y_{-}] = Log@(nn[x, y]);
   dvx[x_{-}, y_{-}] = D[v[x, y], x];
   dvy[x_{-}, y_{-}] = D[v[x, y], y];
   F[s_{x}, x_{y}, y_{y}, \phi_{x}, t_{y}] = \{Cos[\phi], Sin[\phi], 
        dvy[x, y] Cos[\phi] - dvx[x, y] Sin[\phi], Exp@(v[x, y])} // Simplify;
   {s0, s1} = {0, \infty};
    \{x0, y0, \phi0, t0\} = iniDat;
   hstart[] := Module[{f, df, fdf, Y0, x, y, \phi, t, s, tmp},
      Y0 = Abs[{x0, y0, \phi0}];
       f = Take[F[s0, x0, y0, \phi0, t0], 3];
       df = Transpose \left( D[Take[F[s, x, y, \phi, t], 3], \#] \& /@ \{x, y, \phi\} \right) /. s \rightarrow s0 /.
               x \rightarrow x0 /. y \rightarrow y0 /. \phi \rightarrow \phi0];
       fdf = Abs[f.df];
       tmp = Flatten@
          Table \Big[ If \Big[ fdf[[i]] > 0, Min \Big[ \sqrt{\frac{2 \, Y0[[i]]}{fdf[[i]]}}, \frac{Abs[f[[i]]]}{fdf[[i]]} \Big], \infty \Big], \{i, 1, 3\} \Big];
       \sqrt{\delta} Min@tmp];
Clear[sol, tor];
   \{\delta = 10^{-8}, h = hstart[], hmax = \infty, nmax = 10000, ndone = 0, \};
   FIO = F[s0, x0, y0, \phi0, 0];
   sol = NestWhileList[KadaptRK3BS, \{s0, x0, y0, \phi0, t0\},
       (w \ge Abs[#[[2]]] \&\&w \ge Abs[#[[3]]] \&\&#[[1]] < s1 \&\& ndone < nmax) \&];
   Print["ndone= ", ndone];
   tor[tkolor_] :=
     ListPlot[\{\#[[2]], \#[[3]]\} & /@ sol, Joined \rightarrow True, PlotStyle \rightarrow tkolor];
   graf = Show[tor[kolor], PlotRange \rightarrow All, AspectRatio \rightarrow 1];
   Print[Show[{tlo, graf}]];
   graf
```

Rysunek 7.13a

```
gr20 = makeGraph[\{-6, -1.1, \frac{\pi}{180} 20, 0\}, 0.35, 650];
go20 = makeGraph[\{-6, -1.1, \frac{\pi}{180} 20, 0\}, 0.35, 615];
gy20 = makeGraph[\{-6, -1.1, \frac{\pi}{180}, 20, 0\}, 0.35, 590\};
gg20 = makeGraph[\{-6, -1.1, \frac{\pi}{180}, 20, 0\}, 0.35, 510];
gb20 = makeGraph[\{-6, -1.1, \frac{\pi}{180}, 20, 0\}, 0.35, 470];
gp20 = makeGraph[\{-6, -1.1, \frac{\pi}{180}, 20, 0\}, 0.35, 410];
```

```
Show[{tlo, gr20, go20, gy20, gg20, gb20, gp20}]
```

Rysunek 7.13b

```
gr335 = makeGraph[\{-4.5, -0.1, \frac{\pi}{190} 335, 0\}, 0.35, 650\};
go335 = makeGraph[{-4.5, -0.1, \frac{\pi}{180} 335, 0}, 0.35, 615];
gy335 = makeGraph[{-4.5, -0.1, \frac{\pi}{180} 335, 0}, 0.35, 590];
gg335 = makeGraph[\{-4.5, -0.1, \frac{\pi}{180} 335, 0\}, 0.35, 510];
gb335 = makeGraph[\{-4.5, -0.1, \frac{\pi}{180} 335, 0\}, 0.35, 470];
gp335 = makeGraph[\{-4.5, -0.1, \frac{\pi}{180} 335, 0\}, 0.35, 410];
```

```
Show[{tlo, gr335, go335, gy335, gg335, gb335, gp335}]
```

Rysunek 7.14a

```
gr179 = makeGraph[\{5, -2, \frac{\pi}{180} 179, 0\}, 0.35, 650];
go179 = makeGraph[\{5, -2, \frac{\pi}{180} 179, 0\}, 0.35, 615];
gy179 = makeGraph[\{5, -2, \frac{\pi}{180}, 179, 0\}, 0.35, 590\};
gg179 = makeGraph[\{5, -2, \frac{\pi}{180} 179, 0\}, 0.35, 510];
gb179 = makeGraph[\{5, -2, \frac{\pi}{180} 179, 0\}, 0.35, 470];
gp179 = makeGraph[\{5, -2, \frac{\pi}{180} 179, 0\}, 0.35, 410];
```

