KAT - Domácí úkol 1

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• Úloha 1.

$$z^{3} = -4\sqrt{2} + 4\sqrt{2}i$$

$$|z|^{3}(\cos(\phi) + i\sin(\phi))^{3} = \sqrt{(4\sqrt{2})^{2} + (4\sqrt{2})^{2}} * (\cos(\arctan(-1)) + i\sin(\arctan(-1)))$$

$$|z|^{3}(\cos(3\phi) + i\sin(3\phi)) = 8(\cos(\frac{3\pi}{4}) + i\sin(\frac{3\pi}{4}))$$

modul:

$$|z| = \sqrt[3]{8} = 2$$

fáze:

$$\cos(3\phi) + i\sin(3\phi) = \cos(\frac{3\pi}{4}) + i\sin(\frac{3\pi}{4})$$
$$\phi_1 = \frac{\pi}{4}$$
$$\phi_2 = \frac{11\pi}{12}$$
$$\phi_3 = \frac{19\pi}{12}$$

řešení:

$$z_1 = 2\left(\cos\left(\frac{\pi}{4}\right) + i\sin\left(\frac{\pi}{4}\right)\right)$$
$$z_2 = 2\left(\cos\left(\frac{11\pi}{12}\right) + i\sin\left(\frac{11\pi}{12}\right)\right)$$
$$z_3 = 2\left(\cos\left(\frac{19\pi}{12}\right) + i\sin\left(\frac{19\pi}{12}\right)\right)$$