```
Show[{tlo, gr179, go179, gy179, gg179, gb179, gp179}]
```

Rysunek 7.14b

```
Show[{tlo, gr79, go79, gy79, gb79, gp79}]
```

Rysunek 7.15

```
gr135 = makeGraph[{6, 0.01, \frac{\pi}{180} 135, 0}, 0.35, 650];
go135 = makeGraph[{6, 0.01, \frac{\pi}{180} 135, 0}, 0.35, 615];
gy135 = makeGraph[\{6, 0.01, \frac{\pi}{180} 135, 0\}, 0.35, 590];
gg135 = makeGraph[\{6, 0.01, \frac{\pi}{180} 135, 0\}, 0.35, 510];
gb135 = makeGraph[\{6, 0.01, \frac{\pi}{180} 135, 0\}, 0.35, 470];
gp135 = makeGraph[\{6, 0.01, \frac{\pi}{180} 135, 0\}, 0.35, 410];
gr150 = makeGraph[\{6, 0.01, \frac{\pi}{180} 150, 0\}, 0.35, 650];
go150 = makeGraph[\{6, 0.01, \frac{\pi}{180} 150, 0\}, 0.35, 615];
gy150 = makeGraph[\{6, 0.01, \frac{\pi}{180}, 150, 0\}, 0.35, 590];
gg150 = makeGraph[{6, 0.01, \frac{\pi}{180} 150, 0}, 0.35, 510];
gb150 = makeGraph[{6, 0.01, \frac{\pi}{180} 150, 0}, 0.35, 470];
gp150 = makeGraph[\{6, 0.01, \frac{\pi}{180} 150, 0\}, 0.35, 410];
gr165 = makeGraph[\{6, 0.01, \frac{\pi}{180} 165, 0\}, 0.35, 650];
go165 = makeGraph[\{6, 0.01, \frac{\pi}{180} 165, 0\}, 0.35, 615];
gy165 = makeGraph[{6, 0.01, \frac{\pi}{180} 165, 0}, 0.35, 590];
gg165 = makeGraph[{6, 0.01, \frac{\pi}{180} 165, 0}, 0.35, 510];
gb165 = makeGraph[\{6, 0.01, \frac{\pi}{180} 165, 0\}, 0.35, 470];
gp165 = makeGraph[\{6, 0.01, \frac{\pi}{180} 165, 0\}, 0.35, 410];
gr180 = makeGraph[{6, 0.01, \frac{\pi}{180} 179.9, 0}, 0.35, 650];
```

```
go180 = makeGraph[{6, 0.01, \frac{\pi}{180}179.9, 0}, 0.35, 615];
gy180 = makeGraph[{6, 0.01 \frac{\pi}{180} 179.9, 0}, 0.35, 590];
gg180 = makeGraph[{6, 0.01, \frac{\pi}{180} 179.9, 0}, 0.35, 510];
gb180 = makeGraph[\{6, 0.01, \frac{\pi}{180} 179.9, 0\}, 0.35, 470];
gp180 = makeGraph[{6, 0.01, \frac{\pi}{180}179.9, 0}, 0.35, 410];
gr195 = makeGraph[{6, 0.01, \frac{\pi}{180} 195, 0}, 0.35, 650];
go195 = makeGraph[{6, 0.01, \frac{\pi}{180} 195, 0}, 0.35, 615];
gy195 = makeGraph[{6, 0.01, \frac{\pi}{180} 195, 0}, 0.35, 590];
gg195 = makeGraph[\{6, 0.01, \frac{\pi}{180} 195, 0\}, 0.35, 510];
gb195 = makeGraph[\{6, 0.01, \frac{\pi}{180} 195, 0\}, 0.35, 470];
gp195 = makeGraph[\{6, 0.01, \frac{\pi}{180} 195, 0\}, 0.35, 410];
gr210 = makeGraph[{6, 0.01, \frac{\pi}{180} 210, 0}, 0.35, 650];
go210 = makeGraph[\{6, 0.01, \frac{\pi}{180} 210, 0\}, 0.35, 615];
gy210 = makeGraph[\{6, 0.01, \frac{\pi}{180} 210, 0\}, 0.35, 590];
gg210 = makeGraph[\{6, 0.01, \frac{\pi}{180}, 210, 0\}, 0.35, 510];
gb210 = makeGraph[\{6, 0.01, \frac{\pi}{180}, 210, 0\}, 0.35, 470];
gp210 = makeGraph[\{6, 0.01, \frac{\pi}{180} 210, 0\}, 0.35, 410];
gr225 = makeGraph[\{6, 0.01, \frac{\pi}{180} 225, 0\}, 0.35, 650];
go225 = makeGraph[\{6, 0.01, \frac{\pi}{180} 225, 0\}, 0.35, 615];
gy225 = makeGraph[{6, 0.01, \frac{\pi}{180} 225, 0}, 0.35, 590];
gg225 = makeGraph[{6, 0.01, \frac{\pi}{180} 225, 0}, 0.35, 510];
gb225 = makeGraph[{6, 0.01, \frac{\pi}{180} 225, 0}, 0.35, 470];
gp225 = makeGraph[{6, 0.01, \frac{\pi}{180} 225, 0}, 0.35, 410];
```

```
Show[{tlo, gr135, go135, gy135, gg135, gb135, gp135, gr150, go150, gy150, gg150,
  gb150, gp150, gr165, go165, gy165, gg165, gb165, gp165, gr180, go180, gy180,
  gg180, gb180, gp180, gr195, go195, gy195, gg195, gb195, gp195, gr210, go210,
  gy210, gg210, gb210, gp210, gr225, go225, gy225, gg225, gb225, gp225}]
```

Rysunek 7.16

```
gr45 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 45, 0\}, 0.35, 650];
```

```
go45 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 45, 0\}, 0.35, 615];
gy45 = makeGraph[{-3, 0.01, \frac{\pi}{180} 45, 0}, 0.35, 590];
gg45 = makeGraph[{-3, 0.01, \frac{\pi}{180} 45, 0}, 0.35, 510];
gb45 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0\}, 0.35, 470];
gp45 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0\}, 0.35, 410];
gr30 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 30, 0\}, 0.35, 650\};
go30 = makeGraph[{-3, 0.01, \frac{\pi}{180} 30, 0}, 0.35, 615];
gy30 = makeGraph[{-3, 0.01, \frac{\pi}{180} 30, 0}, 0.35, 590];
gg30 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 30, 0\}, 0.35, 510];
gb30 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 30, 0\}, 0.35, 470];
gp30 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 30, 0\}, 0.35, 410\};
gr15 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0\}, 0.35, 650\};
go15 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0\}, 0.35, 615\};
gy15 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 15, 0\}, 0.35, 590];
gg15 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 15, 0\}, 0.35, 510];
gb15 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 15, 0\}, 0.35, 470];
gp15 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0\}, 0.35, 410];
gr0 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0.1, 0\}, 0.35, 650];
go0 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0.1, 0\}, 0.35, 615];
gy0 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0.1, 0\}, 0.35, 590];
gg0 = makeGraph[{-3, 0.01, \frac{\pi}{180} 0.1, 0}, 0.35, 510];
gb0 = makeGraph[{-3, 0.01, \frac{\pi}{180} 0.1, 0}, 0.35, 470];
gp0 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0.1, 0\}, 0.35, 410];
gr345 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 345, 0\}, 0.35, 650];
go345 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 345, 0\}, 0.35, 615];
gy345 = makeGraph[{-3, 0.01, \frac{\pi}{180} 345, 0}, 0.35, 590];
gg345 = makeGraph[{-3, 0.01, \frac{\pi}{180} 345, 0}, 0.35, 510];
gb345 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 345, 0\}, 0.35, 470];
```

```
gp345 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 345, 0\}, 0.35, 410\};
gr330 = makeGraph[{-3, 0.01, \frac{\pi}{180} 330, 0}, 0.35, 650];
go330 = makeGraph[{-3, 0.01, \frac{\pi}{180} 330, 0}, 0.35, 615];
gy330 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 330, 0\}, 0.35, 590];
gg330 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 330, 0\}, 0.35, 510\};
gb330 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 330, 0\}, 0.35, 470\};
gp330 = makeGraph[{-3, 0.01, \frac{\pi}{180} 330, 0}, 0.35, 410];
gr315 = makeGraph[{-3, 0.01, \frac{\pi}{180} 315, 0}, 0.35, 650];
go315 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 315, 0\}, 0.35, 615];
gy315 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 315, 0\}, 0.35, 590\};
gg315 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 315, 0\}, 0.35, 510\};
gb315 = makeGraph[\{-3, 0.01, \frac{\pi}{180}, 0\}, 0.35, 470];
gp315 = makeGraph[\{-3, 0.01, \frac{\pi}{180} 315, 0\}, 0.35, 410];
```

```
Show[{tlo, gr0, go0, gy0, gg0, gb0, gp0, gr15, go15, gy15, gg15, gb15,
  gp15, gr30, go30, gy30, gg30, gb30, gp30, gr45, go45, gy45, gg45,
  gb45, gp45, gr345, go345, gy345, gg345, gb345, gp345, gr330, go330,
  gy330, gg330, gb330, gp330, gr315, go315, gy315, gg315, gb315, gp315}]
```